





# Learning to Walk 

Massachusetts Institute of Technology, 2004

## Learning flapping flight



## Learning flapping flight





## Rapidly Exploring Random Trees (RRTs)

- Steve LaValle, I998; LaValle and Kuffner, I999-200I


Nodes represent feasible configurations Edges represent feasible trajectories

## Rapidly Exploring Random Trees (RRTs)

- Steve LaValle, I998; LaValle and Kuffner, I999-200I



## Rapidly Exploring Random Trees (RRTs)

- Steve LaValle, I998; LaValle and Kuffner, I999-200I



## Rapidly Exploring Random Trees (RRTs)

- Steve LaValle, I998; LaValle and Kuffner, I999-200I



## Rapidly Exploring Random Trees (RRTs)

- Steve LaValle, I998; LaValle and Kuffner, I999-200I



## Rapidly Exploring Random Trees (RRTs)

- Steve LaValle, I998; LaValle and Kuffner, I999-200I







## Example: LittleDog Bounding Over Terrain



- Accurate dynamic model


## Example: LittleDog Bounding Over Terrain



- Accurate dynamic model
- Plan in the space of "halfbound" primitives


## Dynamic Invariant Sets Around Trajectories




## Dynamic Invariant Sets Around Trajectories

- Effectively solve many funnels along the trajectory (making sure that one dumps into the other) [Tobenkin IO].




## Dynamic Invariant Sets Around Trajectories

- Effectively solve many funnels along the trajectory (making sure that one dumps into the other) [Tobenkinl0].




## Dynamic Invariant Sets Around Trajectories

- Effectively solve many funnels along the trajectory (making sure that one dumps into the other) [Tobenkin IO].
- Stability not required (finite-time analysis)




## Dynamic Invariant Sets Around Trajectories

- Effectively solve many funnels along the trajectory (making sure that one dumps into the other) [Tobenkin IO].
- Stability not required (finite-time analysis)


- Optimizing volume is more complex.


## Pendulum "Funnels"



## Pendulum "Funnels"




Erdmann, Mason, Rizzi, Koditschek

## Pendulum "Funnels"




Erdmann, Mason, Rizzi, Koditschek

## The "LQR-Trees" Algorithm



## The "LQR-Trees" Algorithm



## The "LQR-Trees" Algorithm



The "LQR-Trees" Algorithm


## Probabilistic Feedback Coverage

## Probabilistic Feedback Coverage

- Probabilistically covers reachable space with stabilizing controller


## Probabilistic Feedback Coverage

- Probabilistically covers reachable space with stabilizing controller
- Any finite measure region in the controllable set that is not in a funnel will be sampled and added to the tree


## Probabilistic Feedback Coverage

- Probabilistically covers reachable space with stabilizing controller
- Any finite measure region in the controllable set that is not in a funnel will be sampled and added to the tree


