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# Load-Induced Modulation of Signal Transduction Networks

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Biological signal transduction networks are commonly viewed as circuits that pass along information—in the process amplifying signals, enhancing sensitivity, or performing other signal-processing tasks—to transcriptional and other components. Here, we report on a “reverse-causality” phenomenon, which we call load-induced modulation. Through a combination of analytical and experimental tools, we discovered that signaling was modulated, in a surprising way, by downstream targets that receive the signal and, in doing so, apply what in physics is called a load. Specifically, we found that non-intuitive changes in response dynamics occurred for a covalent modification cycle when load was present. Loading altered the response time of a system, depending on whether the activity of one of the enzymes was maximal and the other was operating at its minimal rate or whether both enzymes were operating at submaximal rates. These two conditions, which we call “limit regime” and “intermediate regime,” were associated with increased or decreased response times, respectively. The bandwidth, the range of frequency in which the system can process information, decreased in the presence of load, suggesting that downstream targets participate in establishing a balance between noise-filtering capabilities and a circuit’s ability to process high-frequency stimulation. Nodes in a signaling network are not independent relay devices, but rather are modulated by their downstream targets.

## INTRODUCTION

A promising approach for unraveling the function of complex biological networks is to decompose them into functional modules (1, 2) that have clearly defined functions, such as the sensing of extracellular ligands, signal transduction, gene expression, or control of metabolism. The goal is to characterize the emergent collective function of networks from knowledge of the behaviors of the individual modules, their interconnection topology, and the character of their interactions.

System dynamics, that is, the time-dependent behavior of the system, is critical in the process of delineating modules and determining their collective function as several researchers have remarked [see, for example, (3)]. At the genetic level, transcriptional networks encode various time-varying behaviors, such as the periodic changes of gene expression that are responsible for circadian rhythms and timing of the cell cycle (4, 5). Metabolic reaction pathways are regulated by environmental stimuli that vary over time (6). The transient behavior of signaling systems controls gene activation patterns, as well as diverse physiological processes ranging from bacterial chemotaxis to cytoskeletal reorganization, to checkpoints in the cell cycle, and to apoptosis (7, 8). Even when the steady-state amount of an activated signaling protein is within normal ranges, transient excess activation may result in aberrant signaling with severe consequences, such as cancer (9).

We performed a study of system dynamics and modularity, specifically focusing on signal transduction circuits. A common view is that the operating characteristics of these circuits should not depend on the presence or absence of downstream targets, such as gene promoters or other proteins, to which they convey information. However, theoretical work (10–13) has suggested that the behavior of discrete modules might dramatically change in the presence of downstream targets through the effect of loads, just as in electrical, hydraulic, or mechanical systems. For covalent modification cycles, computational work has studied the effect of substrate sequestration on the cycle behavior (14–16). Specifically, it was shown that sequestration may account for dynamic effects such as signaling delay (15). In the context of gene regulatory networks, theoretical studies have shown that loading can decrease system bandwidth (17, 18).

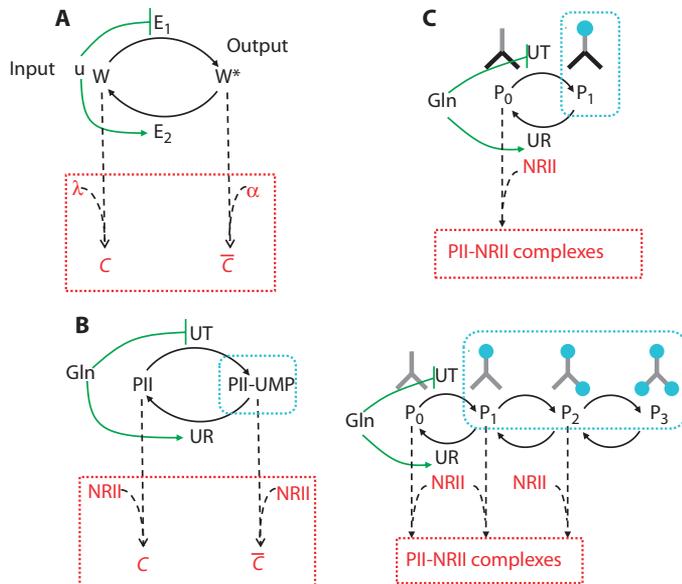
However, there has not been any experimental study of the dynamic effects of loads, nor have there been theoretical studies quantifying how the basic signal-processing time scales (response time and bandwidth) are affected. We used a combination of analytical and experimental tools and found that the time scales of signal communication were modulated by the concentrations of downstream targets (“loads”) through a process that we term “load-induced modulation.”

The present work complements studies of stoichiometric retroactivity (19), that is, the effect of sequestering by downstream targets on the steady states of an upstream system. Stoichiometric retroactivity is a phenomenon different from load-induced modulation, because stoichiometric retroactivity affects systems at steady state (10–12). By contrast, we demonstrate that even under conditions where the steady state of a component is unaffected by the presence of downstream targets (no stoichiometric retroactivity), the dynamic behavior of the system may be significantly altered by load-induced modulation (10–12). We provide mathematical and experimental evidence for the modulation of pathway dynamics by the presence of downstream targets.

As a model system, we chose a ubiquitous motif in signal transduction, the covalent modification cycle (Fig. 1A). Experimentally, we used the

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reconstituted uridylyltransferase/uridylyl-removing enzyme (UTase/UR)–PII cycle, which is a model system derived from the nitrogen assimilation control network of *Escherichia coli* (20) (Fig. 1B). In this system of purified components, there are two enzymes ( $E_1$ , representing UTase, and  $E_2$ , representing UR) that are reciprocally controlled by an allosteric effector ( $u$ , representing Gln).  $E_1$  and  $E_2$  catalyze the interconversion of the un-



**Fig. 1.** The experimental system enables analysis of load-induced modulation of a signal transduction cascade. (A) General depiction of a covalent modification cycle.  $E_1$  and  $E_2$  represent the converter enzymes of the cycle, which are allosterically controlled by stimulatory effector  $u$ . The cycle protein  $W$  is interconverted to a modified form,  $W^*$ .  $\alpha$  and  $\lambda$  represent the effective load applied to  $W^*$  and  $W$ , respectively, forming complexes  $C$  and  $\bar{C}$ , respectively. That is, they represent the amount of downstream targets normalized by their dissociation constants (see Supplementary Materials, Model and Simulation, section 1). The input  $u$  is a periodic signal with frequency  $\omega$  and amplitude  $A_0$ . (B) The UTase/UR–PII system. (Left) An abstracted view so that the correspondence with the modeled covalent modification cycle in (A) is evident. (Right) Detailed view of the double-load UTase/UR–PII cycle using wild-type PII trimers. The sequential modification of the three subunits of the PII trimer is depicted along with the complexes that are bound by NRII. Light blue circles signify the uridylyl groups that modify each subunit. Once modified by a uridylyl group, the modified subunit cannot bind NRII, although the remaining unmodified PII subunits of the trimer can bind NRII. PII-UMP represents the  $P_1$ ,  $P_2$ , and  $P_3$  species of PII because each of these has at least one modified subunit. Thus, the load NRII applies to both sides of the cycle. (C) Detailed view of the mutant UTase/UR–PII cycle used to represent a system with a single load. In most heterotrimeric PIIs, one of the three subunits is wild type, and two of the three subunits contain a mutation that prevents their interaction with NRII or UTase/UR. This “monovalent”  $P_1$  PII heterotrimer is uridylylated and de-uridylylated in response to glutamine, but NRII binds only to the de-uridylylated  $P_0$  PII; thus, the load applies to only one side of the cycle. Monovalent PII is depicted as containing two mutant subunits (black) and one wild-type subunit that can be reversibly modified or bind to NRII.

modified ( $W$ , representing PII) and modified [ $W^*$ , representing PII–UMP (uridine monophosphate)] forms of PII. PII is a homotrimer, and each subunit can be modified by uridylylation; modified subunits cannot bind to the downstream target protein NRII. However, because PII is a homotrimer, incompletely modified trimers can bind NRII through their unmodified subunits (Fig. 1B, right). We represent the effective load of NRII binding to any of the subunits of completely unmodified PII as  $\lambda$  (representing NRII that binds to unmodified trimers of PII) and the effective load resulting from NRII binding to an unmodified PII subunit from singly modified or doubly modified trimers of PII as  $\alpha$ . Although in the experimental system studied here these loads are a protein (NRII), and the same protein interacts with both the modified and the unmodified forms of PII, loads can, in principle, be provided by any type of molecule that binds to either or both forms of the cycle substrate protein. The input of the system,  $u$ , is Gln, and the output of the system is the amount of the modified protein  $W^*$  (PII-UMP). A variety of regulatory patterns are possible, and we consider in detail a model where  $u$  is an activator for  $E_2$  and a non-competitive inhibitor for  $E_1$ , because this pattern matches the UTase/UR–PII system (Fig. 1B). We considered the system “isolated” when there were no loads and “connected” when the load (NRII) was present. We also analyzed a mutated version of the UTase/UR–PII system in which the load (NRII) applied only to one side of the cycle (Fig. 1C). This mutated version of the cycle included a heterotrimeric form of the PII protein that behaved as if it was functionally monomeric.

We analytically derived an extension of the standard Goldbeter-Koshland model for covalent modification (21) to include the effect of loads. On the basis of this mathematical model, we obtained analytical expressions for the response time and bandwidth as functions of the load and cycle parameters. We then used the frequency response, a control theory tool, to determine how time-varying signals were transmitted to measure the signaling system output in response to input signals that oscillated at different frequencies (22). By comparing the frequency response and the step response of the isolated system to those of the connected system, we determined how downstream loads affected system dynamics.

We found that the response to time-varying input stimuli was altered by the presence of loads, a phenomenon that we call load-induced modulation. When the level of the stimulus was either zero or at a high enough level to saturate the sensory capacity of the system, one of the cycle enzymes operates at its maximal rate, whereas the opposing activity operates at its minimal rate. We refer to this regime as the limit regime and found that the presence of the loads increased the response time (the time required for the system to transition between the “on” and the “off” states). By contrast, when the cycle enzymes operate in the presence of intermediate levels of stimulation, both enzymatic activities occur at intermediate rates. We refer to this regime as the intermediate regime and show that the presence of loads decreased the response time. The temporal profile of a stimulus determines how it is selectively transmitted through different cellular processes (23), and the quantity of information a pathway can carry depends on its bandwidth (24). We found that the presence of loads decreased system bandwidth and that the extent of the decrease depended on whether one or both of the modified and the unmodified forms of the substrate protein bound to a load. The effect of loads on bandwidth was more marked when only one of the two forms of the substrate protein was bound. Finally, when only one form of the substrate protein was bound by a downstream interacting target, the dynamical effects of the presence of the load were minimized by increasing the abundance of the cycle enzymes. Conversely, when both modified and unmodified forms of the substrate protein were bound by interacting targets, the dynamical effects of the presence of the loads were minimized by reduction in the abundance of the cycle enzymes.

## RESULTS

## Mathematical model description

We extended the standard ordinary differential equation (ODE) model for covalent modification by Goldbeter and Koshland (21) to include the effect of loads for either the unmodified or the modified substrate protein species (Supplementary Materials, Model and Simulation, section 1). For a species  $X$ , we represent the concentration of that species by  $X$  (italics). In the experimental system, we measured the amount of the total modified protein, that is,  $\overline{W} := W^* + \overline{C}$ , where  $\overline{C}$  is the amount of the complex of the modified substrate protein bound to the load  $\alpha$  (Fig. 1A). The ODE describing the dynamics of  $\overline{W}$  is given by Eq. 1 (derived in the Supplementary Materials, Model and Simulation, section 1):

$$\frac{d\overline{W}}{dt} = \frac{V_1}{(1 + u/k_D') K_1(1 + \lambda) + (W_T - \overline{W})} - V_2 \left( \frac{u}{k_D' + u} \right) \frac{\overline{W}}{K_2(1 + \alpha) + \overline{W}} \quad (1)$$

in which  $K_1$  and  $K_2$  are the Michaelis-Menten constants for the forward and backward modification reactions, respectively;  $W_T$  is the total amount of protein;  $V_1 = k_1 E_{1T}$  and  $V_2 = k_2 E_{2T}$  are the maximal rates of the forward and backward reactions, respectively ( $k_1, k_2$  being the catalytic rates and  $E_{1T}, E_{2T}$  being the total enzymes amounts);  $\lambda$  and  $\alpha$  are the effective loads applied to  $W$  and  $W^*$ , respectively;  $u$  is the concentration of the stimulatory effector; and  $k_D$  and  $k_D'$  are the dissociation constants of the stimulatory effector with enzymes  $E_1$  and  $E_2$ , respectively. When  $u$  is zero or very large, the enzyme activities  $(1 + u/k_D')$  and  $V_2 \left( \frac{u}{k_D' + u} \right)$  operate at their extreme values or limits. We refer to this operating regime as the “limit regime,” and we call the situation in which their activities are not saturated the “intermediate regime.” In the limit regime, the cycle output will reach its extreme values, corresponding to fully modified ( $\overline{W} = W_T$ ) or fully unmodified ( $\overline{W} = 0$ ). In the intermediate regime, the cycle output will not reach its maximum or minimum values. When  $\alpha = 0$ , the load is applied to  $W$  only. From the ODE in Eq. 1, we observed that the presence of the load increased the apparent Michaelis-Menten constants.

## Modeling results for load-induced modulation of rise and decay times

The rise and decay times quantify the time the cycle takes to switch steady state in response to a constant input stimulation. These times are relevant for signaling systems and also for transcriptional networks, in which the turning on and off of a signaling pathway or of a gene has direct consequences on physiology (25). The rise time is the time the output of the cycle  $\overline{W}$  takes to rise from 10 to 90% of its overall response, and the decay time is the time  $\overline{W}$  takes to decay from 90 to 10% of its overall response. (We obtained similar results if we considered the changes of the output between different percentages of the overall responses, such as 5 and 95% or 1 and 99% (see Supplementary Materials, Model and Simulation, section 1.3.1). We analyzed two cases: (i) when the cycle transitions between on ( $\overline{W} = W_T$ ) and off ( $\overline{W} = 0$ ) states in response to extreme inputs  $u = 0$  and  $u$  sufficiently large, respectively, to saturate the enzymes' activities (limit regime); (ii) when the cycle transitions between intermediate states corresponding to values of the input that do not saturate the enzymes' activities (intermediate regime).

Calculations of the rise and decay times using our model (see Supplementary Materials, Model and Simulation, section 1.3.1) gave the follow-

ing expressions for the decay and rise times of the connected system in the limit regime:

$$t_{\text{decay}} = \frac{1}{V_2} (K_2(1 + \alpha) \ln(10/1.1) + 0.8W_T) \quad (2)$$

$$t_{\text{rise}} = \frac{1}{V_1} (K_1(1 + \lambda) \ln(10/1.1) + 0.8W_T) \quad (3)$$

From these two equations, the decay and rise times increase linearly with the amount of load, and we can predict that the system with load on both  $W$  ( $\lambda > 0$ ) and  $W^*$  ( $\alpha > 0$ ) would display increased decay and rise times compared to the isolated system ( $\alpha = \lambda = 0$ ) (Fig. 2A). A system that had load applied only to  $W$  ( $\lambda > 0$ , but  $\alpha = 0$ ) would display an increased rise time but the same decay time as that of the isolated system.

When we set the input stimulation so the enzymes operate in the intermediate regime, the presence of loads is predicted to result in faster responses (Fig. 2B). Specifically, this is predicted to occur when the isolated system operates in the ultrasensitive regime ( $K_1, K_2 \ll W_T$ ), where the response is switch-like, and the load is sufficient to make  $K_1(1 + \lambda), K_2(1 + \alpha) \gg W_T$ , such that the dose response for the loaded system becomes more graded (Supplementary Materials, Model and Simulation, section 1.1; fig. S1). We could achieve this situation in our experimental system by using a concentration of PII that saturated the UTase and UR activities of the UTase/UR in the absence of NR1I, but which was not saturating in the presence of NR1I (19).

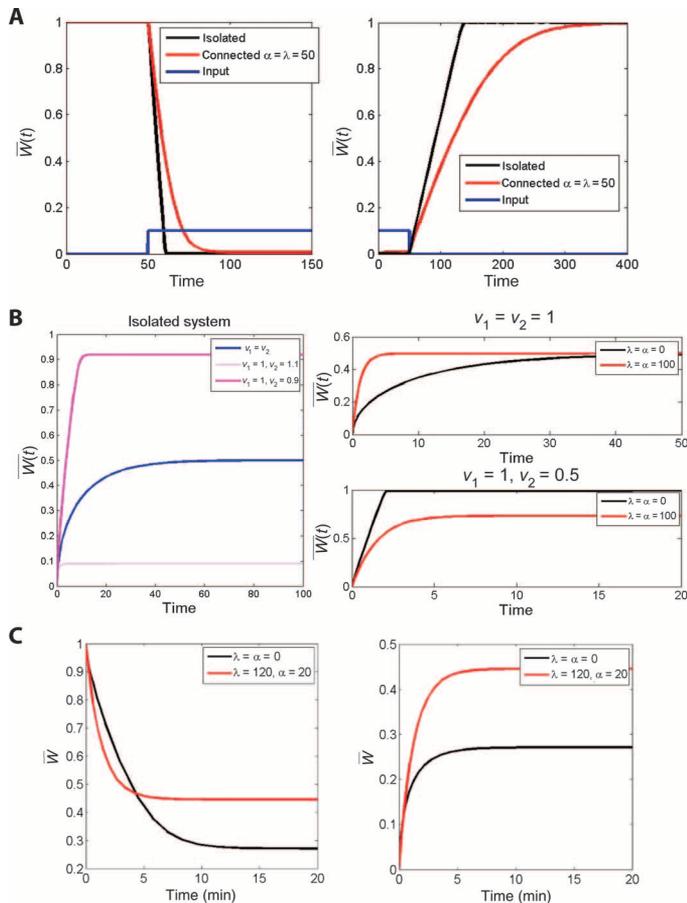
The presence of loads can have asymmetrical effects on the rise and decay times, causing one to increase while the other decreases. This is predicted to occur when, in addition to having  $K_1, K_2 \ll W_T$  and  $K_1(1 + \lambda), K_2(1 + \alpha) \gg W_T$ , the forward and reverse reactions of the covalent modification cycle have different Michaelis-Menten constants or catalytic rates (Fig. 2C). Both of these conditions can be obtained in our experimental system, because the UTase ( $E_1$ ) and UR ( $E_2$ ) activities of the UTase/UR have different Michaelis-Menten constants and catalytic rates.

## Load-induced modulation of the bandwidth

The bandwidth of a system is the frequency band in which the system can process information. Here, we examined how the same cycle can display different bandwidths depending on the specific configuration and amounts of the loads. Let  $A(\omega)$  be the amplitude of the output response to periodic input stimuli of period  $T = 2\pi/\omega$ . The bandwidth, denoted  $\omega_B$ , is defined as the frequency at which the amplitude of the response  $A(\omega)$  drops below the amplitude of the response to constant stimulation divided by the square root of 2 [ $A_0/\sqrt{2}$ ]. A quantitative relationship between the bandwidth and the amounts of load can be determined by calculating the amplitude of response from the model under the assumption of small-amplitude sinusoidal input stimuli (about a mean value of  $u_0$ ) of the form  $u(t) = u_0 + A_0 \sin(\omega t)$  (see Supplementary Materials, Model and Simulation, section 1.4; figs. S2 and S3). Even though sinusoidal inputs may not be biologically relevant, the system response to these inputs provides general information on the amplitude of response and bandwidth for more complicated input profiles. To complement the analysis on the basis of sinusoidal inputs, we also considered input profiles in the form of a train of exponentially decaying pulses, which are biologically relevant and closer to the inputs in the experimental system, and obtained the same qualitative results (see Supplementary Materials, Model and Simulation, section 1.5; fig. S4).

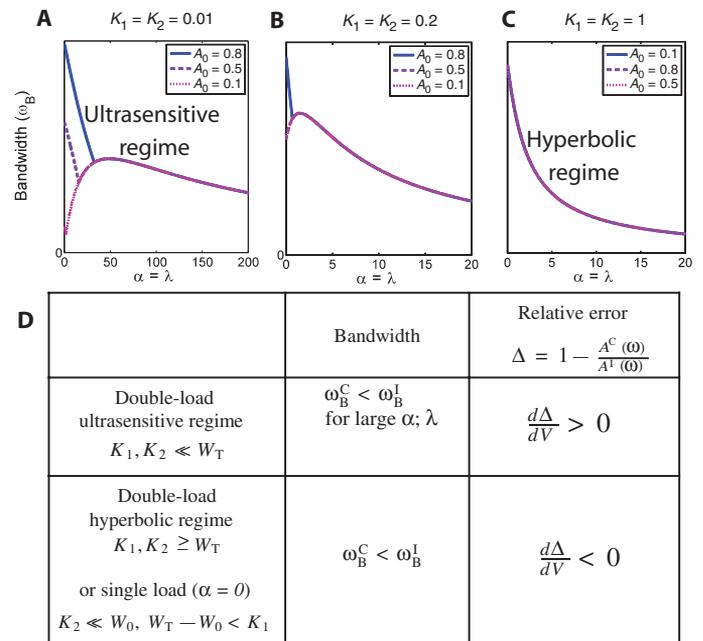
For the connected system, the model states that the bandwidth expression is proportional to the total amounts of enzymes  $E_{1T}$  and  $E_{2T}$  and to

the catalytic rates  $k_1, k_2$  and is inversely proportional to the concentrations of the loads  $\lambda$  and  $\alpha$  when the isolated system steady-state response is hyperbolic ( $K_1, K_2 \geq W_T$ ; see Supplementary Materials, Model and Simulation, section 1.4, for the exact bandwidth calculations). For large



**Fig. 2.** Results of the model predictions for the effects of load-induced modulation on the rise and decay times of a covalent modification cycle. (A) The effect of load on the rise and decay of the reactions in the limit regime. In the simulation, the values of the parameters were set as  $V_1 = 0.012$ ,  $V_2 = 0.12$ ,  $K_1 = K_2 = 0.01$ ,  $W_T = 1$ ,  $k_D = k_D' = 10$ , and  $\alpha = \lambda = 50$ . In the left plots, the input suddenly changes at time 50 from  $u = 0$  to  $u = 50$ , whereas in the right plot it changes from  $u = 50$  to  $u = 0$ . The blue plot shows the input profile normalized by a factor of 500. Both the rise and the decay times increase due to the presence of the load. (B) Effect of load on the rise and decay of the reactions in the intermediate regime. (Left) Effect of the difference  $v_1 - v_2$  on the isolated system rise time. When  $v_1 - v_2 = 0$ , the rise time is substantially larger than when  $v_1 - v_2 \neq 0$ . (Right) When  $v_1 - v_2 = 0$ , the rise time of the isolated system is substantially larger than the rise time of the connected system, whereas as the difference between  $v_1$  and  $v_2$  increases, the rise time of the connected system becomes larger than that of the isolated system. In these simulations, we have set  $K_1 = K_2 = 0.01$  and  $W_T = 1$ . (C) The effect of load on the rise and decay of the reactions in the intermediate when  $K_1 \neq K_2$ . In the simulations, we have set  $K_1 = 0.01$ ,  $K_2 = 0.06$ ,  $\lambda = 120$ ,  $\alpha = 20$ , and  $v_1 = 0.83$ ,  $v_2 = 1$ . Whereas the decay time is smaller for the connected system, the rise times of the connected and isolated systems are about the same.

loads  $\lambda$  and  $\alpha$ , the bandwidth of the connected system is predicted to be lower than that of the isolated system, that is,  $\omega_B^C < \omega_B^I$ , where “C” stands for “Connected” and “I” stands for “Isolated” (Fig. S2). More generally, according to the model, the expressions of the bandwidths depend on the amounts of load, on the operating regime of the isolated system [ultrasensitive ( $K_1, K_2 \ll W_T$ ) or hyperbolic ( $K_1, K_2 \geq W_T$ )], and on the input amplitude (whether it is such that the enzymes operate in the limit or intermediate regimes) (Fig. 3). Sufficiently high amounts of load decreased the bandwidth of the connected system compared to that of the isolated system (Fig. 3). However, for a fixed amount of load, the model predicted that decreasing the input amplitude (making the enzymes operate well within the intermediate regime) would decrease the difference between the isolated and the connected system bandwidths (Fig. 3A). If the input amplitude were set to sufficiently low values so the cycle enzyme operated well within the intermediate regime and the isolated system was operating in the ultrasensitive regime ( $K_1, K_2 \ll W_T$ ), then small amounts of load can theoretically increase system bandwidth (Fig. 3, A and B). If the isolated system was operating in the hyperbolic regime ( $K_1, K_2 \geq W_T$ ), then any amount of load would decrease system bandwidth independently



**Fig. 3.** Results of the model predictions for the effects of load-induced modulation on the bandwidth of a covalent modification cycle. Bandwidth is affected by load, the input amplitude, and the cycle operating regime. (A to C) (A) The effect of load on the bandwidth for different input amplitudes when the cycle operates in the ultrasensitive regime because  $K_1, K_2 \ll W_T$ . (B) The effect of load on the bandwidth for different input amplitudes when the cycle operates between ultrasensitive and hyperbolic regimes. (C) The effect of load on the bandwidth for different input amplitudes when the cycle operates in the hyperbolic regime because  $K_1, K_2 \geq W_T$ . For (A) to (C),  $k_D = k_D' = 2$ ,  $V_2 = k_D V_1$ , and  $W_T = 1$ . The isolated system corresponds to the “0” point on the horizontal axis. (D) Table summarizing the effect of load-induced modulation on bandwidth. Here,  $\omega_B$  denotes the bandwidth of the cycle, the superscripts denote “connected” (C) and “isolated” (I), and  $V$  is proportional to the amounts of enzymes.

of the input amplitude (Fig. 3C). Finally, in the system with single load, the decrease of bandwidth is more dramatic compared to the case in which  $\lambda = \alpha > 0$  (see Supplementary Materials, Model and Simulation, section 1.4).

### Insulation from loading by varying enzyme amounts

To understand whether a covalent modification cycle can operate under conditions that minimize the effects of loading and make the cycle effectively “insulated” from downstream targets, we examined the cycle behavior when the amounts of enzymes were changed. In particular, we examined the relative error  $\Delta = \frac{A^i(\omega) - A^c(\omega)}{A^i(\omega)}$  between the amplitudes of the connected and the isolated system responses as a measure of the extent of the effect of loading (Fig. 3D and fig. S3; Supplementary Materials, Model and Simulation, section 1.4.1). The model predicted that the effect of changing the amounts of the enzymes depended on whether the isolated system operated in the ultrasensitive or hyperbolic regime. Specifically, the model predicted that when the isolated system operated in the ultrasensitive regime, decreasing the amounts of enzymes would make the amplitudes of the isolated and connected systems approach each other, reducing the relative error (Fig. 3D and fig. S3). When the isolated system operated in the hyperbolic regime, decreasing the amounts of enzymes would make the amplitudes of the isolated and the connected systems become far apart from each other, increasing the relative error (Fig. 3D; see Supplementary Materials, Model and Simulation, section 1.4.1). Finally, when the load was applied to one side only, for inputs operating at sufficiently low values (the input mean value  $u_0$  is sufficiently small), decreasing the amounts of enzymes would make the amplitudes of the isolated and connected systems become farther apart from each other (see Supplementary Materials, Model and Simulation, section 1.4.1). These predictions and the results of the simulations are summarized in Fig. 3D, in which we have denoted  $V = V_1$  and  $V_2 = aV_1$ , for some positive constant  $a$ , and  $W_0$  is the equilibrium value corresponding to the input mean value  $u_0$ . In summary, the model predicted that if the isolated system operates in the ultrasensitive regime, an effective mechanism to attain dynamic insulation from loads would be to decrease the amount of the cycle enzymes; if the isolated system operates in hyperbolic regime or the load is applied to one side only, increasing the amounts of enzymes would be an effective mechanism to attain insulation.

### Detailed description of the experimental model system

The reconstituted UTase/UR–PII covalent modification cycle of *E. coli* was used in the experiments (Fig. 1B) (20). The UTase/UR enzyme catalyzes the uridylylation of the PII protein through its UTase activity and catalyzes the de-uridylylation of PII-UMP through its UR activity. These reactions are regulated by glutamine (Gln), an allosteric effector that binds to a sensory domain on the UTase/UR to inhibit the UTase activity and activate the UR activity. Reactions are also regulated by  $\alpha$ -ketoglutarate and adenylate energy charge, which are allosteric regulatory molecules that bind directly to PII and affect its ability to activate or inhibit its downstream targets (26, 27). We performed the experiments at a fixed  $\alpha$ -ketoglutarate concentration and at high adenosine triphosphate (ATP)/adenosine diphosphate (ADP) ratio so that the system responded to glutamine as its sole stimulatory effector, producing changes in PII uridylylation state in response to changes in glutamine (25). This system is analogous to covalent modification cycles involving phosphorylation and dephosphorylation. PII and PII-UMP interact with various downstream targets involved in nitrogen assimilation (28). Here, we studied the effect of one of the PII downstream targets, the NRII protein of *E. coli* (20), on the transient response of the UTase/UR–PII cycle to time-varying concentrations of glutamine. Use of a reconstituted system of purified proteins allowed us to examine conditions where NRII binding to PII provided a substantial load

on the system and allowed us to vary the levels of the UTase/UR more than two orders of magnitude to identify conditions that mitigate load-induced modulation. Hence, our results are likely to be relevant for other signaling systems, where downstream targets are found at high concentrations and substantial loading effects are anticipated [for example, (24, 29–31)].

The PII protein is a trimer; thus, its uridylylation state can vary from zero to three modifications per trimer (Fig. 1C). Hence, comparing the generalized model (Fig. 1A) with the details of the experimental model (Fig. 1B), W represents unmodified PII ( $P_0$  of Fig. 1B), and the modified protein W\* comprises all of the modified forms of PII ( $P_1$ ,  $P_2$ , and  $P_3$  of Fig. 1B). To study a circuit configuration where the load is applied to only one form of the protein (Fig. 1C), we used a mutated system (19) with a population of PII trimers, mostly heterotrimers, in which one of the three subunits is wild type and two of the three subunits contain a mutation that prevents their interaction with NRII or UTase/UR (Fig. 1C). This heterotrimeric form of PII, which we refer to as “monovalent PII,” is uridylylated and de-uridylylated by the UTase/UR in response to glutamine on its wild-type subunit, but its two mutant subunits neither bind to NRII nor are able to become modified (19).

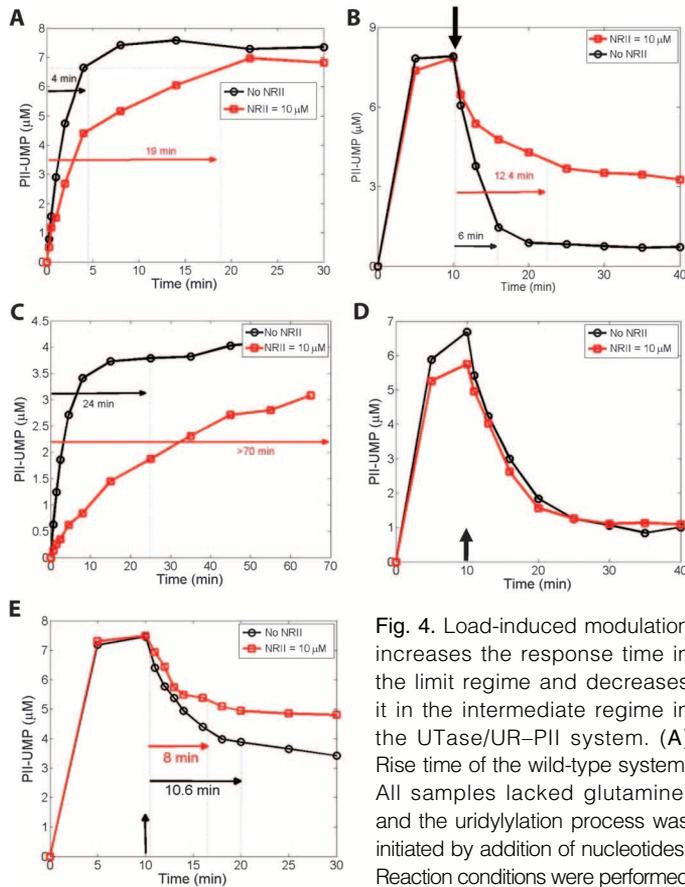
### The effect of load-induced modulation on rise and decay times in the UTase/UR–PII system

We analyzed the behavior of the system when operating in the limit regime. To examine the rise time, we incubated the UTase/UR and PII with all necessary reaction components except uridine triphosphate (UTP) (which contained [ $\alpha$ - $^{32}$ P]UTP to allow measurement of uridylylation), and at time zero in the experiment, we added UTP. To examine the decay time, we incubated the intact system, including UTP, in the absence of glutamine for sufficient time to allow it to reach the steady state corresponding to almost complete uridylylation of PII, after which we added glutamine to the saturating concentration of 10 mM. We performed these experiments for both the isolated (without NRII) and the connected (with NRII) systems, for systems with wild-type PII and monovalent PII. Recall that the rise was defined as the time it takes for the output to rise from 10 to 90% of its overall response, and the decay time is the time it takes for the output to decay from 90 to 10% of its overall response.

As expected from Eqs. 2 and 3, NRII increased both the rise time (Fig. 4A) and the decay time (Fig. 4B) for the double-load system containing wild-type PII (corresponding to Fig. 1B). The presence of load altered only the initial response; the final steady state was not affected. When monovalent PII was used in the single-load system (corresponding to Fig. 1C), NRII increased the rise time (Fig. 4C) but did not affect the decay time (Fig. 4D), as expected from Eqs. 2 and 3, with  $\alpha = 0$ . With the amount of NRII used in our experiments, the decay time doubled (going from 6 min in the isolated system to 12.4 min in the connected system; Fig. 4A), and the rise time increased by a factor of 4.75 (going from 4 min in the isolated system to 19 min in the connected system; Fig. 4B) in the system containing wild-type PII. In the system containing monovalent PII, the rise time was increased by a factor larger than 4, going from 24 min in the isolated system to more than 70 min in the connected system (Fig. 4C).

To measure the decay time upon intermediate stimulation representing the system operating in the intermediate regime, we allowed isolated and connected systems with wild-type PII to evolve in the absence of glutamine until the steady state had been obtained (corresponding to high uridylylation), after which we added glutamine to intermediate values (0.5, 0.8, and 1.5 mM). At 0.8 mM glutamine, the connected system displayed a decreased response time relative to that of the isolated system, because the decay time of the isolated system was 10.6 min, whereas that of the connected system was 8 min (Fig. 4E). That is, the connected system reached its minimum faster than the isolated system. This is consistent

with our theoretical analysis showing that the presence of load made the response faster (Supplementary Materials, Model and Simulation, section 1.3.2). In the parallel experiments where glutamine was 0.5 mM, no significant difference between the decay times of isolated and connected



**Fig. 4.** Load-induced modulation increases the response time in the limit regime and decreases it in the intermediate regime in the UTase/UR-P11 system. (A) Rise time of the wild-type system. All samples lacked glutamine, and the uridylylation process was initiated by addition of nucleotides. Reaction conditions were performed at 30°C with 3 μM P11, 0.025 μM

UTase/UR, 0.2 mM α-ketoglutarate, 1 mM [α-<sup>32</sup>P]UTP, 1 mM ATP, BSA (0.3 mg/ml), and ±10 μM NR11. P11-UMP was measured as previously described (25) (4 min and 19 min represent the rise times for the system without and with NR11, respectively). (B) Decay time for the wild-type system. After allowing the complete uridylylation of P11 in the absence of glutamine, a saturating concentration of glutamine (10 mM) was added at 10 min (down-pointing arrow). Reaction conditions were as in (A), except that UTase/UR was 1.5 μM. The decay times for the system without and with NR11 are 6 and 12.4 min, respectively. (C) Rise time of the system containing monovalent P11. Reaction conditions were as in (A) except that heterotrimeric P11 formed from a 1:6 ratio of wild-type to P11-Δ47-53 subunits was used, at a concentration of 2 μM wild-type subunits, and UTase/UR was 0.012 μM. For the isolated system, the rise time was 24 min. The connected system failed to reach the steady state after more than 70 min. (D) Decay time of system containing monovalent P11. Reaction conditions were as in (C), except that UTase/UR was 0.5 μM and glutamine was added to 10 mM at 10 min (up-pointing arrow). (E) Decay time of system operating in the intermediate regime with wild-type P11 and 0.8 mM glutamine (nonsaturating concentration) added at 10 min (up-pointing arrow). The decay times for the system with and without NR11 are 8 and 10.6 min, respectively. In all panels, black represents the isolated system (without NR11), and red, the connected system (with NR11).

systems could be discerned (fig. S5A), as expected (Supplementary Materials, Model and Simulation, section 1.3.2). When glutamine was 1.5 mM (fig. S5C), the connected system was also faster than the isolated system, but the difference appeared to be smaller than when glutamine was 0.8 mM (fig. S5B).

To measure the rise time upon intermediate stimulation, we included various concentrations of glutamine (0.5, 0.8, and 1.5 mM) in the reaction mixtures from the outset. Under these conditions, the steady-state uridylylation level corresponds to a lower concentration of uridylylated subunits than that obtained in the absence of glutamine. In contrast to the decay times, the rise times were slower in the connected system, and the difference between the connected and isolated systems became smaller as the glutamine concentration was increased (Table 1). We also examined the rise time of the system containing monovalent P11, in the presence of intermediate glutamine concentrations (0.4 and 0.6 mM); under both of these conditions, the difference between connected and isolated systems was larger than was the case in the absence of glutamine. Thus, in our experimental systems, the presence of load had asymmetrical effects at intermediate stimulation; it decreased the decay time but increased the rise time (Fig. 4E and Table 1).

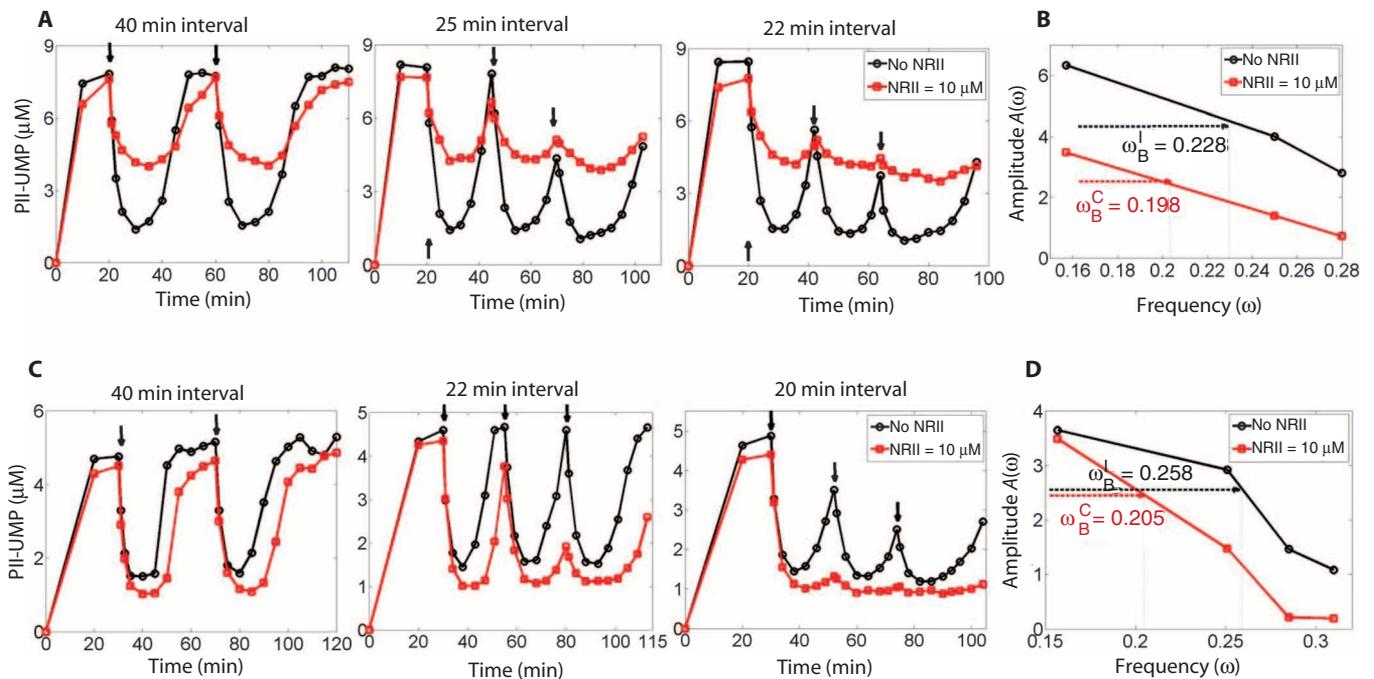
**The effect of load-induced modulation on the bandwidth of the UTase/UR-P11 system**

Experimentally determining system bandwidth requires a method for imposing a time-varying input stimulation on the system. In our experimental system, the stimulatory effector is the amino acid glutamine. To remove glutamine from the system, we included a purified glutaminase [pyridoxal phosphate synthase (PLPS) from *Geobacillus stearothermophilus*]. Periodic injection of glutamine in the presence of the glutaminase resulted in a sharp rise in the glutamine concentration upon injection, followed by an exponential decay of the glutamine concentration, similar to the output that may result from a relaxation-type oscillator. We varied the rate of decay of glutamine and amplitude of the response to glutamine injection by altering the concentration of the glutaminase in the system, varied the amplitude of input stimulation simply by injecting more glutamine (Supplementary Materials, Experimental Systems, section 2; fig. S6), and controlled the frequency of stimulation by injecting glutamine at the desired intervals.

The response of the reconstituted UTase/UR-P11 system to periodic changes in glutamine concentration in the presence or absence of NR11 showed that the presence of load affected both the amplitude and the bandwidth of the wild-type (Fig. 5, A and B) and the monovalent P11 (Fig. 5, C and D) systems. Amplitudes were estimated as described in the Supplementary Materials, Experimental Systems, section 2. In both

**Table 1.** Rise times for isolated (–NR11) and connected (+NR11) systems.

[Glutamine]	[UTase/UR] (μM)	Response time (–NR11) (min)	Response time (+NR11) (min)
Experiments with wild-type P11			
0 nM	0.025	4	15
0.3 mM	0.025	20	42
0.6 mM	0.025	61	70
0.9 mM	0.025	72	78
1.5 mM	0.025	72	80
Experiments with heterotrimeric P11			
0 nM	0.012	12	50
0.4 mM	0.025	40	72
0.6 mM	0.025	68	80



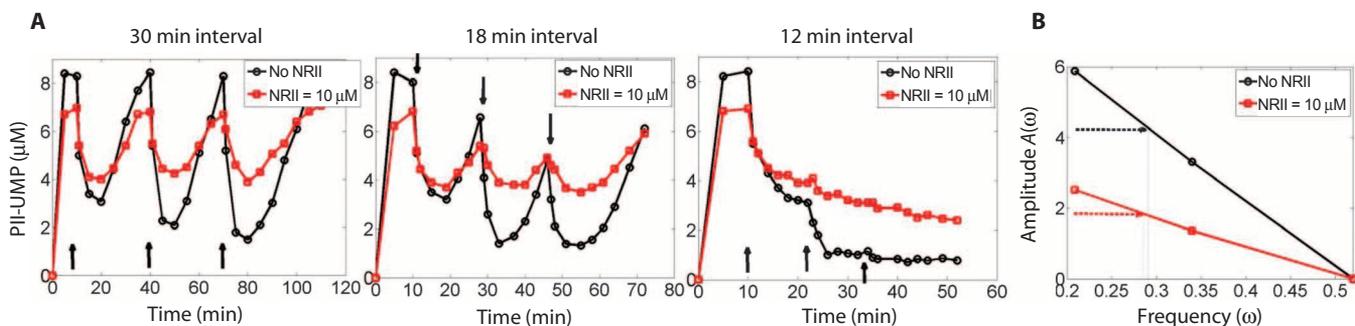
**Fig. 5.** Load-induced modulation decreases system bandwidth in the UTase/UR-PII system. **(A)** Performance of the UTase/UR-PII monocycle with periodic input stimulation of increasing frequency. The reaction mixtures contained 3  $\mu\text{M}$  PII, 1.5  $\mu\text{M}$  UTase, glutaminase consisting of 75  $\mu\text{M}$  PLPS (24-mer) and additional 15  $\mu\text{M}$  PdxT (to ensure saturation of PLPS with the T subunits), and 10  $\mu\text{M}$  NRII (red curves and points  $\square$ ), or with no NRII (black curves and points  $\circ$ ). At indicated times (shown by the arrows), glutamine was added to 5 mM. For the left graph, glutamine was added at 20 and 60 min; for the middle graph, at 20, 45, and 70 min; and for the right graph, at 20, 42, and 64 min. **(B)** Replot of the amplitude as a function of the frequency  $\omega$  of the input stimulation from the graphs in (A).

cases, the presence of NRII caused a decrease in the amplitude of the response and in the bandwidth (Fig. 5, B and D). With wild-type PII, the presence of load caused a 13.2% decrease in bandwidth (Fig. 5B). In the single-load system with monovalent PII, load caused a 21% decrease of bandwidth. Also, for the single load, the amplitudes of responses at low frequency are the same for the isolated and connected system, and they diverge only at higher frequencies (Fig. 5D). The amplitude of response at low frequency was similar for the isolated and connected systems, but as the frequency of stimulation increased, the connected system amplitude dropped much faster than that of the isolated system (Fig. 5D). For both systems (with wild-type and monovalent PII), we identified an input frequency where the isolated system demonstrated a substantial response, whereas the connected system essentially failed to respond (Fig. 5, A, right, and C, right). Thus, the presence of load decreased the bandwidth of the covalent modification cycle and the amplitude of response.

Some characteristics of the experimental system also affected the profile of the response to changes in stimulation frequency. When the frequency of the input stimulation (addition of glutamine) increased, the peaks of the response tended to monotonically decrease. This is likely due in part to the transient response of the system, which was not yet extinguished in the duration of the experiment. (Simply stated, by the time the second injection of glutamine was applied, the system was still re-

sponding to the first injection.) This effect is due to the lag between changes in the glutamine concentration and changes in the PII modification state being sufficiently large, such that the PII modification state never reached its steady state before the next addition of glutamine. Also, when the input frequency was at the highest tested (Fig. 5, A, right, and C, right), it is likely that glutamine was not completely removed by the glutaminase and accumulated so that eventually the trajectories saturated to their low values. Finally, slow decay in the rate of the glutaminase activity during the course of the experiments seems to have occurred, because we observed a slight widening of each peak as the experiments progressed.

Theory predicted that for a fixed amount of load, decreasing input amplitude would decrease the difference between the isolated and the connected system bandwidths (Fig. 3, A and B). To study this, we performed experiments where a lower (nonsaturating) amount of glutamine was added with each injection. Figure 6 shows the responses to inputs at different injection frequencies, where each injection raised the glutamine concentration by 1.5 mM (as opposed to each injection raising the glutamine concentration by 5 mM, as in Fig. 5). Glutamine at 1.5 mM is well within the range that the system can sense (32), and a low concentration of glutaminase was used in the experiments, such that the rate of decay of glutamine was reduced compared to the experiments of Fig. 5. Unlike the experimental results obtained when a saturating concentration of glutamine was the



**Fig. 6.** Isolated and connected systems exhibit the same bandwidth under conditions of low-amplitude stimulation. **(A)** The UTase/UR–PII wild-type monocyte response to periodic input stimulation with increasing frequency for the isolated (black curves and points  $\circ$ ) and connected (red curves and points  $\square$ ) system with  $10\ \mu\text{M}$  NRII. The reaction conditions were the same as in Fig. 5A, except that pyridoxal phosphate syn-

input, none of the frequencies tested with this lower concentration of glutamine as the input resulted in a condition in which the isolated system responded and the connected system did not (compare Fig. 5C, right, where the injections were every 22 min, with Fig. 6, middle, where the injections were every 18 min). The bandwidths of the isolated and connected systems were similar (Fig. 6B), confirming the theoretical predictions. In our experiments, there is a limit to the frequency at which one can add glutamine, which is related to the concentration of glutamine added and the decay rate (glutaminase level). When the decay rate is very slow and the frequency of addition is high, glutamine will not be completely degraded after each pulse and will build up in the system. The accumulation of glutamine will result in lower amounts of PII uridylation, as appeared to have occurred at the highest frequency of  $1.5\ \text{mM}$  glutamine addition (Fig. 6, right).

### Insulation from load-induced modulation by varying the amounts of the cycle enzymes

The UTase/UR enzyme has both uridylyltransferase- and uridylyl-removing activities, so the activities of both cycle enzymes can be simultaneously altered by performing experiments with different concentrations of UTase/UR. We performed experiments with the double-load system containing wild-type PII and the single-load system containing monovalent PII similar to those presented in Fig. 5, except with different amounts of UTase/UR. In the system with wild-type PII, decreasing the enzyme amounts decreased the difference between the output amplitudes of the isolated and connected systems (Fig. 7, A and B). The opposite pattern was observed when the system with monovalent PII was examined; increasing the amounts of enzyme made the amplitudes of the connected and isolated systems closer to each other (Fig. 7, C and D). The plots of the amplitudes as a function of the enzyme amounts (Fig. 7, B and D) include data from Fig. 5 with the same stimulation frequency at high enzyme concentration. This opposite effect of cycle enzyme concentration on the amplitudes of double load or single load connected compared to the amplitudes of the isolated systems is consistent with our theoretical predictions (Fig. 3D).

## DISCUSSION

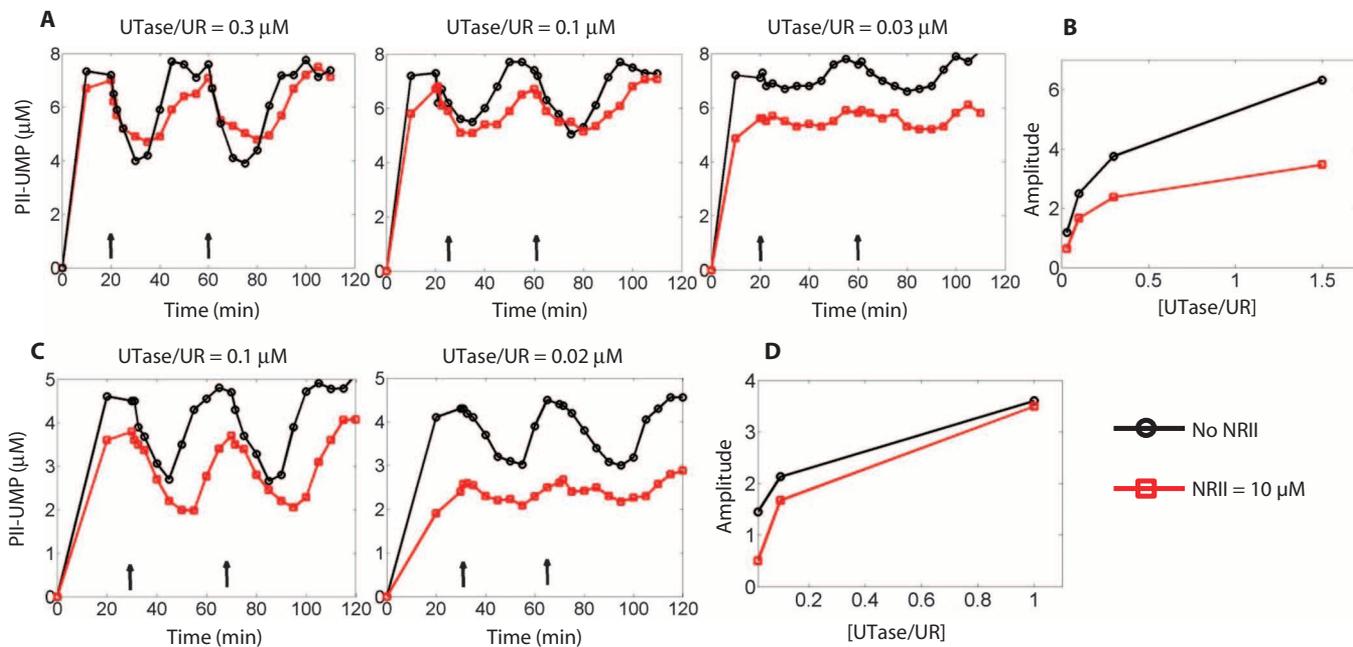
We illustrated through theory and experiments how the presence of load affects the dynamics of a covalent modification cycle, a common compo-

nent of signaling networks. Specifically, we found that load-induced modulation controls the defining characteristics of dynamic behavior, response time, and bandwidth, in non-intuitive ways. Our methodology is based on comparing the step and frequency responses of a signaling component in an isolated system lacking any load to the same responses when the signaling component is connected to its downstream targets that function as load, which allowed us to capture the interaction between individual network modules and determine the emergent network behavior. We used as the experimental system a reconstituted covalent modification cycle of *E. coli*, which was used under conditions (amounts of substrate proteins, enzymes, and load targets) that are relevant for native signaling cascades. Hence, the effects that we report are expected to be observed in many signaling systems *in vivo*.

The frequency response determines a system's ability to respond to physiologically relevant signals with high amplitude and low frequency, while filtering out high-frequency, low-amplitude input signals that are not physiologically relevant (noise) (33). We found that the presence of downstream targets reduced the bandwidth of the system, thus altering the system's responsiveness by making it more limited than it would be in the absence of targets (Fig. 5). One potential application of this phenomenon that load-induced modulation can quench responses to time-varying stimulation is the development of small molecules as therapeutic loads that diminish aberrant signaling occurring in various disease states (9).

Evolution or human engineering of complex signaling networks may be facilitated by conditions that minimize load-induced modulation, because this would ensure modular behavior of the network. We showed that the amounts of the converting enzymes in a signaling system control the extent of the dynamic effects of load molecules and that dynamic insulation from these loads may be obtained by changing the amounts of cycle enzymes. This finding suggests a possible mechanism for attaining insulation from load molecules and hence for engineering insulation devices in synthetic biology (10, 34). Of course, when engineering signaling systems, the presence of explicit negative feedbacks in signaling networks enhances robustness to downstream perturbations and hence also enables unidirectional signal propagation (13).

Load-induced modulation may be beneficial, providing an additional mechanism to tune the dynamic behavior of a system. For example, tuning the bandwidth of a system may be advantageous for increasing robustness to noise or for reducing crosstalk between pathways sharing common components (35).



**Fig. 7.** Changing the enzyme amount affects the effect of load on the UTase/UR–PII system. **(A)** The double-load UTase/UR–PII wild-type system under periodic input stimulation with decreasing UTase amounts, with 10  $\mu\text{M}$  NRII ( $\square$  red points and curves) or with no NRII ( $\circ$  black points and curves). The reaction conditions were the same as in Fig. 5A, except that the UTase amount was varied. For the left graph, UTase was 0.3  $\mu\text{M}$ ; for the middle graph, UTase was 0.1  $\mu\text{M}$ ; and for the right graph, UTase

was 0.03  $\mu\text{M}$ . **(B)** Replot of amplitude as a function of UTase amounts from the graphs in (A) and from Fig. 5A (left). **(C)** The single-load UTase/UR–PII system with monovalent PII. The reaction conditions were the same as that of Fig. 5C, except that the UTase amount was varied. For the left graph, UTase was 0.1  $\mu\text{M}$ , and for the right graph, UTase was 0.02  $\mu\text{M}$ . **(D)** Replot of amplitude as a function of UTase amounts from graphs in (C) and from Fig. 5C (left).

Our study provided a mathematical and experimental basis for understanding how signaling modules and downstream targets are linked, due to load-induced modulation of signaling dynamics. This load-induced modulation of signaling properties has direct repercussions on emergent network behavior and, ultimately, on physiology.

## MATERIALS AND METHODS

### Model and simulation

Details of the model and derivations are described in the Supplementary Materials, Model and Simulation. Simulations were performed with MATLAB 7.11 and Simulink. Models are available as Simulink files.

### Purified proteins

PII, UTase/UR, and NRII were prepared as described (25). Heterotrimeric monovalent PII was prepared as described (19). Briefly, we formed heterotrimeric PII by gently dissociating the subunits of wild-type and  $\Delta 47$ -53 mutant PII trimers, mixing at a ratio of six mutant subunits per wild-type subunit, and then allowing the subunits to reassociate. Under these conditions, most wild-type subunits become incorporated into trimers with two mutant subunits. For a glutaminase enzyme, we used PLPS from the thermophile *G. stearothermophilus*, which was purified as described (36). This glutaminase has a low  $K_m$  of  $\sim 0.5$  mM glutamine, can be produced at high concentration, has suitable activity, and apparently does not interfere with our reconstituted systems.

### UTase/UR–PII monocycle dynamic experiments

The reaction mixture contained 100 mM tris-Cl (pH 7.5), 10 mM  $\text{MgCl}_2$ , 100 mM KCl, bovine serum albumin (BSA; 0.3 mg/ml), 0.2 mM  $\alpha$ -ketoglutarate, 1 mM ATP, 2 mM [ $\alpha$ - $^{32}\text{P}$ ]UTP or as indicated, 3  $\mu\text{M}$  PII (homotrimers), UTase/UR as indicated, NRII as indicated, and PLPS (24-meric complex, concentration stated as the concentration of each of the two types of subunits) as indicated. The reactions were performed at 30°C and were initiated by addition of a mixture of the nucleotides (UTP and ATP). After incubation for 10 to 30 min, glutamine was added to 5 mM (or as indicated). Aliquots were taken at time intervals and spotted onto P81 cellulose-phosphate filters (Whatman) and washed extensively in 5% trichloroacetic acid. The incorporation of radioactive label into PII was quantified by liquid scintillation counting. For dynamic experiments with monovalent PII, the reaction conditions and procedure were the same except wild-type PII was substituted by 2  $\mu\text{M}$  heterotrimeric PII mixture, which was formed from a sixfold excess of  $\Delta 47$ -53 subunits over wild-type subunits (25). Figure S7 shows experiments testing the effect of applying the first injection of glutamine before the system had reached its steady state.

### SUPPLEMENTARY MATERIALS

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Text

Fig. S1. Steady-state effects of loading.

Fig. S2. Effect of loading on the frequency response.

Fig. S3. Effects of enzyme amounts.

Fig. S4. Effect of the load on the amplitude of response to a train of pulses.

Fig. S5. Response of the UTase/UR–PII cycle to stimulation with nonsaturating concentrations of glutamine.

Fig. S6. Using glutaminase and injections of glutamine to impose time-varying input stimulation.

Fig. S7. Amplitude of the initial response to glutamine addition depends on whether or not the system has achieved a steady state before glutamine addition.

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SimulinkModel (.mdl file)

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