### 18.01A Problem Set 3

(due Thurs., Oct. 11 )
Due after the exam, but do the problems for classes 10-12 to help study for the exam.
Part I (25 points)
$\mathrm{TB}=$ Simmons; $\mathrm{SN}=18.01 \mathrm{~A}$ Supplementary Notes (all have solutions) The problems marked 'other' are not to be handed in.

Class 10 (Thurs., Sep. 27 pset 2 due) Integration by parts, numerical integration.
Read: TB: 10.7, 10.9.
Hand in: 5F/1a, 2bd, 3; 3G/1ad, 3, 4
Others: $5 \mathrm{~F} / 6 ; 3 \mathrm{G} / 1 \mathrm{~b}$
Class 11 (Mon., Oct. 1) Improper integrals.
Read: TB: 12.4, SN: INT
Hand in: $6 \mathrm{~B} / 1,2,4,7 \mathrm{adfp}$ (for p think about $x=\pi / 2$ ), 8 a .
Others: $6 \mathrm{~B} / 7 \mathrm{~km}, 8 \mathrm{a}$.
Class 12 (Tues., Oct. 2) Infinite series, harmonic series convergence tests.
Read: TB: 13.1 and 13.2 quickly, 13.3 to top p.442, 13.5 to p. $453,13.6$ to p. 457
Hand in: 6C/1ad, 3a; 7A/1a; 7B/1abd, 2cef.
Others: 7A/1bc; 7B/1f, 2ad.
Continuation: (Wed., Oct. 3) Discussion, review and catch up.
Exam: (Thurs., Oct. 4) Exam 2 (covers 8-12)
Class 13 (Wed., Oct. 10) Geometric series, power series, ratio test.
Read: TB: 13.7 to middle p.463, 13.8, 14.2
Class 14 (Thurs., Oct. 11 pset 3 due) Introduction to probability, discrete random variables.

Read: SN: P section 1

## Part II (24 points)

Directions: Try each problem alone for 20 minutes. If, after this, you collaborate, you must write up your solutions independently.

Problem 1 (Class 11, 2 pts)
Textbook 10.7/26.
Problem 2 (Class 11, 3 pts )
Let $R$ be the region below the graph of $\frac{1}{x^{p}}$ and above the interval $1 \leq x<\infty$ on the $x$-axis. For which values of $p>0$ is the area of $R$ finite, but the volume of revolution of $R$ about the $y$-axis infinite?

Problem 3 (Class 11, 3 pts )
Show that $\int_{0}^{\infty} \frac{1}{1+x^{6}} d x<\frac{6}{5}$. (Hint: break the integral into two pieces.)
Problem 4 (Part a-class 12, part b-class 13, 4 pts: 2,2)
a) Textbook p. 4609 b $\quad$ b) Textbook p. 4444

Problem 5 (Class 14, 12 pts: 2,2,2,2,2,2)
Notes 8A/1,3,4,6,7,8

