### 18.01A Problem Set 4

(due Wed., Oct. 17 )

## Part I (15 points)

$\mathrm{TB}=$ Simmons; $\mathrm{SN}=18.01 \mathrm{~A}$ Supplementary Notes (all have solutions) The problems marked 'other' are not to be handed in.

Class 14 (Thurs., Oct. 11 pset 3 due) Intro. to probability, discrete random variables. Read: SN: P section 1
Hand in: $8 \mathrm{~A} / 1,3,4,6,7,8$
Others:
Class 15 (Mon., Oct. 15) Continuous random variables, standard deviation.
Read: SN: P sections 2,3
Hand in: 8B/2, 3,$5 ; 8 \mathrm{C} / 1$
Others: 8B/1, 4
Class 16 (Tues., Oct. 16) Normal distributions.
Read: SN: P section 4
Hand in: 8D/1bd, 2, 3
Others: 8D/1ac, 4
Continuation: (Wed., Oct. 17) Discussion, review and catch up. pset 4 due
Exam: (Thurs., Oct. 18) Exam 3 (covers 12-16)

## Part II (21 points)

Directions: Try each problem alone for 20 minutes. If, after this, you collaborate, you must write up your solutions independently.

Problem $0 \quad$ (Class 13, 4 pts: 2,2)
a) Work $473 / 28$ b) Work $494 / 3$ a.

Problem 1 (Class 15, 4 pts: 2,2)
a) Work $8 \mathrm{C} / 2 \mathrm{a}(E(X)$ only $)$ b) Work $8 \mathrm{C} / 2 \mathrm{~b}$ ( $\sigma$ only).

Problem 2 (Class 16, 5 pts: 3,2)
a) Work $8 \mathrm{D} / 5$. b) Work $8 \mathrm{D} / 7$.

Problem 3 (Class 16, 8 pts: 2,2,2,2) Let $f(x)=C \frac{1}{\left(1+x^{2}\right)^{2}}$.
a) Find the value of $C$ so that $f(x)$ is a probability density function on the whole $x$-axis.
b) Using this value of $C$, find its mean and standard deviation.
c) Sketch the graph of $f(x)$.
d) For what values of the parameter $k$ will there be a probability density function on the entire $x$-axis of the form $g(x)=C \frac{1}{\left(1+x^{2}\right)^{k}} ?$
For what values of $k$ will it have a finite standard deviation?

