Probing the low-x structure of nuclear matter with diffractive hadron production

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in collaboration with Yang Li





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Outline

Motivation: low-x is a novel exciting regime of QCD:

- decay of CGC ↔ quantum tunneling, QGP formation, Early Universe etc.

Evidence for gluon saturation in ep DIS (diffraction, geometric scaling etc.) and in pA and AA at RHIC (inclusive processes).

There are many open questions about the dynamics in transition regions, validity of the mean-field approximation, NLO effects etc. NEED MORE QUANTITATIVE STUDY!

Study of diffractive hadron production at EIC can provide important insights

Diffraction

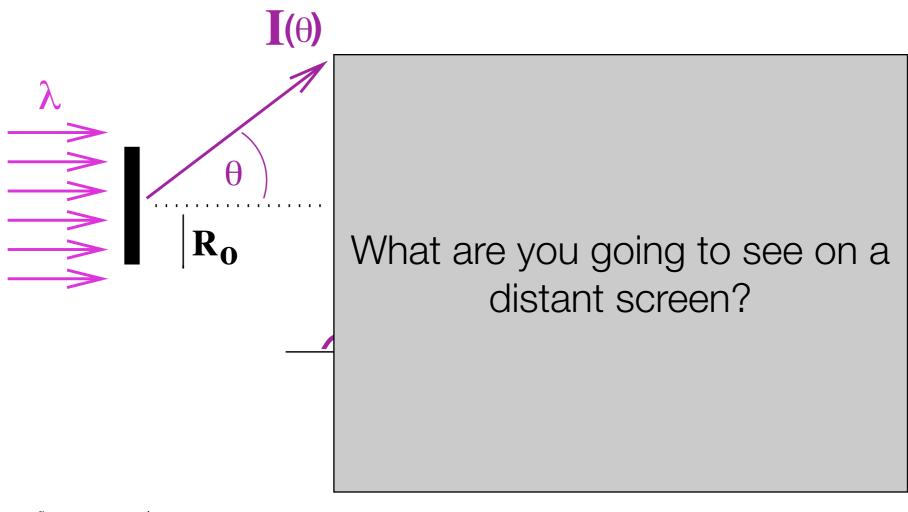


fig. courtesy by Arneodo and Diehl

Diffraction

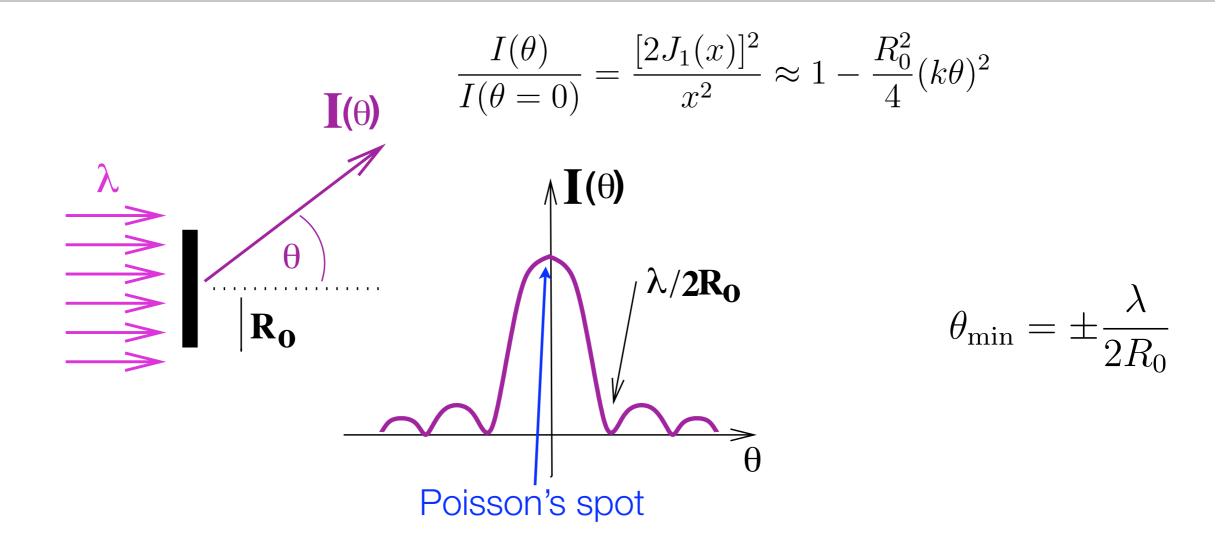


fig. courtesy by Arneodo and Diehl

Diffraction: light is a wave! (1818)





Fresnel Poisson

Diffraction: light is a wave! (1818)



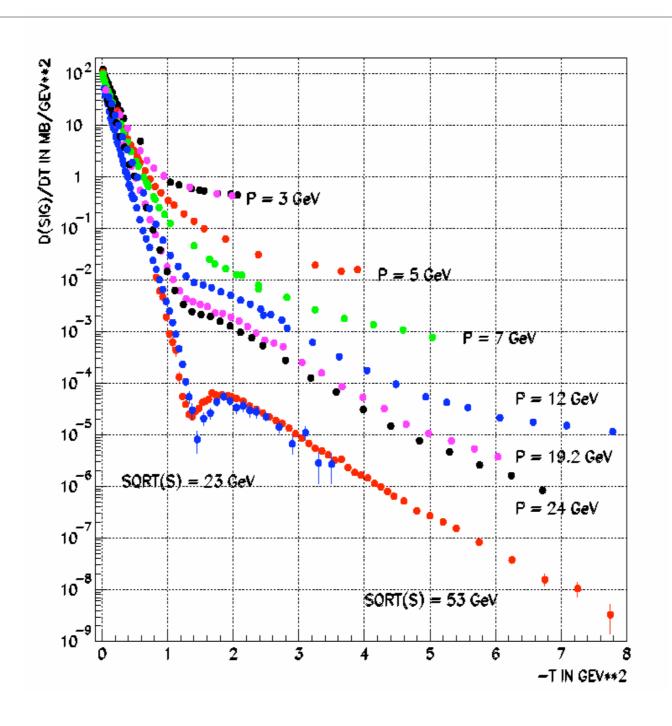
Fresnel



Poisson

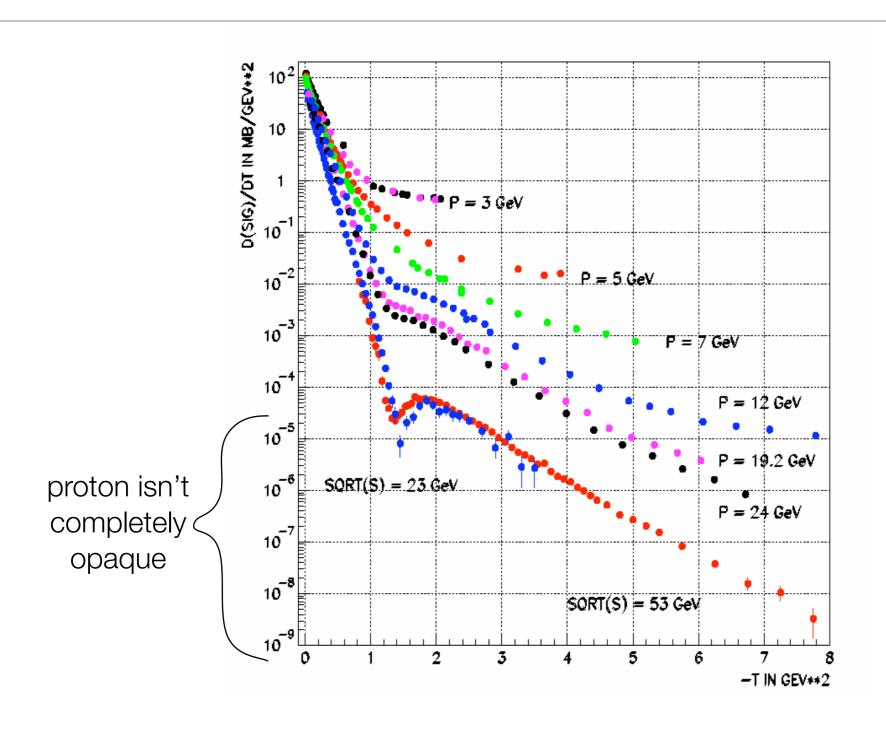
Arago experiment

Diffraction in pp collisions



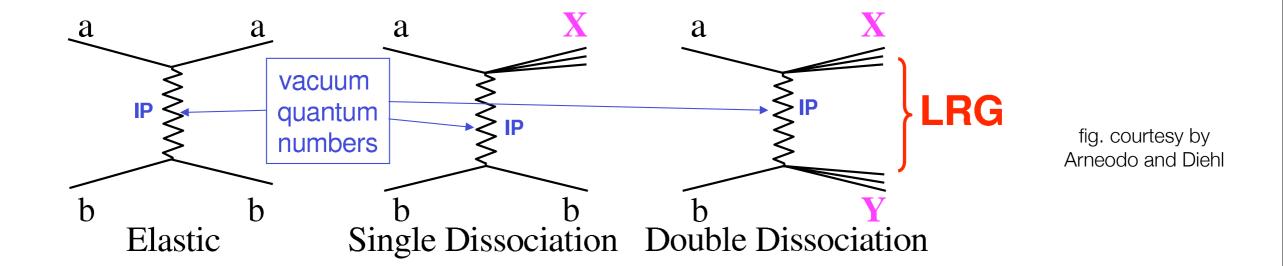
Elastic pp scattering

Diffraction in pp collisions

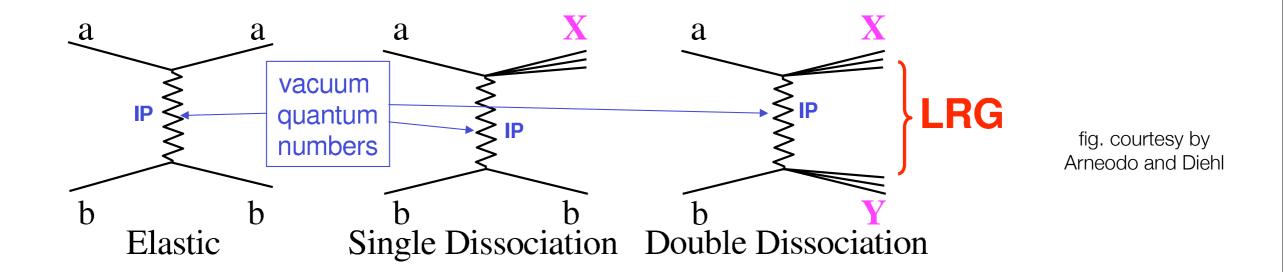


Elastic pp scattering

Diffraction in particle physics

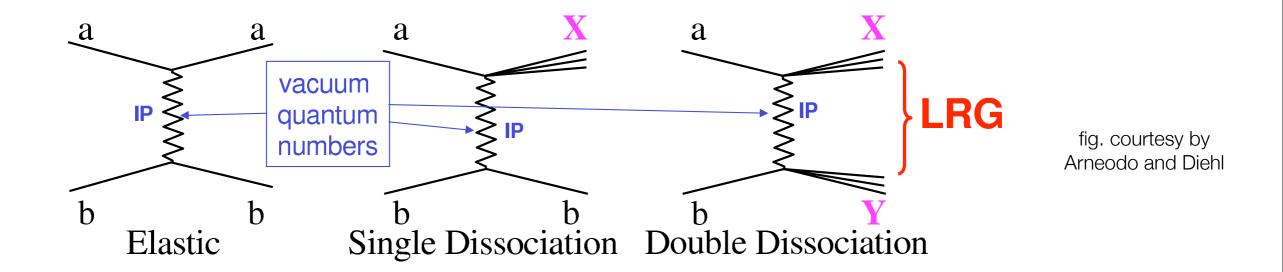


Diffraction in particle physics



Pomerantchuk theorem: in any process $a+b \to X$ t-channel state must have vacuum quantum numbers at $s \to \infty$.

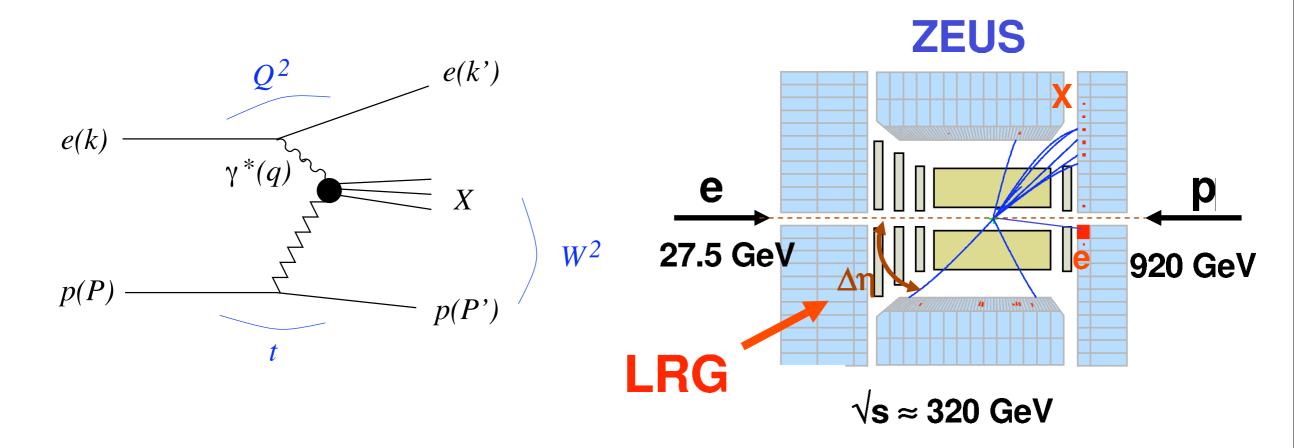
Diffraction in particle physics



Pomerantchuk theorem: in any process $a+b \rightarrow X$ t-channel state must have vacuum quantum numbers at $s\rightarrow\infty$.

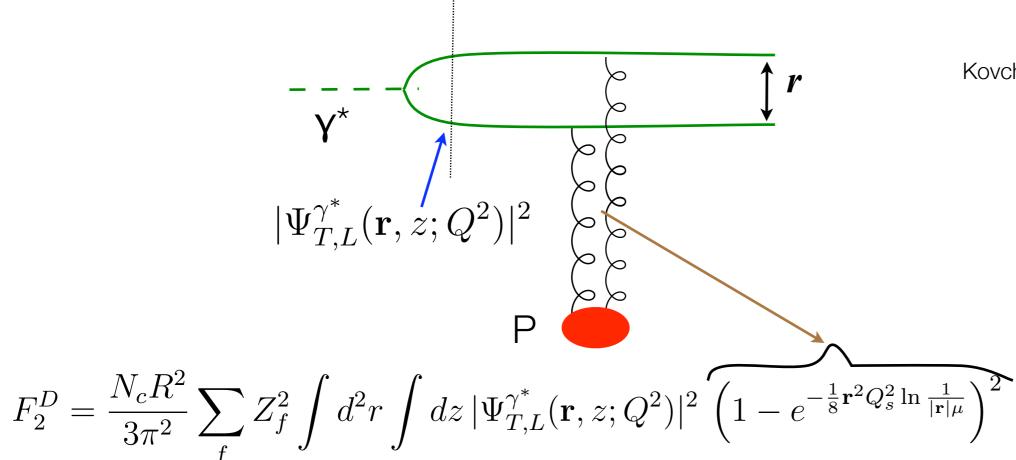
⇒ Diffraction directly probes the high energy asymptotic.

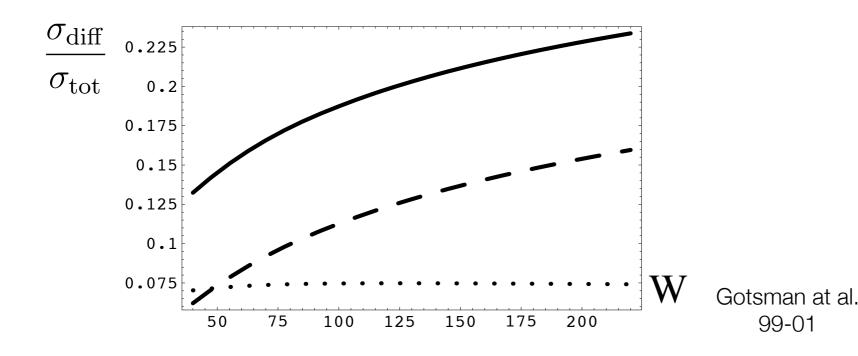
Diffraction at HERA

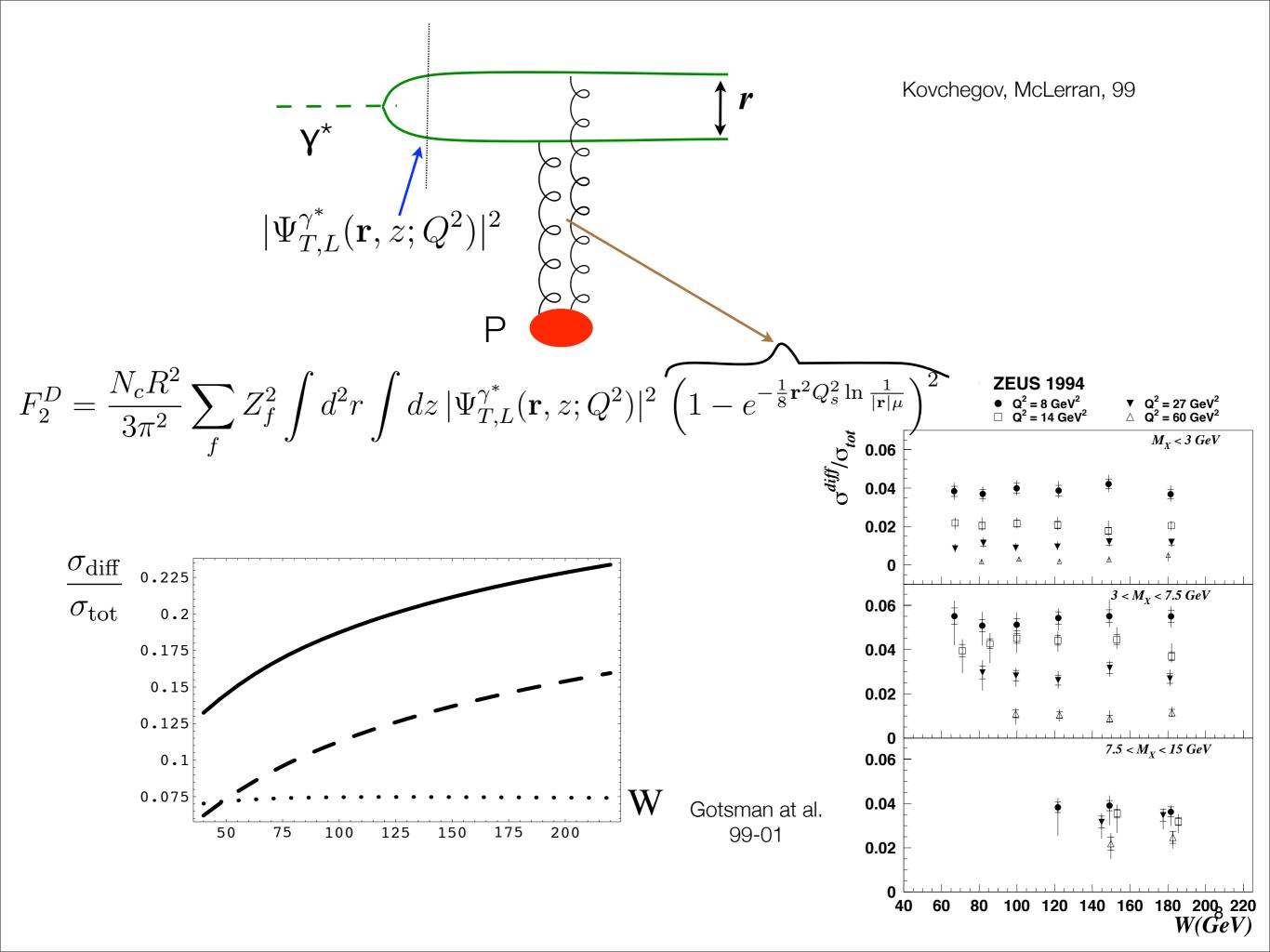


Unlike in pp, in DIS at $|t| >> \Lambda^2$ diffractive cross section can be calculated in pQCD

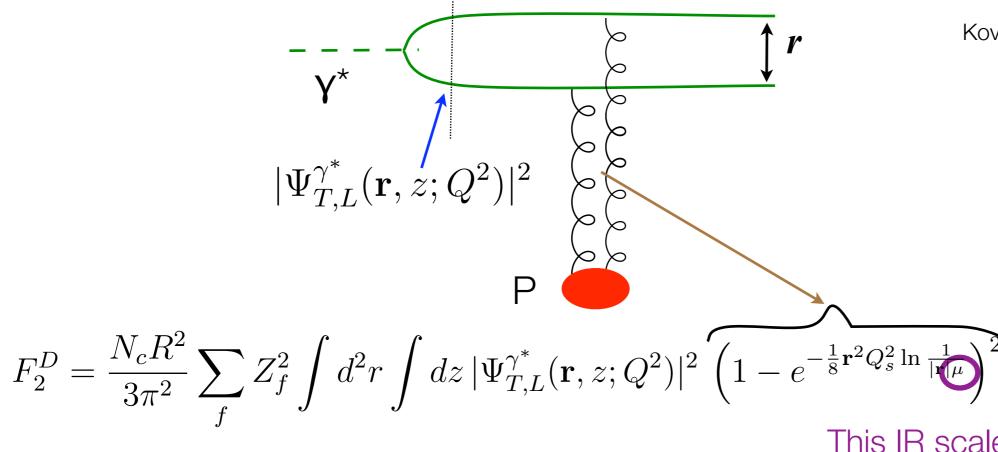
At low x $Q_s >> \Lambda$, so that even for small Q^2 : $\alpha_s(Q_s) << 1$.





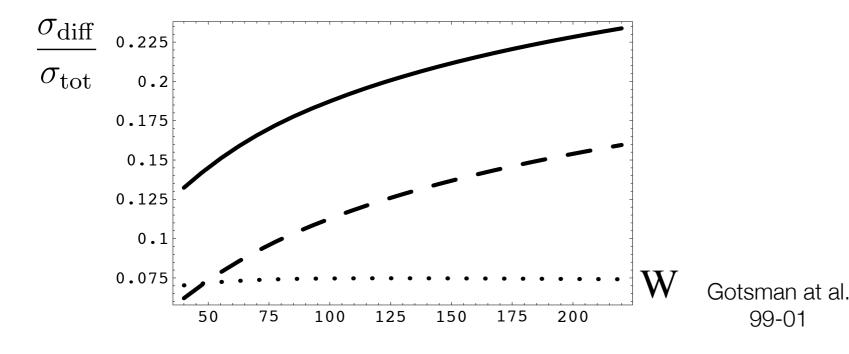


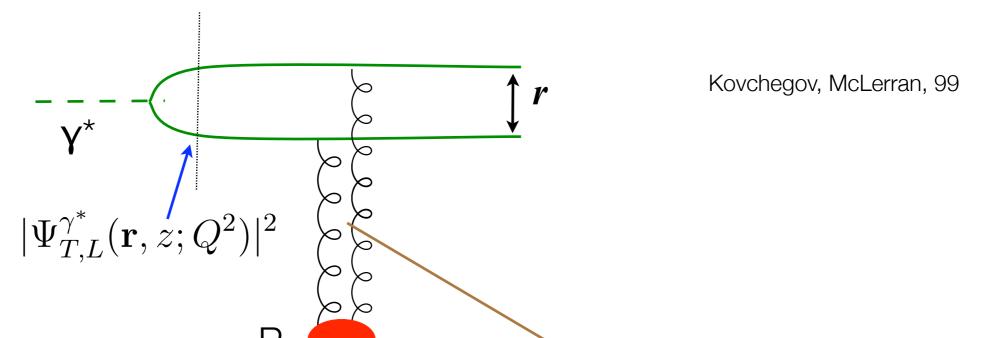




This IR scale breaks the geometric scaling

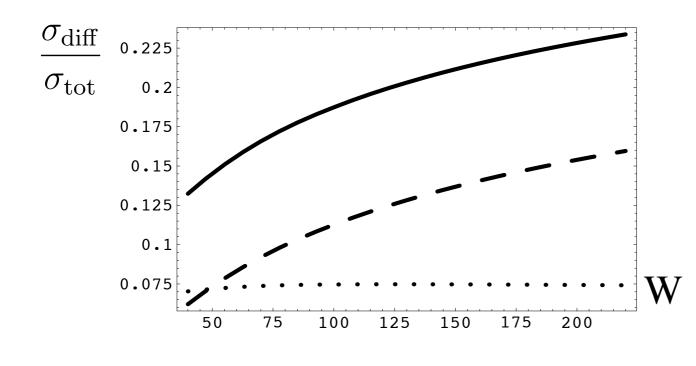
99-01





$$F_2^D = \frac{N_c R^2}{3\pi^2} \sum_f Z_f^2 \int d^2r \int dz \, |\Psi_{T,L}^{\gamma^*}(\mathbf{r}, z; Q^2)|^2 \left(1 - e^{-\frac{1}{8}\mathbf{r}^2 Q_s^2 \ln \frac{1}{|\mathbf{r}|}}\right)^2$$

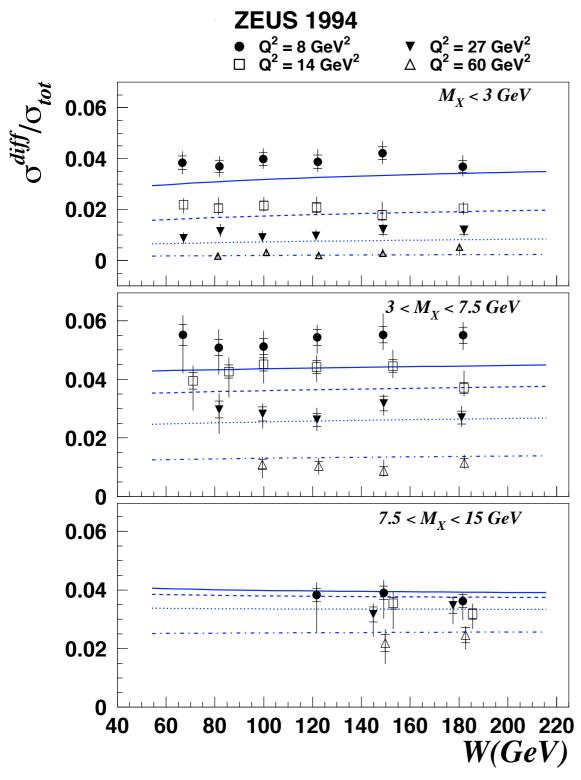
This IR scale breaks the geometric scaling



Low-x evolution removes dependence on the IR scale

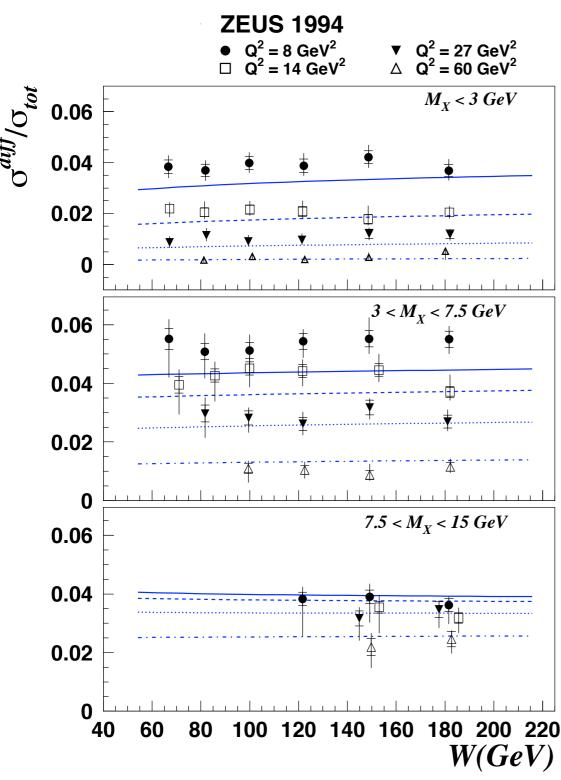
Gotsman at al. 99-01

Nonlinear evolution: Geometric Scaling

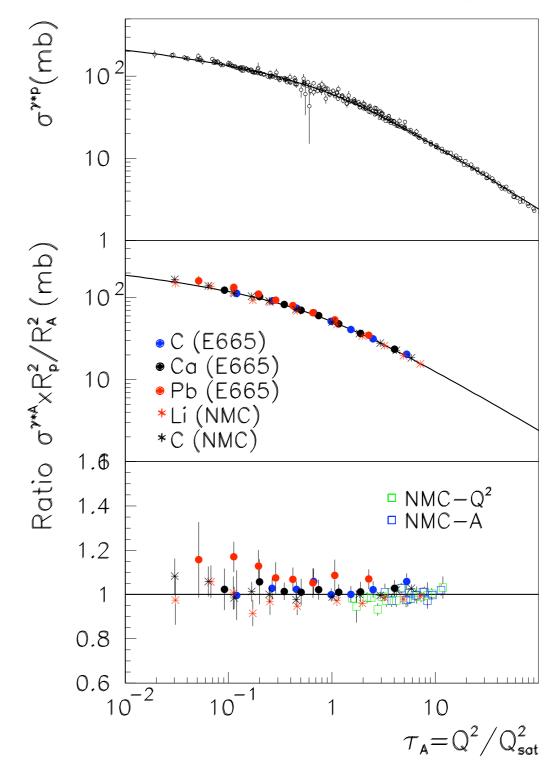


Golec-Biernat-Wusthoff, 99

Nonlinear evolution: Geometric Scaling

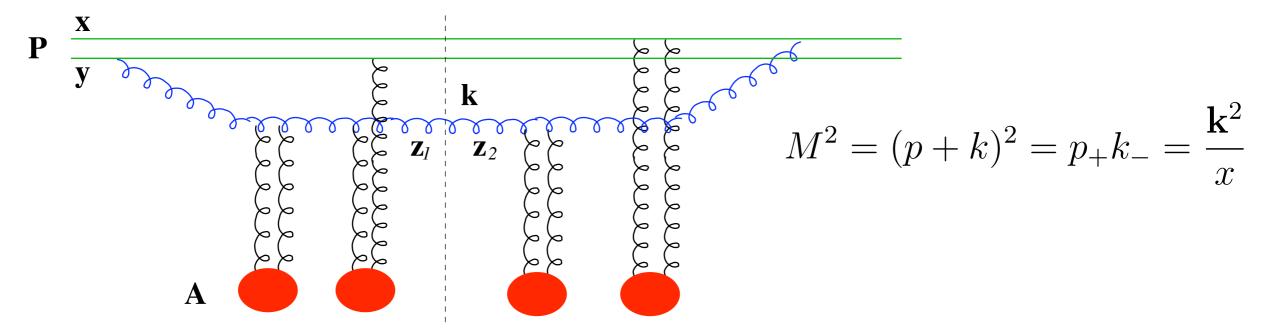


Golec-Biernat-Wusthoff, 99



Stasto, Golec-Biernat, Kwiecinski, 00 Armesto, Salgado, Wiedemann, 04

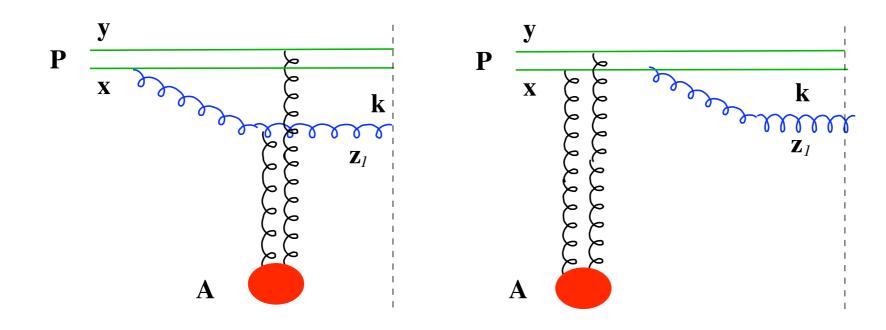
Simple model: onium-nucleus collisions



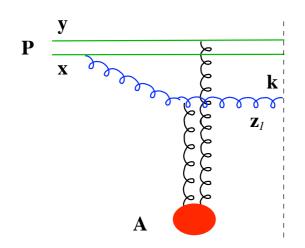
Coherent scattering if
$$l_c \approx \frac{1}{2m_N x} \gg R_A$$
 R_{Au} = 6.5 fm = 32 GeV⁻¹ x<<0.016

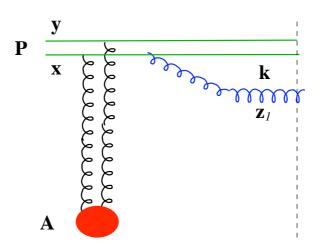
⇒ interaction is instantaneous

Two possible topologies:



All gluon attachments to the onium must be summed up.





qq propagator (Glauber-Mueller formula): $e^{-\frac{C_F}{4N_c}(\mathbf{x}-\mathbf{y})^2Q_{s0}^2}$ Mueller, 90

$$\text{qqg propagator: } \exp\{-P(\mathbf{x},\mathbf{y},\mathbf{z})\} = \exp\left(-\frac{1}{8}(\mathbf{x}-\mathbf{z})^2Q_{s0}^2 - \frac{1}{8}(\mathbf{y}-\mathbf{z})^2Q_{s0}^2 + \frac{1}{8N_c^2}(\mathbf{x}-\mathbf{y})^2Q_{s0}^2\right) \; .$$

Kopeliovich, Tarasov, Schafer,99

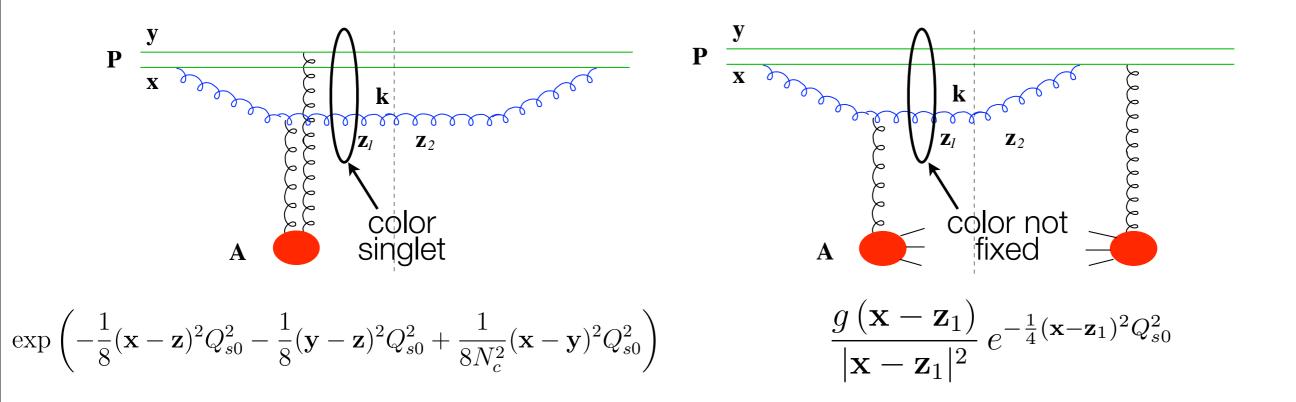
'initial' *gluon* saturation scale $Q_{s0}^2 = \frac{4\pi^2\alpha_sN_c}{N_c^2-1}\,\rho\,T(\mathbf{b})\,xG(x,1/\mathbf{r}^2)$

$$\frac{d\sigma(k,y)}{d^2k\,dy} = \frac{\alpha_s C_F}{\pi^2} \frac{1}{(2\pi)^2} \int d^2b\,d^2z_1\,d^2z_2 \left(\frac{\mathbf{z}_1 - \mathbf{x}}{|\mathbf{z}_1 - \mathbf{x}|^2} - \frac{\mathbf{z}_1 - \mathbf{y}}{|\mathbf{z}_1 - \mathbf{y}|^2}\right) \cdot \left(\frac{\mathbf{z}_2 - \mathbf{x}}{|\mathbf{z}_2 - \mathbf{x}|^2} - \frac{\mathbf{z}_2 - \mathbf{y}}{|\mathbf{z}_2 - \mathbf{y}|^2}\right)$$

$$\times e^{-i\mathbf{k}\cdot(\mathbf{z}_1 - \mathbf{z}_2)} \left(e^{-P(\mathbf{x},\mathbf{y},\mathbf{z}_1)} - e^{-\frac{C_F}{4N_c}(\mathbf{x} - \mathbf{y})^2 Q_{s0}^2}\right) \left(e^{-P(\mathbf{x},\mathbf{y},\mathbf{z}_2)} - e^{-\frac{C_F}{4N_c}(\mathbf{x} - \mathbf{y})^2 Q_{s0}^2}\right)$$

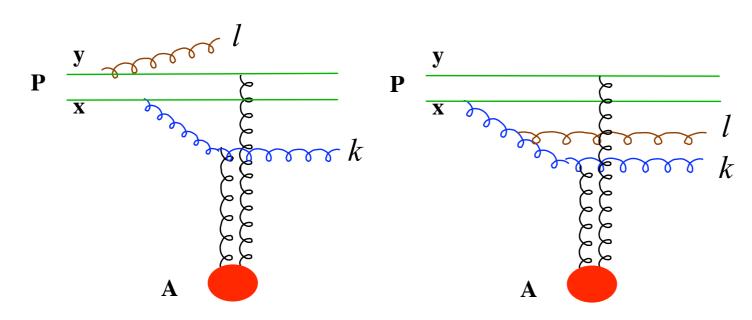
If log is dropped these integrals can be done.

Diffractive vs Inclusive gluon production



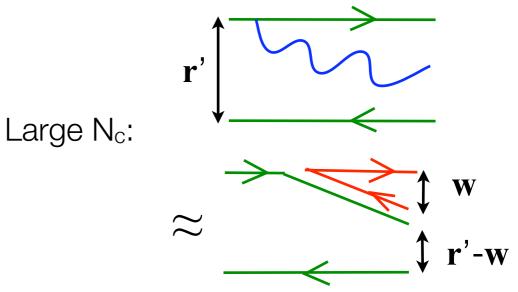
Unlike the inclusive gluon production, the diffractive one vanishes when the onium size $\mathbf{r}=\mathbf{x}-\mathbf{y}$ larger than 1/Qs.

Including small-x corrections



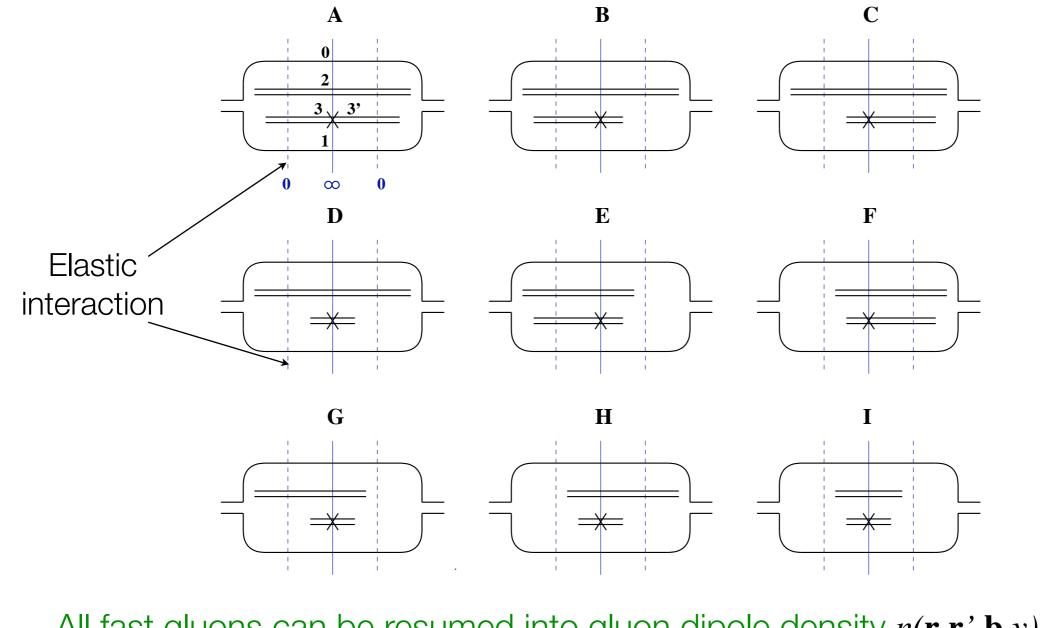
There are two cases:

- (1) Fast gluons $l_+>>k_+$ and
- (2) Slow gluons $k_+>>l_+$



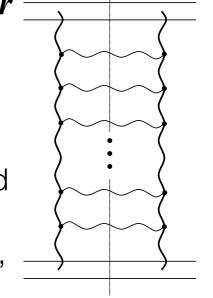
Fast gluons $l_+>>k_+$

Only diagrams contributing in the LLA are shown



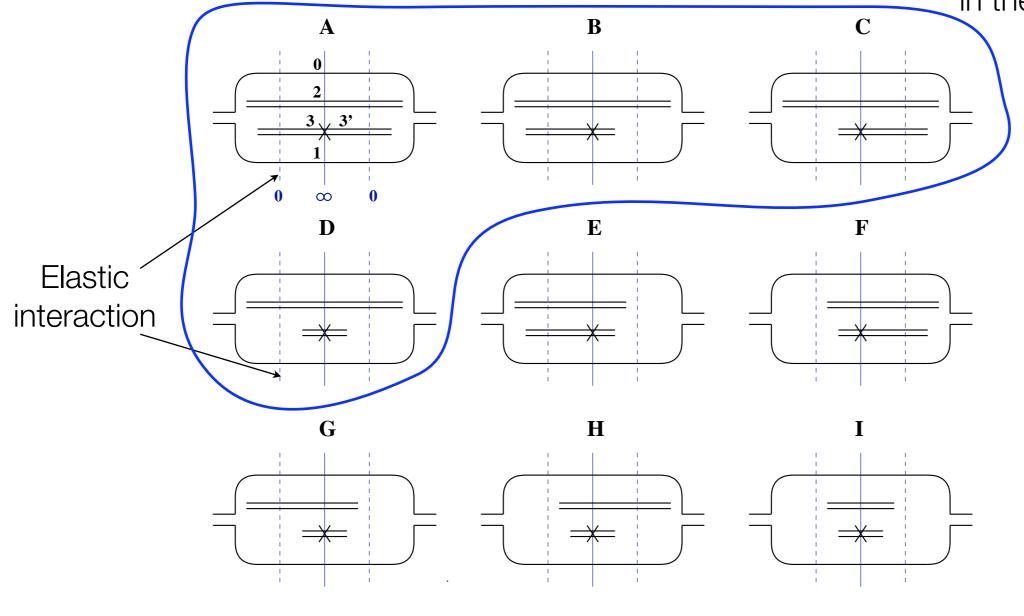
All fast gluons can be resumed into gluon dipole density $n(\mathbf{r},\mathbf{r}',\mathbf{b},y)$

This corresponds to the Pomeron hanging out from the incoming dipole \emph{r} and connecting with the emitting dipole \emph{r}'



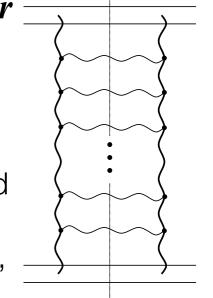
Fast gluons $l_+>>k_+$

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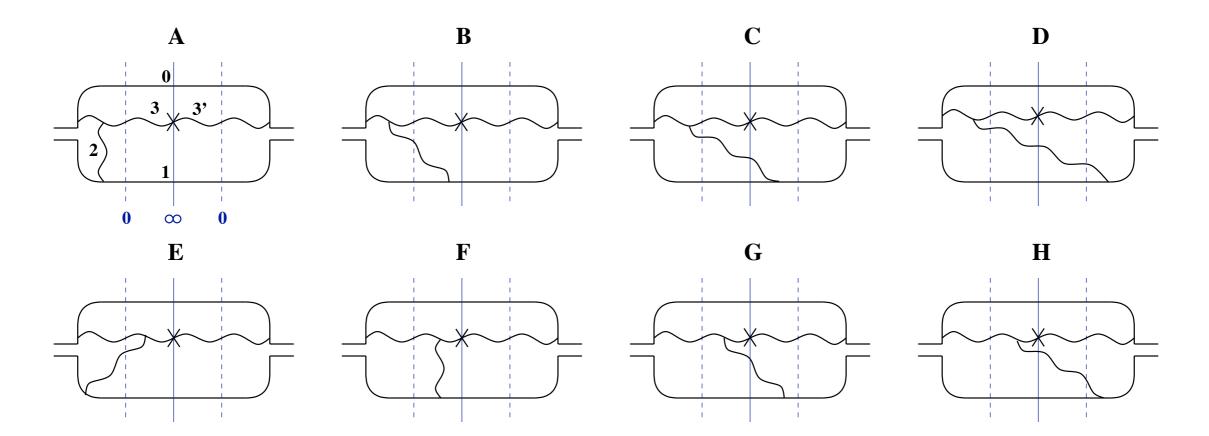


All fast gluons can be resumed into gluon dipole density $n(\mathbf{r},\mathbf{r}',\mathbf{b},y)$

This corresponds to the Pomeron hanging out from the incoming dipole ${\it r}$ and connecting with the emitting dipole ${\it r}$ '



Slow gluons $k_+>>l_+$

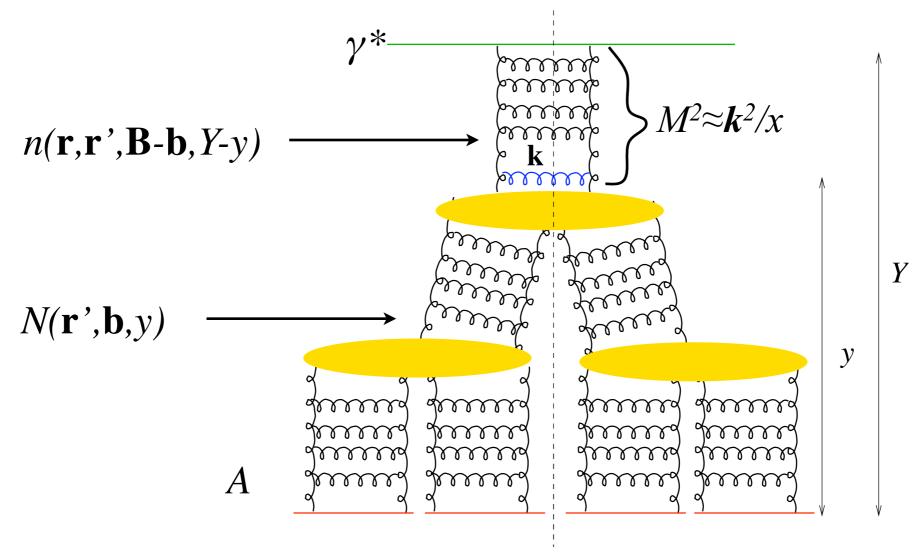


All slow gluons can be resumed into the forward elastic gluon dipole \mathbf{r} ' scattering amplitude $N(\mathbf{r}',\mathbf{b},y)$

if

the measured gluon is adjacent to the rapidity gap

(this is the most interesting case for phenomenology: $M^2 = k^2/x$)

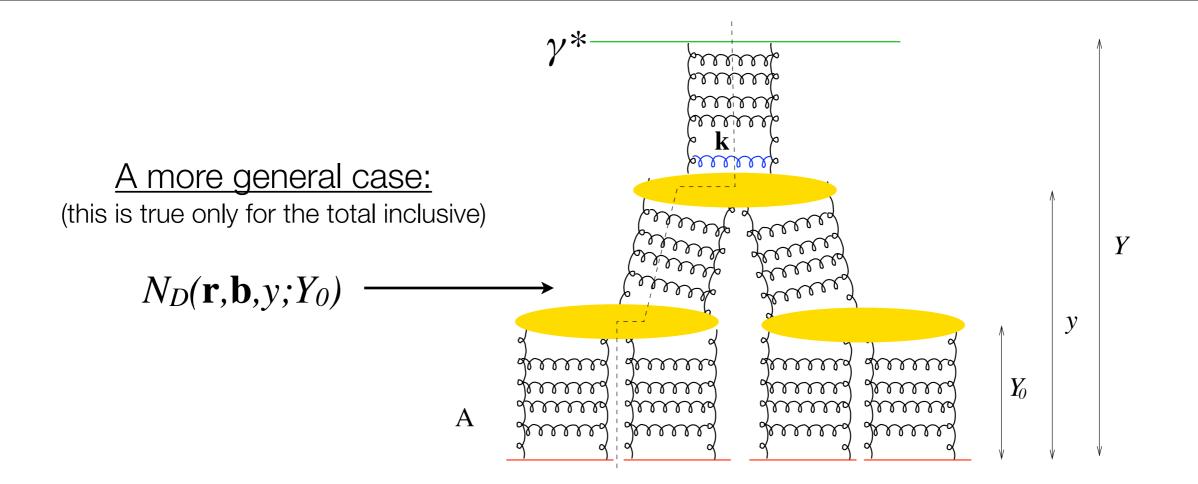


 $N(\mathbf{r}', \mathbf{b}, y)$ satisfies the BK equation

$$\frac{\partial N(\mathbf{x} - \mathbf{y}, \mathbf{b}, y)}{\partial y} = \frac{\alpha_s N_c}{2\pi^2} \int d^2 z \, \frac{(\mathbf{x} - \mathbf{y})^2}{(\mathbf{x} - \mathbf{z})^2 (\mathbf{y} - \mathbf{z})^2} \left[N(\mathbf{x} - \mathbf{z}, \mathbf{b}, y) + N(\mathbf{y} - \mathbf{z}, \mathbf{b}, y) - N(\mathbf{x} - \mathbf{y}, \mathbf{b}, y) - N(\mathbf{x} - \mathbf{z}, \mathbf{b}, y) N(\mathbf{y} - \mathbf{z}, \mathbf{b}, y) \right]$$

with the initial condition $N_A(\mathbf{r}, \mathbf{b}, 0) = 1 - e^{-\frac{1}{8}\mathbf{r}^2 Q_{s0}^2}$

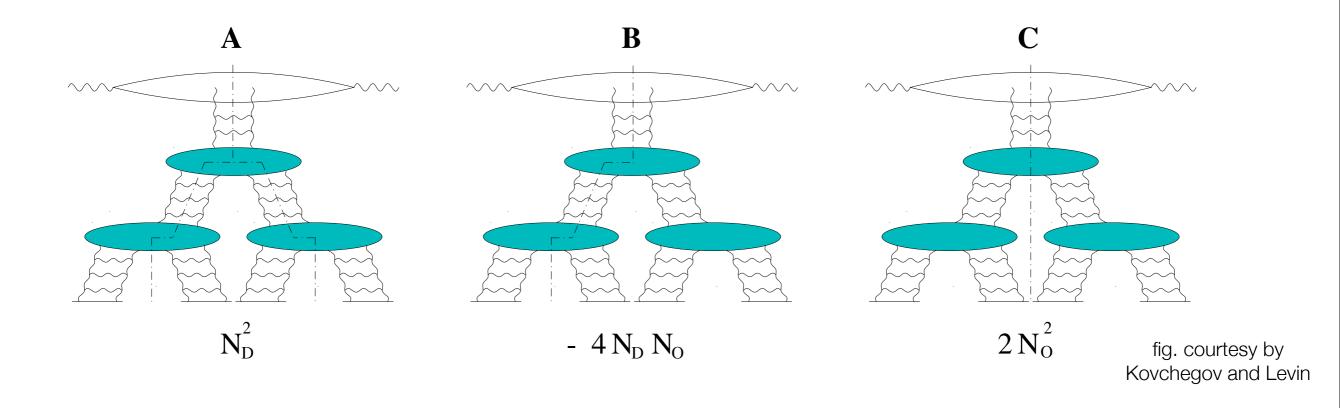
 $n(\mathbf{r}, \mathbf{r}', \mathbf{B} - \mathbf{b}, Y - y)$ satisfies the BFKL equation (in accordance with the AGK cutting rules) with the initial condition $n(\mathbf{r}, \mathbf{r}', \mathbf{b}, 0) = \delta(\mathbf{r} - \mathbf{r}') \, \delta(\mathbf{b})$



 $N_D(\mathbf{r}, \mathbf{b}, y; Y_0)$ satisfies the Kovchegov-Levin equation

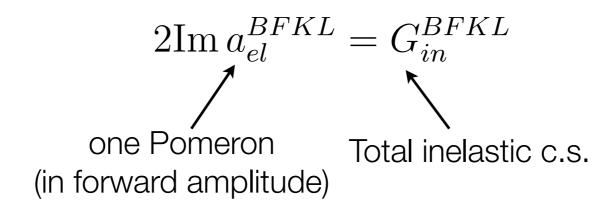
$$\frac{\partial N_D(\mathbf{x} - \mathbf{y}, \mathbf{b}, y; Y_0)}{\partial y} = \frac{2\alpha_s C_F}{\pi^2} \int d^2 z \left[\frac{(\mathbf{x} - \mathbf{y})^2}{(\mathbf{x} - \mathbf{z})^2 (\mathbf{y} - \mathbf{z})^2} - 2\pi \delta(\mathbf{y} - \mathbf{z}) \ln(|\mathbf{x} - \mathbf{y}| \Lambda) \right] N_D(\mathbf{x} - \mathbf{z}, \mathbf{b}, y; Y_0)
+ \frac{\alpha_s C_F}{\pi^2} \int d^2 z \frac{(\mathbf{x} - \mathbf{y})^2}{(\mathbf{x} - \mathbf{z})^2 (\mathbf{y} - \mathbf{z})^2} \left[N_D(\mathbf{x} - \mathbf{z}, \mathbf{b}, y; Y_0) N_D(\mathbf{y} - \mathbf{z}, \mathbf{b}, y; Y_0) \right]
4N_D(\mathbf{x} - \mathbf{z}, \mathbf{b}, y; Y_0) N(\mathbf{y} - \mathbf{z}, \mathbf{b}, y) + 2N(\mathbf{x} - \mathbf{z}, \mathbf{b}, y) N(\mathbf{y} - \mathbf{z}, \mathbf{b}, y) \right]$$

with the initial condition $N_D(\mathbf{r}, \mathbf{b}, y = Y_0; Y_0) = N^2(\mathbf{r}, \mathbf{b}, Y_0)$



Various terms in the Kovchegov-Levin equation comply with the AGK cutting rules

- A) (cut Pomeron 2) \times (symmetry factor 1/2) = 1
- B) (cut Pomeron 2) \times (number of diagrams 2) = 4
- C) (cut Pomeron 2) = 2



Effect of evolution in the onium

$$\frac{d\sigma(k,y)}{d^2kdy} = \frac{\alpha_s C_F}{\pi^2} \frac{1}{(2\pi)^2} \, S_A \int d^2r' \, n_p(\mathbf{r},\mathbf{r}',Y-y) \, |\mathbf{I}(\mathbf{r}',\mathbf{k},y)|^2 \qquad \text{we assume cylindrical nuclei}$$
 original intermediate dipole dipole

where
$$\mathbf{I}(\mathbf{r}', \mathbf{k}, y) = -e^{-i\mathbf{k}\cdot\mathbf{r}'}i\nabla_{\mathbf{k}}Q(\mathbf{r}', \mathbf{k}, y) + i\nabla_{\mathbf{k}}Q^*(\mathbf{r}', \mathbf{k}, y)$$

$$Q(\mathbf{r}', \mathbf{k}, y) = -\int d^2w \, e^{i\mathbf{k}\cdot\mathbf{w}} \frac{1}{w^2} \left[N(\mathbf{r}', \mathbf{b}, y) - N(\mathbf{w} - \mathbf{r}', \mathbf{b}, y) - N(\mathbf{w}, \mathbf{b}, y) + N(\mathbf{w} - \mathbf{r}', \mathbf{b}, y) N(\mathbf{w}, \mathbf{b}, y) \right]$$

As rapidity interval Y-y between the onium and the gluon increases, the dipole density evolves with BFKL:

$$n_{p}(\mathbf{r}, \mathbf{r}', y) = \frac{1}{2\pi^{2}r'^{2}} \int_{-\infty}^{\infty} d\nu \, e^{2\bar{\alpha}_{s}\chi(\nu)y} \, (r/r')^{1+2i\nu} \qquad n_{p}(\mathbf{r}, \mathbf{r}', 0) = \delta(\mathbf{r} - \mathbf{r}')$$

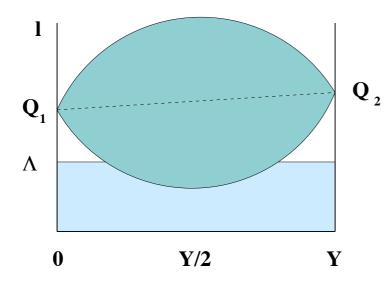
$$\chi(\nu) = \psi(1) - \frac{1}{2}\psi(\frac{1}{2} - i\nu) - \frac{1}{2}\psi(\frac{1}{2} + i\nu) \,, \qquad \psi(\nu) = \frac{\Gamma'(\nu)}{\Gamma(\nu)} \,.$$

Diffusion approximation: $\chi(\nu) \approx 2 \ln 2 - 7\zeta(3)\nu^2$,

$$n_p(r, r', Y - y) = \frac{1}{2\pi^2} \frac{1}{rr'} \sqrt{\frac{\pi}{14\zeta(3)\bar{\alpha}_s d(Y - y)}} e^{(\alpha_P - 1)(Y - y)} e^{-\frac{\ln^2 \frac{r}{r'}}{14\zeta(3)\bar{\alpha}_s d(Y - y)}}.$$

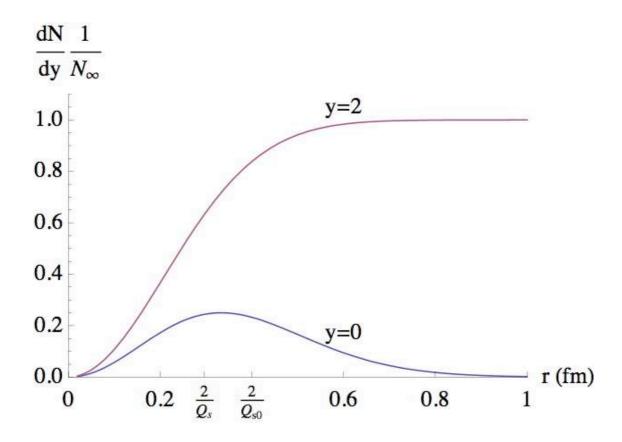
$$\alpha_s(Y - y) \gg \ln^2 \frac{r}{r'}$$

For large enough (Y-y) (corresponding to central and backward rapidities at RHIC), BFKL evolution produces dipoles of various sizes.



Particularly, there appear many dipoles of smaller size $r << 1/Q_s \Rightarrow$ no suppression!

Effect of evolution on diffractive hadron multiplicity



Evolution in nucleus

 $N(\mathbf{r}, \mathbf{b}, y)$ satisfies the BK equation with the initial condition $N(\mathbf{r}, \mathbf{b}, 0) = 1 - e^{-\frac{1}{8}\mathbf{r}^2 Q_{s0}^2}$

Linear regime $rQ_s \ll 1$

$$N(\mathbf{r}, \mathbf{b}, y)_{LT} = \frac{1}{8\pi} \int_{-\infty}^{\infty} d\nu \, e^{2\bar{\alpha}_s \chi(\nu) y} \, (rQ_{s0})^{1+2i\nu} \, \frac{1 + (1 - 2i\nu) \ln \frac{Q_{s0}}{\Lambda}}{(1 - 2i\nu)^2} \,.$$



Diffusion approximation

$$N(\mathbf{r}, \mathbf{b}, y)_{\text{diff}} = \frac{rQ_{s0}}{8\pi} \sqrt{\frac{\pi}{14\zeta(3)\bar{\alpha}_s y}} \ln\left(\frac{Q_{s0}}{\Lambda}\right) e^{(\alpha_P - 1)y} e^{-\frac{\ln^2(rQ_{s0})}{14\zeta(3)\bar{\alpha}_s y}}, \quad \alpha_s y \gg \ln^2\left(\frac{1}{rQ_{s0}}\right)$$

Double-log approximation $\chi(\nu)_{DLA} \approx \frac{1}{1-2i\mu}$

$$N(\mathbf{r}, \mathbf{b}, y)_{DLA} = \frac{\sqrt{\pi}}{16\pi} \frac{\ln^{1/4} \left(\frac{1}{rQ_{s0}}\right)}{(2\bar{\alpha}_s y)^{3/4}} r^2 Q_{s0}^2 \left(1 + \sqrt{\frac{2\alpha_s y}{\ln \frac{1}{rQ_{s0}}}} \ln \frac{Q_{s0}}{\Lambda}\right) e^{2\sqrt{2\bar{\alpha}_s y \ln \frac{1}{rQ_{s0}}}} \qquad \ln \frac{1}{rQ_{s0}} \gg \alpha_s y$$

Gluon saturation regime

$$\frac{\partial N(\mathbf{x} - \mathbf{y}, \mathbf{b}, y)}{\partial y} = \frac{\alpha_s N_c}{2\pi^2} \int d^2z \frac{(\mathbf{x} - \mathbf{y})^2}{(\mathbf{x} - \mathbf{z})^2 (\mathbf{y} - \mathbf{z})^2} \left[N(\mathbf{x} - \mathbf{z}, \mathbf{b}, y) + N(\mathbf{y} - \mathbf{z}, \mathbf{b}, y) - N(\mathbf{x} - \mathbf{y}, \mathbf{b}, y) - N(\mathbf{x} - \mathbf{z}, \mathbf{b}, y) N(\mathbf{y} - \mathbf{z}, \mathbf{b}, y) \right]$$

$$\frac{\partial N(\mathbf{r}, \mathbf{b}, y)}{\partial y} \approx \frac{\alpha_s C_F}{\pi} 2 \int_{1/Q_s^2}^{r^2} \frac{dw^2}{w^2} \left[N(\mathbf{w}, \mathbf{b}, y) - N(\mathbf{w}, \mathbf{b}, y) N(\mathbf{r}, \mathbf{b}, y) \right]$$

$$-\frac{\partial \{1 - N(\mathbf{r}, \mathbf{b}, y)\}}{\partial y} \approx \frac{\alpha_s C_F}{\pi} 2 \int_{1/Q_s^2}^{r^2} \frac{dw^2}{w^2} \{1 - N(\mathbf{r}, \mathbf{b}, y)\} = \frac{2\alpha_s C_F}{\pi} \ln(r^2 Q_s^2) \{1 - N(\mathbf{r}, \mathbf{b}, y)\}$$

Define the scaling variable $\tau = \ln(r^2Q_s^2)$

$$N(\mathbf{r}, \mathbf{b}, y) = 1 - S_0 e^{-\tau^2/8} = 1 - S_0 e^{-\frac{1}{8} \ln^2(r^2 Q_s^2)}, \quad r \gg \frac{1}{Q_s}$$
 Levin, KT, 99

Possible kinematic regions:

- Small onium r<<Qs
- Large onium r>>Qs

- Hard gluon k_T>>Q_s
- Soft gluon k_T<<Q_s

Emission of hard gluons by large onium r

Emission of soft gluons by large onium **r**

$$\frac{d\sigma}{d^2k \, dy} = \frac{\alpha_s C_F}{8\pi^{5/2}} \, \frac{S_A}{Q_s^2} \, \frac{(2\bar{\alpha}_s (Y - y))^{1/4}}{\ln^{3/4} (rQ_s)} \, e^{2\sqrt{2\bar{\alpha}_s (Y - y) \ln(rQ_s)}} \,, \quad r, \frac{1}{k} > \frac{1}{Q_s}$$

Multiplicity comes from the cut Pomeron connecting the incident onium and the daughter dipole r'

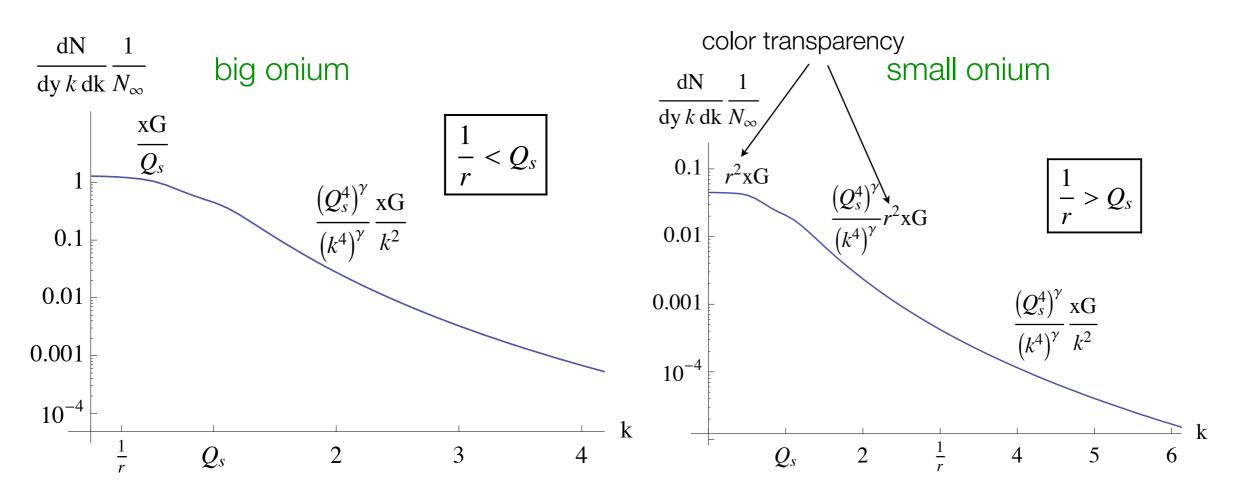
Emission of hard gluons by small onium ${f r}$

$$\frac{d\sigma}{d^{2}k\,dy} = \frac{\alpha_{s}C_{F}}{\pi^{5/2}}\,S_{A}\,r^{2}\,N^{2}(k^{-1}\hat{\mathbf{k}},\mathbf{b},y)\,\frac{1}{\left(2\bar{\alpha}_{s}(Y-y)\ln\frac{1}{kr}\right)^{1/4}}\,e^{2\sqrt{2\bar{\alpha}_{s}(Y-y)\ln\frac{1}{kr}}}\,,\quad r<\frac{1}{k}<\frac{1}{Q_{s}}$$
 Color transparency

Emission of soft gluons by small onium ${f r}$

$$\frac{d\sigma}{d^2k \, dy} = \frac{\alpha_s C_F}{4\pi^{5/2}} \, S_A \, r^2 \, \frac{1}{\left(2\bar{\alpha}_s(Y-y) \ln \frac{1}{rQ_s}\right)^{1/4}} \, e^{2\sqrt{2\bar{\alpha}_s(Y-y) \ln \frac{1}{rQ_s}}} \,, \quad r < \frac{1}{Q_s} < \frac{1}{k}$$

Diffractive gluon spectrum: Summary



In the geometric scaling region: $\gamma \approx 1/2$, in hard perturbative QCD $\gamma \approx 1 \Rightarrow$ different dependence on Q_s(y,A) in different kinematic regions

Nuclear dependence

"Nuclear modification factor":
$$R^{OA}(k,y) = \frac{\frac{d\sigma^{OA}(k,y)}{d^2kdy}}{A\,\frac{d\sigma^{OP}(k,y)}{d^2kdy}}$$
 pQCD limit (DLA):
$$R^{pA}(k,y) = \frac{S_{A}}{A\,S_p} \sqrt{\frac{\ln\frac{k}{Q_{s0}}}{\ln\frac{k}{\Lambda}}} \frac{Q_{s0}^4}{\Lambda^4} \left(1 + \sqrt{\frac{2\bar{\alpha}_s y}{\ln\frac{k}{Q_{s0}}}}\right)^2 e^{4\sqrt{2\bar{\alpha}_s y}\left(\sqrt{\ln\frac{k}{Q_{s0}}} - \sqrt{\ln\frac{k}{\Lambda}}\right)} \,, \quad k \gg Q_g$$

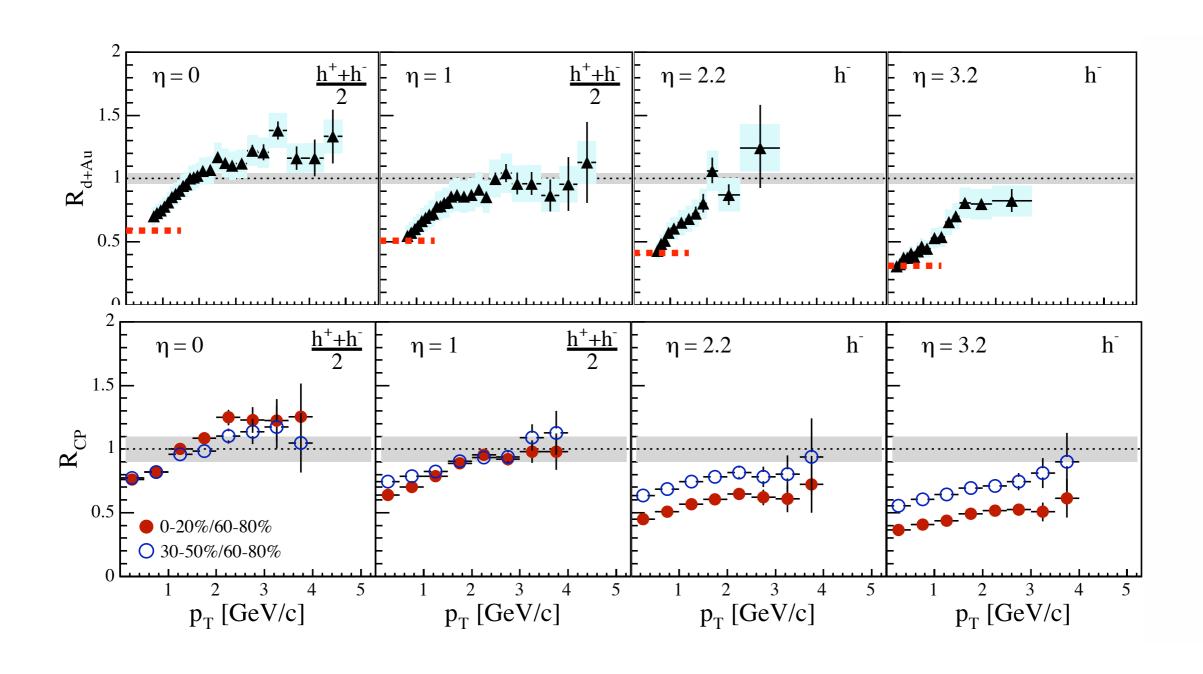
$$R^{pA}(k,y) \approx A^{1/3} \left(1 - 32\,\bar{\alpha}_s\,y\,\frac{\ln\frac{Q_{s0}}{\Lambda}\,\ln\frac{k}{Q_{s0}}}{\ln\frac{k}{\Lambda}}\right)$$

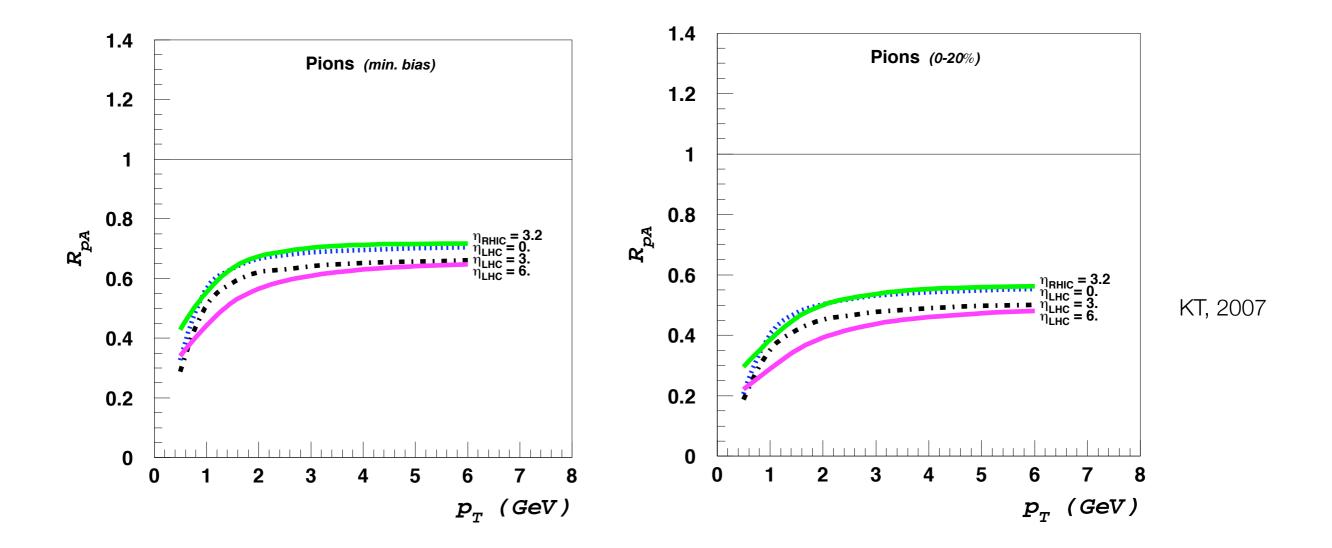
enhancement since it's a higher twist!

no A dependence!

$$R^{pA}(Q_g(y),y) \sim A^{1/3}\,e^{-4\sqrt{\bar{\alpha}_s\lambda}\,y} \quad \mbox{suppression at higher energies/rapidities}$$

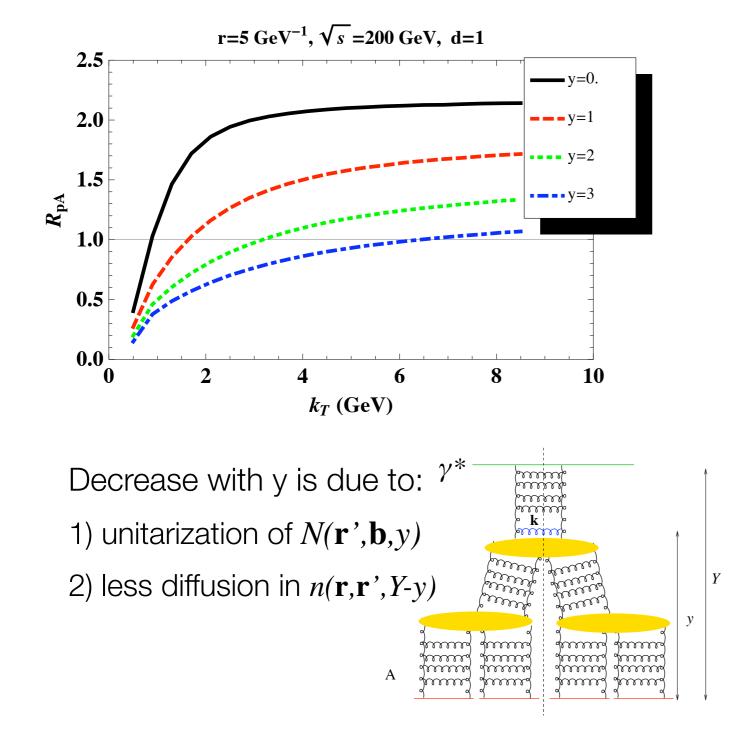
Comparing diffractive and inclusive production



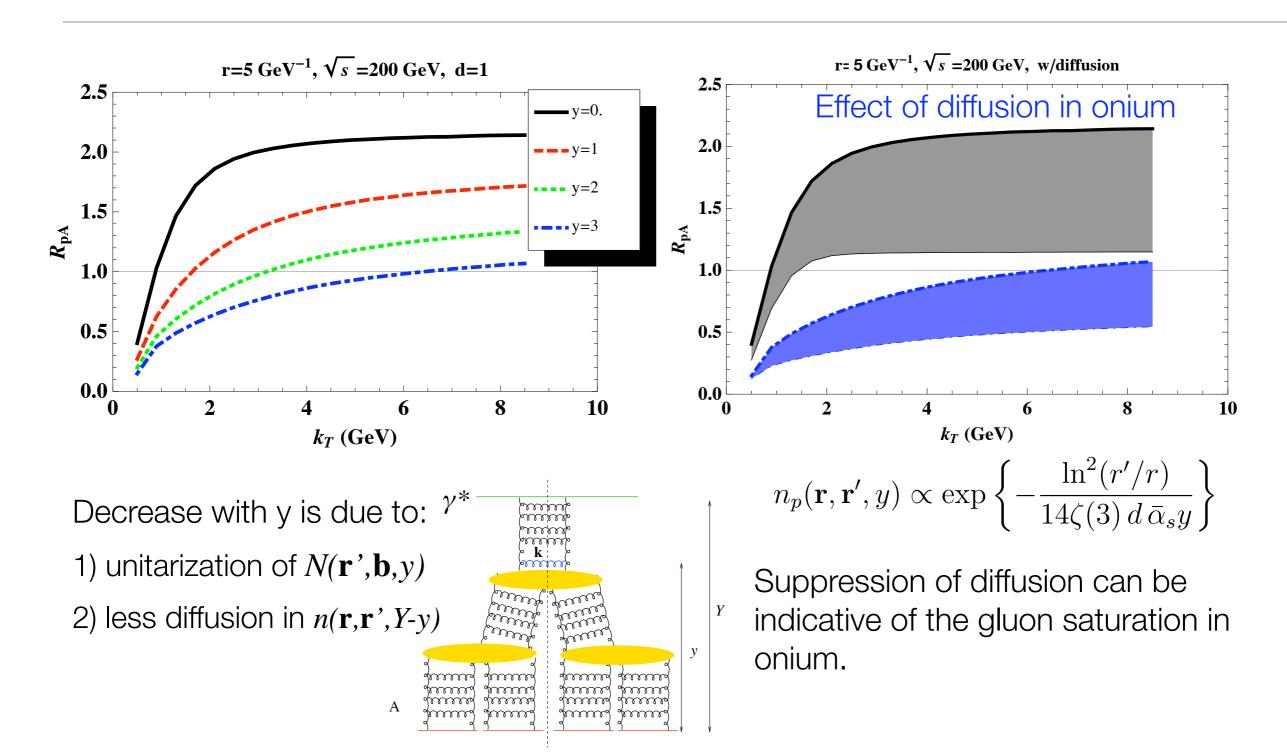


Inclusive gluon production at not very high momenta is expected to be rather trivial ... unlike the diffractive production

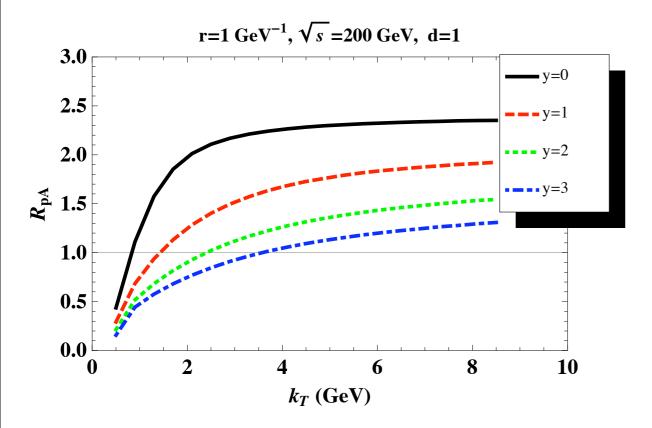
Large dipoles at RHIC energy



Large dipoles at RHIC energy

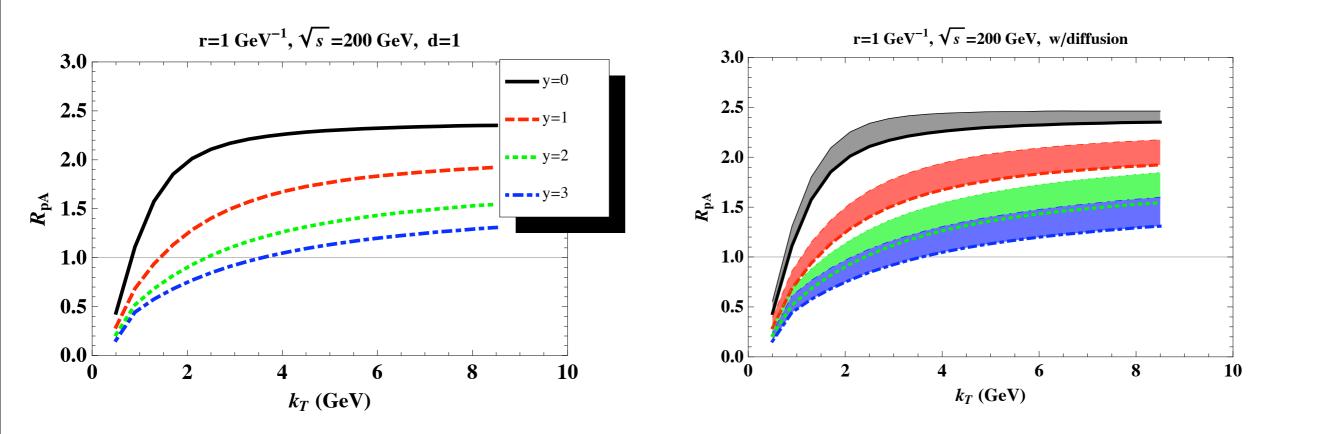


Small dipoles at RHIC energy



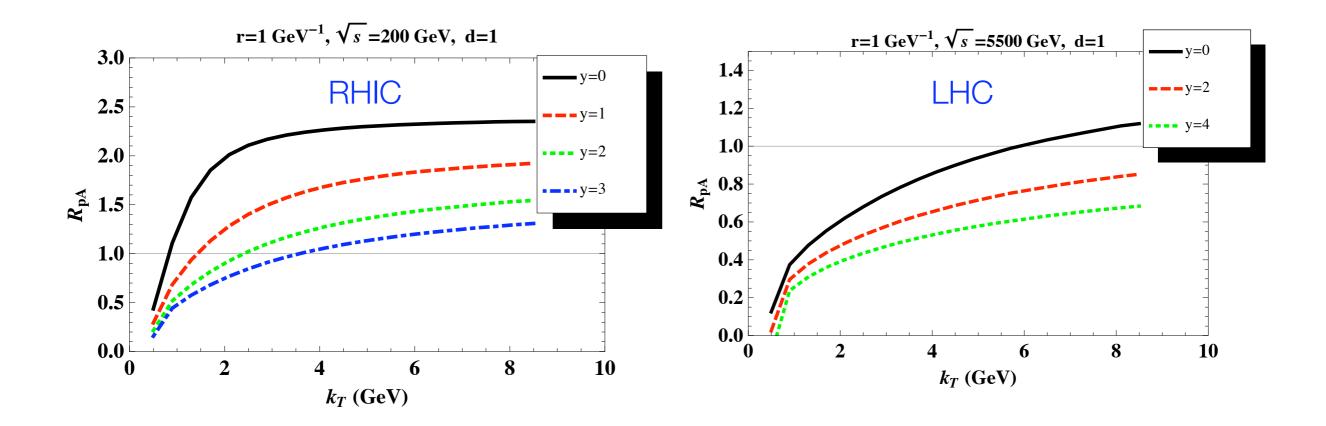
Small dipoles are much less sensitive to the details of the low-x evolution in onium

Small dipoles at RHIC energy



Small dipoles are much less sensitive to the details of the low-x evolution in onium

RHIC vs LHC



Summary

- 1. Diffractive gluon production in eA and pA collisions has remarkable sensitivity to the low-x dynamics in onium and nucleus.
- 2. Dependence on r, y, A and k provide a convenient handles on behavior of gluon densities in various kinematic regions.
- 3. It can become a valuable tool for pA and DIS phenomenology at RHIC, LHC and EIC.