The seismological signature of temperature and grain size variations in the upper mantle

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Abstract

The shear modulus and attenuation of pure and therefore genuinely melt-free polycrystalline aggregates of $\text{Fo}_{90}$ olivine have recently been measured over a wide range of mean grain size at upper mantle temperatures and seismic frequencies [1,2] [B.H. Tan, I. Jackson, J.D. Fitz Gerald, High-temperature viscoelasticity of fine-grained polycrystalline olivine, Phys. Chem. Miner. 28 (2001) 641–664; I. Jackson, J.D. Fitz Gerald, U.H. Faul, B.H. Tan, Grain-size sensitive seismic wave attenuation in polycrystalline olivine, J. Geophys. Res. 107 (B12 2360) (2002) doi:10.1029/2001JB001225]. Here for the first time we fit the experimental shear modulus and attenuation data to a common model that provides an internally consistent description of the observed variations with frequency, temperature and grain size. This model is used to perform indicative calculations of shear wave speed ($V_s$) and attenuation ($Q$) along geotherms representative of both oceanic and continental settings, intended to highlight the sensitivity of $V_s$ and $Q$ to variations of temperature and grain size. Comparison of the results of these calculations with seismological models suggests the following: (1) The low velocity zone (LVZ), commonly observed below ocean basins, and its tendency to become less pronounced and deeper with increasing lithospheric age, can be explained by solid state mechanisms without the presence of melt or fluids. (2) The relatively large velocity variations in the upper mantle seen in global tomographic models can be explained by reasonable temperature differences within continents and between continents and oceans. (3) The velocity increase below ~200 km seen in most seismological models may indicate an increase in grain size from order of mm in the shallow upper mantle to ~cm above the transition zone.

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1. Introduction

Inferring the physical state of the upper mantle from regional and global seismological models has been the aim of number of recent papers (e.g. [3–7]). While it is widely accepted that most of the variability in wave speeds seen in these models is due to variations in temperature, conversion of velocities to temperatures has been hampered by lack of direct measurements of the shear modulus of olivine at high temperatures and seismic frequencies. The contribu-
tion of anelasticity to the temperature sensitivity of shear wave velocities has previously only been estimated indirectly through the temperature sensitivity of attenuation \(Q\) [8,9]. Here we use for the first time simultaneous laboratory measurements of shear modulus and \(Q\) at seismic frequencies and mantle temperatures [1,2] to constrain temperatures in both oceanic and continental upper mantle.

Among the key questions regarding the structure of the upper mantle are the thickness of continental roots [10] and the origin of the zone of low seismic shear wave velocity in the Earth’s upper mantle. This low velocity zone (LVZ) is commonly equated with a zone of low viscosity that facilitates the movement of tectonic plates (e.g. [11]). However, the physical mechanisms giving rise to the low-velocity, high-attenuation zone have been the subject of debate since it was first discovered more than 50 years ago [12]. Partial melting is usually invoked to explain the low velocity zone [13], but the presence of water has also been suggested [14]. Goetze [15] suggested a solid-state mechanism, but no directly relevant laboratory data were then available to support this hypothesis.

In the following we describe the procedure for fitting the experimental data and then use the fits to calculate temperatures for the oceanic upper mantle for conductively cooling lithosphere overlying adiabatic mantle. For continents, the calculated geotherms include heat production in upper and lower crust and mantle lithosphere. The geotherms are constrained by the observed surface temperature and heat flow. We use the new laboratory data to show that many first-order features of the seismologically observed structure of the olivine-dominated upper mantle for both oceans and continents can be explained by the transition in dry crystalline material from elastic to viscoelastic behaviour, along with the competing effects of temperature and pressure on the shear modulus of olivine.

2. Description of the experimental shear modulus and attenuation data by a creep function

During the past few years the application of seismic-frequency laboratory methods has begun to revolutionize our understanding of seismic wave speeds and attenuation in olivine-dominated upper-mantle materials [16,17]. The observed modulus reduction and enhanced attenuation at high temperatures are most plausibly explained by grain boundary sliding [2,16,18–22].

Microcreep tests on olivine polycrystals show that their mechanical response to the application of a step-function stress is characterized by three distinct regimes [2]. The instantaneous, elastic response is followed by a transient, anelastic strain that is recoverable, and lastly by permanent (irrecoverable) viscous deformation. This behavior is qualitatively that of a Burgers model solid, consisting of a suitable combination of springs and dashpots (e.g. [23], Ch. 3; [24], Ch. 4.5, 4.6 and 6.5).

The time-dependent response (strain) of the Burgers model system to application at time \(t=0\) of unit step-function stress defines the creep function:

\[
J(t) = J_U \left( 1 + \Delta \left( 1 - e^{-\frac{t}{\tau_M}} \right) + \frac{t}{\tau_M} \right)
\]

where \(J_U\) is the unrelaxed compliance, given by the reciprocal of the unrelaxed (elastic) shear modulus \(G_U\). The anelastic relaxation strength \(\Delta\) is given by \(\Delta = \frac{G_U - G_R}{G_R}\), with \(G_R\) the relaxed modulus (anelastic relaxation only). The Maxwell relaxation time associated with the steady state (Newtonian) viscous element of viscosity \(\eta\) is given by:

\[
\tau_M = \eta J_U.
\]

The Debye-type anelastic relaxation of this simple Burgers model solid involves a unique relaxation time \(\tau\). However, seismological observations of a broad absorption band within which \(Q^{-1}\) varies weakly with frequency indicate that a distribution of relaxation times is required. Anderson and Minster [8] introduced a normalized distribution of relaxation times as

\[
D(\tau) = \frac{2 Q \tau^2 \tau^{-1}}{\tau_H^2 - \tau_L^2}, \tau_L < \tau < \tau_H
\]

between the lower and upper cutoff times \(\tau_L\) and \(\tau_H\) and zero elsewhere. They suggested that the upper and lower cutoff times depend on physical and geometrical variables as well as thermodynamic conditions. The seismologically inferred value for
the parameter $a_Q$, which characterizes the weak frequency dependence, is very similar to the value much more tightly constrained by experiments (e.g. [2,16]).

The temperature and grain size dependence of the Maxwell relaxation time (Eq. (2)) is derived from the temperature and grain size dependence of the viscosity $\eta \sim d^m \exp(E/RT)$ (e.g. [18,24]) and expressed in the following form:

$$\tau = Ad^m e^{\left(\frac{E}{RT}\right)}$$  \hspace{1cm} (4)

where $A$ is a constant, $E$ is the activation energy, $R$ is the gas constant, $T$ is absolute temperature and $d$ is the grain size with exponent $m$.

The experimental observations confirm the suggestion of Anderson and Minster [8] that the cutoff times for the distribution of anelastic relaxation times are similarly temperature and grain size dependent. For example, the deviation from linearity of attenuation in log–log space at the longest periods and highest temperatures for the most fine-grained sample (Fig. 1c) indicates the transition from anelastic to viscous behavior. Such variations with grain size and temperature are conveniently expressed by a modified version of Eq. (4):

$$\tau_i = \tau_{R} \left(\frac{d}{d_{R}}\right)^m e^{\left\{\left(\frac{E}{R T}\right)\left(\frac{1}{d} - \frac{1}{d_{R}}\right)\right\}}$$  \hspace{1cm} (5)

where the $\tau_i$ are the upper and lower cutoff times ($\tau_L$ and $\tau_H$) and the Maxwell time ($\tau_M$). The parameters $\tau_{R}$ are the values of the $\tau_i$ at the reference temperature $T_R$ and the reference grain size $d_R$ [22]. Different grain-size exponents $m_A$ for $\tau_L$ and $\tau_H$.
and $m_v$ for $\tau_M$ are allowed (Table 1), reflecting the different diffusion distances involved in anelastic and viscous relaxation.

The experimental data presented in Fig. 1 from two representative melt-free specimens shows their high temperature, viscoelastic behavior characterized by systematic variation of both shear modulus and attenuation with period, temperature and grain size. We observe the transition from elastic to viscoelastic behavior near 900 °C in the form of an appreciable enhancement of the temperature sensitivity of $G$ and $Q$ ([1], their Fig. 10). To capture this behavior, and to incorporate pressure dependence, Eq. (1) has to be suitably modified to:

$$J(t, d, T, P) = J_U(P)\left(1 + \delta \ln J_U + \Delta \int_{\tau_L}^{\tau_H} D(\tau) \times \left(1 - e^{-\frac{\tau}{\tau_M}}\right) d\tau + \mathcal{A} \right)$$

where $J_U(P)$ is the unrelaxed compliance with its usual anharmonic (elastic) pressure dependence.

The term $\delta \ln J_U$ is a fractional adjustment to $J_U$, which in the elastic regime (below about 900 °C) is simply the anharmonic temperature dependence of $J_U$ (e.g. [25]). Within the viscoelastic regime (above about 900 °C) the unrelaxed shear modulus ($G_U = J_U^{-1}$) fitted to data for periods of 1–1020 s is found to be more strongly temperature dependent than can be reconciled with the simple anharmonic temperature sensitivity of $G_U$. This suggests that the distribution of anelastic relaxation times must extend well below 1 s (i.e. $\tau_L < 1$ s). This lower end of the distribution is not well constrained by our current experiments. Since this additional relaxation is anelastic in nature it should be grain-size sensitive, as observed. To account for this additional relaxation we define for the viscoelastic regime:

$$\delta \ln J_U = \left(\frac{\partial \ln J_U}{\partial T}\right)_R \left(\frac{d}{dT}\right)^{-m_j} (T - T_R).$$

As part of our fit to the data, the unrelaxed modulus at the reference temperature of 950 °C is found to be $67.1$ GPa. Using the anharmonic temperature derivative of $-0.0136$ GPa/K [25], this corresponds to a shear modulus at room temperature of 80 GPa, within the upper end of the range of experimentally determined values [26].

For the application of a periodic shear stress in our torsional forced oscillation experiments the stress can be expressed as:

$$\sigma(t) = \sigma_0 e^{i\omega t}$$

where $\sigma_0$ is the stress amplitude and $\omega$ the circular frequency. The resulting shear strain lags behind by an angle $\phi$:

$$\varepsilon(t) = \varepsilon_0 e^{i(\omega t - \phi)}.$$ 

The complex compliance $J^*(\omega)$

$$J^*(\omega) = \frac{\varepsilon(t)}{\sigma(t)} = |J(\omega)||e^{i\phi(\omega)}$$

is essentially the Laplace (or Fourier) transform of $J(t)$ [23]. The frequency dependent shear modulus $G$ and
strain energy dissipation $Q^{-1}$ are calculated as follows:

$$G(\omega) = \left( J_1^2(\omega) + J_2^2(\omega) \right)^{-\frac{1}{2}}$$

(11)

and

$$Q^{-1} = \frac{J_2(\omega)}{J_1(\omega)}$$

(12)

with

$$J_1(\omega, d, T, P) = J_U(P) \left( 1 + 6\ln J_U + \frac{\alpha \omega A}{\tau_H - \tau_L} \right)$$

$$\times \int_{\tau_L}^{\tau_H} \frac{\tau^{\alpha - 1}}{1 + \omega^2 \tau^2} d\tau$$

(13)

and

$$J_2(\omega, d, T, P) = J_U(P) \left( \frac{\omega \alpha A}{\tau_H - \tau_L} \int_{\tau_L}^{\tau_H} \frac{\tau^{\alpha - 1}}{1 + \omega^2 \tau^2} d\tau + \frac{1}{\omega \tau_M} \right)$$

(14)

This rheology with suitably optimised values of the model parameters given in Table 1 provides an entirely adequate description of the variation with period (1–1020 s), temperature (1000–1300 °C) and grain size (3–165 µm) of both the shear modulus and dissipation measured for genuinely melt-free olivine polycrystals [1,2] (Fig. 1).

The large dataset, comprising a total of 206 individual measurements of shear modulus and dissipation on four specimens, allows the refinement of the 9 model parameters (Table 1) needed to fully specify the creep function. The advantage of this approach is that the transition from elastic through anelastic to viscous behaviour is captured in a way that provides for an internally consistent treatment of the modulus and dissipation. Thus this model, unlike the simpler $Q^{-1}$-period power-law alternative (e.g., [2]), accommodates the systematic trend towards more strongly frequency-dependent $Q^{-1}$ with increasing period for the fine-grained specimen of Fig. 1.

On application of the Burgers model to upper mantle conditions our experimental data require only moderate extrapolation in grain size and temperature (Fig. 2). In the calculations below, we account for the effect of pressure $P$ on both shear modulus and attenuation by using the anharmonic derivative ($dG/dP=1.8 \ [27]$) and scaling the relaxation times (Eq. (5)) by a factor $\exp(PV*/RT)$ with a suitable activation volume $V^*$ (see Section 4.2). The period in the calculations is roughly scaled to depth as appropriate for surface waves [28].

Fig. 2. Shear modulus and dissipation as functions of inverse temperature, contoured for grain size at a representative fixed period of 8.2 s. Dots represent experimental data, solid lines the extended Burgers model fit at the corresponding grain size. Dashed lines indicate extrapolation in grain size; only a modest extrapolation in temperature is necessary for upper mantle conditions. At a fixed temperature the shear modulus increases and attenuation decreases with increasing grain size.
3. Temperature calculation

3.1. Adiabat and geotherm beneath ocean basins

Adiabatic temperatures are calculated from

\[ T_{ad} \approx T_0 \left( 1 + \frac{x_T g z}{c_p} \right), \tag{15} \]

where \( T_0 \) is the potential temperature, \( z \) is depth and \( g \) is acceleration due to gravity (e.g. [29]). The coefficient of thermal expansion \( x_T \) and specific heat at constant pressure \( c_p \) are assumed to be independent of pressure and temperature. With potential temperatures between 1300 and 1400 °C, adiabatic temperatures at 400 km depth do not exceed 1550 °C. Over this temperature range \( c_p \) varies by less than 4% around an approximate value of 1350 J kg⁻¹ K⁻¹ [30]. The variation in the coefficient of thermal expansion in this temperature range is larger, and it is also significantly pressure dependent. On an adiabat with a potential temperature of 1300 °C from 100 to 400 km depth, \( x_T \) decreases from \( \sim 3.5 \times 10^{-5} \) K⁻¹ to \( \sim 2.3 \times 10^{-5} \) K⁻¹ [31]. We used \( x_T = 2.9 \times 10^{-5} \) K⁻¹ in our calculations, but the decrease in \( x_T \) with depth means that adiabatic temperatures are overestimated below 200 km and hence velocities somewhat underestimated.

Density and pressure are calculated with constant adiabatic compressibility \( \beta_a \) from [29]:

\[ \rho = \frac{\rho_0}{1 - \rho_0 g \beta_a z}, \quad P = -\ln(1 - \rho_0 g \beta_a z) \beta_a \tag{16} \]

It is well established that the structure and properties of oceanic lithosphere up to ages of 80–100 My are consistent with a conductively cooling half-space model. Age-dependent geotherms can be calculated from [29]:

\[ T = T_S + (T_{ad} - T_S) \text{erf} \left( \frac{z}{2 \sqrt{(\kappa t)}} \right) \tag{17} \]

where \( T_S \) is the temperature at the ocean floor, \( t \) is the age of the ocean floor and \( \kappa \) is the thermal diffusivity. Again \( \kappa \) is assumed constant, but experimentally determined values decrease by a factor of two in the temperature range from 300 to 1000 °C, and are constant only at higher temperatures [32]. If the observed decrease is taken into account, temperature gradients are less steep below 800 °C and steeper from 800–1200 °C. Above 1200 °C the temperatures are the same as for constant \( \kappa \) [33].

3.2. Continental geotherms

Temperatures in the continental lithosphere are calculated for a model that includes different values for heat production and conduction in upper and lower crust as well as the lithospheric part of the mantle. Following Chapman [34] temperature and heat flow \( q \) are calculated from:

\[ T_b = T_t + \frac{q_t}{k} \Delta z - \frac{\rho H}{2k} \Delta z^2 \quad \text{and} \quad q_b = q_t - \rho H \Delta z \tag{18} \]

where the subscripts \( t \) and \( b \) indicate top and bottom of a layer with thickness \( \Delta z \), \( k \) is the thermal conductivity and \( \rho H \) the volumetric heat production. Fig. 3 shows the boundary conditions used in the calculations.

Fig. 3. Sketch of the three-layer model used in the calculation of continental geotherms. Surface temperature, surface heat flow and Moho depth are given by McLaren et al. [48] and Clitheroe et al. [49], respectively. Thermal conductivity in upper and lower crust is fixed (\( k_{UC} = k_{LC} = 2.5 \) W m⁻¹ K⁻¹). This is an oversimplification but results only in a small trade-off with heat production for the same geotherm. \( k_{li} \) is calculated as a function of temperature from Eq. (19).
The thermal conductivity in the crust is fixed, thermal conductivity in the mantle part of the lithosphere is calculated from [35]

\[
k(T) = \frac{1}{0.174 + 0.000265T} + 3.68 \times 10^{-10}T^3. \tag{19}
\]

Changes in the values of thermal conductivity are compensated by slight changes in heat production to result in essentially the same geotherm. The intersection of the geotherms with the adiabat is smoothed to avoid artificial kinks in the velocity-depth profiles.

## 4. Results

### 4.1. Oceans

Fig. 4 shows adiabats and resulting shear velocity and \( Q \) calculated for 100 My old oceanic lithosphere. Also shown in Fig. 4b is the model PA5 of Gaherty et al. [36] for the Tonga-Hawaii corridor for which the age of the oceanic crust is close to 100 My. Below the crust (which is not modelled) there is a moderate decrease in the calculated velocity to a depth of ~80 km corresponding to 900 °C. At greater depths, the stronger temperature sensitivity due to viscoelastic

![Diagram](image_url)
behaviour combines with the still large temperature gradients in the conductively cooling part of the lithosphere. The velocity minimum occurs at ~170 km depth, where the conductive part of the geotherm grades into the adiabat with its much smaller temperature gradient.

The increase in velocity at greater depth is due to the pressure effect on the shear modulus, which overwhelms the modest temperature induced decrease. Anharmonic, viscoelastic and pressure effects on the shear modulus of melt-free olivine thus combine to produce a pronounced low velocity zone. With variable thermal diffusivity [33] (see Section 3.1), the shallow lithospheric velocity gradients would be somewhat reduced, and the onset of the low velocity zone somewhat more pronounced.

Velocities calculated with a (uniform) grain size of 1 mm are significantly lower deeper than ~200 km than those of seismological models [36–38], while those calculated with a grain size of 5 cm do not match the velocity minimum shown by these models (Fig. 4b). One way to match the increase in shear velocity below the LVZ is to progressively increase the grain size by about one order of magnitude from ~mm to ~cm. The increase in grain size is modeled to begin below 165 km depth where Gaherty et al. [36] find that significant anisotropy is no longer resolvable. The maximum grain size is reached at 350 km depth.

Fig. 4c shows a comparison of $Q$ calculated with the same parameters as $V_s$ in Fig. 4b with seismological $Q$ models. The important point here is that both $V_s$ and $Q$ are calculated self consistently, and simultaneously match seismological $V_s$ and $Q$ models.

Fig. 4d–f illustrate the trade-offs between temperature, grain size and activation volume. A higher potential temperature (1400 °C) can be partially compensated by a correspondingly larger grain size. The fit to the $V_s$ model is still satisfactory while the calculated $Q$ is somewhat low relative to the seismological models. Similarly, a lower activation volume can be compensated by a larger grain size for $V_s$, but since global $Q$ models show a recovery from the minimum in the LVZ [39–41], $Q$ does not fit the models as well. Increasing $V^*$ from the preferred value of $1.2 \times 10^{-5} \text{ m}^3 \text{ mol}^{-1}$ to $2 \times 10^{-5} \text{ m}^3 \text{ mol}^{-1}$ while keeping the grain size fixed at 1 mm does not fit either $V_s$ or $Q$ models.

![Fig. 5. Age dependence of depth and magnitude of the velocity reduction of the LVZ. (a) Geotherms as a function of age for conductively cooling oceanic lithosphere, and (b) the corresponding shear velocities. The symbols are from a model by Nishimura and Forsyth [37], the solid lines are the velocities calculated for the geotherms in (a). The ages shown in (a) correspond to the middle of the age range for the seismological model.](image-url)
The need to match both $V_s$ and $Q$ models places therefore relatively tight constraints on $V^*$, while there is some trade off possible between temperature and grain size. The parameters for $V^*$ and $T_p$ shown in Fig. 4a–c are used in all the following calculations. Our preferred value of $V^*$ is well within the range of the available experimental estimates (e.g. [42,43]); it is also possible that $V^*$ is pressure dependent (e.g. [44]).

The increase in the LVZ shear velocity minimum and its deepening with age have been observed in a number of seismological studies [37,45]. Fig. 5 shows a comparison of calculated velocities with the seismological model of Nishimura and Forsyth [37] for the same ages. The main features of an increasing velocity minimum in the LVZ and its deepening with age are clearly reproduced. For the youngest lithosphere the seismological indications of a deeper and more pronounced LVZ than calculated are suggestive of an additional velocity reduction due to the presence of melt, for example beneath the East Pacific Rise. For ages greater than 80–100 My it has previously been noted that the high-velocity lid approaches a constant thickness (e.g. [28] and references therein).

4.2. Continents

4.2.1. Background

Seismic velocities calculated for continental geotherms are compared with three different velocity-depth profiles extracted from a recent surface wave model of the Australasian region by Fishwick et al. [38]. This model is an extension of the Debayle and Kennett model [46] with additional data for Western Australia including both fundamental and higher

Fig. 6. Tomographic image of the shear velocities at 200 km depth of Australia and surrounding oceans from Fishwick et al. [38]. The squares indicate the locations of the three continental and one oceanic area for which the averaged model velocity structures are compared with calculated ones. The locations were chosen to sample relatively uniform velocity structures of the three major geologic regions in Australia: the Archean Yilgarn craton, Proterozoic terrains that have high heat flow relative to global averages of terrains of the same age, and Paleozoic southeastern Australia. Inclusion of an averaged velocity depth profile from the Tasman Sea/Lord Howe Rise covers the shear velocity variations of nearly $\pm 8\%$ generally seen in global and regional models.
modes. The seismic velocity-depth profiles represent three geologically different parts of the continent: the Archean Yilgarn craton in the Southwest, Proterozoic parts of the Northern Territory and Phanerozoic South-Eastern Australia (Fig. 6) and thus three different Australian heat flow provinces [47]. The average surface heat flow for each province is given by McLaren et al. [48] (see Table 2). The total crustal thickness at each location ($h_M$) is derived from Clitheroe et al. [49].

The seismic velocity-depth profiles are averages of more than 20 grid points through the model of Fishwick et al. [38]. In order to find the geotherm that produces the closest match in shear velocities to the seismological model a grid search is performed over upper and lower crustal heat production ($q_{\text{UC}}$ and $q_{\text{LC}}$) as well as upper crustal thickness $h_{\text{UC}}$. The ranges used in the grid search ($q_{\text{UC}} = 1–5 \ \text{mW m}^{-3}$, $q_{\text{LC}} = 0.2–1 \ \text{mW m}^{-3}$, $h_{\text{UC}} = 5–12 \ \text{km}$) are based on work by McLaren et al. [48]. The value for lithospheric mantle heat production ($q_{\text{Li}} = 0.03 \ \text{mW m}^{-3}$) is taken from Rudnick et al. [50]. The mismatch between calculated velocities and the seismological model is estimated by calculating an rms misfit.

Table 2

<table>
<thead>
<tr>
<th>Location</th>
<th>$q_S$ (mW m$^{-2}$)</th>
<th>$h_M$ (km)</th>
<th>$h_{\text{UC}}$ (km)</th>
<th>$\rho H_{\text{UC}}$ (mW m$^{-3}$)</th>
<th>$\rho H_{\text{LC}}$ (mW m$^{-3}$)</th>
<th>$T_M$ (°C)</th>
<th>$q_M$ (mW m$^{-2}$)</th>
<th>$q_L$ (mW m$^{-2}$)</th>
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</thead>
<tbody>
<tr>
<td>Yilgarn</td>
<td>51</td>
<td>37</td>
<td>6.6</td>
<td>2.2</td>
<td>0.8</td>
<td>430</td>
<td>12.2</td>
<td>1.3</td>
</tr>
<tr>
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<td>83</td>
<td>42</td>
<td>9.8</td>
<td>4.0</td>
<td>1.0</td>
<td>630</td>
<td>11.6</td>
<td>0.9</td>
</tr>
<tr>
<td>SE Australia</td>
<td>79</td>
<td>39</td>
<td>11.2</td>
<td>3.0</td>
<td>1.0</td>
<td>650</td>
<td>17.6</td>
<td>6.8</td>
</tr>
</tbody>
</table>

Fig. 7. (a) Geotherms and (b) corresponding velocities (solid lines) calculated for the locations shown in Fig. 6. The symbols are averages calculated through the model of Fishwick et al. [38], the horizontal bars indicate standard deviations. Thermal parameters and grain sizes used in the calculations are given in Tables 2 and 3. Dashed line in (a) indicates the 1300 °C adiabat. The oceanic geotherm was calculated as those in Figs. 4 and 5 for 35 My old lithosphere, the approximate age for this region of the Tasman Sea [63]. The parameters used in the calculations were kept as simple and uniform as practical, no attempt was made to match second order variations in the seismic velocity model (e.g. increase the grain size in the oceanic profile at 300 km depth and below to increase the calculated velocities). To first order all profiles other than for the Yilgarn craton can be matched with a common adiabat and a lower grain size of 5 cm. The largest velocity differences between relatively young oceanic lithosphere and archean craton are found between 100 and 200 km depth, corresponding to temperature differences of around 500–600 °C.
4.2.2. Results

Geotherms that satisfy the heat flow constraints and best fit the surface wave model for Australia are shown in Fig. 7. Table 2 shows the corresponding thermal parameters and Table 3 lithospheric thickness and grain sizes. It is not possible to construct geotherms that result in strongly positive velocity-depth gradients in the upper 100 km, as this is the depth region with the highest sub-crustal temperature gradients, which inherently lead to negative velocity gradients. Accordingly, the 50 km and 75 km points of the seismological model are not considered in the misfit calculations.

The seismological model shows high velocities at all depths for the Yilgarn craton; these can only be matched for significantly sub-adiabatic temperatures extending to the transition zone. Temperatures below Northern Australia are also sub-adiabatic to at least 300 km; the geotherm approaches the adiabat asymptotically below this depth, so that the lithospheric thickness is not well defined. The lithosphere beneath South-Eastern Australia is relatively thin, consistent with its lesser age and widespread Cenozoic magmatism. Simons et al. [51] similarly found an age dependence of the seismically detected lithospheric thickness; our somewhat different thickness estimates for Western Australia may be related to the increased coverage of this area by the data set of Fishwick et al. [38].

The deeper transition to larger grain size relative to the oceanic models (Table 3) reflects the greater depth to which anisotropy is observed beneath Australia [46,52]. Beneath the Tasman Sea the transition depth for the increase in grain size is the same as for the Pacific models (Table 3).

Table 3
Modelling parameters and results

<table>
<thead>
<tr>
<th></th>
<th>Lithospheric thickness (km)</th>
<th>T at 400 km depth (°C)</th>
<th>Grain size transition depth (°C)</th>
<th>Range in grain size (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Yilgarn</td>
<td>400</td>
<td>1310</td>
<td>250–350</td>
<td>0.5–5</td>
</tr>
<tr>
<td>N. Australia</td>
<td>370</td>
<td>adiabatic</td>
<td>250–350</td>
<td>0.5–5</td>
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<tr>
<td>SE Australia</td>
<td>175</td>
<td>adiabatic</td>
<td>250–350</td>
<td>0.5–5</td>
</tr>
<tr>
<td>Tasman Sea</td>
<td>135</td>
<td>adiabatic</td>
<td>165–350</td>
<td>0.1–5</td>
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<tr>
<td>Tonga-Hawaii</td>
<td>230</td>
<td>adiabatic</td>
<td>165–350</td>
<td>0.1–5</td>
</tr>
<tr>
<td>Pacific</td>
<td>age dependent</td>
<td>adiabatic</td>
<td>165–350</td>
<td>0.1–5</td>
</tr>
</tbody>
</table>

a The adiabatic temperature at 400 km depth for an adibat with a potential temperature of 1300 °C is ~1440 °C.

Calculated geotherms for the Yilgarn craton and Northern Australia are comparable to geotherms determined by Jaupart and Mareschal [35] for Eastern Canadian provinces of the same age. One of their main conclusions was that the heat flow across the Moho is relatively low, which is also the case in our models (Table 2). The anomalously high heat flow observed in Proterozoic regions of Australia is therefore due to relatively high upper crustal heat production, since the seismological model indicates high velocities and hence relatively low temperatures in the 100–300 km depth range. Moreover, when heat production in the mantle portion of the lithosphere is included, the heat-flow from the convecting mantle into the lithosphere is very small. South Eastern Australia is somewhat different in this regard, possibly related to the more recent magmatism.

5. Discussion

5.1. General

Our main aim is to explore how much of the range in velocities observed in continental and oceanic shear wave models can be explained by temperature variations. Our modeling, based on new seismic frequency laboratory data, sought to produce reasonable fits to the seismological models while remaining as simple as possible. The seismological models in this study were chosen because they covered specific regional settings. The main features of those models (LVZ and its age dependence for the Pacific Ocean, substantial high velocity lid below continents, relative velocity variations of up to ±8%) are typical of the much wider suite of published models.

Features which we could not match with our modeling are the constant velocity lid for the Pacific ([36,37]) and the constant or increasing velocities below the crust of the Australian model [38]. Our thermal models like those of Karato and Jung [14] predict decreasing velocities in this depth interval with the highest temperature gradients (see also Section 5.4). With thermal constraints in inversions, Shapiro and Ritzwoller [53] found that for oceanic lithosphere negative gradients in the lid (rather than constant velocity) are compatible with their surface wave data.
Similarly for continents they reject models with positive gradients in the shallow lithosphere in favor of slightly negative gradients, consistent with our modeling.

5.2. Experimental

As highlighted in Section 2 we do not extrapolate very far in temperature or grain size from our experimental conditions in the application of our data to the mantle. The similarity of the exponent of the powerlaw behavior of attenuation in the anelastic regime from laboratory measurements and seismological observations has recently been confirmed by Shito et al. [54], who also emphasized that a value of $\alpha Q$ between 0.2 and 0.4 is inconsistent with the presence of melt. Moreover, the activation volume, needed to constrain the pressure dependence of the relaxation times, is apparently relatively well constrained by seismological observation of $V_s$ and $Q$ (Fig. 4). Although we have established a robust experimentally based model for the viscoelastic behavior of polycrystalline olivine, some aspects of the data and modeling require further investigation.

The upper cutoff time and the Maxwell time have different sensitivities to grain size (i.e. $m_A < m_\alpha$, Table 1). At small grain sizes, $\tau_H$ and $\tau_M$ are close, but they separate at larger grain sizes. Because the steady state behavior of the coarser grained samples is not very well constrained by our experiments with periods to 1020 s [2], the extrapolated behavior at relatively long periods (>100 s) at high temperatures (>1300 °C) for large grain sizes (>10 mm) needs further experimental investigation.

Similarly, our experiments effectively place only an upper bound on the lower cutoff time, necessitating the introduction of the adjustment $\delta \ln J_A(d, T)$ (Eq. (7)). More detailed experiments at relatively low temperature (700–900 °C) are needed to document the attenuation associated with the cumulative dispersion at periods <1 s at higher temperatures.

We have already pointed out the need for a revision of the widely used Raj-Ashby model of grain boundary sliding [18,19] to resolve differences between the model predictions and experimental observations [21].

Finally the viscoelastic relaxation associated with stress-induced migration of dislocations (both dry and in the presence of water) needs to be investigated experimentally.

5.3. Grain size

Our experimental data clearly show the intrinsic grain size dependence of shear modulus and attenuation; therefore grain size needs to be specified in our model calculations. Common estimates of upper mantle grain sizes are in the mm to cm range (e.g. [55] and references therein); this is the grain size range used here. The grain size increase with depth is not uniquely constrained with the current modeling. For a constant grain size of 1 mm it would be difficult to find a mechanism to systematically increase the shear velocity below 200 km (Fig. 4c), but for a grain size of 5 cm the presence of water or melt could reduce velocity and $Q$ in the LVZ. However, the water loss predicted by current models of mantle flow and melt generation at mid-ocean ridges would not readily explain the age dependent deepening and lessening of the LVZ up to ~80–100 My (e.g. [14]) shown by seismological models (Fig. 5).

A possible explanation for the increase in grain size with depth is a change in deformation mechanism. Karato and Wu [56] suggested that a transition from dislocation to diffusion creep occurs with increasing depth at about 200 km, depending on a range of conditions. Hirth and Kohlstedt [55] calculate a similar transition depth for a constant grain size of 1 cm; the transition depth is again dependent on a range of parameters in the flow laws. They point out that the grain size at a depth of 100 km would have to be $<10 \mu$m for diffusion creep to dominate. In the dislocation creep regime the grain size is determined by dynamic recrystallisation, whereas in the diffusion creep regime the grain size is largely determined by grain growth. Seismic anisotropy, which is produced only by dislocation creep, is observed to depths of about 160–200 km beneath the Pacific. It is therefore plausible that grain sizes in the shallow upper mantle, particularly at the relatively low temperatures in the plastically deforming portions of the thermal boundary layer, are smaller due to dynamic recrystallisation during dislocation creep. Grain sizes may be larger in the deeper upper mantle deforming predominantly by diffusion creep (but with a dislocation creep component, see discussion e.g. in [55]). For
continents with their thicker cold, high velocity lid
and shallower temperature gradients in the lithosphere
the transition may be more gradual and extend to
greater depth as indicated by the greater depth of
anisotropy [52] (Table 3).

5.4. Water

The effect of structurally bound water on the
viscoelastic behavior of olivine has not yet been
investigated experimentally; its possible significant
influence is to some extent inferred by analogy with
its effect on viscous behavior observed in finite-strain
deforation experiments [57].

Karato and Jung [14] attribute the seismologically
modeled sharpness of the velocity drop at 60–80 km
below ocean basins (sometimes referred to as Gutenberg discontinuity) to the effect of water. However, in
contrast to seismological models Karato and Jung’s
[14] dry thermal modelling, as well as that of Shapiro
and Ritzwoller [53] and ours (Fig. 4) predicts a
significant negative velocity gradient in the high
velocity lid above the Gutenberg discontinuity, as this
is the depth interval with the largest temperature
gradients in the upper mantle. Gaherty et al. [36]
describe the Gutenberg discontinuity as an impedance
drop occurring within a depth interval of less than 30
km, with surface wave attenuation data consistent with
but not requiring a large drop (p. 22305). A negative
velocity gradient in the lid (decreasing the required
velocity drop below) together with the enhanced
velocity decrease at the onset of anelasticity at ~900
°C (see also Karato and Jung’s [14] dry modelling)
appears therefore consistent with a seismologically
inferred impedance drop over a 30 km depth interval. A
ubiquitous contribution of water to a drop in velocity
below ocean basins is therefore not required; however,
water may plausibly affect the velocity and attenuation
structure for example at subduction zones.

5.5. Major element compositional variations

The primary origin of relatively large scale
compositional variations in the upper mantle (e.g.
the contrast between oceanic and cratonic continental
lithosphere) is assumed to be partial melting and
removal of the melt from “fertile” source rocks. Melt
removal depletes the source rock of lower melting
point components. Regarding shear modulus and
density the important consequences are the simulta-
neous depletion of the residuum in FeO and Al2O3. To
first order, FeO depletion increases the shear modulus
of olivine (and orthopyroxene) and hence the shear
velocity of the bulk rock, but decreases olivine and
bulk rock density. The removal of Al2O3 decreases the
proportion of the aluminous phase (garnet) in the
whole rock. Since garnet is more dense and has a
higher shear modulus than olivine and pyroxenes, a
decrease in the garnet proportion decreases both the
whole rock density and shear modulus.

The combined effects of simultaneous removal of
FeO and Al2O3 on the shear modulus therefore tend to
cancel each other (the olivine shear modulus increases
while the garnet proportion decreases), while both
garnet removal and decreasing iron content decrease
the density. This was pointed out by Jordan [58] and
has recently been substantially updated by Schutt and
Lesher [59]. Jordan [58] and Schutt and Lesher [59]
parameterize bulk rock compositional changes from
experimental melting studies and find that there is
essentially no change in shear velocity in the garnet
stability field as a function of depletion with up to
40% melt removed (a change in olivine mode from
56% to 86%, Mg# ~90–93).

In a different approach, Lee [60] calculates seismic
velocities and density of mantle rocks from the
composition of natural peridotites with a range of
compositions. The compositions of a significant
number of the natural peridotites fall off the “melting
trend” defined by a correlated increase in Mg# and the
proportion of olivine. The main cause in the scatter of
the compositions is likely the re-fertilization by
unrelated, secondary melts after primary melt extrac-
tion. Natural peridotites also originate from a range of
pressure and temperature conditions. Assessing
whether the compositional variability of individual
xenoliths reflects localised or regional variations (at
least on the length scale of surface waves of order of
100 km) is difficult. On a continental scale, a velocity
increase of ~1.2% [60] associated with the extremes in
the range in bulk Mg# (89–93) can not explain the
velocity variation of >10% at 100–200 km depth
between cratonic Western Australia and South Eastern
Australia (Figs. 6 and 7).

A common result of both approaches is that the
difference between olivine shear velocity and bulk
shear velocity is small (≤1%, [60], Table 1; [59], Tables 9 and 11) and not greatly affected by changes in bulk composition (anelasticity is not considered in these studies). The error associated with calculations based only on olivine shear velocity is therefore probably smaller than the uncertainties in most seismological models and the uncertainties in other parameters in the calculations.

An increasing proportion of garnet between 200 and 400 km could contribute to the shear velocity increase shown by seismological models in this depth range. However, Irifune and Ringwood [61] and Irifune [62] demonstrate that the progressive dissolution of pyroxene in garnet with increasing pressure for pyrolite bulk composition occurs mainly at pressures corresponding to depths of 400–480 km. The expected velocity increase for the depth range 200–400 km can be no greater than about 0.06 km/s.

Attenuation is likely to be even less sensitive to composition than shear velocity. Because $Q$ is calculated from the ratio of the real and imaginary parts of the creep function, it is not a function of the unrelaxed compliance ($J_U$), i.e. does not depend on the (anharmonic) value of the shear modulus of the rock. Our experiments so far suggest that the grain boundary viscosity (the key parameter for attenuation due to grain boundary sliding [2,21]) does not vary significantly between high-purity sol–gel derived polycrystals and those saturated with olivine-incompatible trace elements. In more detail, grain boundaries in samples originating from San Carlos olivine contain detectable Ca, Al and Ti, while in grain boundaries of olivine of Sol–Gel origin no trace elements are detectable. Despite this compositional difference, we can not resolve any difference in attenuation or shear modulus (the major element composition of the olivine (~Fo90) is the same for both types of sample). Therefore $Q$ should be even less sensitive to composition than $V_s$ and a primary indicator for lateral temperature variations in the absence of melt.

In summary, while shear velocity and $Q$ are primarily dependent on temperature and grain size, combined seismological and gravity studies may better resolve lateral compositional variations in the upper mantle (e.g. [64,65]). The secondary effect of compositional relative to temperature variations on seismic velocities has also been found in a number of other studies (e.g. [5,7]).

5.6. Depth extent of cratons

A key question regarding the structure of continents is the thickness of lithosphere in cratonic areas [10]. Potential problems for surface-wave models in resolving the depth extent of cratons are their diminishing resolution with depth and the limited availability of models with paths that fall entirely into relatively uniform tectonic provinces. Seismological studies show at most a modest and very deep low velocity zone beneath old cratons [66–69]. A comparison of these shear wave models with velocity profiles calculated from our experimental data shows that for conductive geotherms that join the adiabat at depths less than 200 km a pronounced low velocity zone is unavoidable (Fig. 7). For geotherms joining the adiabat below 250–350 km depth a mild velocity decrease occurs at those depths, as seen in a number of seismological models. For $V_s$ to be near constant throughout the upper mantle, the geotherm needs to join the adiabat deeper than 350 km. Seismological models showing velocities at 300–400 km depth in archean cratic areas that are significantly higher than those for non-cratonic continental areas or beneath ocean basins suggest that temperatures beneath cratons are subadiabatic to transition zone depths.

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