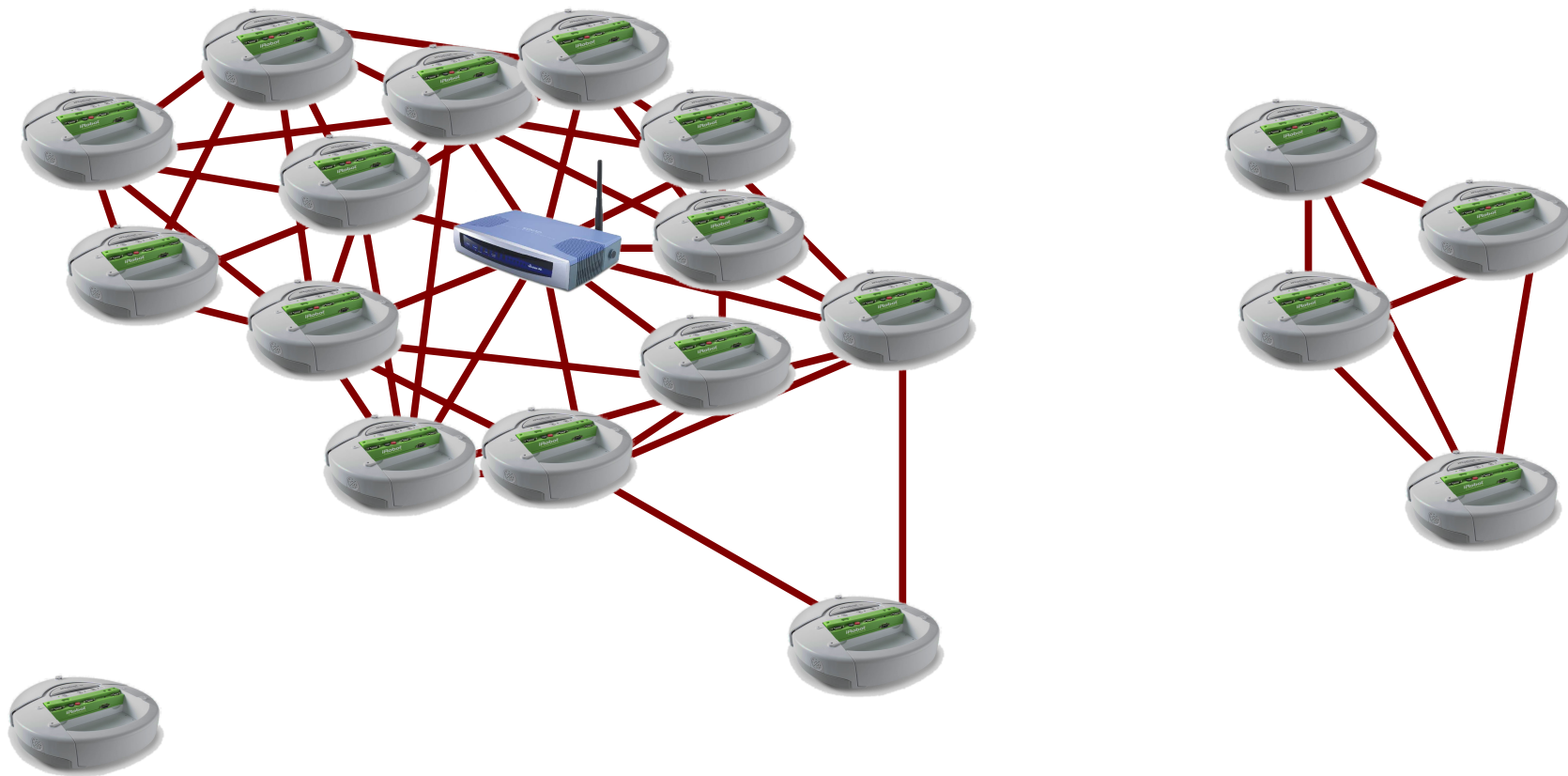


# Behavior Modes for Randomized Robotic Coverage

**Jacob Beal (BBN)**, Nikolaus Correll (MIT),  
Leonardo Urbina (MIT), Jonathan Bachrach  
(Makani Power)

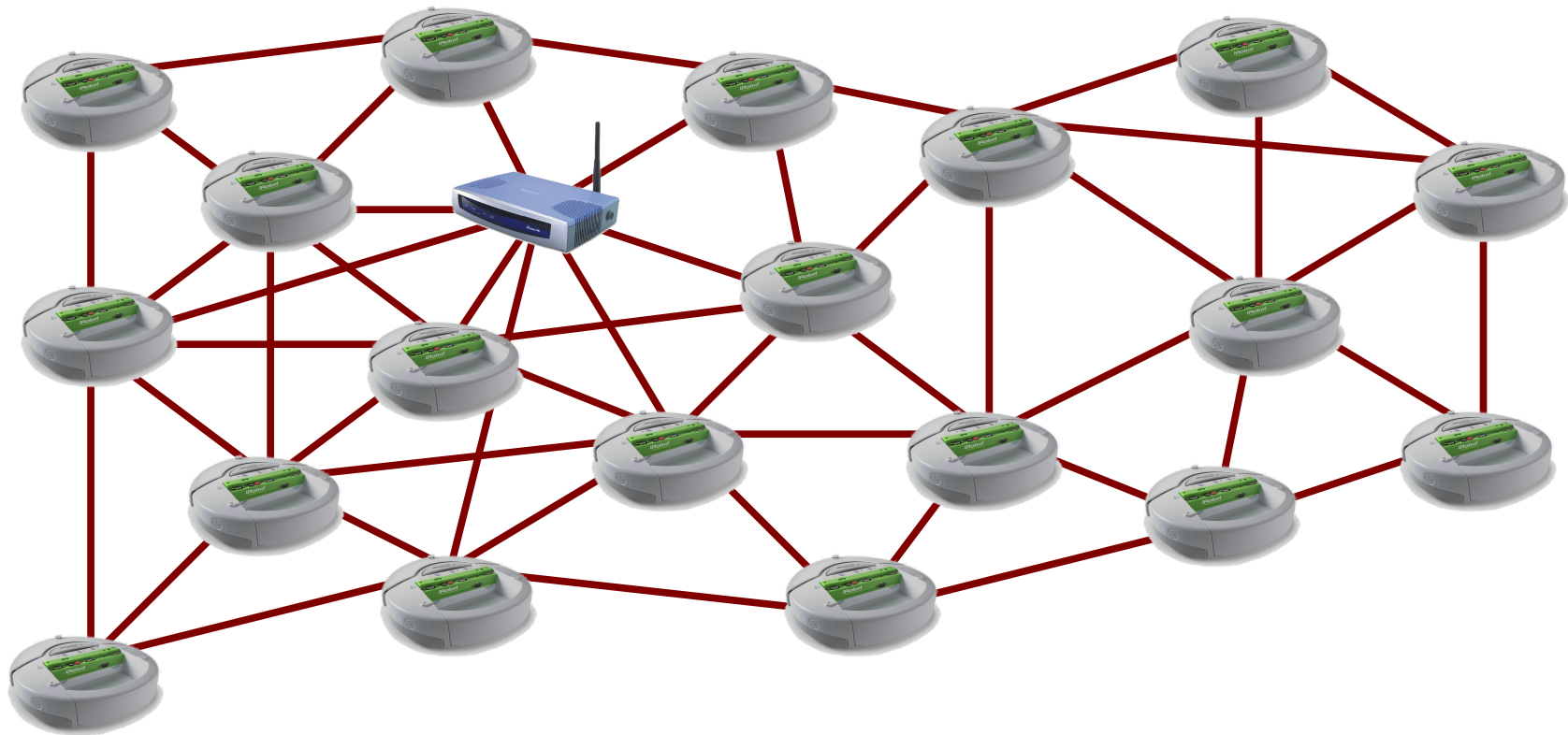
# Coverage

From some initial distribution, move to provide “good” network coverage over a large area



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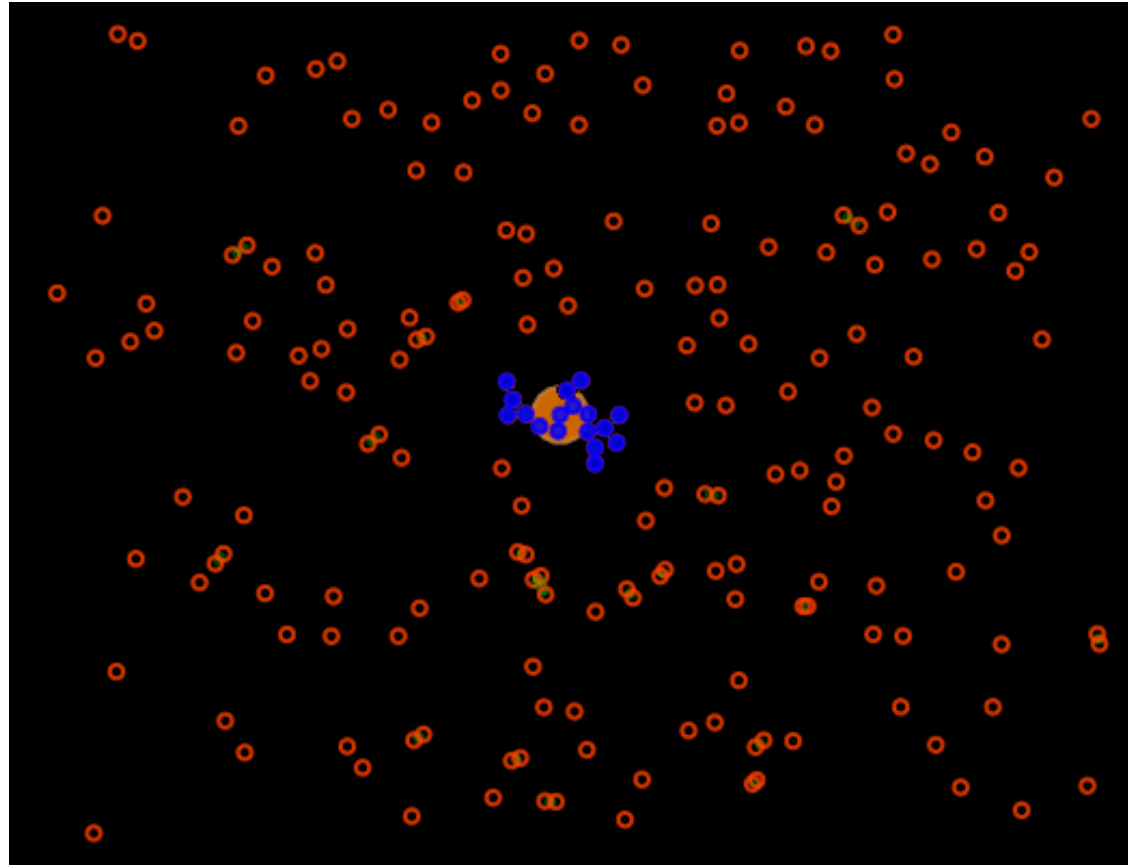
How much coordination is necessary?

# Randomized Coalescence Algorithm

For robot  $i$ :  
IF  $\alpha \leq |nbrs(i)| \leq \beta$   
AND **connected to seed**  
THEN **do nothing**  
ELSE **move**  $v \cdot W_t$   
(where  $W_t$  is a Wiener process)

- Poduri & Sukhatme (DLA)  $O(1/\sqrt{n})$
- Correll (Generalized)

# But does it work?



```
proto -m -l -c "(mov (coalesce (red (= (mid) 0)) 1 5 15))" -n 200 -r 2 -s 0.1 -dist-dim -40 40 -40 40 -fixedpt 0 0
```

# Preview of Results

- Five qualitative domains of behavior
- Random navigation is not sufficient
- Some long-range coordination is necessary

*And now the details...*

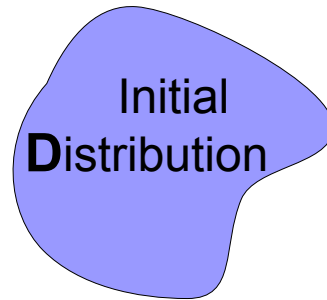
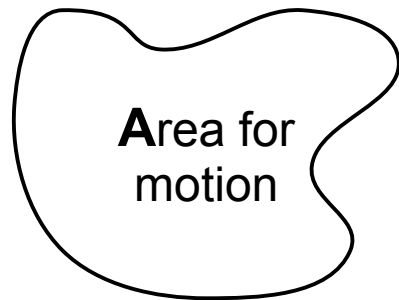
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*(where  $W_t$  is a Wiener process)*

```
(def coalescence (gateway b a max)
  (if (muxor gateway
        (muxand (< (hop-gradient gateway) max)
                 (and (>= (num-nbr) b)
                      (<= (num-nbr) a))))
      (all (blue 1) (tup 0 0))
      (brownian)))
```

# Network Model

- $n$  nodes, radius  $r$  unit disc communication

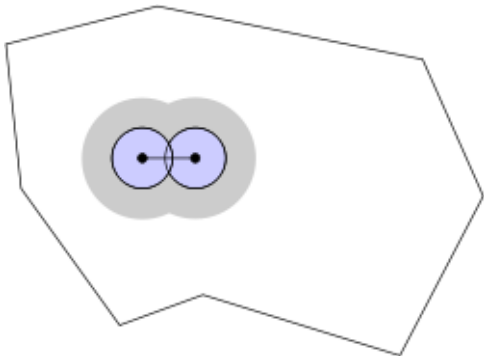




# Bounds on Convergence Area

Tightest

$$T \geq \frac{\pi r^2 n}{4(\beta + 1)}$$



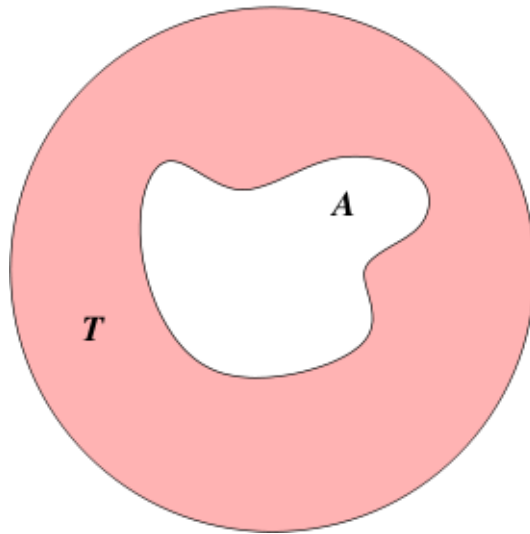
Loosest

$$L \leq n \frac{4r^2}{\alpha}$$



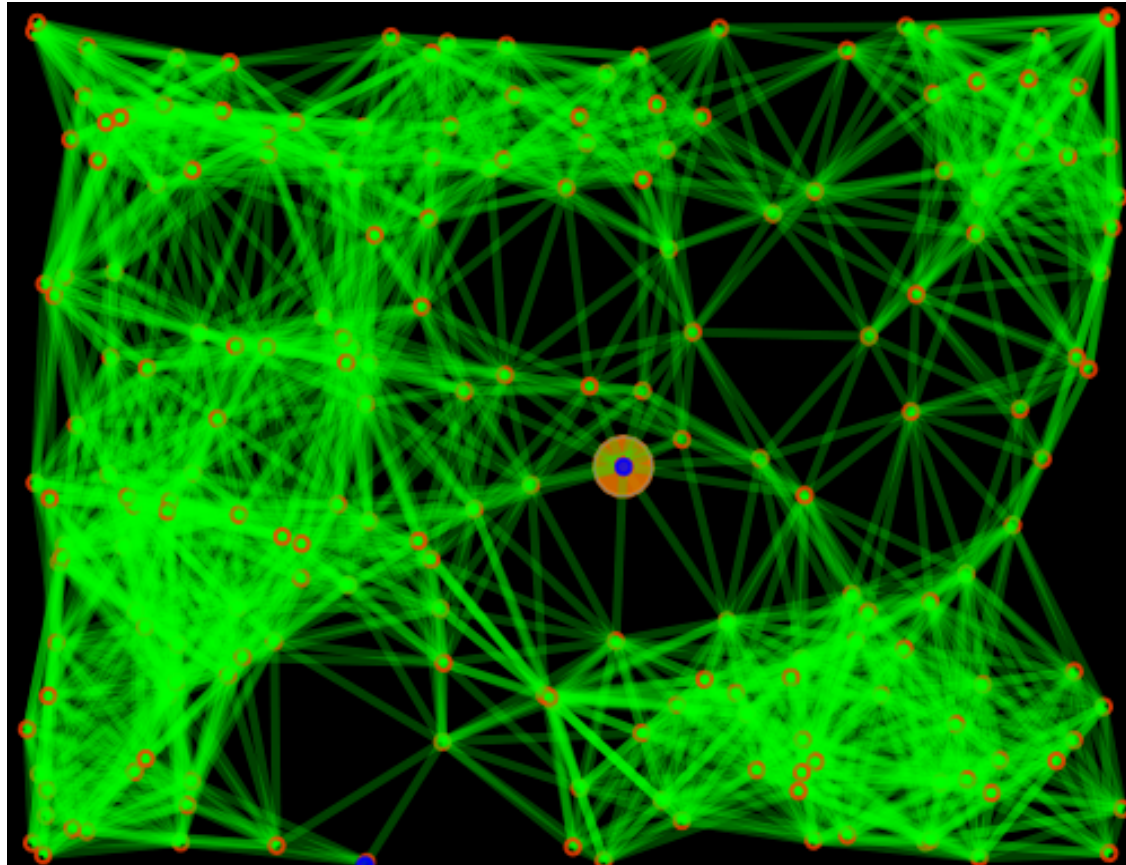
(assuming unit disc connectivity w. radius  $r$ , ignoring edge effects)

# Impossible Conditions



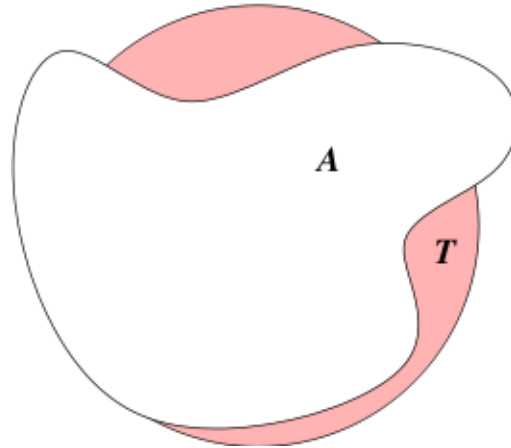
Tightest possible distribution is larger than area

# Impossible Conditions



```
proto -w -m -l -c "(mov (coalesce (red (= (mid) 0)) 1 5 15))" -n 200 -r 20 -s 0.1 -fixedpt 0 0
```

# Critical Conditions

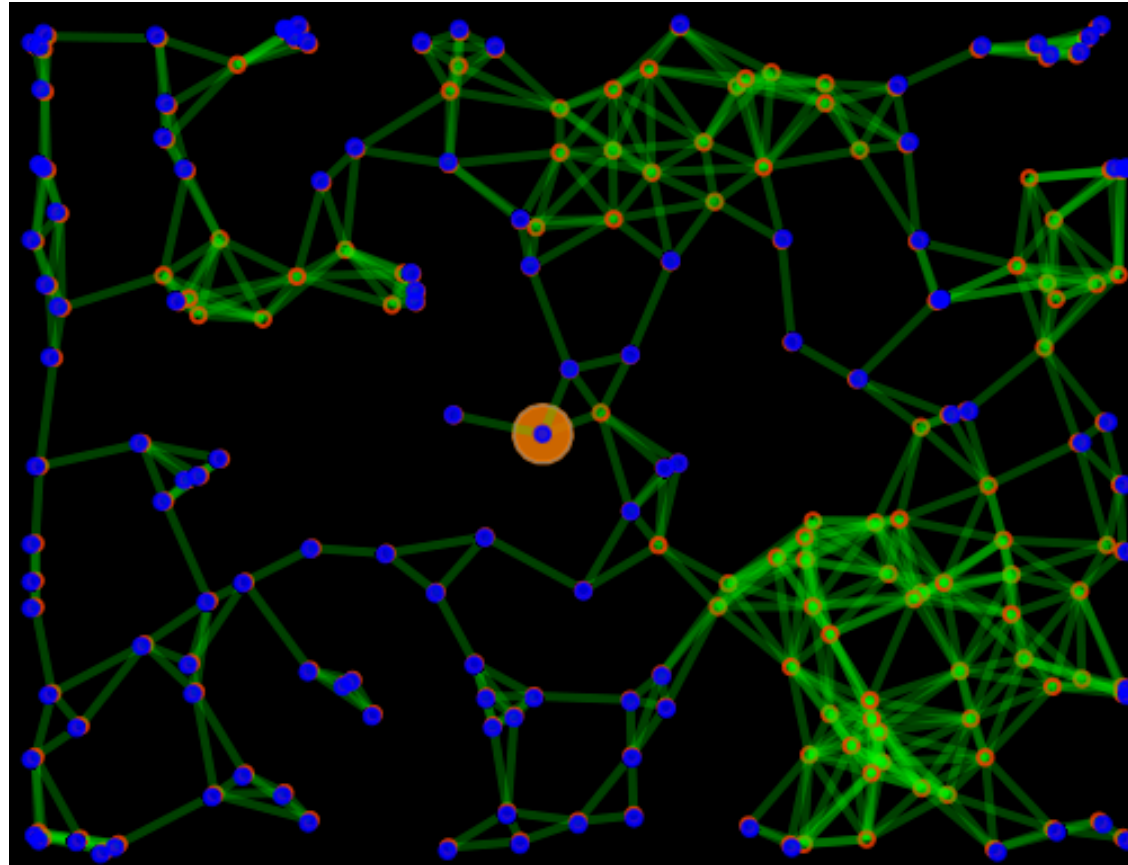


e.g. 2 robots in a 1D space,  $\text{diam}=2r+\epsilon$ ,  $\alpha=\beta=1$ :



$$P(\text{converge}) < \epsilon / (2r + \epsilon)$$

# Critical Conditions



```
proto -w -m -l -c "(mov (coalesce (red (= (mid) 0)) 1 5 15))" -n 200 -r 11 -s 0.1 -fixedpt 0 0
```

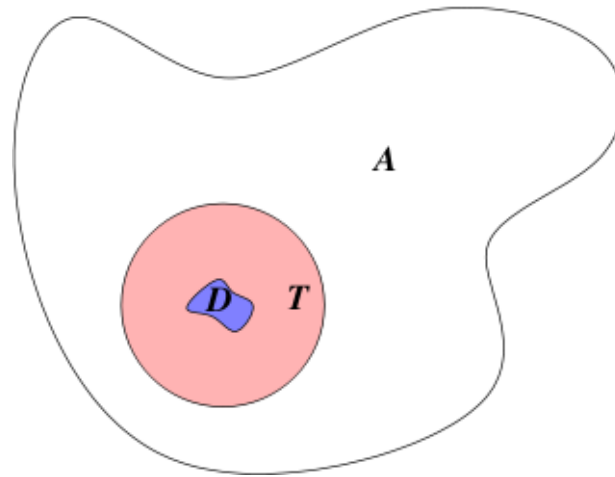
# The Importance of Initial Conditions

- Consider the initial distribution of robots  $D$ :
  - Previous simulations have used  $A \approx D \approx [T, L]$
  - More realistic: box-of-bots ( $D \ll T$ ), airdrop ( $D \gg L$ )
- Random Motion = Diffusion
  - $O(d^2)$  time to move expected distance  $d$

*Diffusion is slow!*

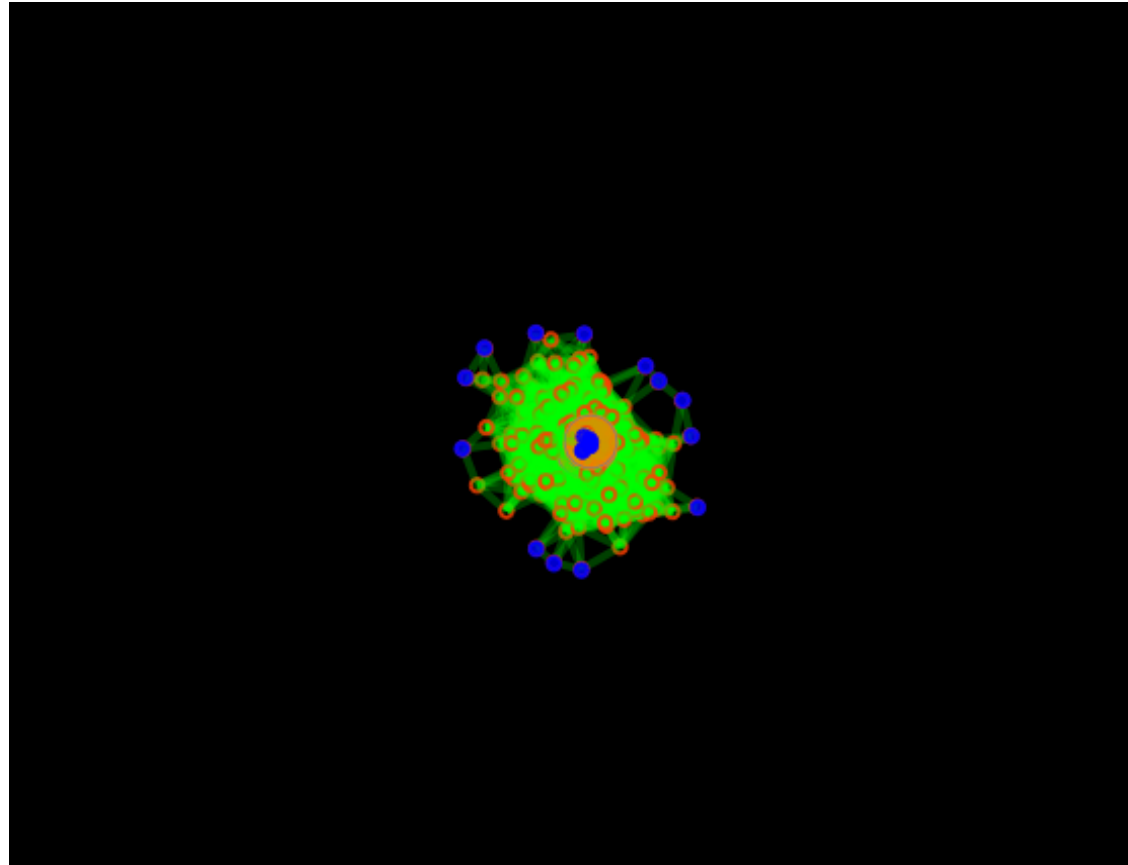
# Dispersion Dominated

Consider opening a box full of robots:



Random walk expected to move  $\sqrt{T}$  in  $\Omega(T)=\Omega(n)$  time

# Dispersion Dominated

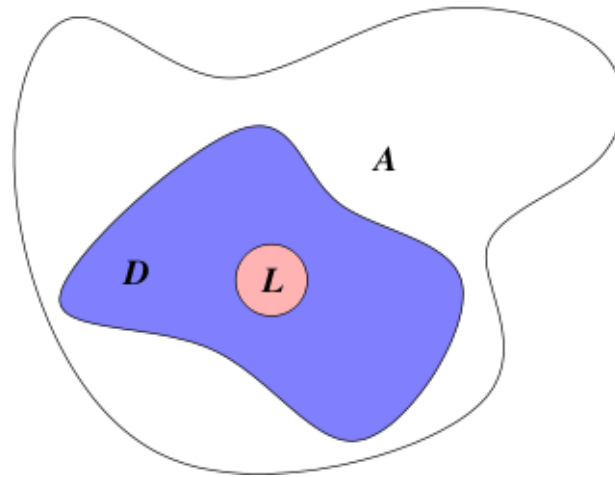


```
proto -w -m -l -c "(mov (coalesce (red (= (mid) 0)) 1 5 15))" -n 200 -r 5 -s 0.1 -dist-dim -5 5 -5 5 -fixedpt 0 0
```



# Discovery Dominated

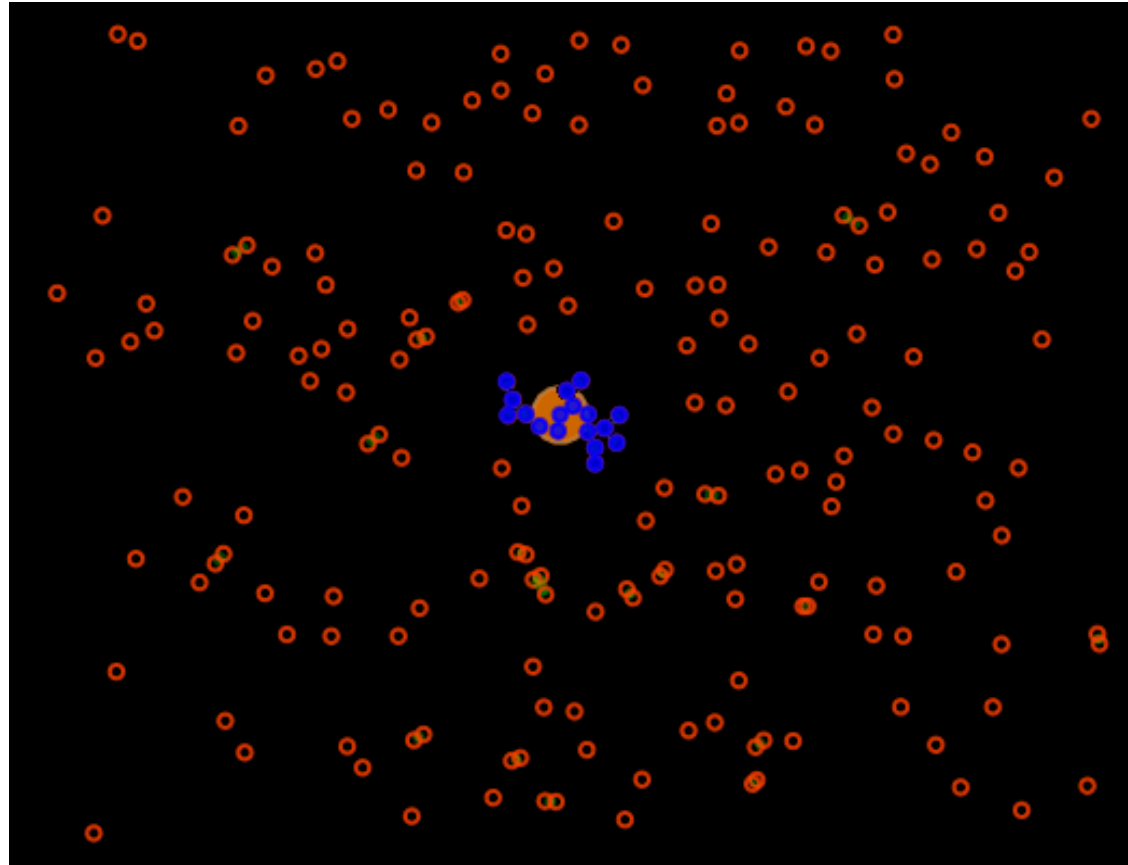
Consider air-dropped robots looking for the seed:



Random walk expected to move  $\sqrt{D}$  in  $\Omega(D)$  time

*Can't be improved without global localization!*

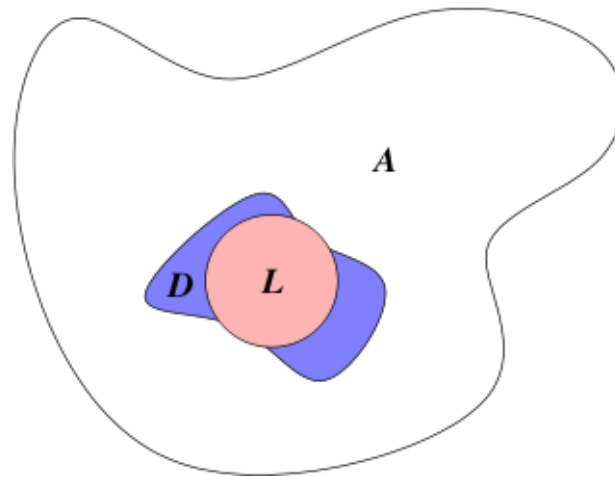
# Discovery Dominated



```
proto -w -m -l -c "(mov (coalesce (red (= (mid) 0)) 1 5 15))" -n 200 -r 2 -s 0.1 -dist-dim -40 40 -40 40 -fixedpt 0 0
```

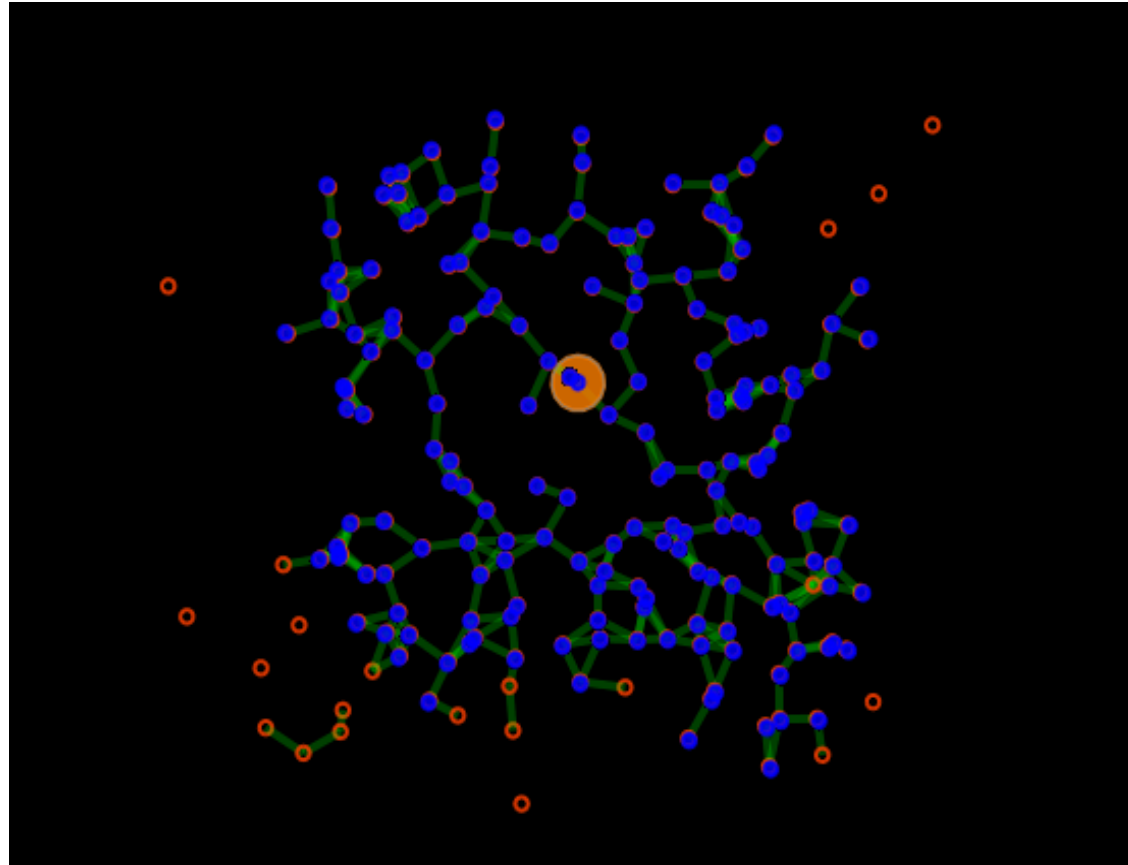
# Fast Convergence

When initial and final distributions are similar, the robots seem to “crystallize”:



Minimum time for message to move seed to edge:  $\Theta(\sqrt{n})$

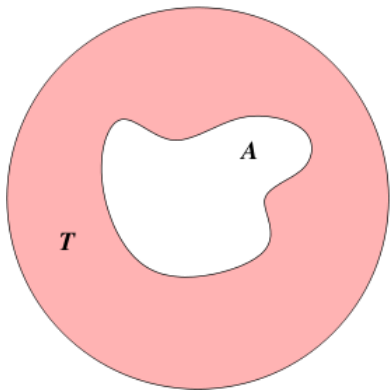
# Fast Convergence



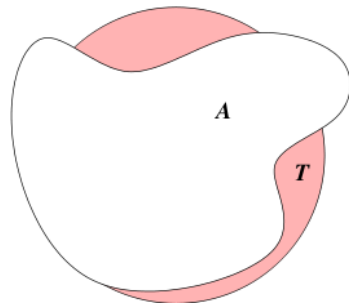
```
proto -w -m -l -c "(mov (coalesce (red (= (mid) 0)) 1 5 15))" -n 200 -r 5 -s 0.1 -dist-dim -30 30 -30 30 -fixedpt 0 0
```

# Results

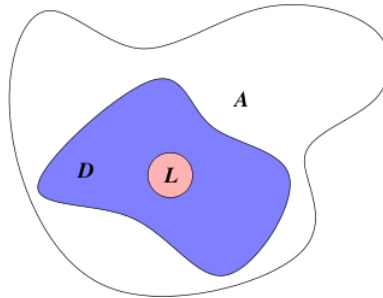
Name	Condition	Convergence	Dominant Phenomenon
Impossible	$A < T$	Impossible	Density too high
Critical	$A \approx T$	Arbitrarily Long	Unlikely perfect arrangement
Discovery	$A \gg D \gg L$	$\Omega(D)$	Difficulty in finding seed
Fast Aggregation	$A \gg D \approx [T, L]$	$\Theta(\sqrt{n})$	“Crystallization” from seed (unproved)
Dispersion	$A \gg T \gg D$	$\Omega(n)$	Diffusion from initial distribution



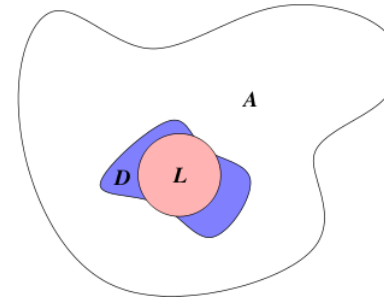
Impossible



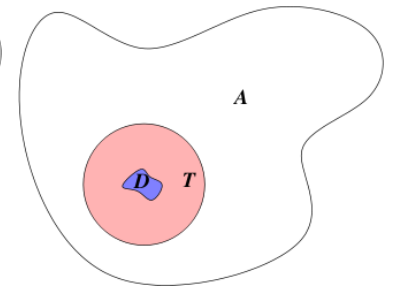
Critical



Discovery



Fast Aggregation



Dispersion

# Contributions

- Five qualitative domains of behavior
- Random navigation is not sufficient
- Some long-range coordination is necessary