

# DeltaRCWA

**A nanophotonics solver for inverse design**

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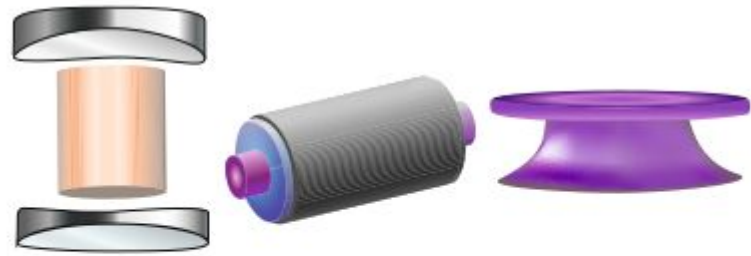
[2] Massachusetts Institute of Technology

# Overview

- *Background:* Photonics
  - *Applications:* Metasurface Design
  - *Key Concept:* Physics-Enhanced Deep Surrogates (PEDS) for PDEs
  - *Conclusion:* DeltaRCWA Progress
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# ***Background: Photonics***

Light (photons) is transformed as it passes through materials, obeying Maxwell's equations



Cavities

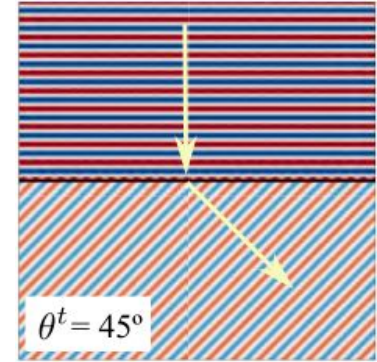
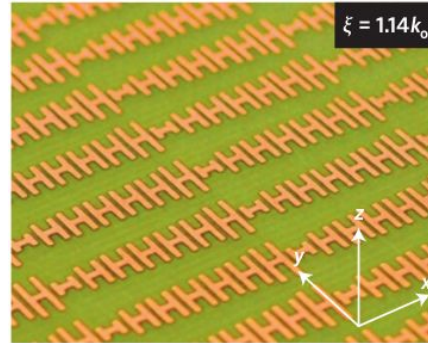
Fibers

Resonators

Molesky et al. (2018) "Inverse Design in Nanophotonics"

# Background: Metasurfaces

Miniaturization of photonic devices leads to improved control of the reflection, transmission, polarization, and phase of light

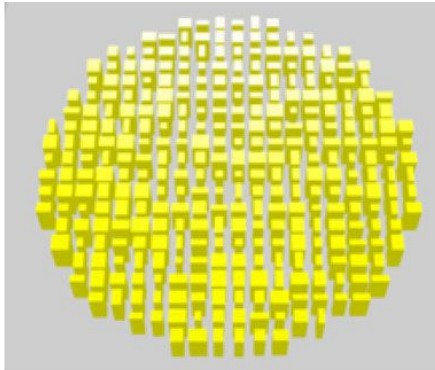


Pérez-Arancibia et al. (2018)  
“Sideways adiabaticity: beyond ray optics for slowly varying metasurfaces”

Yu and Capasso (2014) “Flat Optics with Designer Metasurfaces”

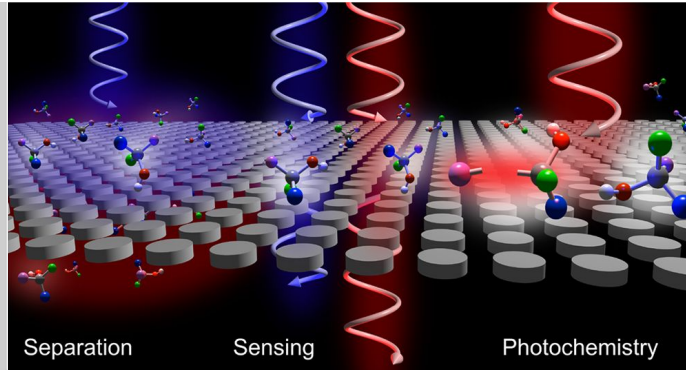
# Applications: Metasurface Design

Special lenses & demultiplexers



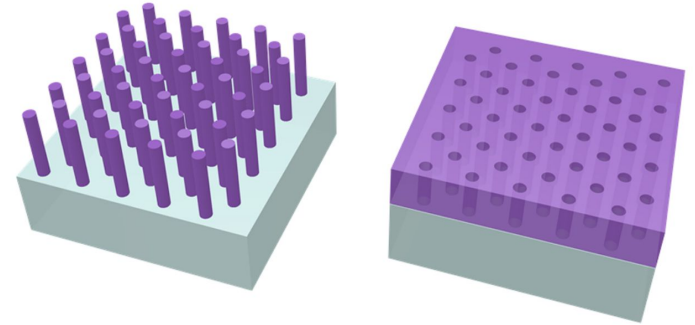
Pestourie et al. (2020)  
“Active learning of deep surrogates for PDEs: application to metasurface design”

Chemistry using chiral light



Solomon et al. (2020)  
“Nanophotonic Platforms for Chiral Sensing and Separation”

Light trapping in ultra-thin solar cells

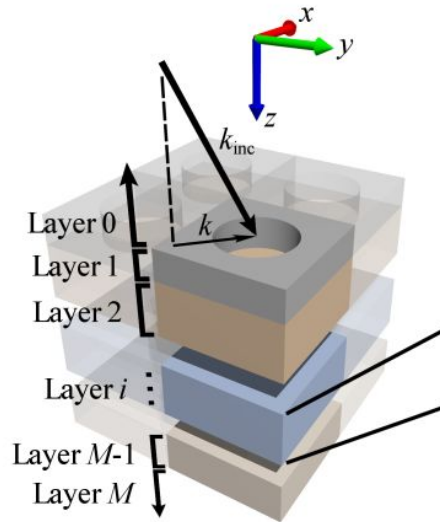


Bauser et al. (2020)  
“Photonic Crystal Waveguides for >90% Light Trapping Efficiency in Luminescent Solar Concentrators”

How do we design  
metasurfaces by  
efficiently solving  
Maxwell's equations?

# Key Concept: Mapping 3d structures to 2d sheets

DeltaRCWA efficiently solves an approximate problem to capture key qualitative physics



Actual metasurface

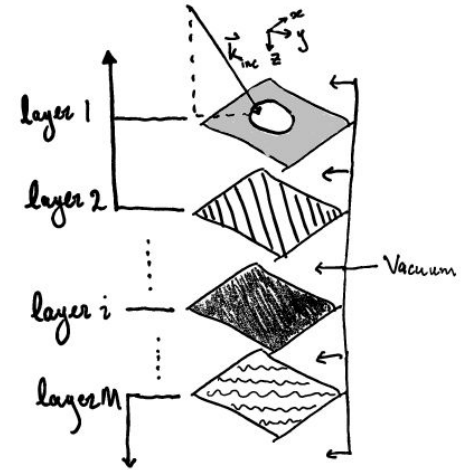
Geometry coarsening



Physics-Enhanced  
Deep Learning

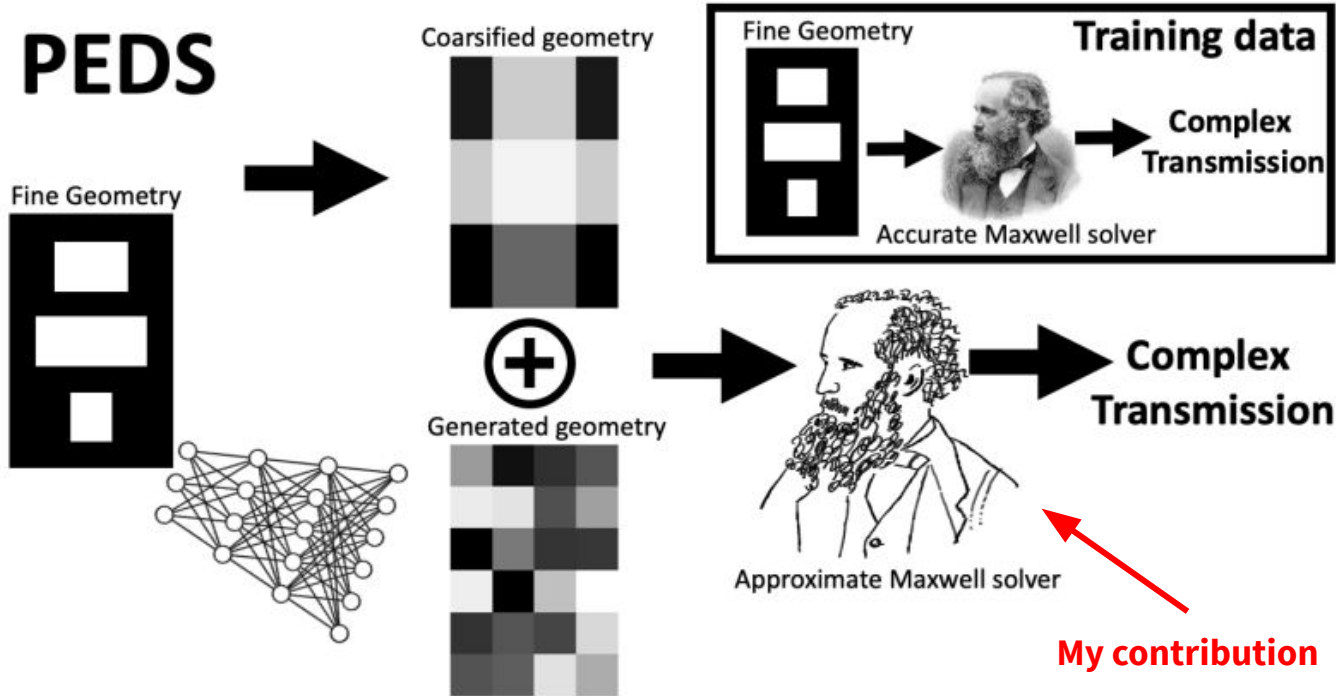


Surrogate solution



Approximate metasurface

# Key Concept: Physics-Enhanced Deep Surrogates





# Conclusion

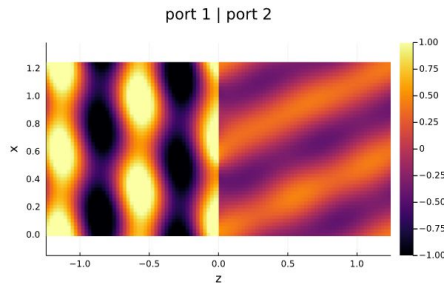
## Progress on DeltaRCWA

- Derived scattering matrix for full 3D simulations
- Implemented scattering matrix and Redheffer star product in a Julia package
- Explored matrix-free methods with iterative solvers to do the same

This project is still active research!

- Thorough validation of DeltaRCWA against different solvers (BIE method)
- Automatic differentiation of DeltaRCWA (Zygote.jl)
- Integration with the deep-learning framework + training with full-wave solvers ( $S^4$ )

Project URL: <https://github.com/lxvm/DeltaRCWA.jl>



# ***Acknowledgements***

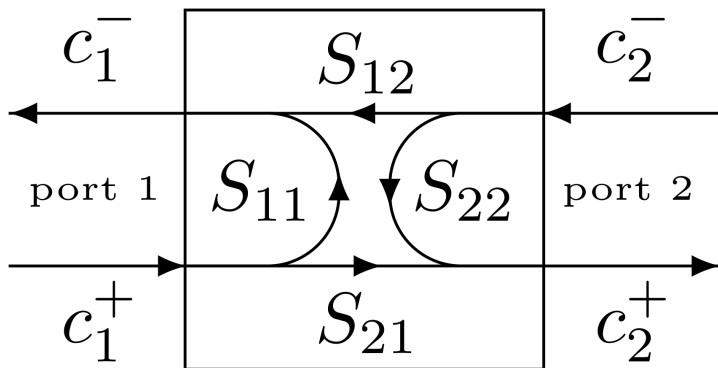
- Funding: Mellon Mays Foundation
- Mentorship: Professor Steven Johnson and Dr. Raphaël Pestourie
- Support: Sarah Zeichner and the Caltech MMUF Cohort



# Questions!



# Numerical Methods Scattering matrices



A Generalized Sheet Transition Condition (GSTC) relates the fields on either side of the sheet in terms of the metasurface parameters

$$\hat{\mathbf{n}} \times (\mathbf{H}_{\parallel}^{i+1} - \mathbf{H}_{\parallel}^i) = \sigma^e (\mathbf{E}_{\parallel}^{i+1} + \mathbf{E}_{\parallel}^i) / 2$$
$$-\hat{\mathbf{n}} \times (\mathbf{E}_{\parallel}^{i+1} - \mathbf{E}_{\parallel}^i) = \sigma^m (\mathbf{H}_{\parallel}^{i+1} + \mathbf{H}_{\parallel}^i) / 2$$

# ***Numerical Methods: Redheffer star product***

Given two scattering matrices from different linear scatterers, this binary operation yields the combined scattering matrix produced by connecting some of the output channels of each scatterer to inputs of the other

