Trivial Mathematics: Solution

- I. Find the values of the constants:
 - **1.** A = 301 (Game that can be won in R V throws (but no fewer))
 - **2.** B = 47 (Smallest number that is a Keith, Carol, and Lucas number)
 - **3.** C = 259 (Decimal representation of K, if K is interpreted as a hexadecimal number)
 - 4. D = 2 (Half of the name of a band who peaked at number P + I on the *Billboard* Hot 100 in 1992 with a song called H (spelled out))
 - **5.** E = 66 (Order that serves a major plot point in *Star Wars: Episode* N G)
 - 6. F = 20 (Episode number in which "I will not do that thing with my tongue" is written repeatedly)
 - 7. G = 17 (Least random number)
 - 8. H = 1 (Building connected to building L and building G U)
 - **9.** I = 8 (Largest perfect power that is one less than a perfect power)
 - 10. J = 2 (Admittees to MIT's class of 2017 with an SAT math score in 600–640)
 - **11.** K = 103 (*A* reversed)
 - 12. L = 5 (Nickname of a comic-strip character whose last name is 95472)
 - **13.** M = 18 (Ed Sheeran-penned song from the album Four)
 - 14. N = 20 (Biological Engineering)
 - **15.** O = 13 (Triskaidekaphobes' fear)

16.
$$P = 2 \left(\sum_{i=0}^{\infty} \frac{1}{2^i} \right)$$

- 17. Q = 4383347 (Patent number for a "Four-bar linkage door hinge")
- 18. R = 19 (Smallest palindromic Roman numeral made from more than one distinct character)
- **19.** S = 223 (Only positive integer that cannot be written as the sum of fewer than 37 positive fifth powers)
- **20.** T = 8 (How many times U has been retired in Major League Baseball)
- **21.** U = 14 (Year of the Roman census in which 4,937,000 citizens were recorded)
- 22. V = 13 (Number on a Tarot card whose Rider-Waite version features a pale horse)
- **23.** W = 10753 (NW 11th & Johnson, to a Portland public-transit app)
- II. Plug the constants into the formula:

$$\left(ABL\left(D^{J}\left(CIM+V\right)\left(EQ+G\right)\left(KP\left(FNU+S\right)\left(TW+\frac{J}{R-H}\right)+O\right)+R\right)\right)^{H}$$

= 315131615199205191612211915145

III. Split 315131615199205191612211915145 into 1- and 2-digit numbers each in $\{1, 2, ..., 26\}$:

 $3\ 15\ 13\ 16\ 15\ 19\ 9\ 20\ 5\ 19\ 16\ 12\ 21\ 19\ 15\ 14\ 5$

IV. Apply the substitution $1 \mapsto A, 2 \mapsto B, \dots, 26 \mapsto Z$:

COMPOSITESPLUSONE

V. Take the values of the constants in positions 4, 6, 8, 9, 10, 12, 14, 15, 16, 18, 20, 21, 22 (the composite-numbered positions)—D, F, H, I, J, L, N, O, P, R, T, U, V—and add 1 to each:

```
2 \ 20 \ 1 \ 8 \ 2 \ 5 \ 20 \ 13 \ 2 \ 19 \ 8 \ 14 \ 13
```

```
\downarrow \\ 3 \ 21 \ 2 \ 9 \ 3 \ 6 \ 21 \ 14 \ 3 \ 20 \ 9 \ 15 \ 14 \\
```

VI. Apply the substitution $1 \mapsto A, 2 \mapsto B, \dots, 26 \mapsto Z$ to get the final answer:

CUBIC FUNCTION

Miscellanea

- $D\,$ The band is U2
- F The show is *The Simpsons*
- $I\ 2^3=8$ and $3^2=9$ are actually the only such pair of perfect powers—a fact first proved in 2002 (Mihǎilescu)
- L "5" (né 555 95472) is from Peanuts
- M The song is by One Direction
- ${\cal N}$ The MIT course number
- S The generalization of g(5) = 37 was conjectured (by Leonard Euler's eldest son Johann) to be $g(n) = 2^n + \left|\left(\frac{3}{2}\right)^n\right| 2$ —so far shown at least for $n \le 471600000$