DISCOVERING AND RECONCILING VALUE CONFLICTS FOR DATA INTEGRATION

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Discovering and Reconciling Value Conflicts for Data Integration

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Abstract

The integration of data from autonomous and heterogeneous sources calls for the prior identification and resolution of semantic conflicts that may be present. Unfortunately, this requires the system integrator to sift through the data from disparate systems in a painstaking manner. In this paper, we suggest that this process can be (at least) partially automated by presenting a methodology and techniques for the discovery of potential semantic conflicts as well as the underlying data transformation needed to resolve the conflicts. Our methodology begins by classifying data value conflicts into two categories: context independent and context dependent. While context independent conflicts are usually caused by unexpected errors, the context dependent conflicts are primarily a result of the heterogeneity of underlying data sources. To facilitate data integration, data value conversion rules are proposed to describe the quantitative relationships among data values involving context dependent conflicts. A general approach is proposed to discover data value conversion rules from the data. The approach consists of five major steps: relevant attribute analysis, candidate model selection, conversion function generation, conversion function selection and conversion rule formation. It is being implemented in a prototype system, DIRECT, for business data using statistics based techniques. Preliminary study indicated that the proposed approach is promising.

1 Introduction

The problem of discovering and resolving data value conflicts for data integration has been studied in the context of heterogeneous and autonomous database systems. In an earlier work, Dayal proposed the use of aggregate functions, e.g. average, maximum, minimum, etc. to resolve discrepancies in attribute values (Dayal 1983). DeMichiel proposed to use virtual attributes and partial values to solve the problem of failing to map an attribute value to a definite value (Demichiel 1989). However, no details given how to map conflicting values in to the common domain of virtual attributes. Tseng, Chen, Yang further generalized the concept of partial values into probabilistic partial values to capture the uncertainty in attributes values (Tseng, Chen & Yang 1993): The possible values of an attribute are listed and given probabilities to indicate their likelihood. Lim, Srisvastava and Shekhar proposed an extended relational model based on Dempster-Shafer Theory of Evidence to deal with the situation where uncertain information arise when the database integration process require information not directly represented in the component databases but can be obtained through some of the data (Lim, Srisvastava & Shekhar 1996). The extended relation uses evidence sets to represent uncertainty information, which allow probabilities to be attached to subsets of possible domain values. Scheuermann and Chong adopted a different view of conflicting attribute values:
different values mean different roles the attribute is performing (Scheuermann & Chong 1994, Scheuermann, Li & Clifton 1996). Therefore, it is not necessary to reconcile the conflicts. What needed is to be able to use appropriate values for different applications. The work of Agarwal et. al addressed the same problem addressed in this paper: resolving conflicts in non-key attributes (Agarwal, Keller, Wiederhold & Saraswat 1995). They proposed an extended relational model, flexible relation to handle the conflicting data values from multiple sources. No attempts were made to resolve the conflicts by converting the values.

As evident from the above brief review, most of the work in the existing literature have placed their emphasis on determining the value of an attribute involving semantic conflicts. In this paper, we argue that those conflicts caused by genuine semantic heterogeneity can be reconciled systematically using data value conversion rules. We proposed a methodology and associated techniques that “mine” data conversion rules from data originating from disparate systems that are to be integrated. The approach requires a training data set consisting of tuples merged from data sources to be integrated or exchanged. Each tuple in the data set should represent a real world entity and its attributes (from multiple data sources) model the properties of the entity. If semantic conflicts exist among the data sources, the values of those attributes that model the same property of the entity will have different values. A mining process first identifies attribute sets each of which involves some conflicts. After identifying the relevant attributes, models for possible conversion functions, the core part of conversion rules are selected. The selected models are then used to analyze the data to generate candidate conversion functions. Finally, a set of most appropriate functions are selected and used to form the conversion rules for the involved data sources. A prototype system for integrating financial and business data, DIRECT (DIscovering and REconciling Conflicts), has been implemented using statistics-based techniques. The system uses partial correlation analysis to identify relevant attributes, Bayesian information criterion for candidate model selection, and robust regression for conversion function generation. Conversion function selection is based on the support of rules. Experiment conducted using a real world data set indicated that the system successfully discovered the conversion rules among data sources containing both context dependent and independent conflicts.

The contributions of our work are as follows. First, we adopted a simple classification scheme for semantic conflicts which is more practical than previous proposals from practitioners’ view. For those context dependent conflicts, proposed data value conversion rules can effectively represent the quantitative relationships among the conflicts. Such rules, once defined or discovered, can be used in resolving the conflicts during data integration. Second, a general approach for mining the data conversion rules from actual data values is proposed. Although the use of conversion functions to solve the semantic heterogeneity problem has been mentioned in the literature (Sciore, Siegel & Rosenthal 1994), no details of discovering such functions were not provided. Our approach can be partially (and in some cases, even fully) automated. Moreover, the proposed approach mines such rules from the data itself and requires limited priori knowledge. The results of preliminary experiments has been promising.

The remainder of the paper is organized as follows. In Section 2, we suggest that conflicts in data values can be categorized into two groups. We show that (data value) conversion rules can be used to describe commonly-encountered quantitative relationships among data gathered from disparate sources. Section 3 describes a general approach aimed at discovering conversion rules from actual data values. A prototype system that implements the proposed approach using statistical techniques is described in
Section 4. Experience with a set of real world data using the system is discussed in Section 5. Finally, Section 6 concludes the paper with discussions on related and future work.

2 Data Value Conflicts and Conversion Rules

For our purposes, conflicts among data values can be of two types: context dependent conflicts and context independent conflicts. Context dependent conflicts represent systemic disparities which are consequences of conflicting assumptions or interpretations in different systems. In many instances, these conflicts involve data conversions of a quantitative nature: this presents opportunities for introducing data conversion rules that can be used for facilitating the resolution of these conflicts. Context independent conflicts, on the other hand, are idiosyncratic in nature and are consequences of random events, human errors, or imperfect instrumentation. By virtue of their idiosyncratic nature, there are no systematic procedures for resolving context independent conflicts. For simplicity, we shall only be concerned with context dependent conflicts in this paper.

2.1 Data value conflicts

To motivate our discussion, we begin with an example of data integration. A stock broker produces manages an investment portfolio for her clients by constantly scanning for opportunities to divest in other counters. Information on current portfolio is generated by some in-house information system, and present the stocks currently held by a customer and their current value. The broker relies on a real-time data feed for updates on other investment opportunities. In our scenario, stocks in the first source forms a subset of all instruments that are reported in the second. As illustrated in Table 1, there may be stocks which can be found in stock (the data-feed) which are not in stk_rpt (the portfolio held by a customer).

Table 1: Example tuples from real-time data feed (stock) and data generated by legacy information source (stk_rpt).

<table>
<thead>
<tr>
<th>stock</th>
<th>stk_rpt</th>
</tr>
</thead>
<tbody>
<tr>
<td>stock</td>
<td>price</td>
</tr>
<tr>
<td>100</td>
<td>65.18</td>
</tr>
<tr>
<td>101</td>
<td>164.43</td>
</tr>
<tr>
<td>102</td>
<td>31.78</td>
</tr>
<tr>
<td>104</td>
<td>69.33</td>
</tr>
</tbody>
</table>

Since we are primarily concerned with data value conflicts in this study, we assume that the schema integration problem and the entity identification (Wang & Madnick 1989) problem are largely solved. Therefore, it is understood that both stk_rpt.price and stock.close are the closing price of a stock of the day despite having different attribute names. Similarly, both stock.volume and stk_rpt.volume are the number of shares traded during the day. Furthermore, it is safe to assume that two entries with the same
key (stock) value refer to the same company’s stock. For example, tuple with stock = 100 in relation stock and tuple with stock = 100 in relation stk_rpt refer to the same stock.

With these assumptions, it will be reasonable to expect that, for a tuple s|s ∈ stock and a tuple t|t ∈ stk_rpt, if s.stock = t.stock, then s.close = t.price and s.volume = t.volume. However, from the sample data, this does not hold. In other words, data value conflicts exist among two data sources. In general, we can define data value conflicts as follows.

**Definition** Given two data sources DS_1 and DS_2 and two attributes A_1 and A_2 that refer to the same property of a real world entity type in DS_1 and DS_2 respectively, if t_1 ∈ DS_1 and t_2 ∈ DS_2 correspond to the same real world object but t_1.A_1 ≠ t_2.A_2, then we say that a data value conflict exists between DS_1 and DS_2.

In the above definition, attributes A_1 and A_2 are often referred as *semantically equivalent* attributes. We refer to the conflict in attribute values as *value conflicts.* Value conflicts is therefore a form of semantic conflict and may occur when similarly defined attributes take on different values in different databases, including synonyms, homonyms, different coding schemes, incomplete information, recording errors, different system generated surrogates and synchronous updates (see (Sheth & Kashyap 1992) for a classification of the various incompatibility problems in heterogeneous databases).

While a detailed classification of various conflicts or incompatibility problems may be of theoretical importance to some, it is also true that over-classification may introduce unnecessary complexity that are not useful for finding solutions to the problem. We adopt instead the Occam’s razor in this instance and suggest that data value conflicts among data sources can be classified into two categories: context dependent and context independent. Context dependent conflicts exist because data from different sources are stored and manipulated under different context, defined by the systems and applications, including physical data representation and database design considerations. Most conflicts mentioned above, including different data type and formats, units, and granularity, synonyms, different coding schemes are context dependent conflicts. On the other hand, context independent conflicts are those conflicts caused by somehow random factors, such as erroneous input, hardware and software malfunctions, asynchronous updates, database state changes caused by external factors, etc. It can be seen that context independent conflicts are caused by poor quality control at some data sources. Such conflicts would not exist if the data are “manufactured” in accordance to the specifications of their owner. On the contrary, data values involving context dependent conflicts are perfectly good data in their respective systems and applications.

The rationale for our classification scheme lies in the observation that the two types of conflicts command different strategies for their resolution. Context independent conflicts are more or less random and non-deterministic, hence cannot be resolved systematically or automatically. For example, it is very difficult, if not impossible, to define a mapping which can correct typographical errors. Human intervention and ad hoc methods are probably the best strategy for resolving such conflicts. On the contrary, context dependent conflicts have more predictable behavior. They are uniformly reflected among all corresponding real world instances in the underlying data sources. Once a context dependent conflict has been identified, it is possible to establish some mapping function that allows the conflict to be resolved automatically. For example, a simple unit conversion function can be used to resolve scaling conflicts, and synonyms can be resolved using mapping tables.
2.2 Data value conversion rules

In this subsection, we define data value conversion rules (or simply conversion rules) which are used for describing quantitative relationships among the attribute values from multiple data sources. For ease of exposition, we shall adopt the notation of Datalog for representing these conversion rules. Thus, a conversion rule takes the form head ← body. The head of the rule is a predicate representing a relation in one data source. The body of a rule is a conjunction of a number of predicates, which can either be extensional relations present in underlying data sources, or built-in predicates representing arithmetic or aggregate functions. Some examples of data conversion rules are described below.

**Example:** For the example given at the beginning of this section, we can have:

\[
\text{stk rpt}(\text{stock, price, volume, value}) \leftarrow \\
\text{exchange-rate}(\text{currency, rate}), \text{stock}(\text{stock, currency, volume_in_K, high, low, close}), \\
\text{price} = \text{close} \times \text{rate}, \text{volume} = \text{volume_in_K} \times 1000, \text{value} = \text{price} \times \text{volume}.
\]

**Example:** For conflicts caused by synonyms or different representations, it is always possible to create lookup tables which forms part of the conversion rules. For example, to integrate the data from two relations \(D_1.\text{student}(\text{sid, sname, major})\) and \(D_2.\text{employee}(\text{eid, ename, salary})\), into a new relation \(D_1.\text{std_emp}(\text{id, name, major, salary})\), we can have a rule

\[
D_1.\text{std_emp}(\text{id, name, major, salary}) \leftarrow \\
D_1.\text{student}(\text{id, name, major}), D_2.\text{employee}(\text{eid, name, salary}), D_1.\text{same_person}(\text{id,eid}).
\]

where \(\text{same_person}\) is a relation that defines the correspondence between the student id and employee id. When the size of the lookup table is small, it can be defined as rules without bodies. One widely cited example of conflicts among student grade points and scores can be specified by the following set of rules:

\[
D_1.\text{student}(\text{id, name, grade}) \leftarrow D_2.\text{student}(\text{id, name, score}), \text{score-grade}(\text{score, grade}). \\
\text{score-grade}(4, 'A'). \\
\text{score-grade}(3, 'B'). \\
\text{score-grade}(2, 'C'). \\
\text{score-grade}(1, 'D'). \\
\text{score-grade}(0, 'F').
\]

One important type of conflicts mentioned in literature in business applications is aggregation conflict (Kashyap & Sheth 1996). Aggregation conflicts arise when an aggregation is used in one database to identify a set of entities in another database. To be able to define conversion rules for attributes involving aggregation conflicts, we can extend the traditional datalog to include aggregate functions. For example,

\[
\text{sales_summary}(\text{part, sales}) \leftarrow \text{sales}(\text{date, customer, part, amount}), \text{sales} = \text{SUM}(\text{part, amount}).
\]

can be used to resolve the conflicts between \text{sales}\_\text{summary} and \text{sales}, where \text{sales}\_\text{summary}.\text{sales} is the total sales for a particular part in the \text{sales} table. Here, \(\text{SUM}(\text{part, amount})\) is an aggregate function with two arguments. Attribute \text{part} is the \text{group} - by attribute and \text{amount} is the attribute on
which the aggregate function applies. In general, an aggregate function can take \( n + 1 \) attributes where the last attribute is used in the aggregation and others represent the “group-by” attributes. For example, if the \( \text{sales\_summary} \) is defined as the relation containing the total sales of different parts to different customers. The conversion rule could be defined as follows:

\[
\text{sales\_summary}(\text{part}, \text{customer}, \text{sales}) \leftarrow \\
\text{sales}(\text{date}, \text{customer}, \text{part}, \text{amount}), \text{sales} = \text{SUM}(\text{part}, \text{customer}, \text{amount}).
\]

We like to emphasize that it is not our intention to argue about appropriate notations for data value conversion rules and their respective expressive power. For different application domains, the complexity of quantitative relationships among conflicting attributes could vary dramatically and this will require conversion rules having different expressive power (and complexity). The research reported here is primarily driven by problems reported for the financial and business domains; for these types of applications, a simple Datalog-like representation has been shown to provide more than adequate representations. For other applications (e.g., in the realm of scientific data), the form of rules could be extended. Whatever the case may be, the framework set forth in this paper can be used profitably to identify conversion rules that are used for specifying the relationships among attribute values involving context dependent conflicts.

### 3 Mining Conversion Rules from Data

In this section, we describe our approach for circumventing semantic conflicts is to discover data conversion rules from data that are redundantly present in multiple overlapping data sources. The methodology underlying this approach is depicted schematically in Figure 1 and has been implemented in a prototype system. The system consists of two subsystems: Data Preparation and Rule Mining. The data preparation subsystem prepares a data set – the training data set – to be used in the rule mining process. The rule mining subsystem analyzes the training data to generate candidate conversion functions. The data value conversion rules are then formed using the selected conversion functions.

#### 3.1 Training data preparation

The objective of this subsystem is to form a training data set to be used in the subsequent mining process. The training data set should contain a sufficient number of tuples from two data sources with value conflicts, that is, tuples referring to the same real world entity but having different values for the same property (attribute).

To determine if two tuples \( t_1, t_1 \in DS_1 \) and \( t_2, t_2 \in DS_2 \) represent the same real world entity is an entity identification problem. In some cases, this problem can be easily resolved. For example, the common keys of entities, such as a person’s social security number and a company’s registration number, can be used to identify the person or the company in most of the cases. However, in large number of cases, entity identification is still a rather difficult problem (Lim, Srivastava, Shekhar & Richardson 1993, Wang & Madnick 1989). To determine whether two attributes \( A_1 \) and \( A_2 \) in \( t_1 \) and \( t_2 \) model the same property of the entity is sometimes referred to as the attribute equivalence problem. This problem has received much attention in the schema integration literature (see for instance, (Chatterjee & Segev 1991, Larson, Navathe
& Elmasri 1989, Litwin & A.Abdellatif 1986)). One of the major difficulties in identifying equivalent attributes lies in the fact that the anomaly cannot be simply determined by the syntactic or structural information of the attributes. Two attributes modeling the same property may have different names and different structures but two attributes modeling different properties can have the same name and same structures.

In our study, we will not address the entity identification problem and assume that the data to be integrated have common identifiers so that tuples with the same key represent the same real world entity. This assumption is not unreasonable if we are dealing with a specific application domain. Especially for training data set, we can verify the data manually in the worst case. As for attribute equivalence, as we can see later, the rule mining process has to implicitly solve part of the problem.

3.2 Data value conversion rule mining

Like any knowledge discovery process, the process of mining data value conversion rules is a complex one. More importantly, the techniques to be used could vary dramatically depending on the application domain and what is known about the data sources. In this subsection, we will only briefly discuss each of the modules. A specific implementation for financial and business data based on statistical techniques will be discussed in the next section.

As shown in Figure 1 the rule mining process consists of the following major modules: Relevant Attribute Analysis, Candidate Model Selection, Conversion Function Generation, Conversion Function Selection, and Conversion Rule Formation. In case no satisfactory conversion functions are discovered, training data is reorganized and the mining process is re-applied to confirm that there indeed no functions exist. The system also tries to learn from the mining process by storing used model and discovered
functions in a database to assist later mining activities.

3.2.1 Relevant attribute analysis

The first step of the mining process is to find sets of relevant attributes. These are either attributes that are semantically equivalent or those required for determining the values of semantically equivalent attributes. As mentioned earlier, semantically equivalent attributes refer to those attributes that model the same property of an entity type. In the previous stock and stk_rqpt example, stock.close and stk_rqpt.price are semantically equivalent attributes because both of them represent the last trading price of the day. On the other hand, stock.high (stock.low) and stk_rqpt.price are not semantically equivalent, although both of them represent prices of a stock, have the same data type and domain.

The process of solving this attribute equivalence problem can be conducted at two levels: at the metadata level or at the data level. At the metadata level, equivalent attributes can be identified by analyzing the available metadata, such as the name of the attributes, the data type, the descriptions of the attributes, etc. DELTA is an example of such a system (Benkley, Fandozzi, Housman & Woodhouse 1995). It uses the available metadata about attributes and converts them into text strings. Finding corresponding attributes becomes a process of searching for similar patterns in text strings. Attribute equivalence can also be discovered by analyzing the data. An example of such a system is SemInt (Wen-Syan Li 1994), where corresponding attributes from multiple databases are identified by analyzing the data using neural networks. In statistics, techniques have been developed to find correlations among variables of different data types. In our implementation described in the next section, partial correlation analysis is used to find correlated numeric attributes. Of course, equivalent attributes could be part of available metadata. In this case, the analysis becomes a simple retrieval of relevant metadata.

In addition to finding the semantically equivalent attributes, the relevant attributes also include those attributes required to resolve the data value conflicts. Most of the time, both metadata and data would contain some useful information about attributes. For example, in relation stock, the attribute currency in fact contains certain information related to attributes low, high and close. Such informative attributes are often useful in resolving data value conflicts. The relevant attribute sets should also contain such attributes.

3.2.2 Conversion function generation

With a given set of relevant attributes, \{A_1, ... A_k, B_1, ... B_l\} with A_1 and B_1 being semantically equivalent attributes, the conversion function to be discovered

\[ A_1 = f(B_1, ..., B_l, A_2, ..., A_k) \]  

should hold for all tuples in the training data set. The conversion function should also hold for other unseen data from the same sources. This problem is essentially the same as the problem of learning quantitative laws from the given data set, which has been a classic research area in machine learning. Various systems have been reported in the literature (Langley, Simon, G.Brashaw & Żytkow 1987, Kokar 1986, Wu & Wang 1991, Żytkow & Baker 1991) Statisticians have also developed both theories and sophisticated
techniques to solve the problems of associations among variables and prediction of values of dependent variables from the values of independent variables.

Most of the systems and techniques require some prior knowledge about the relationships to be discovered, which is usually referred as models. With the given models, the data points are tested to see whether the data fit the models. Those models that provide the minimum errors will be identified as discovered laws or functions. We divided the task into two modules, the candidate model selection and conversion function generation. The first module focuses on searching for potential models for the data from which the conversion functions are to be discovered. Those models may contain certain undefined parameters. The main task of the second module is to have efficient algorithms to determine the values of the parameters and the goodness of the candidate models in these models. The techniques developed in other fields could be used in both modules. User knowledge can also be incorporated into the system. For example, the model base is used to store potential models for data in different domains so that the candidate model selection module can search the database to build the candidate models.

### 3.2.3 Conversion function selection and conversion rule formation

It is often the case that the mining process generates more than one conversion functions because it is usually difficult for the system to determine the optimal ones. The conversion function selection module needs to develop some measurement or heuristics to select the conversion functions from the candidates. With the selected functions, some syntactic transformations are applied to form the data conversion rules as specified in Section 2.

### 3.2.4 Training data reorganization

It is possible that no satisfactory conversion function is discovered with a given relevant attribute set because no such conversion function exists. However, there is another possibility from our observations: the conflict cannot be reconciled using a single function, but is reconcilable using a suitable collection of different functions. To accommodate for this possibility, our approach includes a training data reorganization module. The training data set is reorganized whenever a single suitable conversion function cannot be found. The reorganization process usually partitions the data into a number of partitions. The mining process is then applied in attempting to identify appropriate functions for each of the partition taken one at a time. This partitioning can be done in a number of different ways by using simple heuristics or complex clustering techniques. In the case of our implementation (to be described in the next section), a simple heuristic of partitioning the data set based on categorical attributes present in the data set is used. The rationale is, if multiple functions exist for different partitions of data, data records in the same partition must have some common property, which may be reflected by values assumed by some attributes within the data being investigated.

### 4 DIRECT: A Prototype System

The strategy which we have described in the preceding section has been implemented in a prototype system, DIRECT (DIscovers and REconciles ConflicTs), thus allowing the proposed methodology
and techniques to be verified both experimentally and in the context of a real application. The system is developed with a focus on financial and business data for a number of reasons. First, the relationships among the attribute values for financial and business data are relatively simpler compared to engineering or scientific data. Most relationships are linear or products of attributes. Second, business data do have some complex factors. Most monetary figures in business data are rounded up to the unit of currency. Such rounding errors can be viewed as noises that are mixed with the value conflicts caused by context. As such, our focus is to develop a system that can discover conversion rules from data with noises. The basic techniques used are from statistics and the core part of the system is implemented using S-Plus, a programming environment for data analysis. In this section, we describe the major statistical techniques used in the system.

4.1 The basic techniques

DIRECT uses Partial Correlation Analysis (PCA) to identify relevant attributes since it is well known that properly used, partial correlation analysis can uncover spurious relationships, identify intervening variables, and detect hidden relationships that are present in a data set.

It is important to take note that correlation and semantic equivalence are two different concepts. A person’s height and weight may be highly correlated, but are semantically distinct. However, since semantic conflicts arise from differences in the representation schemes and these differences are uniformly applied to each entity, we expect a high correlation to exist among the values of semantically equivalent attributes. Partial correlation analysis can at least isolate the attributes that are likely to be related to one another for further analysis.

In order to discover quantitative relationships among the identified relevant attributes, another well known statistical technique, regression analysis is implement in DIRECT. To deal with noises in data, such as rounding errors, we implemented the Least Trimmed Squares (LTS) regression method (Rousseeuw & Hubert 1997). LTS regression, unlike the traditional Least Square (LS) regression that tries to minimize the sum of squared residuals of all data points, minimizes a subset of the ordered squared residuals, and leave out those large squared residuals, thereby allowing the fit to stay away from those outliers and leverage points. Compared with other robust techniques, like Least Median Square (LMS) regression, LTS also has a very high breakdown point: 50%. That is, it can still give a good estimation of model parameters even half of the data points are contaminated. More importantly, a faster algorithm exists to estimate the parameters (Burns 1992).

4.2 Bayesian information criterion based candidate model selection

Given a set of relevant attributes, a model is required before performing regression. The model specifies the number of attributes that should actually be included and the basic relationship among them, e.g., linear, polynomial, logarithmic, and etc. There are a number of difficulties regarding selecting the model for regression. First, with \( n \) independent attributes, a model can include 1 to \( n \) attributes with any combinations. That is, even just considering the linear functions, there could be a large number of possible models. Second, it is often the case that, a given data set can fit into more than one model. Some of them

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\[^5\]Aggregation conflicts are not considered in this paper.
are equally good. Third, if there is in fact no valid model, the regression may still try to fit the data into the model that may give the false impression that the relationship given is valid.

A number of techniques have been developed to automatically select and rank models from a set of attributes (Miller 1990). Recently, Raftery introduced the BIC, Bayesian Information Criterion, an approximate to Bayes factors used to compare two models based on Bayes’s theorem (Raftery 1995). For different regression functions, the BIC takes different forms. In the case of linear regression, $BIC_k$ of a model $M_k$ can be computed as

$$BIC = N\log(1 - R^2_k) + p_k \log N$$  \hspace{1cm} (2)$$

where $N$ is the number of data points, $R^2_k$ is the value of adjusted $R^2$ for model $M_k$ and $p_k$ is the number of independent attributes. Using the BIC values of models, we can rank the models. The smaller the BIC is, the better the model is to fit the data. One important principle in comparing two nested models is so called Occam’s Window. For two models, $M_k$ and $M_{k+1}$ where $k$ is the number of independent attributes. The essential idea is that, if $M_k$ is better than $M_{k+1}$, model $M_{k+1}$ is removed. However, if model $M_{k+1}$ is better, it requires a certain "difference" between two models to cause $M_k$ to be removed. That is, there is an area, the Occam’s Window, where $M_{k+1}$ is better than $M_k$ but not better enough to cause $M_k$ being removed. The size of Occam’s Window can be adjusted. Smaller Occam’s Window size will cause more models to be removed, as we can see from the example given in the next subsection. The following procedure highlights this candidate model selection process.

1. Given a set of relevant attributes, form the candidate model set by including all possible models;
2. From the candidate model set, remove all the models that are vastly inferior compared to the model which provides the best prediction;
3. Remove those models which receive less support from the data than any of their simpler submodels, i.e., models with less independent attributes;
4. Whenever a model is removed from the candidate model set in the above two steps, all its submodels are also removed.

### 4.3 Acceptance criteria of generated conversion functions

Since regression can always generate some conversion functions given a data set, one key issue in our implementation is to find the criteria that can be used to determine the genuine conversion functions. To address this issue of acceptance criterion, we defined a measure, support, to evaluate the goodness of a discovered regression function (conversion function) based on recent work of Hoeting, Raftery and Madigan (Hoeting, Raftery & Madigan 1995). A function generated from the regression analysis is accepted as a conversion function only if its support is greater than a user specified threshold $\gamma$. The support of a regression function is defined as

$$support = \frac{\text{Count}\{|y'_i|(|y_i - y'_i|/\text{scale}) <= \epsilon\}}{N}$$

(3)
where \( i \in (1, N) \), \( y_i \) is the actual value of the dependent attributes for the \( i_{th} \) point, \( y'_i \) is the predicted value of the dependent value using the function for the \( i_{th} \) point, \( \epsilon \) is a user-defined parameter that represents the required prediction accuracy, \( N \) is the number of the total points in the data set and \( Count \) is a function that returns the number of data points satisfying the conditions. \( scale \) in Equation 3 is a robust estimate of the residuals from the regression function, defined as follows:

\[
scale = 1.4826 \cdot \text{median}(|(Y - Y') - \text{median}(Y - Y')|)
\]

(4)

where \( \text{median}(\cdot) \) is a function that returns the median value of its vector. \( Y \) and \( Y' \) are the vector of the actual value and the predicted value using the regression function for the dependent attribute respectively. Figure 2 summarizes the procedure of conversion function generation.

---

**Conversion Function Generation**

*Input:* Training data set \( D \), Candidate model set \( M \), \( \epsilon, \gamma \).

*Output:* Set of the conversion functions: \( F \).

\[
F = \{ \} ;
\]

**foreach** model \( m \in M \) **do**

Perform LTS regression using \( D \) and \( m \) to obtain a regression function \( f \);

Compute \( scale \) using Equation 4 for \( D \);

Compute \( support \) using Equation 3 with given \( \epsilon \);

if \( support \geq \gamma \) then \( F = F + \{f\} \);

---

The \( support \) indicates the percentage of data points whose residuals are within certain range of the scale estimate, \( \epsilon \cdot scale \). In other words, those points with residuals greater than \( \epsilon \cdot scale \) are identified as outliers. To determine whether a regression function should be accepted, user specifies a minimum support, \( \gamma \). The system only generates those functions with \( support > \gamma \). Two parameters, \( \epsilon \) and \( \gamma \) have different meanings. \( \epsilon \) *in fact specifies the requirement of the conversion precision required* in our case. Taking simple unit conversion as an example. One foot is equal to 0.3048 meters. If two length attributes \( L_1 \) and \( L_2 \) in two data sources are represented in foot and meter respectively, because of the effect of rounding, values of \( L_2 \) corresponding to \( L_1 = \{10000, 1000, 100\} \) will be \( \{3048.0, 304.8, 30.5\} \). A conversion function

\[
L_2 = 0.3048 \cdot L_1
\]

(5)

is the correct function although the point \((100, 30.5)\) does not lie on the line. It cannot be viewed as a genuine outlier. With properly specified \( \epsilon \) value, the support of Equation 5 can be still 100%. On the other hand, \( \gamma \) *reflects our confidence to the quality of data: with \( \gamma < 1 \), we are prepared to accept the fact that there will be at least \( N \cdot (1 - \gamma) \) erroneous data points*. Of course, this is only valid if we have good estimate of \( \epsilon \). A good practice is to first set a bit low \( \gamma \) and a bit tight \( \epsilon \) so that some candidate functions could be generated even with large number of outliers. Depending on whether the detected outliers are
genuine outliers or data points still with acceptable accuracy, the value of $\epsilon$ and $\gamma$ can be adjusted.

### 4.4 A running example with synthetic data

To illustrate the workings of the prototype system, we present here the detailed results obtained from DIRECT when a synthetic data set is used as the training data. The data set simulates the stock data integration process mentioned at the beginning in this paper: A broker receives stock information and integrates it into his/her own stock report. For this experiment, we created a data set of 6000 tuples. The attributes and their domain are listed in Table 2.

<table>
<thead>
<tr>
<th>Attr. No.</th>
<th>Relation</th>
<th>Name</th>
<th>Value Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>A1</td>
<td>stock, stk.rpt</td>
<td>scode</td>
<td>[1, 500]</td>
</tr>
<tr>
<td>A2</td>
<td>stk.rpt</td>
<td>price</td>
<td>stock.close * exchange.rate[stock.currency]</td>
</tr>
<tr>
<td>A3</td>
<td>stk.rpt</td>
<td>volume</td>
<td>stock.volume * 1000</td>
</tr>
<tr>
<td>A4</td>
<td>stk.rpt</td>
<td>value</td>
<td>stk.rpt.price * stk.rpt.volume</td>
</tr>
<tr>
<td>A5</td>
<td>stock</td>
<td>currency</td>
<td>1, 2, 3, 4, 5, random</td>
</tr>
<tr>
<td>A6</td>
<td>stock</td>
<td>volume</td>
<td>20-500, uniform distribution</td>
</tr>
<tr>
<td>A7</td>
<td>stock</td>
<td>high</td>
<td>[stock.close, 1.2*stock.close]</td>
</tr>
<tr>
<td>A8</td>
<td>stock</td>
<td>low</td>
<td>[0.85*stock.close, stock.close]</td>
</tr>
<tr>
<td>A9</td>
<td>stock</td>
<td>close</td>
<td>[0.50, 100], uniform distribution</td>
</tr>
</tbody>
</table>

#### 4.4.1 Relevant attribute analysis

The zero-order correlation analysis was first applied to the training data. If the correlation efficient between two attributes is greater than the threshold, which was set to 0.1 in the experiment, they were considered relevant. The results and relevant attribute sets are shown in Table 3.

<table>
<thead>
<tr>
<th>Set</th>
<th>Attribute</th>
<th>Correlated Attributes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>A3</td>
<td>A6</td>
</tr>
<tr>
<td>2</td>
<td>A4</td>
<td>A6, A7, A8, A9</td>
</tr>
<tr>
<td>3</td>
<td>A2</td>
<td>A7, A8, A9</td>
</tr>
</tbody>
</table>

Partial correlation analysis was conducted by controlling $A6, A7, A8$ and $A9$ in turn to see whether there are more attributes that should be included in the obtained relevant attribute sets. In this example, there were no such attributes; and the relevant attribute sets remained the same.
4.4.2 Candidate model selection and conversion function generation

Each of the relevant attribute sets was used to generate conversion functions in turn. Set 1 contains only two variables. There is only one possible model \((A_3 = A_6)\) that generates

\[ A_3 = 1000 \times A_6. \]  

with 100% support:

Set 2 consists of five attributes, \(A_4, A_6, A_7, A_8,\) and \(A_9\). \(A_4\) is correlated to four other attributes. Without any prior knowledge, and considering only a linear model with first-order and second-order terms (an acceptable practice for most financial and business data), the initial model includes all the attributes.

\[ A_4 = A_6 + A_7 + A_8 + A_9 + A_6 \times A_7 + A_6 \times A_8 + A_6 \times A_9 + A_7 \times A_9 + A_8 \times A_9 \]  

(7)

Table 4 lists the output of the model selection module for different Occam’s Window sizes. It can be seen that with larger window size, the number of candidate models selected increases and more attributes were included in the model. When window size is 20 and 30, only one model with attributes \(A_6\) and \(A_9\) was selected. When the window size increased to 40, four models were selected and attributes \(A_8\) and \(A_7\) appeared in some of the models.

Table 5: Functions discovered for selected models

<table>
<thead>
<tr>
<th>Model</th>
<th>Function generated</th>
<th>Support (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(A_4 = A_6 \times A_9)</td>
<td>(A_4 = 708.04 \times A_6 \times A_9)</td>
<td>81.73</td>
</tr>
<tr>
<td>(A_4 = A_7 + A_6 \times A_9)</td>
<td>(A_4 = 9980 \times A_7 + 678.05 \times A_6 \times A_9)</td>
<td>81.22</td>
</tr>
<tr>
<td>(A_4 = A_8 + A_6 \times A_9)</td>
<td>(A_4 = 10875.13 \times A_8 + 685.14 \times A_6 \times A_9)</td>
<td>81.08</td>
</tr>
<tr>
<td>(A_4 = A_9 + A_6 \times A_9)</td>
<td>(A_4 = 9970.88 \times A_9 + 677.84 \times A_6 \times A_9)</td>
<td>81.31</td>
</tr>
<tr>
<td>(A_4 = A_6 \times A_9 + A_7 \times A_8)</td>
<td>(A_4 = 685.90 \times A_6 \times A_9 + 102.15 \times A_7 \times A_8)</td>
<td>81.54</td>
</tr>
<tr>
<td>(A_4 = A_6 \times A_9 + A_8 \times A_9)</td>
<td>(A_4 = 681.94 \times A_6 \times A_9 + 127.34 \times A_8 \times A_9)</td>
<td>81.58</td>
</tr>
</tbody>
</table>

In the conversion function generation process, the selected model was used to generate conversion functions. For the models in Table 4, the system in fact did not report any functions. By further examining the process, we found that all the models resulted in functions with support lower than specified threshold.
Table 5.

As illustrated in Figure 1, when a selected model does not generate any single conversion function with sufficient support, there is a possibility that there exist multiple functions for the data set. To discover such multiple functions, the data set should be reorganized. In our implementation, a simple heuristic is used, that is, to partition the data using categorical attributes in the data set. After the data was partitioned based on a categorical attribute $A_5$, the model selected are shown in Table 6.

<table>
<thead>
<tr>
<th>Window size</th>
<th>Model selected</th>
<th>Support (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>$A_4 = A_6 \times A_9$</td>
<td>100</td>
</tr>
<tr>
<td>40</td>
<td>$A_4 = A_6 \times A_9$</td>
<td>100</td>
</tr>
<tr>
<td>60</td>
<td>$A_4 = A_6 \times A_9$</td>
<td>100</td>
</tr>
<tr>
<td></td>
<td>$A_4 = A_7 + A_6 \times A_9$</td>
<td>100</td>
</tr>
<tr>
<td></td>
<td>$A_4 = A_9 + A_6 \times A_9$</td>
<td>100</td>
</tr>
<tr>
<td></td>
<td>$A_4 = A_6 \times A_8 + A_6 \times A_9$</td>
<td>100</td>
</tr>
<tr>
<td></td>
<td>$A_4 = A_6 \times A_9 + A_7 \times A_9$</td>
<td>100</td>
</tr>
</tbody>
</table>

The conversion function generation module estimates the coefficients for each of the models selected for each partition. There is only one conversion function reported for each partition, since all the coefficients for the terms other than $A_6 \times A_9$ were zero. The results are summarize in Table 7.

Table 7: The conversion functions generated from Set 2 and 3

<table>
<thead>
<tr>
<th>Conversion functions for $A_4$</th>
<th>Support (%)</th>
<th>Conversion functions for $A_2$</th>
<th>Support (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_4 = 400 \times A_6 \times A_9$</td>
<td>100</td>
<td>$A_2 = 0.4 \times A_9$</td>
<td>100</td>
</tr>
<tr>
<td>$A_4 = 700 \times A_6 \times A_9$</td>
<td>100</td>
<td>$A_2 = 0.7 \times A_9$</td>
<td>100</td>
</tr>
<tr>
<td>$A_4 = 1000 \times A_6 \times A_9$</td>
<td>100</td>
<td>$A_2 = 1.0 \times A_9$</td>
<td>100</td>
</tr>
<tr>
<td>$A_4 = 1800 \times A_6 \times A_9$</td>
<td>100</td>
<td>$A_2 = 1.8 \times A_9$</td>
<td>100</td>
</tr>
<tr>
<td>$A_4 = 5800 \times A_6 \times A_9$</td>
<td>100</td>
<td>$A_2 = 5.8 \times A_9$</td>
<td>100</td>
</tr>
</tbody>
</table>

The process for relevant attribute $Set 3: \{A_2, A_7, A_8, A_9\}$ is similar to what described for Set 2. The initial model used is

$$A_2 = A_7 + A_8 + A_9 + A_7 \times A_8 + A_7 \times A_9 + A_8 \times A_9$$  \hspace{1cm} (8)$$

and the model selection module selected 10 models without producing functions with enough support. Using the data sets partitioned using $A_5$ and the conversion functions listed in Table 7 were obtained.

4.4.3 Conversion function selection and data conversion rule formation

Since there is only one set of candidate functions obtained for each set of relevant attribute set with 100% support. The functions generated were selected to form the data conversion rules. By some syntactic
transformation, we can obtain the following data conversion rules for our example:

\[
\text{stk.rpt}(stock, price, rpt.volume, value) \leftarrow \\
\text{stock}(stock, currency, stk.volume, high, low, close), \\
\text{price} = \text{rate} \times \text{close}, \text{rpt.volume} = 1000 \times \text{stk.volume}, \\
\text{value} = \text{rate} \times 1000 \times \text{stk.volume} \times \text{close}, \text{exchange.rate(currency, rate)}. \\
\text{exchange.rate}(0, 0.4). \\
\text{exchange.rate}(1, 0.7). \\
\text{exchange.rate}(2, 1.0). \\
\text{exchange.rate}(3, 1.8). \\
\text{exchange.rate}(4, 5.8).
\]

It is obvious that the discovered rule can be used to integrate data from \textit{stock} to \textit{stk.rpt}.

5 Experience with a real world data set

In this section, we present the experimental results on a set of real world data using the system described in the previous section. The motivation for this exercise is to demonstrate that the techniques and framework remain applicable in the context of a real-world application.

The data used in this experiment was collected from a trading company. Each record consists of 10 attributes. Attribute A1 to A8 are from a transaction database, \(T(\text{month}, \text{invoice.no}, \text{amount}, \text{sales.type}, \text{GST.rate}, \text{currency}, \text{exchange.rate}, \text{GST.amount})\), which records the details of each invoice billed, hence all the amounts involved are in the original currency. Attribute A9, \(\text{C.amount}\) is extracted from a system for cost/profit analysis, which captures the sales figure in local currency exclusive of tax. Finally, attribute A10, \(\text{A.amount}\), is from the accounting department, A, where all the monetary figures are in the local currency. Therefore, although attributes A3, A9 and A10 have the same semantics, i.e., all refer to the amount billed in an invoice, their values are different. That is, value conflict exists among the attributes.

From the context of the business, the following relationship among the attributes should exist:

\[
\text{A.amount} = T.\text{amount} \times T.\text{exchange.rate}. \\
\text{C.amount} = (T.\text{amount} - T.\text{GST.\amount}) \times T.\text{exchange.rate} \\
= \text{A.amount} - T.\text{exchange.rate} \times T.\text{GST.\amount}. \\
\]

The goods and service tax (GST), is computed based on the amount charged for the sales of goods or services. As \(\text{C.amount}\) is in the local currency and all transaction data are in the original currency, we have the following relationship:

\[
T.\text{GST.\amount} = \text{C.amount}/T.\text{exchange.rate} \times T.\text{GST.rate} \\
\]

where GST rate depends on the nature of business and clients. For example, exports are exempted from GST (tax rate is 0%) and domestic sales are taxed in a fixed rate of 3% in our case.
The training data set collected contains 7,898 tuples corresponding to the invoices issued during the first 6 months of a financial year. The discovery process and the results are summarized in the following subsections.

5.1 Identifying relevant attribute sets

As our current system only works for numeric data, the categorical attributes are not included in analysis. That is, among eight attributes from data source \( T \), only attributes \( A_3, A_5, A_7 \) and \( A_8 \) are taken into the correlation analysis. The results of partial analysis indicated that both \( A_9 \) and \( A_{10} \) are highly related to all four attributes (Refer to Appendix A.1 for the details).

5.2 Conversion function generation

The conversion function generation process produced the following functions with 100% support.

\[
A_{10} = A_3 \times A_7. \\
A_9 = A_3 \times A_7 - A_7 \times A_8. 
\]

Note that none of the above two functions involves attribute \( A_5 \) which was highly correlated with both \( A_9 \) and \( A_{10} \). This invokes the data reorganization process, the data set is partitioned according to categorical attribute \( A_4 \) that has two distinct values. The conversion functions obtained from the partitioned data are listed in Table 8

<table>
<thead>
<tr>
<th>( A_4 )</th>
<th>No</th>
<th>Conversion functions</th>
<th>Support</th>
<th>Number of Outliers</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>( A_9 = 0.9708738 \times A_3 \times A_7 )</td>
<td>99.94</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>( A_9 = 33.33333 \times A_7 \times A_8 )</td>
<td>99.36</td>
<td>21</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>( A_9 = A_3 \times A_7 )</td>
<td>100.00</td>
<td>0</td>
</tr>
</tbody>
</table>

The functions with higher support in each group, i.e., Function 1 and 3 are selected as the conversion functions. Although these two functions do not match with any one in 10-12, they in fact represent the same function as shown in Appendix A.2.

5.3 Context independent conflict detection

What seems unnatural is that the support of Function 1 in the previous subsection is not 100% as it should be. We found the following two tuples listed in Table 9 that were identified as the outliers. They are indeed the tuples with errors contained in the original data: Both tuples have incorrect value of GST amount.  

\(^6\)We realized that the system allows data entry clerk to modify GST values calculated and prompted by the system. It is obvious that for these two invoices, incorrect tax values were entered.
Table 9: Two erroneous tuple discovered

<table>
<thead>
<tr>
<th>month</th>
<th>inv-no</th>
<th>amt.</th>
<th>GST type</th>
<th>GST rate</th>
<th>currency</th>
<th>exch. rate</th>
<th>GST</th>
<th>C.amount</th>
<th>A.amount</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>8237</td>
<td>45.50</td>
<td>1</td>
<td>3</td>
<td>1</td>
<td>1.00</td>
<td>0.00</td>
<td>45.50</td>
<td>45.50</td>
</tr>
<tr>
<td>6</td>
<td>12991</td>
<td>311.03</td>
<td>1</td>
<td>3</td>
<td>1</td>
<td>1.00</td>
<td>6.53</td>
<td>304.50</td>
<td>311.03</td>
</tr>
</tbody>
</table>

5.4 Applying the discovered function to test data

In order to verify the functions obtained, the sales data of the 7th month containing 1,472 tuples were collected. We applied discovered functions to calculate $A9$ and $A10$. It was found that there was no difference between the values calculated using the discovered functions and the values collected from the databases.

5.5 Discussion

From the experimental results of the real world data set, we made the following observations.

1. In the systems from which the sales data were collected, the exchange rate has 6 digits after the decimal point. All other computed amount has only 2 digits after the decimal point. Furthermore, a number of attributes are derived by a number of arithmetic operations. Therefore, the data values contain rounding errors introduced during calculations. In addition to the rounding errors, the data set also contains two error entries. Under our classification, the data set contains both context dependent and context independent conflicts.

   Our first conclusion is this: although the training data set contains noises (rounding errors) and both context dependent and independent conflicts (two outliers), the system was still able to discover the correct conversion functions.

2. One interesting function discovered by the system but not selected (eventually) is Function 2 in Table 8. Note that, from the expression itself, it is derivable from the other correct functions: Since $A8$ is the amount of tax in the original currency, $A9$ is the amount of sales in the local currency, $A7$ is the exchange rate, and $A5$ is the tax rate(percentage), we have

\[
A8 = \frac{A9}{A7} \times 0.01 \times A5
\]

That is,

\[
A9 = \frac{A7 \times A8}{0.01 \times A5} \quad \text{for } A5 \neq 0
\]

When $A4 = 1$, $A5 = 3$, so we should have

\[
A9 = \frac{A7 \times A8}{0.01 \times 3} = 33.33333 \times A7 \times A8.
\]

which is the same as Function 2. The function was discarded because of its low support (99.36%). It seems puzzling that a function that is derivable from the correct functions has such low support.
so that it should be discarded.

It turns out that this phenomenon can be explained. Since, the derivation process is purely mathematical, it does not take into any consideration how the original data value is computed. In the real data set, the tax amount stored has been rounded up to 0.01. The rounding error may get propagated and enlarged when Function 2 is used. If exchange rate is 1.00 (i.e., the invoice is in the local currency), the possible error of $A_9$ introduced by using Function 2 to compute the sales amount from the tax amount could be as large as 33.33333*0.005. This is much larger than the precision of $A_9$ which is 0.005. To verify the reasoning, we modified the function into

$$A_9 = \frac{A_7 \times A_8}{0.01 \times 3} = 33.33333 \times A_7 \times \text{roundup}(A_8)$$

where \text{roundup} is a function that rounds $A_8$ to 0.01; and calculated $A_9$ using the modified function. Comparing the calculated values and the corresponding values in the data set, the differences for all tuples are less than 0.005.

This leads to our second conclusion: 

because noises such as rounding errors existing in the data and different ways in which the original data were produced, we should not expect a conversion function mining system to reproduce the functions that are used in generating the original data. The objective of such systems is to find the functions that data from multiple sources can be integrated or exchanged with specified requirement of accuracy.

6 Conclusion

In this paper, we addressed the problem of discovering and resolving data value conflicts for data integration. We first proposed a simple classification scheme for data value conflicts based on how they can be reconciled. We argue that those conflicts caused by genuine semantic heterogeneity can be reconciled systematically using data value conversion rules. A general approach for discovering data conversion rules from data was proposed. statistical techniques are integrated in to a prototype system to implement the approach for financial and business data. The system was tested using some both synthetic and real world data.

The approach advocated in this paper identify conversion rules which are defined on data sources on a pairwise basis (i.e., between any two systems at a time). One drawback of this is that we may have to be defined a large number of rules if a large number of sources are involved. It will be beneficial if we are able to go a step further to to elicit meta-data information from conversion rules obtained. This will allow us to introduce appropriate meta-data tags to each of the data source while allowing postponing the decision of which conversion rule should be applied (Bressan, Fynn, Goh, Jakobisiak, Hussein, Kon, Lee, Madnick, Pena, Qu, Shum & Siegel 1997). This will be advantageous because it will help reduce the volume of information that the underlying context mediator has to deal with. For example, in the example given in Section 5, the conversion rules only indicate the ways to compute the sales and tax based on tax rate. It would be more economical if we are able to match the tax rate to yet another data source furnishing the sales type and tax rate and figure out that different sales have different tax by virtual of the type of sales. Thus, if we know that all sales in a company have been charged 3% tax, we can conclude that the
company only has domestic sales.

References


Miller, A. (1990), Subset Selection in Regression, Chapman and Hall.


Appendix A: Results with Real World Data

A.1 Results of partial correlation analysis

The following table lists the results of the partial correlation analysis. Note that, the correlation coefficients between $A_{10}$ and $A_5$, $A_{10}$ and $A_7$ are rather small in the zero-order test. However, this alone is not sufficient to conclude that $A_{10}$ is not related to $A_5$ and $A_7$. By the PCA test with controlling $A_3$, the correlation between $A_{10}$ and $A_7$ became rather obvious and the correlation coefficient between $A_{10}$ and $A_5$ also increased. With one more PCA test that controls $A_8$, the correlation between $A_{10}$ and $A_5$ became more obvious. Thus, all the four attributes are included into the quantitative relationship analysis.

Table 10: Partial correlation analysis between $A_{10}$ and $\{A_{3}, A_{5}, A_{7}, A_{8}\}$

<table>
<thead>
<tr>
<th></th>
<th>Zero-order</th>
<th>Controlling A3</th>
<th>Controlling A8</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_3$</td>
<td>0.91778708</td>
<td>-</td>
<td>0.8727613</td>
</tr>
<tr>
<td>$A_5$</td>
<td>0.02049382</td>
<td>0.1453855</td>
<td>-0.2968708</td>
</tr>
<tr>
<td>$A_7$</td>
<td>0.02492715</td>
<td>0.4562510</td>
<td>-0.00639451</td>
</tr>
<tr>
<td>$A_8$</td>
<td>0.71552943</td>
<td>0.5122901</td>
<td>-</td>
</tr>
</tbody>
</table>

Table 11: Partial correlation analysis between $A_9$ and $\{A_{3}, A_{5}, A_{7}, A_{8}\}$

<table>
<thead>
<tr>
<th></th>
<th>Zero-order</th>
<th>Controlling A3</th>
<th>Controlling A8</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_3$</td>
<td>0.91953641</td>
<td>-</td>
<td>0.8739174</td>
</tr>
<tr>
<td>$A_5$</td>
<td>0.01350388</td>
<td>0.1292704</td>
<td>-0.2976056</td>
</tr>
<tr>
<td>$A_7$</td>
<td>0.02355110</td>
<td>0.4581783</td>
<td>-0.007597317</td>
</tr>
<tr>
<td>$A_8$</td>
<td>0.70452050</td>
<td>0.4791232</td>
<td>-</td>
</tr>
</tbody>
</table>

A.2: Tests with partitioned data

In this section, we show the detailed deduction that the functions generated for $A_9$,

\[
A_9 = 0.9708738 \times A_3 \times A_7 \quad (15)
\]

\[
A_9 = A_3 \times A_7 \quad (16)
\]

conform the original functions.

Using the attribute numbers instead of the name, we can rewrite Equation 11 as

\[
A_9 = A_3 \times A_7 - A_8 \times A_7
\]

The tax rate, $A_5$, is stored as the percentage, Equation 12 can be rewritten as

\[
A_8 = \frac{A_9}{A_7} \times 0.01 \times A_5
\]
Thus we have

$$A9 = A3 \cdot A7 - \frac{A9}{A7} \cdot 0.01 \cdot A5 \cdot A7$$

$$= A3 \cdot A7 - 0.01 \cdot A9 \cdot A5$$

Therefore,

$$A9 = \frac{A3 \cdot A7}{1 + 0.01 \cdot A5} \quad \text{(17)}$$

From the data, we have

$$A5 = \begin{cases} 3 & \text{for } A4 = 1 \\ 0 & \text{for } A4 = 2 \end{cases}$$

Substituting this into Equation 17, we have

$$A9 = \begin{cases} \frac{A3 \cdot A7}{1.03} = 0.9708738 \cdot A3 \cdot A7 & \text{for } A4 = 1 \\ A3 \cdot A7 & \text{for } A4 = 2 \end{cases}$$

which are the functions 16 and 16. In other words, although the two functions have different forms, they do represent the original relationship among the data values specified by Equation 17.