

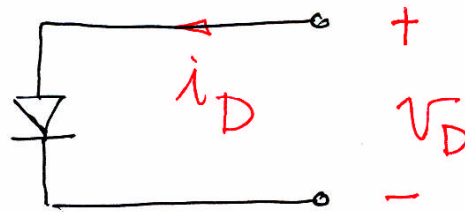
6.002 - Lecture 23

Diodes Revisited

- Diode Review
- Several Views
- Piece-wise Linear Models
- Method Of Assumed States

Exponential Diode I

Nonlinear
Resistor



$$i_D = I_s (e^{v_D/V_T} - 1)$$

$$V_T = \frac{KT}{q} \approx 26 \text{ mV @ } 27^\circ\text{C}$$

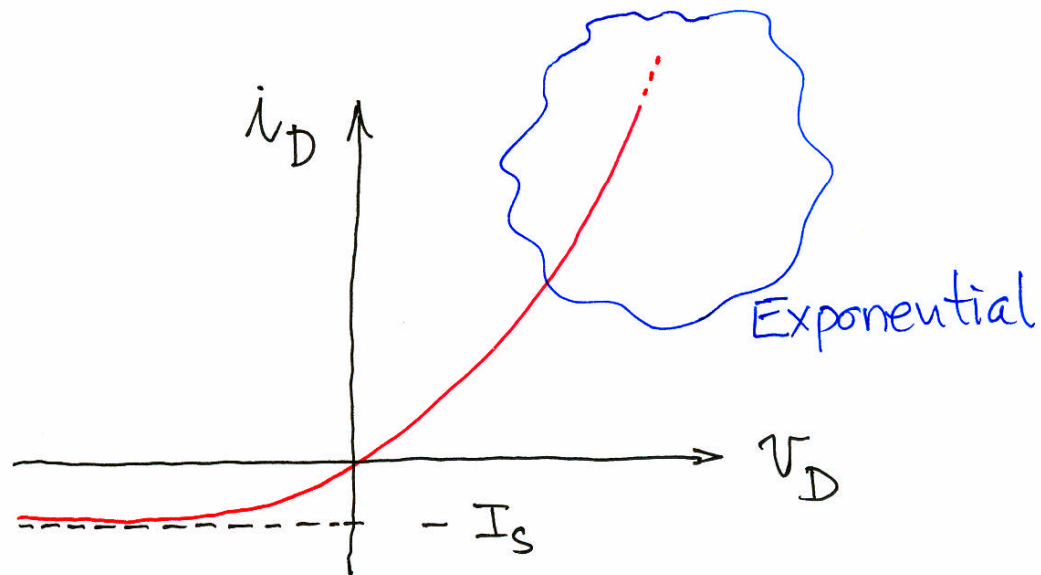
$$I_s = \text{Saturation Current} = 10^{-13} \text{ A} \dots 10^{-9} \text{ A}$$

$$K = \text{Boltzmann's Constant} = 1.38 \times 10^{-23} \text{ J/K}$$

$$T = \text{Temperature [K]}$$

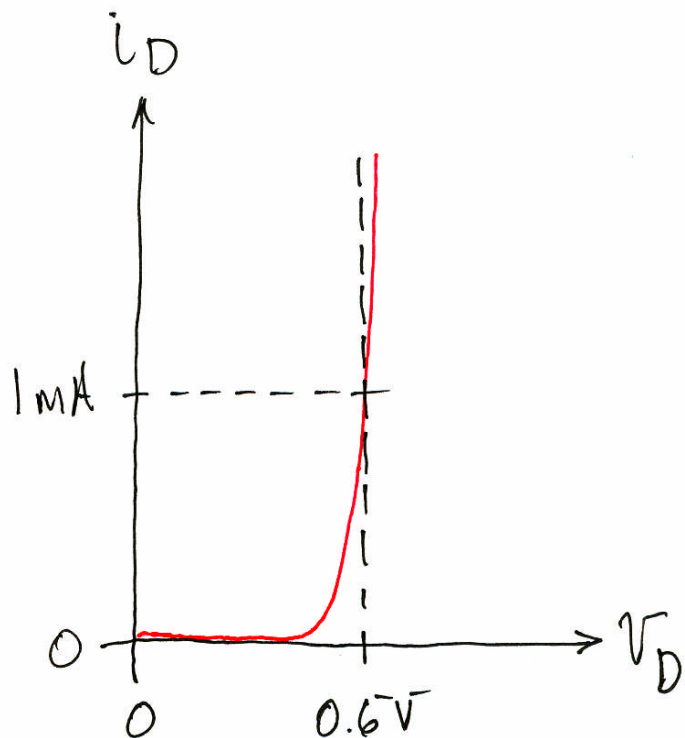
$$q = \text{Electron Charge} = 1.6 \times 10^{-19} \text{ C}$$

Exponential Diode II



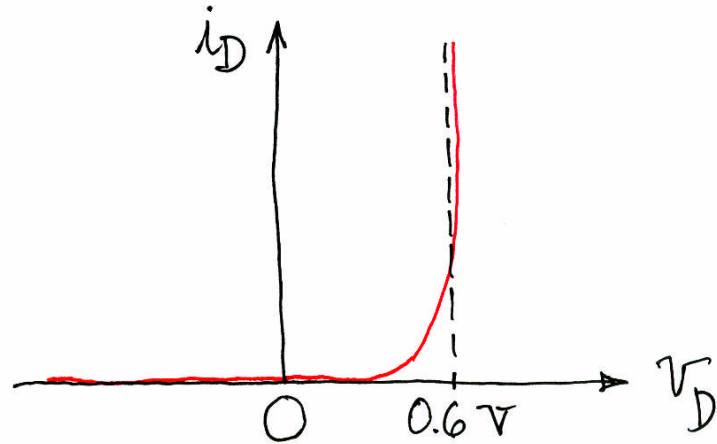
v_D	i_D
0.54 V	100 nA
0.60 V	1 mA
0.66 V	10 mA
0.72 V	100 mA
0.78 V	1 A
0.84 V	10 A

$$I_S \equiv 10^{-13} \text{ A}$$

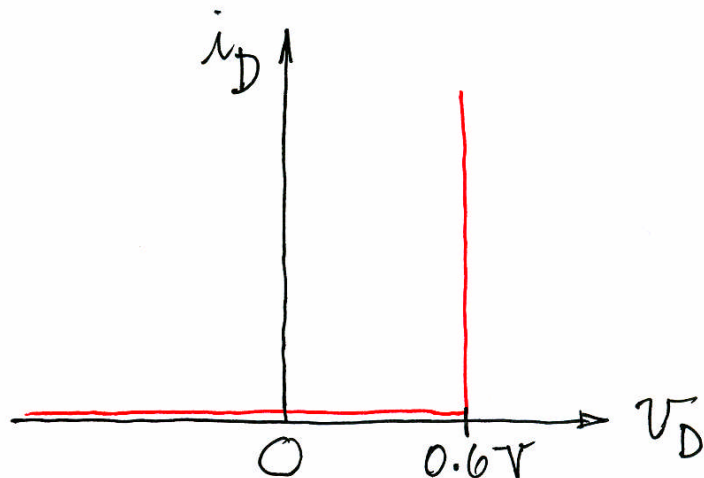
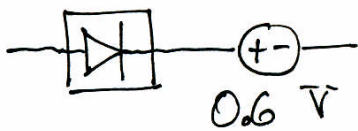


Several Models

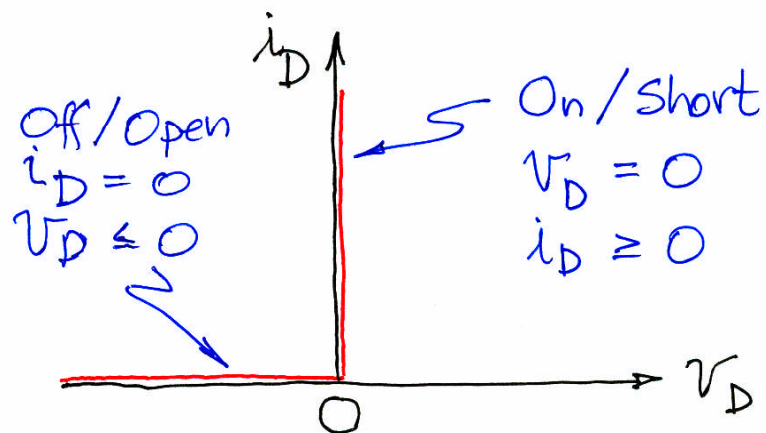
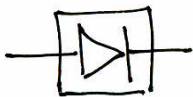
Exponential



Compromise

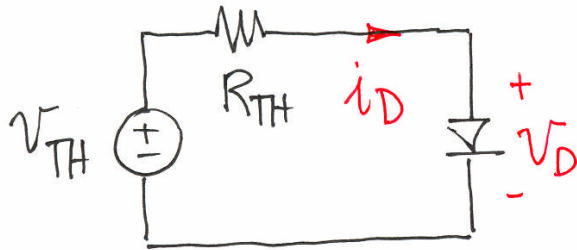


Ideal



Model selection depends on the viewpoint.

Analyses Revisited



$$i_D = I_S (e^{\frac{V_D}{V_T}} - 1)$$

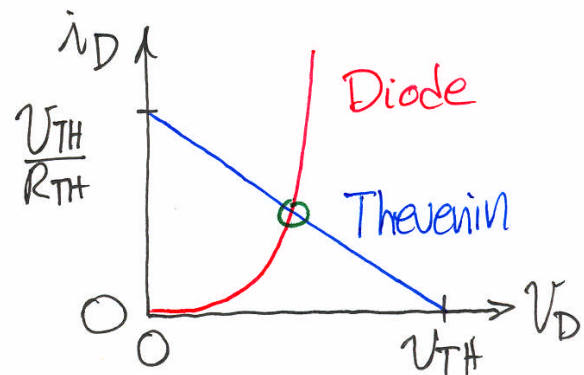
$$V_{TH} - R_{TH} i_D = V_D$$

- Node Analysis (No closed-form solution)
- Graphical Analysis (Valuable for insight)
- Numerical Analysis (Initial value: $V_D = 0.6V$)
- Incremental Analysis (Requires bias analysis)
- Approximate Models $\rightarrow$ Method of Assumed states

Node Analysis:

$$V_{TH} = R_{TH} I_S (e^{\frac{V_D}{V_T}} - 1) + V_D$$

Graphical Analysis:



Method Of Assumed States

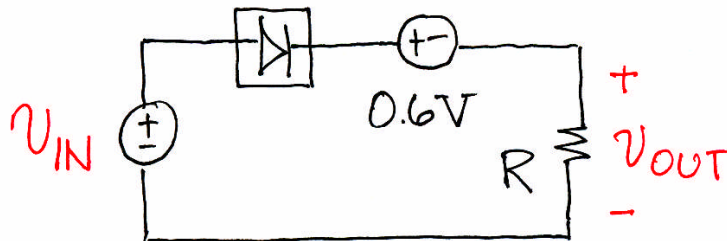
Model each diode as ideal with an optional voltage offset or series resistance

- Diode = On/off $\Rightarrow$ 2 States
- N Diodes $\rightarrow 2^N$ possible state combinations

For each state combination, analyze the network/circuit. Use the constraints on V_D (On $\Rightarrow i_D \geq 0$) and i_D (Off $\Rightarrow V_D \leq 0$) to determine the valid operating range for each state-combination analysis.

- Advantage: diode models become simple
- Disadvantage: 2^N analyses

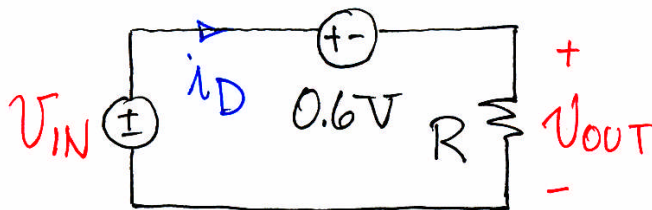
Half-Wave Rectifier I



2 States:

Diode = On/off

Diode $\equiv$ On ($v_D = 0$ $i_D \geq 0$)

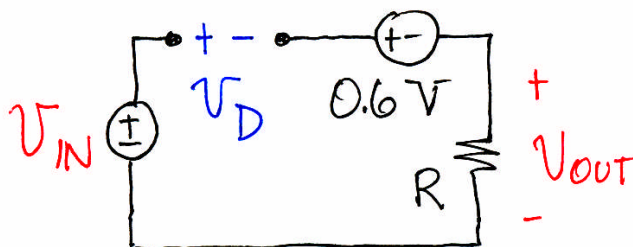


$$V_{OUT} = V_{IN} - 0.6V$$

$$i_D = \frac{V_{IN} - 0.6V}{R} \geq 0$$

$$V_{IN} \geq 0.6V$$

Diode $\equiv$ Off ($i_D = 0$ $v_D \leq 0$)

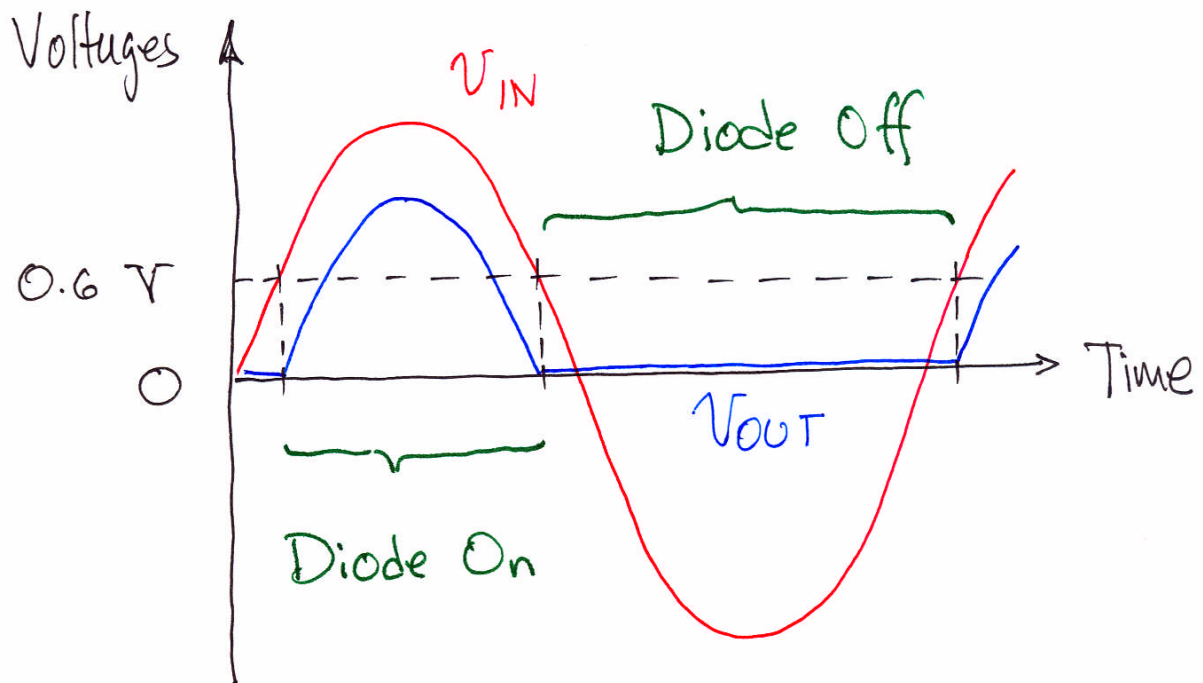
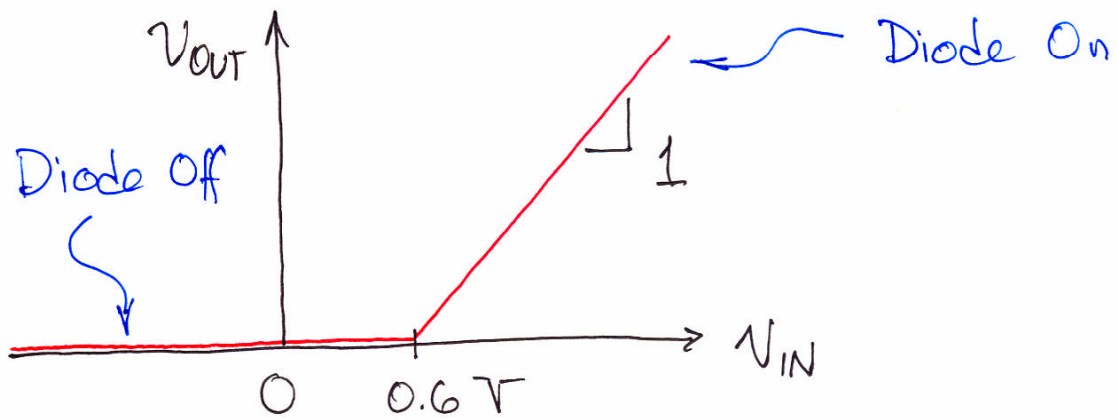


$$V_{OUT} = 0$$

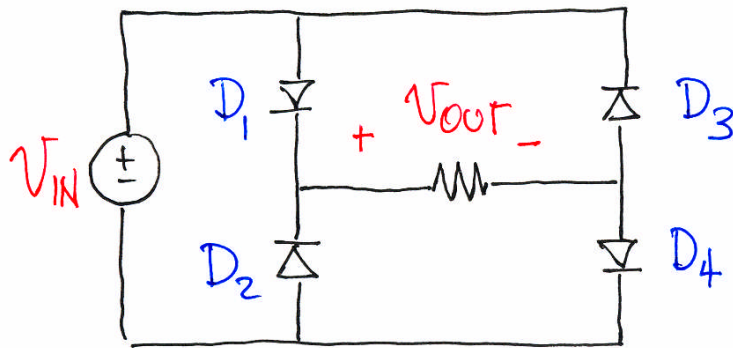
$$v_D = V_{IN} - 0.6V \leq 0$$

$$V_{IN} \leq 0.6V$$

Half - Wave Rectifier II



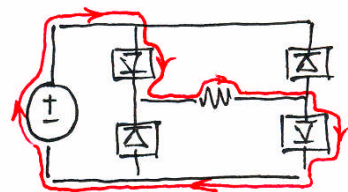
Full-Wave Rectifier



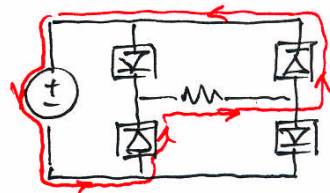
4 Diodes
→ 16 states

Only 3 diode state combinations are feasible.

① $V_{IN} > 0 \Rightarrow D_1 = D_4 = \text{On}$
 $D_2 = D_3 = \text{Off}$



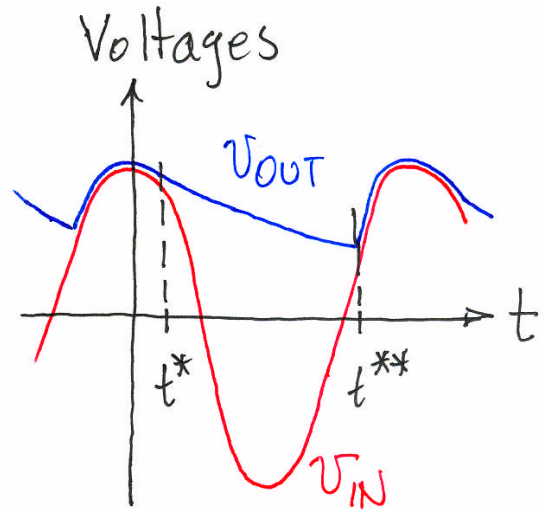
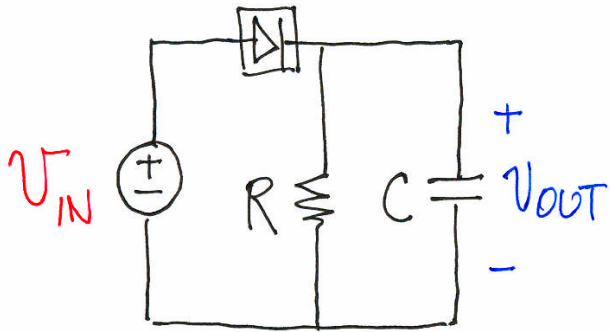
② $V_{IN} < 0 \Rightarrow D_1 = D_4 = \text{Off}$
 $D_2 = D_3 = \text{On}$



③ $V_{IN} = 0 \Rightarrow D_1 = D_2 = D_3 = D_4 = \text{Off}$

$V_{OUT} = |V_{IN}|$ (Also useful for power supplies)

Peak Detector / Power Supply



Suppose $V_{IN} = V \cos(\omega t)$, for example.

Diode On: $i_D = \frac{V}{R} \cos(\omega t) - C V \omega \sin(\omega t) \geq 0$

Departure $\Rightarrow \frac{1}{\omega RC} = \tan^{-1}(\omega t^*)$

Diode Off: $V_D = V \cos(\omega t) - V \cos(\omega t^*) e^{-\frac{(t-t^*)}{RC}} \leq 0$

Intersection $\Rightarrow \cos(\omega t^{**}) = \cos(\omega t^*) e^{-\frac{(t^{**}-t^*)}{RC}}$