

# Interest Rates and Fundamental Fluctuations in Home Values

**Albert Saiz** 

**DUSPMIT** 









Changes in the user cost of capital driven by lower interest/mortgage rates and financial innovations (risk premium on real estate investments)

Without a doubt, these have been the main factor used to explain evolution of housing prices during the boom





#### Real Estate Valuation

Gordon valuation model (Poterba, 1984)

$$V = \frac{7}{i - g}$$

Cap rate method (income comparables)

$$V = \frac{r}{c}$$

**Comparables** 







## Agenda

Combine the urban economics model (Alonso-Muth-Mills) with the asset pricing (Poterba, 1984) approaches

Study impact of changes in user cost of capital

**Examine the roles of:** 

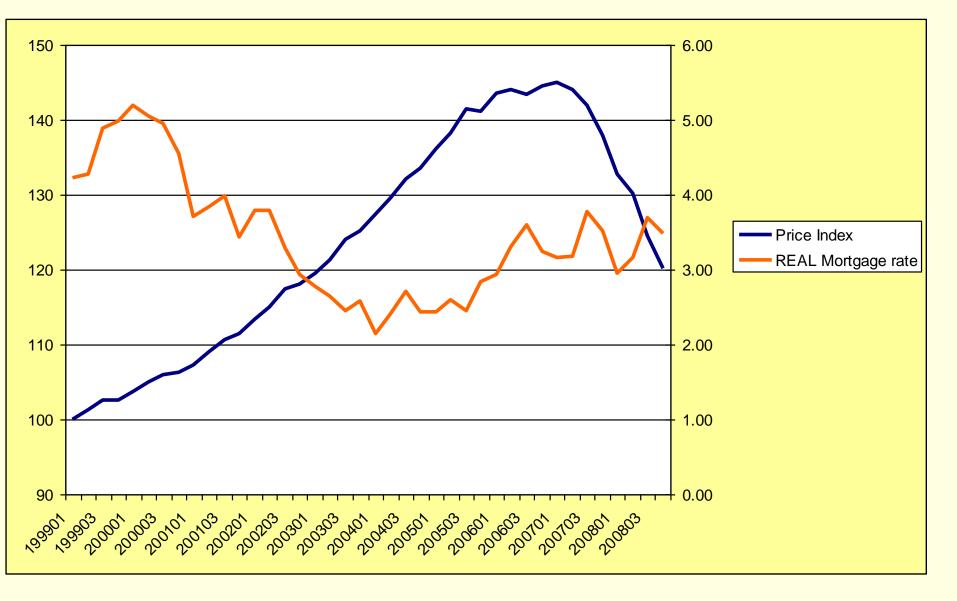
- Replacement costs
- Housing/land Supply elasticity
- Demand for space
- Rent endogeneity
- •Heterogeneity in rents

## **Parsimony**





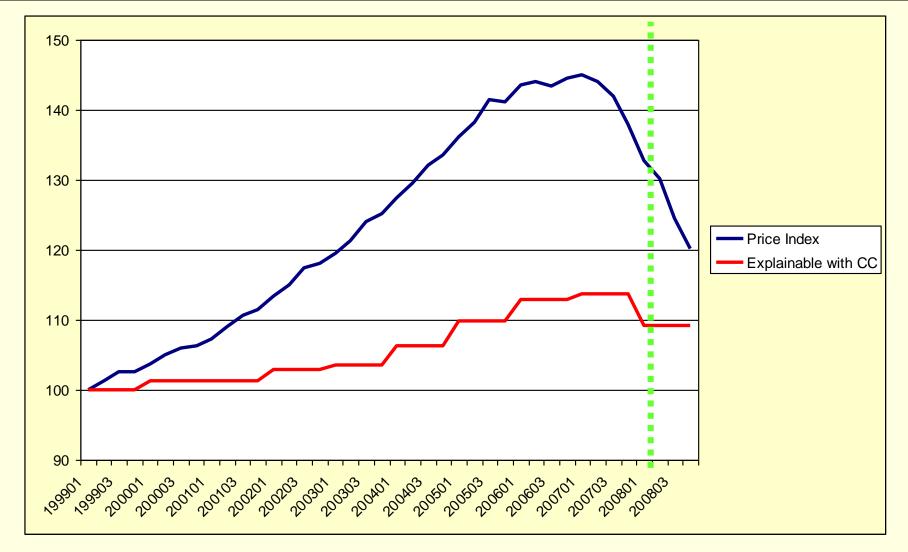








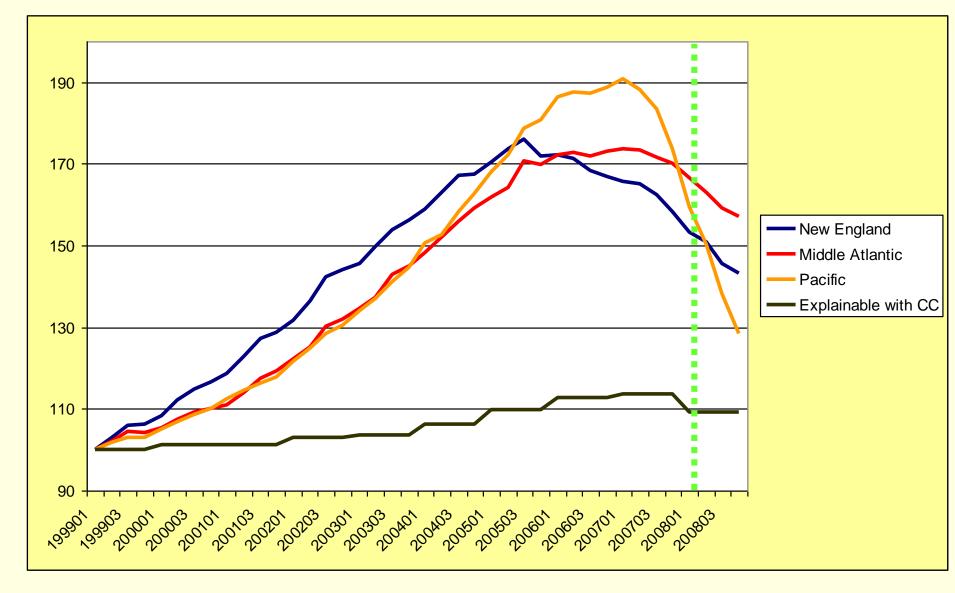








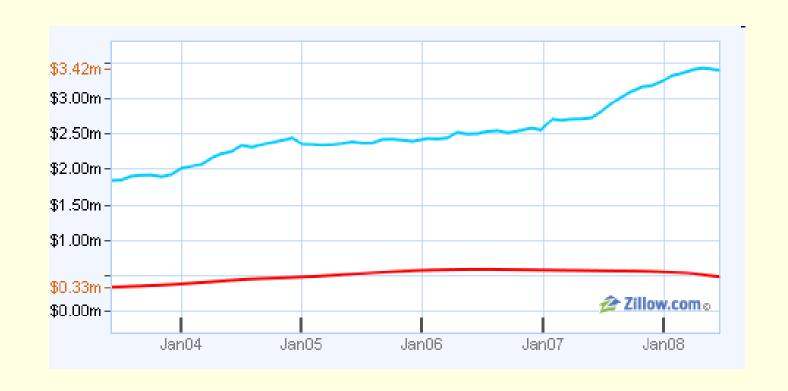








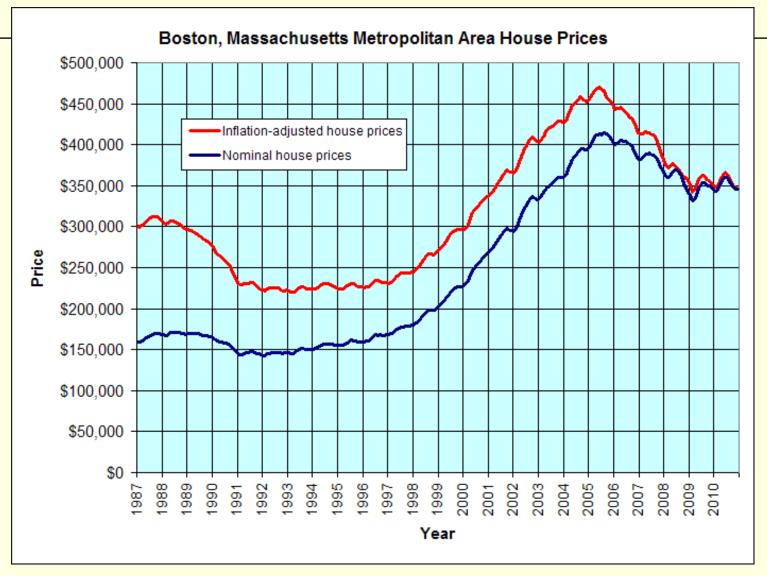
# Beverly Hills (Zip Code 90210): from Matt Kahn







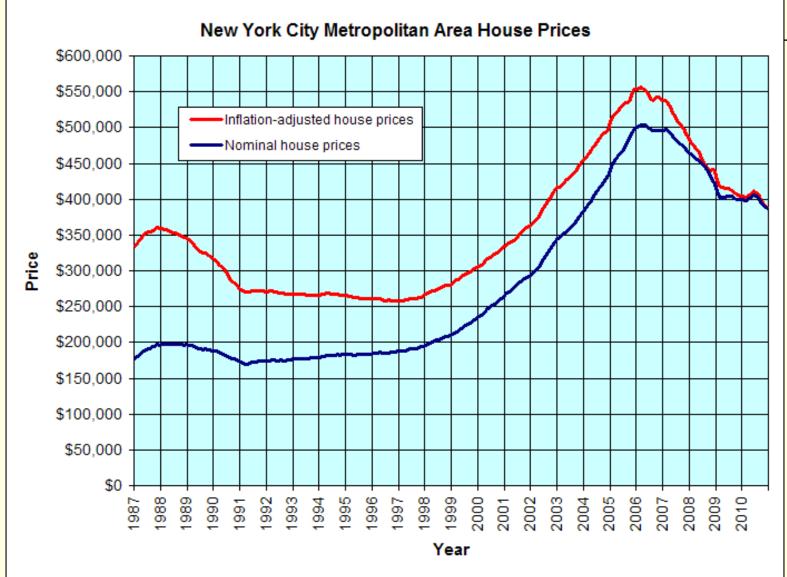






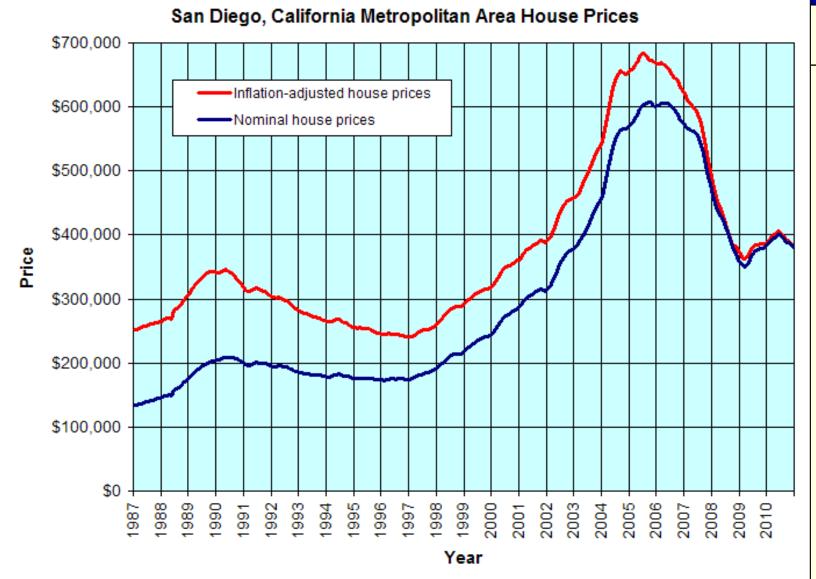








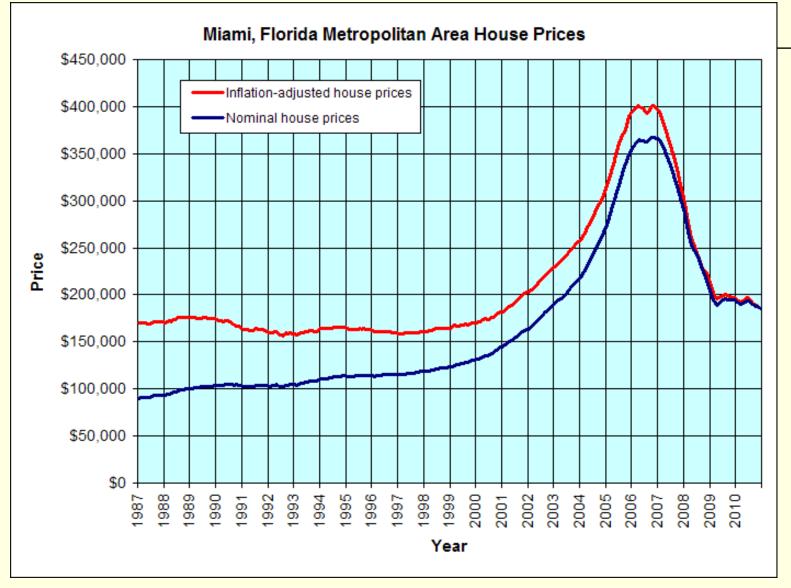
Soiz Interest Potes and Fundamentals







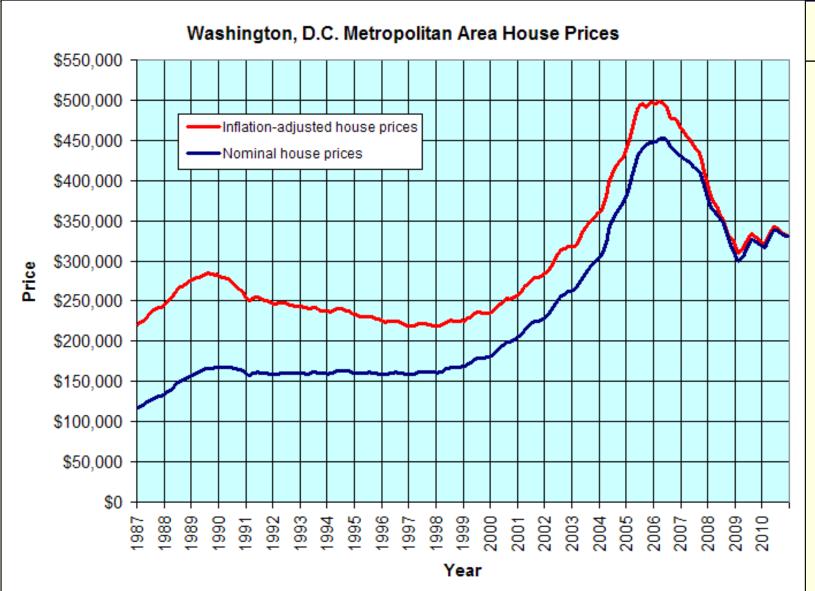








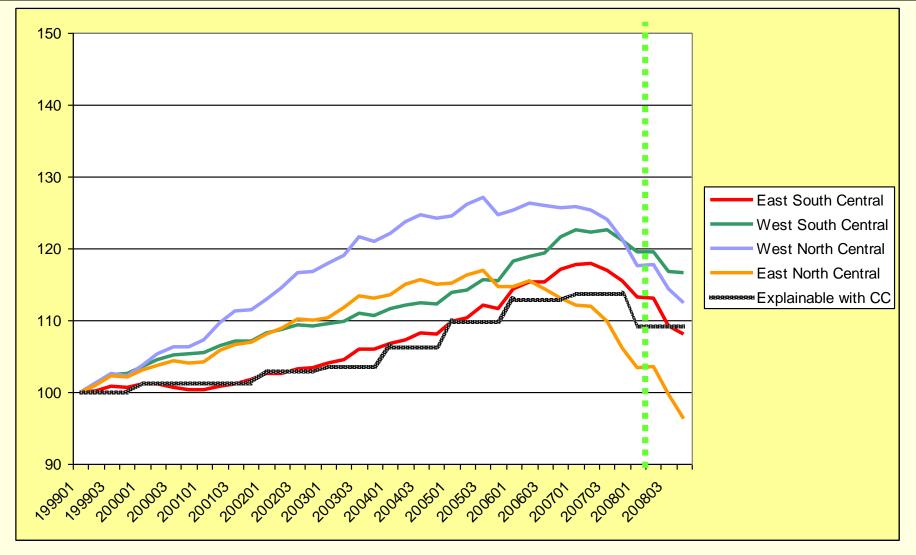




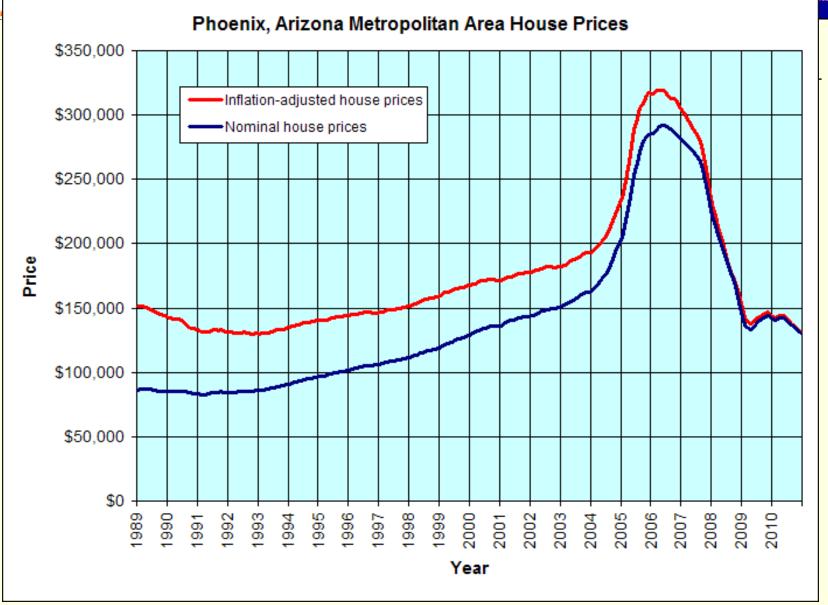








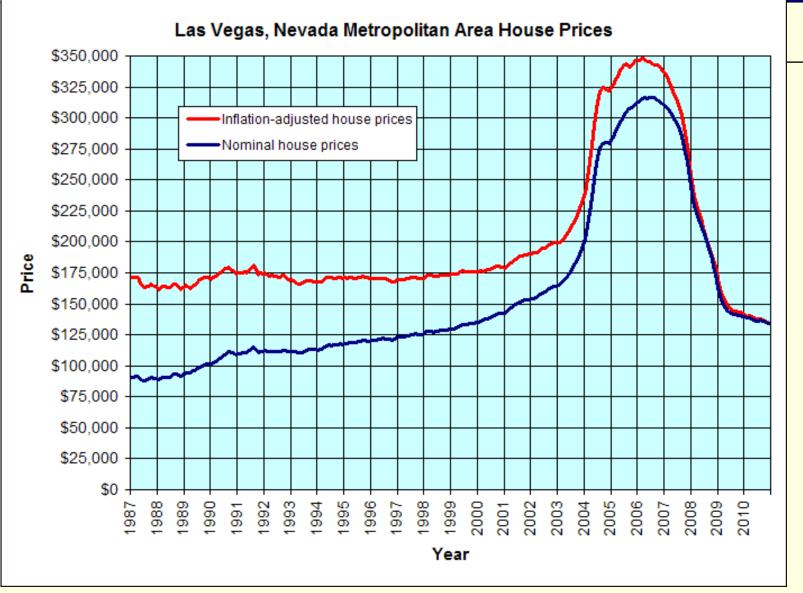


















## The Model

Most parsimonious AMM that captures main issues









#### Owner-renter assumption

In this paper I conceptually and conventionally assume everyone is a renter

Arbitrage between buyers: landlords versus owner-occupiers

Can think of owners as leasing property to themselves





Consumer Utility

$$U(C_k, d, h) = w_k - tD + \frac{h^{1-\mu'}}{1-\mu'} - rh$$

$$h = \left(\frac{1}{r}\right)^{\mu} \qquad \mu = \frac{1}{\mu'}$$





# Rental Price of a Housing Unit

a non-arbitrage condition defines the rent profile with respect to distance all city inhabitants attain utility  $\overline{U_k}$ 

$$\frac{dr}{dD} = -\frac{t}{h} = -tr^{\mu}$$

$$r(D) = [(1 - \mu) [C_1 - tD]]^{\frac{1}{1-\mu}}$$



### The Fundamental Rental Arbitrage Condition

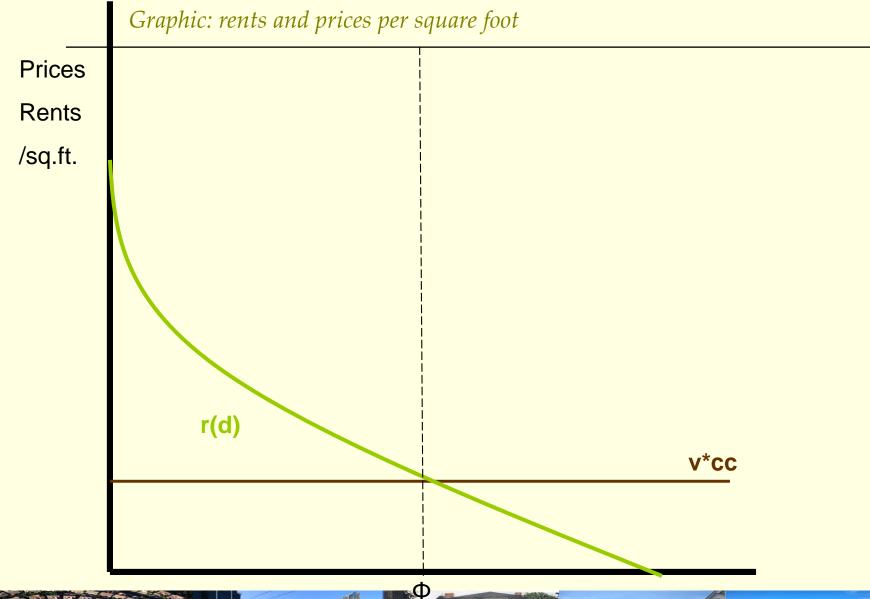
$$r(\Phi) = v \cdot cc$$

$$r(D) = \left[1 + \frac{(1-\mu)t(\Phi-D)}{[v\cdot cc]^{1-\mu}}\right]^{\frac{1}{1-\mu}}v\cdot cc$$
 Ricardian markup















#### Growth

Utility at border

$$V(\Phi) = w_k - t\Phi - \frac{[vcc]^{1-\mu}}{1-\mu}$$

Utility at exurbs:

$$V(Exurb) = \underline{w} - \frac{[vcc]^{1-\mu}}{1-\mu}$$

$$\Phi = \frac{w_k - \underline{w}}{t}$$

And posit:

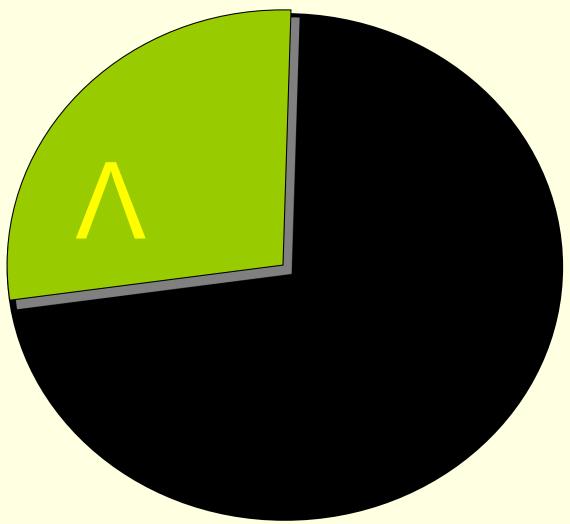
$$w_k(\tau)$$







# Radius and Population: Inelastic Land Supply



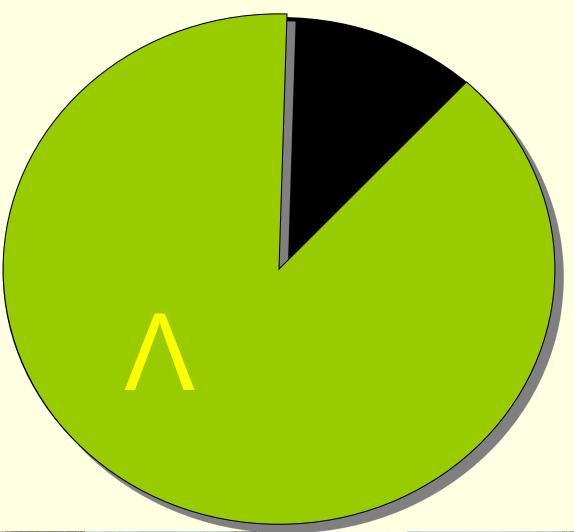








# Radius and Population: Elastic Land Supply









## Housing Asset Pricing Equation: Theory

At any point in time, asset market arbitrage for home-owner (can think of this as natural tendency)

Main arbitrage formula in housing markets (Poterba, 1984)

- τ stands for time (e.g. 2015)
- d stands for distance to employment/amenities

$$v \cdot p(\tau, d) \, = \, \stackrel{\circ}{p}(\tau, d) \, + \, r(\tau, d)$$

- With  $v = \delta + k + (1 \theta)i \theta\pi$  being the user cost of the capital invested (frozen) into housing
- The formula simply reads: the annual cost to the owner has to be equal to the annual benefit (capital appreciation plus rent)





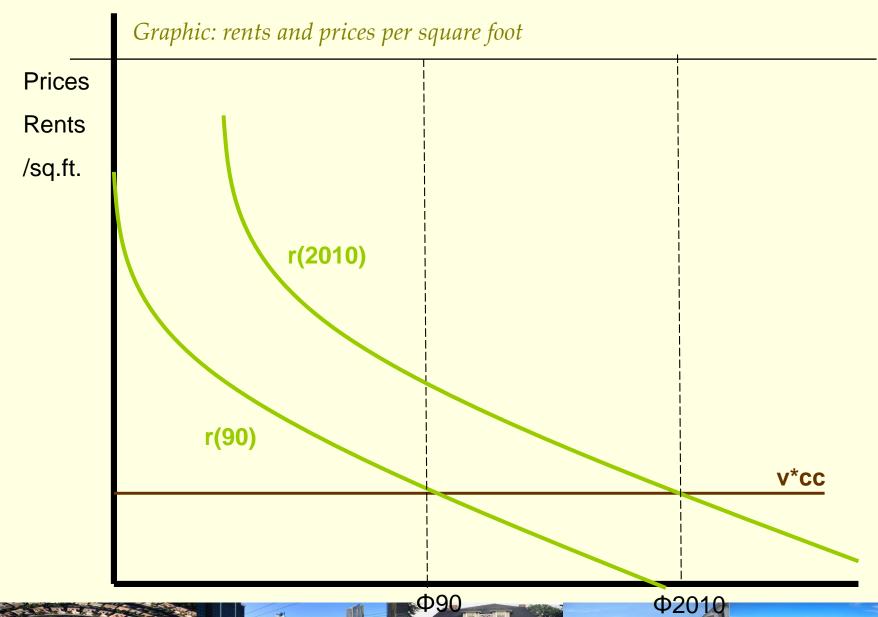


- The previous differential equation can be solved if we have an expected rental-equivalent growth "temporal path" for every period and distance :  $r(\tau,d)$
- In fact, the path of rental (use value) growth is quite predictable in most markets
- As discussed in economics part of the class, rental growth quite predictable by economic, demographic, and consumption trends
- These trends are quite persistent





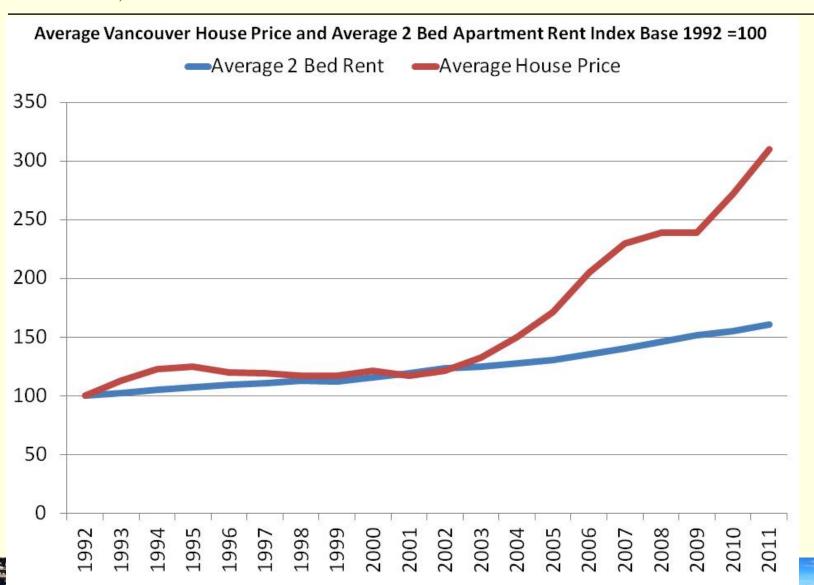








#### Vancouver, Canada



Sources: CMHC

# $p(\tau = 0, D) = \int_{0}^{\infty} r(\tau, D) \cdot e^{-v\tau} \cdot d\tau = \int_{0}^{\infty} \left[ 1 + \frac{(1 - \mu)t(\Phi(\tau) - D)}{[v \cdot cc]^{1 - \mu}} \right]^{\frac{1}{1 - \mu}} v \cdot cc \cdot e^{-v\tau} \cdot d\tau$

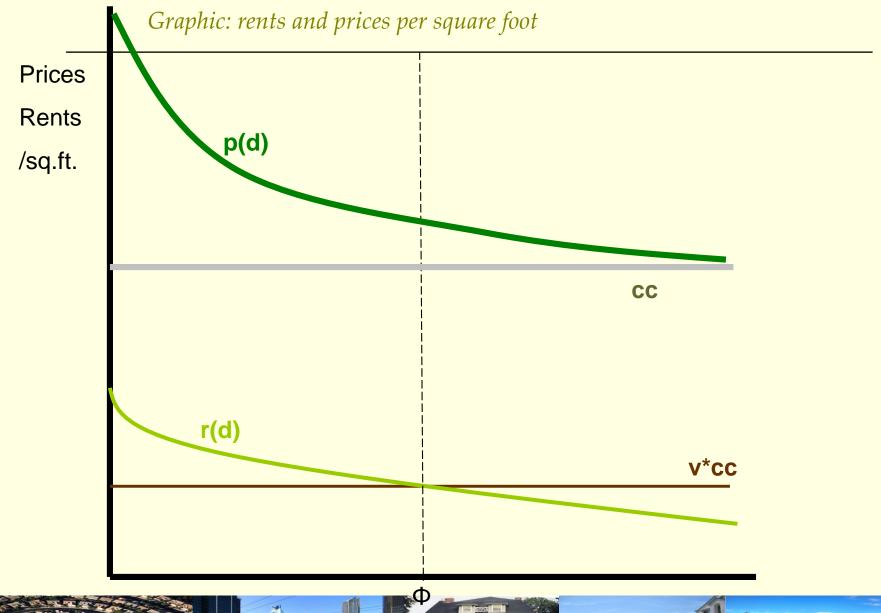
An exponential growth rate can be rationalized for 1 'representative' location:

$$p(\tau = 0, \widetilde{D}) = \left(\frac{v}{v - g}\right) \left[1 + \frac{(1 - \mu)t(\Phi - \widetilde{D})}{\left[v \cdot cc\right]^{1 - \mu}}\right]^{\frac{1}{1 - \mu}} cc$$















#### Changes in User Cost in the AMM Model

- In the short to medium run I will assume that population is not mobile. Note that there are four main effects of changes in *v*:
- Decrease in structural user rents
- Increase in demand for space and larger homes: land rents increase everywhere
- Structure-intensive locations more attractive: land rents decrease in central locations
- Discounting effect in price equation: applicable only to land







# **Other Manufactured Durables**

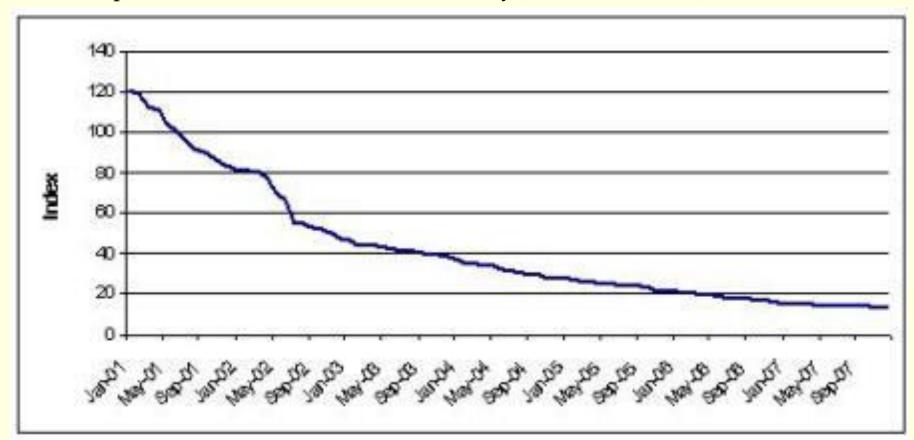






## Other Manufactured Durables

Computer Price Index, consumer, monthly (index, 2001=100)



Leasing cost with decreasing interest rates?









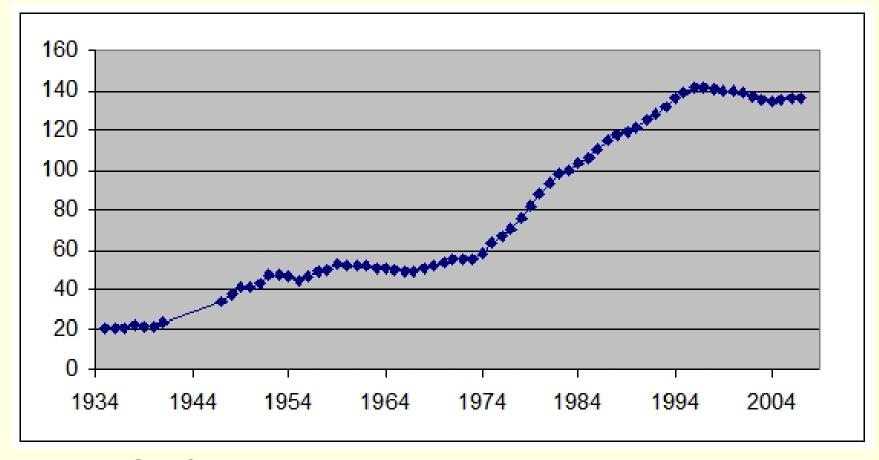
# Other Manufactured Durables







#### Consumer Price Index: New Cars



Leasing Costs?







### Manufactured Homes

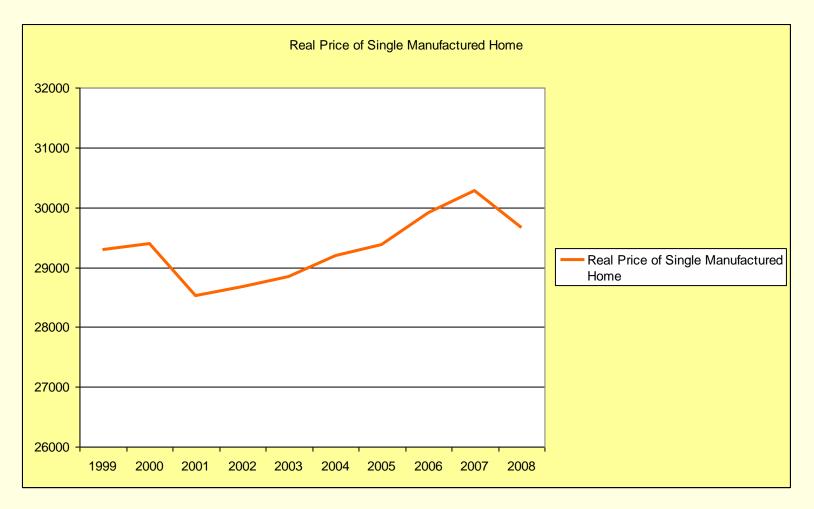








#### Evolution of Home Prices: Manufactured Single









#### Financing/leasing a mobile home

#### Buy a 30,000 mobile structure:

Mortgage rate 8%: Annual payment 2,641

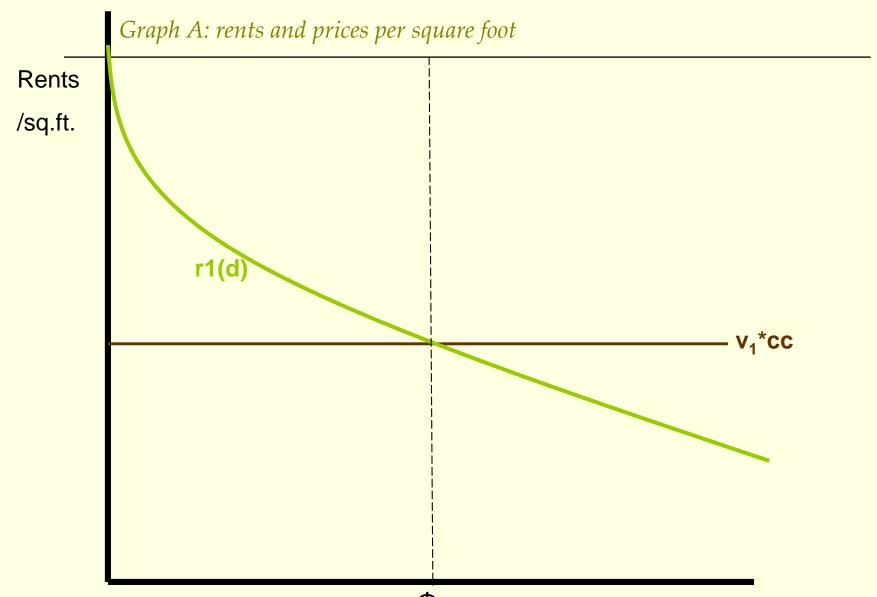
Mortgage Rate 6% Annual Payment 2,158

20% percent cheaper (v\*cc)





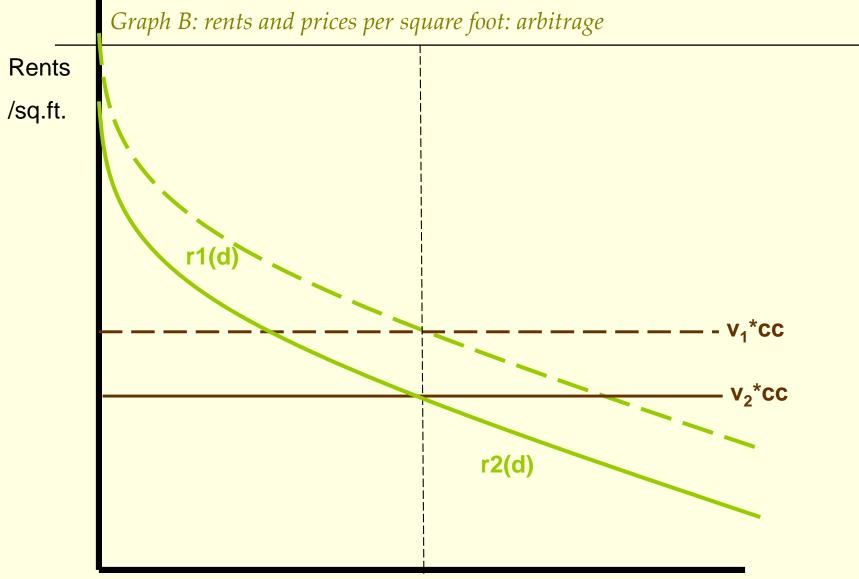






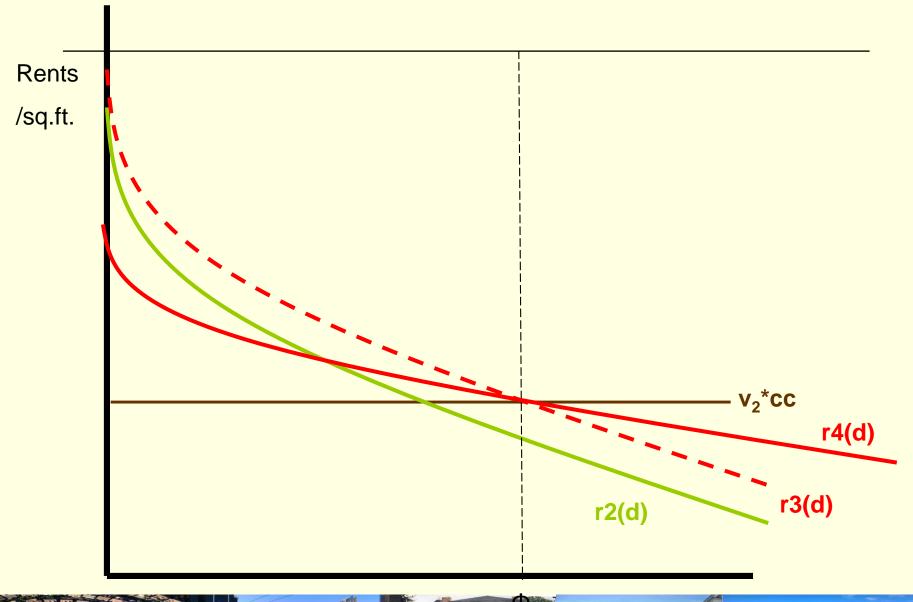








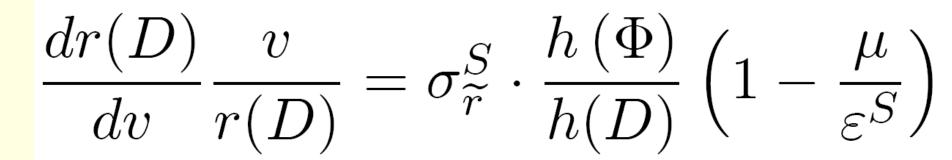


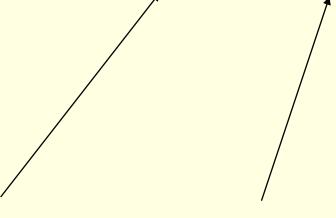






#### Notional Rents are Endogenous to User Costs





Structural Share on Rents

(versus land)

Relative Size at Edge

Demand Supply of Space (Land)





Housing Values and Changes in User Cost

$$\frac{dp(\widetilde{D})}{dv} \frac{v}{p(\widetilde{D})} = \left(\frac{v}{v - g}\right) \left[\sigma_{\widetilde{p}}^S \cdot \frac{h(\Phi)}{h(\widetilde{D})} \left(1 - \frac{\mu}{\varepsilon^S}\right) - 1\right]$$







#### Main takeaways

- Rents should decline with lower user costs: proportionally more in areas where land is not valuable
- Demand for space goes up
- Land rents go up generally... but less in land-intensive locations
- Rental payments may go down, but less so in elastic supply areas
- Land values should go up unambiguously, but structure values should not change!
- Final increase in home values depends on:
  - •Land shares (discounting effect + increase in land rents )
  - •Supply elasticity (impact of increased demand on land rental payments)







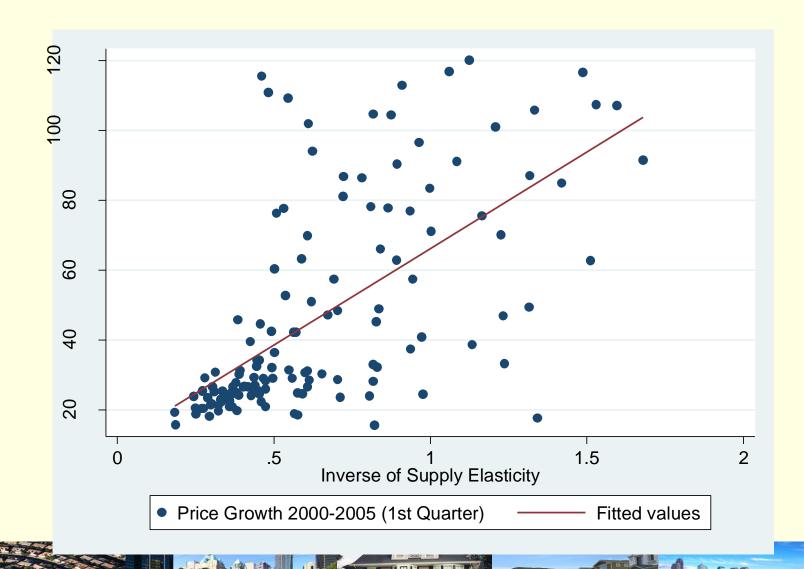
Empirics: Boom, Elasticity and Land Shares





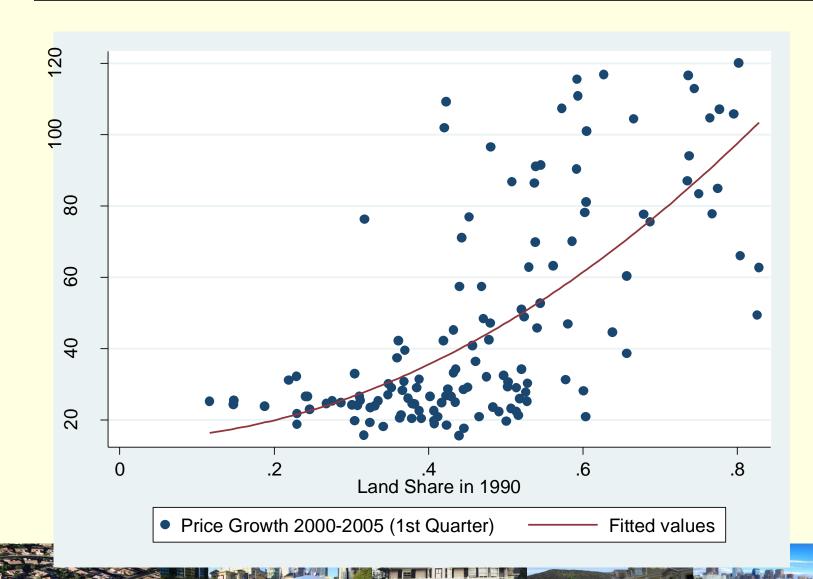


#### Price Growth During the Boom and Supply Elasticity





#### Price Growth During the Boom and Land Shares







#### Real Estate Boom and Fundamentals

	Price Growth 2000-2005 (1st Quarter)	
Inverse of Supply Elasticity	31.445 26.013 32.138 22.349 (6.605)*** (5.549)*** (6.556)*** (6.418)***	ŧ
Land Share in 1990	85.802 99.675 104.469 65.224 (14.574)*** (14.654)*** (17.572)*** (15.150)**	
Log Price 2000 - Log Price 1970	-18.631 (9.993)*	
Middle Atlantic	-1.535	
East North Central	(20.037) -10.304	
West North Central	(20.207) -5.673	
South Atlantic	(20.979) 2.53	
East South Central	(19.732) -17.299	
West South Central	(20.722) -17.963	
Mountain	(20.631) -14.237	
Pacific	(20.117) 14.931	
Observations	(19.594) 137 137 137 137	
R-squared	0.52 0.6 0.53 0.62	

Standard errors in parentheses





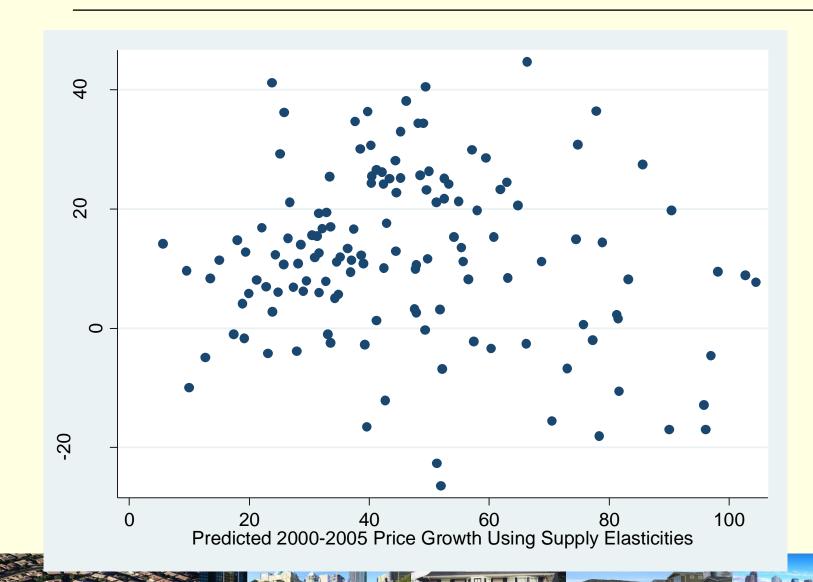


# "Expected" Growth and Bust



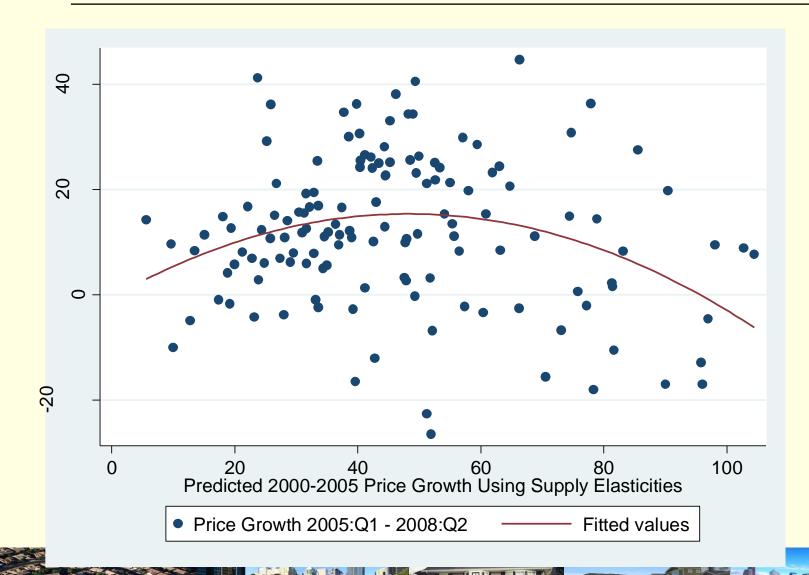


## "Expected" Growth and Subsequent Bust





## "Expected" Growth and Subsequent Bust







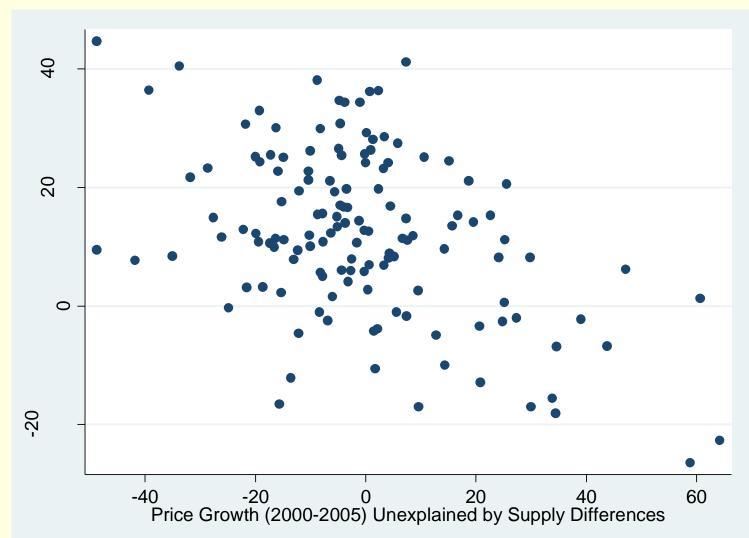
# Unexplained Growth and Bust







## Unexplained Growth and Subsequent Bust

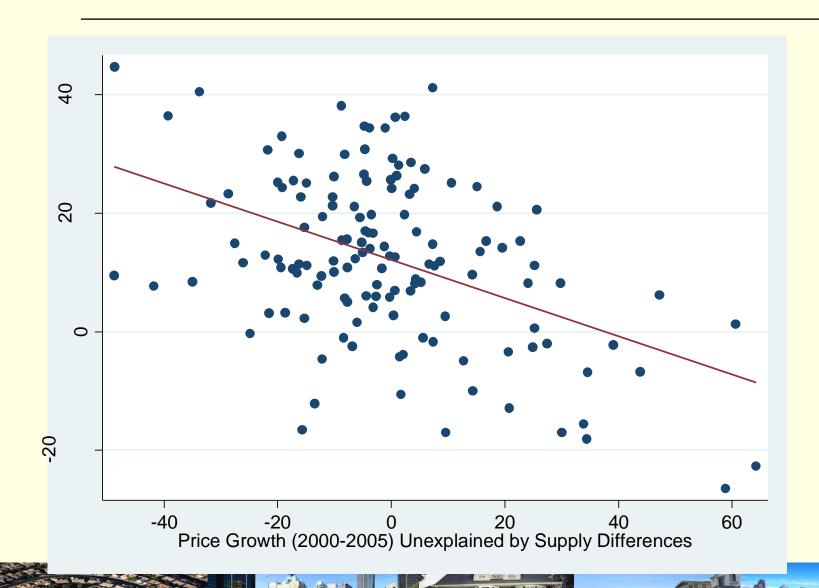








## Unexplained Growth and Subsequent Bust







# Under the null of common shocks to the user cost of housing capital:

- Rents on structure should fall
- •Land rents should increase in most locations...
- ... but less so in land-intensive areas
- Aggregate rents should decrease, specially with low land values
- Rental payments should decrease with inelastic demand
- •Rents endogenous and contingent: P/R ratios not useful
- •Land Rental payments should increase more with inelastic supply
- •Land prices should increase: discounting + rental growth
- Construction value should not change
- Home values should go up more in areas with high land ratios