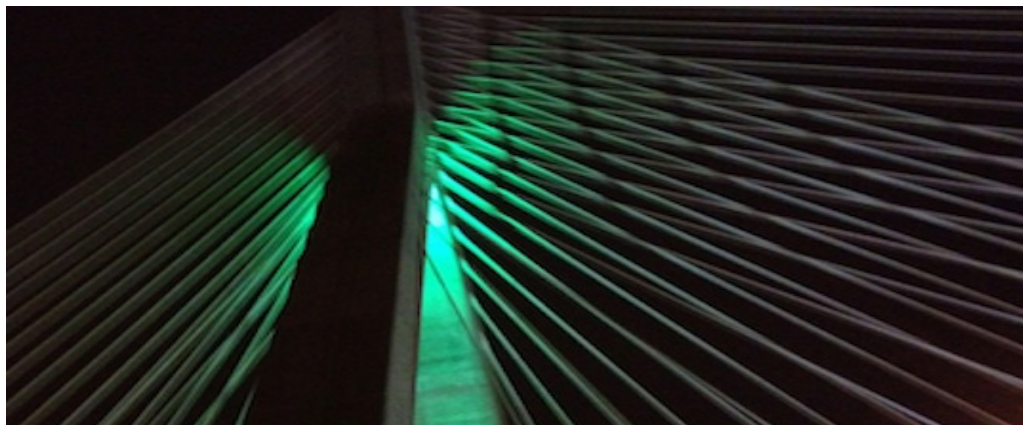


# What is the Digital Learning Lab?

- Collaborative program between ODL and MIT's academic departments with a mission to learn, collaborate, and innovate on the use of digital learning on campus and beyond.
- Digital learning experts in the departments
  - Departmental teaching staff that serve as liaisons between ODL and academic departments
  - Collaborate with faculty on MOOC and residential courses
  - Work together to build and develop digital learning projects
- A community of practice sharing innovations, developing tools, supporting best practices

# Blended Learning in Mechanical Engineering [2.01: Elements of Structures]



Simona Socrate

- First run (traditional) Fall 2012
- Online content developed spring/summer 2013
- Blended-learning model since Fall 2013

Each week a new chapter is released  
Material for each week include:

a mandatory Learning Sequence with  
videos and worked example problems



a mandatory Problem Set



an in-class Quizlet



optional worked example problems



lecture and recitation Notes



Week 2

**Weekly Overview**

**Introduction to  
MATLAB: Part 2**

Lesson Sequence due  
Apr 07, 2014 at 01:00

**Learning Sequence 2**

Lesson Sequence due  
Apr 07, 2014 at 01:00

**Problem Set 2**

Problem Set due Apr 10,  
2014 at 01:00



**Quizlet 1 (Axial  
Loading)**

**Example Problems**

**Board Notes**

- Each week students are assigned a learning sequence: Expert solution strategies are demonstrated in interactive exercises and videos

## QUIZ 1

## Week 4

## Weekly Overview

Learning Sequence 4 [video time: 37m]  
Learning Sequence due October 05, 2015 at 01:00

Problem Set 4  
Problem Set due Oct 08, 2015 at 01:00

## Quizlet 3

## Example Problems

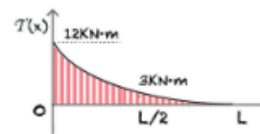
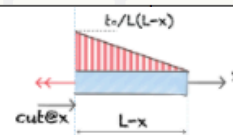
## Board Notes W4

## Week 5

## Week 6

## QUIZ 2

## V5\_4: THE AXIAL TORQUE DIAGRAM FOR DISTRIBUTED LOADS



Remember: a positive  $t_x(x)$  has the double arrow pointing in the  $+x$  direction!

Then, we plot  $t_x(x)$  and note that  $t(x=0) = t_0 = 8 \text{ kN}$ .

To obtain  $\mathcal{T}(x)$ , we cut the shaft at  $x$ , draw the FBD, and impose equilibrium ( $\sum M_x = 0$ ).

$$\sum M_x = 0 = -\mathcal{T}(x) + \underbrace{\int_x^L \frac{t_0}{L} (L-x') dx'}_{\text{area under curve}} = -\mathcal{T}(x) - \frac{t_0}{L} \left[ \frac{(L-x')^2}{2} \right]_x^L$$

(If you cut at  $x$ , remember to use  $x'$  inside the integrall)

$$\mathcal{T}(x) = \frac{t_0}{L} (L-x)^2$$

Note the dimensions:

$$\frac{[\text{N}]}{[\text{m}]} \cdot [\text{m}]^2 = [\text{N} \cdot \text{m}] \checkmark$$

Note: you can also obtain this as the area under the curve:

$$\frac{t_0}{L} (L-x) (L-x) \frac{1}{2}$$

## Courseware Course Info Piazza Progress Instructor

## Week 1

## Week 2

## Week 3

## QUIZ 1

## Week 4

## Weekly Overview

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## Quizlet 3

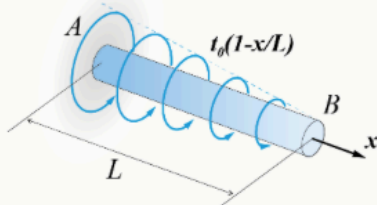
## Example Problems

## Board Notes W4

## Week 5

## E5\_3: AXIAL TORQUE DIAGRAM FOR DISTRIBUTED LOADING

The shaft in the figure has length  $L = 3 \text{ m}$  and is loaded by a distributed torque  $t_x(x) = t_0 \left(1 - \frac{x}{L}\right)$ , linearly varying from a maximum value of  $t_x(x=0) = t_0$  at the fixed support  $A$  to a value of  $t_x(x=L) = 0$  at the free end of the shaft  $B$ . The parameter  $t_0$  has a value of  $8 \text{ kN}\cdot\text{m/m}$ .



E5\_3\_1 (1 point possible)

Obtain a symbolic expression (in terms of  $t_0$ ,  $x$ , and  $L$ ) for the axial torque resultant  $\mathcal{T}(x)$  along the shaft:

$\mathcal{T}(x) =$



CHECK

SHOW ANSWER

- Each week, students are assigned an interactive problem set with immediate feedback on each answer. Students rely on embedded tools (MATLAB) to diminish algebra burden

Now, using the MATLAB window below to do the integration, obtain a symbolic expression for the axial torque resultant  $\mathcal{T}(x)$  along the shaft. For these quantities use corresponding symbolic MATLAB variables `t_0`, `x`, `L` and `T(x)` in your script. Also, remember to use `xp` as the variable of integration.

1 % Your code here

Unanswered

Week 1

Week 2

Week 3

QUIZ 1

Week 4

Weekly Overview

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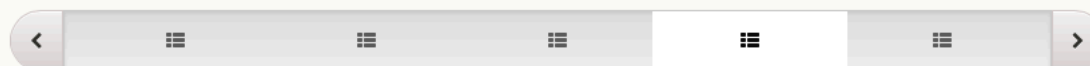
Quizlet 3

Example Problems

Board Notes W4

Week 5

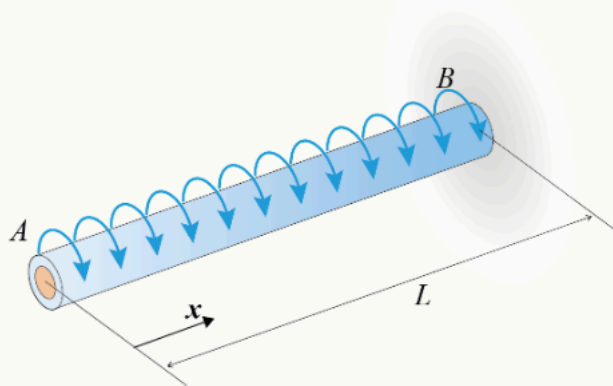
Week 6



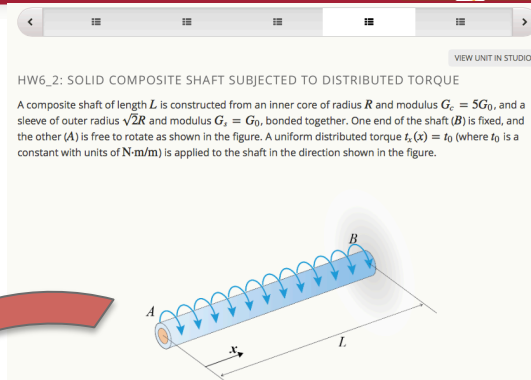
[VIEW UNIT IN STUDIO](#)

### HW6\_2: SOLID COMPOSITE SHAFT SUBJECTED TO DISTRIBUTED TORQUE

A composite shaft of length  $L$  is constructed from an inner core of radius  $R$  and modulus  $G_c = 5G_0$ , and a sleeve of outer radius  $\sqrt{2}R$  and modulus  $G_s = G_0$ , bonded together. One end of the shaft ( $B$ ) is fixed, and the other ( $A$ ) is free to rotate as shown in the figure. A uniform distributed torque  $t_x(x) = t_0$  (where  $t_0$  is a constant with units of  $\text{N}\cdot\text{m}/\text{m}$ ) is applied to the shaft in the direction shown in the figure.



- 4 days after Pset is due and solutions are posted, students take a Quizlet:
- in class, 15 minutes, pen/paper, identical to one of the previous week Lseq or Pset problems.



FALL 2015  
2.01-Elements of Structures

Quizlet 4

Your name: \_\_\_\_\_

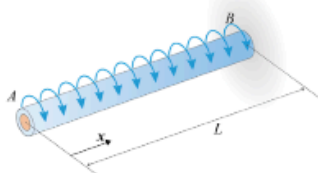
$$\frac{d\varphi}{dx}(x) = \frac{T(x)}{(GI_p)_{eff}(x)}; \quad \gamma(x, r) = r \frac{d\varphi}{dx}(x); \quad \tau(x, r) = G(x, r) \cdot \gamma(x, r);$$

$$I_p \text{ (thin wall)} = 2\pi R^3 t; \quad I_p \text{ (solid)} = \pi R^4 / 2$$

Note that you need to draw FBDs and check your units work in all the answers (e.g.,  $\frac{F \cdot L}{m} \cdot m^3 = N$ )

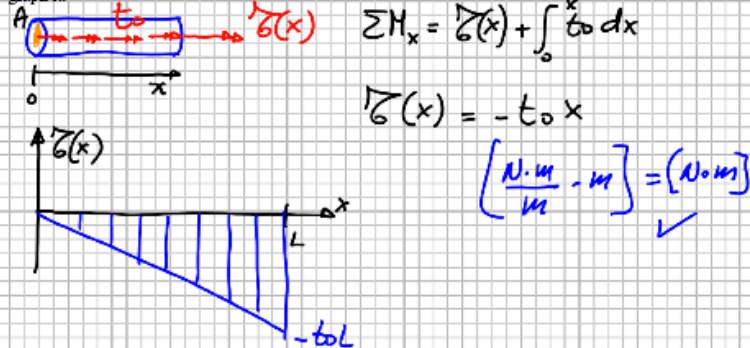
Problem HW6\_2 [5 pts]

A composite shaft of length  $L$  is constructed from an inner core of radius  $R$  and modulus  $G_c = 5G_0$ , and a sleeve of outer radius  $2\sqrt{R}$  and modulus  $G_s = G_0$ , bonded together. One end of the shaft ( $B$ ) is fixed, and the other ( $A$ ) is free to rotate as shown in the figure. A uniform distributed torque  $t_x(x) = t_0$  (where  $t_0$  is a constant with units of N-m/m) is applied to the shaft in the direction shown in the figure.



ANSWER ALL questions below in symbolic form in terms (as needed) of position ( $x$ ) and of the known quantities  $R, L, G_0, t_0$ .

1] (1.5 pt) Draw a free body diagram to obtain an expression for the axial torque resultant  $T(x)$ , and graph it:



2] (1.5 pt) Obtain an expression for the twist rate  $\frac{d\varphi}{dx}$ :

$$(GI_p)_{eff}(x) = G_c I_c + G_s I_s = 5G_0 \left( \frac{\pi R^4}{2} \right) + G_0 \frac{\pi}{2} \left( (\sqrt{2}R)^4 - R^4 \right)$$

$$= \left( \frac{5}{2} + \frac{3}{2} \right) G_0 \pi R^4 = 4G_0 \pi R^4$$

$$\frac{d\varphi}{dx} = \frac{T(x)}{(GI_p)_{eff}(x)} = \frac{-t_0 x}{4\pi G_0 R^4} \left[ \frac{\frac{N \cdot m}{m} \cdot m}{\frac{N \cdot m}{m^2} \cdot m^4} \right] = \left[ \frac{1}{m} \right] \checkmark$$

3] (2pt) Obtain a symbolic expression for the maximum magnitude of the shear stress in the shaft  $\tau_{max}$ . (Hint: where does the maximum magnitude of twist rate occur?). Sketch the profile of shear stress, as a function of radial position, on the section where  $\tau_{max}$  occurs

$|T| = |G \gamma| = \left| G r \frac{d\varphi}{dx} \right|$

for constant cross section max  $r$  where  $\left| \frac{d\varphi}{dx} \right|$  is max

$\left| \frac{d\varphi}{dx} \right|_{max} = \frac{t_0 L}{4\pi G_0 R^4}$

Shear on cross section  $x=L$

@ outer radius of core:  
 $G = 5G_0, r = R$

$|T_c| = 5G_0 R \frac{t_0 L}{4\pi G_0 R^4}$

$= \frac{5}{4} \frac{t_0 L}{\pi R^3}$  MAX

$|T_s| = G_0 \sqrt{2} R \frac{t_0 L}{4\pi G_0 R^4}$

$|T_s| = \frac{\sqrt{2}}{4} \frac{t_0 L}{\pi R^3}$

$\left[ \frac{\frac{N \cdot m}{m} \cdot m}{\frac{N \cdot m}{m^2} \cdot m^3} \right] = \left[ \frac{N}{m^2} \right] \checkmark$



each new “task” reactivates mental skemes of previous tasks

Courseware Course Info Piazza Progress Instructor

Week 1

Week 2

Week 3

QUIZ 1

Week 4

#### Weekly Overview

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Problem Set due Oct 08, 2015 at 01:00

#### Quizlet 3

#### Example Problems

#### Board Notes W4

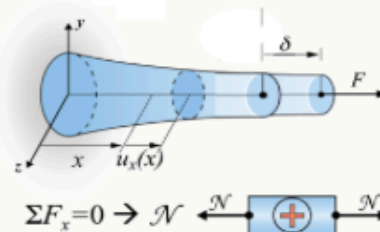
Week 5

Week 6

QUIZ 2

### D6\_1: SYNOPSIS OF TORSION

#### Uniaxial Loading



Sections  $\perp x$ : stay flat, translate in  $x$  by  $u(x)$

$$\mathcal{N}(x) = \int_A \sigma_n(x, y, z) dA$$

$$\frac{du(x)}{dx}$$

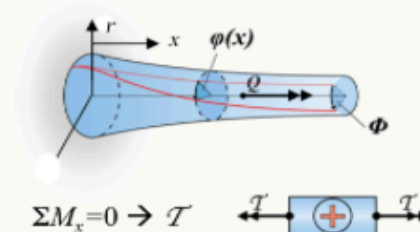
$$\varepsilon_a(x) = \frac{du(x)}{dx}$$

$$\sigma_n(x, y, z) = E(x, y, z) \cdot \varepsilon_a(x)$$

$$\frac{du(x)}{dx} = \frac{\mathcal{N}(x)}{(EA)_{\text{eff}}(x)}$$

$$(EA)_{\text{eff}}(x) = \int E(x, y, z) dA$$

#### Torsion



Sections  $\perp x$ : stay flat, rotate around  $x$  by  $\varphi(x)$

$$\mathcal{T}(x) = \int_A r \cdot \tau(r, x) \cdot dA$$

$$\frac{d\varphi(x)}{dx}$$

$$\gamma(x, r) = r \frac{d\varphi(x)}{dx}$$

$$\tau(x, r) = G(x, r) \cdot \gamma(x, r)$$

$$\frac{d\varphi(x)}{dx} = \frac{\mathcal{T}(x)}{(GI_p)_{\text{eff}}(x)}$$

$$(GI_p)_{\text{eff}}(x) = \int r^2 G(x, r) dA$$



In class more time is spent on simple demonstrations / exploration with every-day props, with student discussions, interaction.

The online platform allows integration of computational tools (FE methods) where students can actively explore solutions to more complex (“real life”) problems



Courseware Course Info Piazza Progress Instructor

Week 1  
Week 2  
Week 3  
QUIZ 1  
Week 4  
Week 5  
Week 6  
QUIZ 2  
Quiz 2 Info  
Xtra Quiz Prep Q2  
Quiz 2 (Torsion & Bending)

F13Q2\_2: STATICALLY-INDETERMINATE COMPOSITE BEAM

The statically-indeterminate composite beam  $AB$  of length  $2L$  is fixed at  $A$  ( $x = 0$ ) and is simply supported at  $B$  ( $x = 2L$ ). The beam is composed of a core of modulus  $E_0$  of constant square cross section of dimensions  $2h_0 \times 2h_0$  bonded inside a sleeve of modulus  $2E_0$  and constant square cross section of outer dimensions  $4h_0 \times 4h_0$ , as indicated in the figure. The beam is loaded by a downward concentrated load of magnitude  $P$  applied at the midspan of the beam ( $x = L$ ) as indicated.

Courseware Course Info Piazza Progress Instructor







Week 1  
Week 2  
Week 3  
QUIZ 1  
Week 4  
Week 5  
Week 6  
QUIZ 2  
Finite Elements (Optional)  
Introduction to the Finite Elements Method: Part 1  
Introduction to the Finite Element Method: Part 2  
Introduction to the Finite Element Method: Part 3

EF1\_2: STRESS CONCENTRATION IN A STEPPED BAR IN AXIAL LOADING: THE FE SOLUTION

Solve







## 2.01 Fall 2014 survey: factors that contributed to learning

Rating Scale: 1=Strongly Disagree, 7=Strongly Agree, N/A=Not Applicable (7 is best)

	AVG	1 2 3 4 5 6 7	RESPONSES	STDEV
Pset with instant feedback	6.2		33	1.44
Video Lectures	6.2		32	1.17
Lecture Notes	6.2		31	1.26
Interactive Practice Problems	6.6		33	0.61
Quizlets	6.4		34	0.92
embedded MATLAB	5.0		33	1.79

## 2.01 Spring 2015 survey: factors that contributed to learning

Rating Scale: 1=Strongly Disagree, 7=Strongly Agree, N/A=Not Applicable  
(7 is best)

	AVG	1 2 3 4 5 6 7	RESPONSES	MEDIAN	STDEV
Pset with instant feedback	6.2		17	7.0	1.19
Video Lectures	6.2		16	7.0	1.11
Lecture Notes	5.9		16	6.5	1.39
Interactive Practice Problems	6.6		17	7.0	0.62
Quizlets	6.3		17	6.0	0.85
Embedded MATLAB	6.2		16	7.0	1.56

## Open Response

### Quizlet feedback

- The quizlets were good - they helped me check in and stay on track with understanding material.
- I like having the quizlets. It makes me stay on top of my work and it made the semester much easier.
- The weekly quizlets ensured I had learned what was taught in the previous week.
- I would prefer that quizlets are not exact copies of problem set questions

### Comments from Fall 2012 and Spring 2013 : Traditional, no MITx

- We needed more time to work on the things we learned like recitations or working together. Class and reading wasn't enough for me.
- I relied on the lectures to explain concepts because the textbook was not easy to read or understand, and had poor examples.
- I just didn't have enough opportunity to solidify what I learned because we had OH once a week and recitation once a week. not enough problem solving to understand the topics.
- The last 30 minutes of lecture often felt rushed.

### Comments from Fall 2013 : total flip on ~ ½ of the course

- I liked having edX videos as a supplement to lectures, but I don't think videos are a suitable replacement for in-person lessons. For example, there was an entire video on distributed moments on edX but we didn't really go over it in class (we only did example problems). Rather than including lectures in learning sequences, the material would be more accessible if done in a recitation.
- learning sequences are ridiculously long. Some even 90 min.. thats a whole other lecture!
- ..the edx segment of the course and I felt it was very beneficial to my learning. Having the material available at all times, with example problems and study guides, greatly improved my ability to learn the material and study for examinations.
- ..I also really liked the edX platform for its instant feedback on whether or not your answer was correct.

## Open Response

### Comments from Spring 14, Fall 14, Spring 15: Blended learning

#### **in class demos**

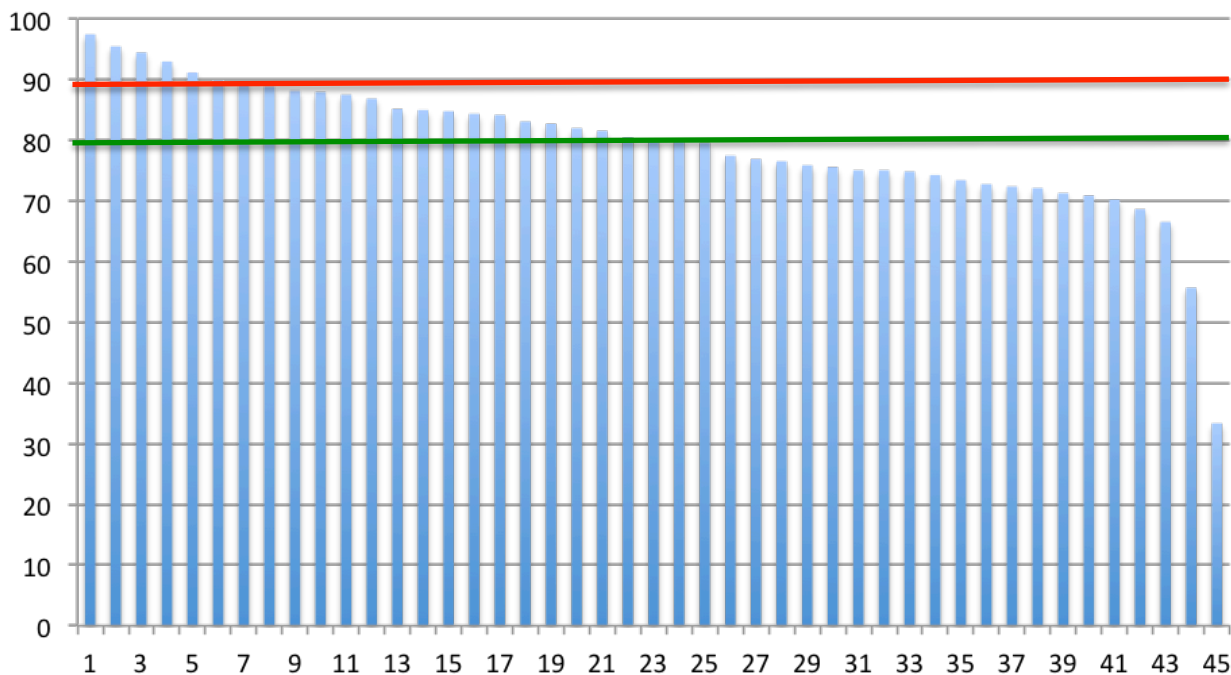
- Her in-class physical objects helped to appreciate the real world application of the theory we were learning.
- I love how you incorporate real-life (high-tech) demonstrations in class every time you explain a new concept
- .. the visualization really helps me understand exactly what a certain variable or equation means!

#### **MITx material**

- the lecture videos were very helpful.
- I like learning sequences for practice.
- mitX platform is a little more concise and can be watched at 2x speed so it is much more efficient than attending lectures.
- I thought the integration of MITx in this course is fantastic. I really liked having the Psets online because you can see the solutions right away and learn from your mistakes. While having video lectures online are pretty time consuming (kind of like having another class period) I did actually think they helped me understand the material better.
- The online components of this class were perfect. It really embodies the type of class I would like to take at MIT for all my 4 years. The ability to have online lectures, psets, lecture notes greatly increases my time that I dedicate to work on other things while still maintaining a great standard of learning the material.

Fall 2012: 2.01 traditional format: **45 students: 10% >90; 50% > 80**

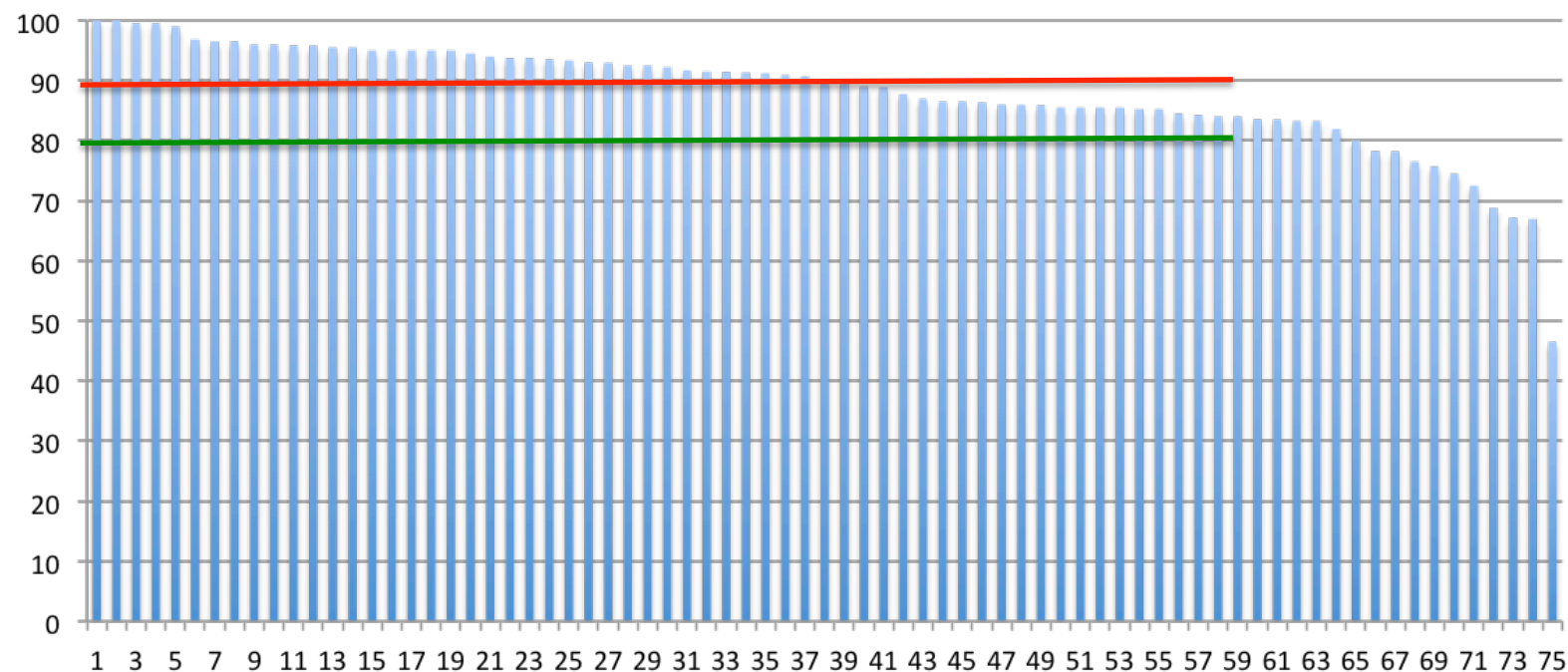
**Cumulative 2.01 grades F12**



Fall 2012: 2.01 traditional format: **45 students: 10% >90; 50% > 80**

Fall 2013: first run of 2.01 on MITx: **75 students: 50% >90; 87% > 80**

cumulative 2.01 grades F13



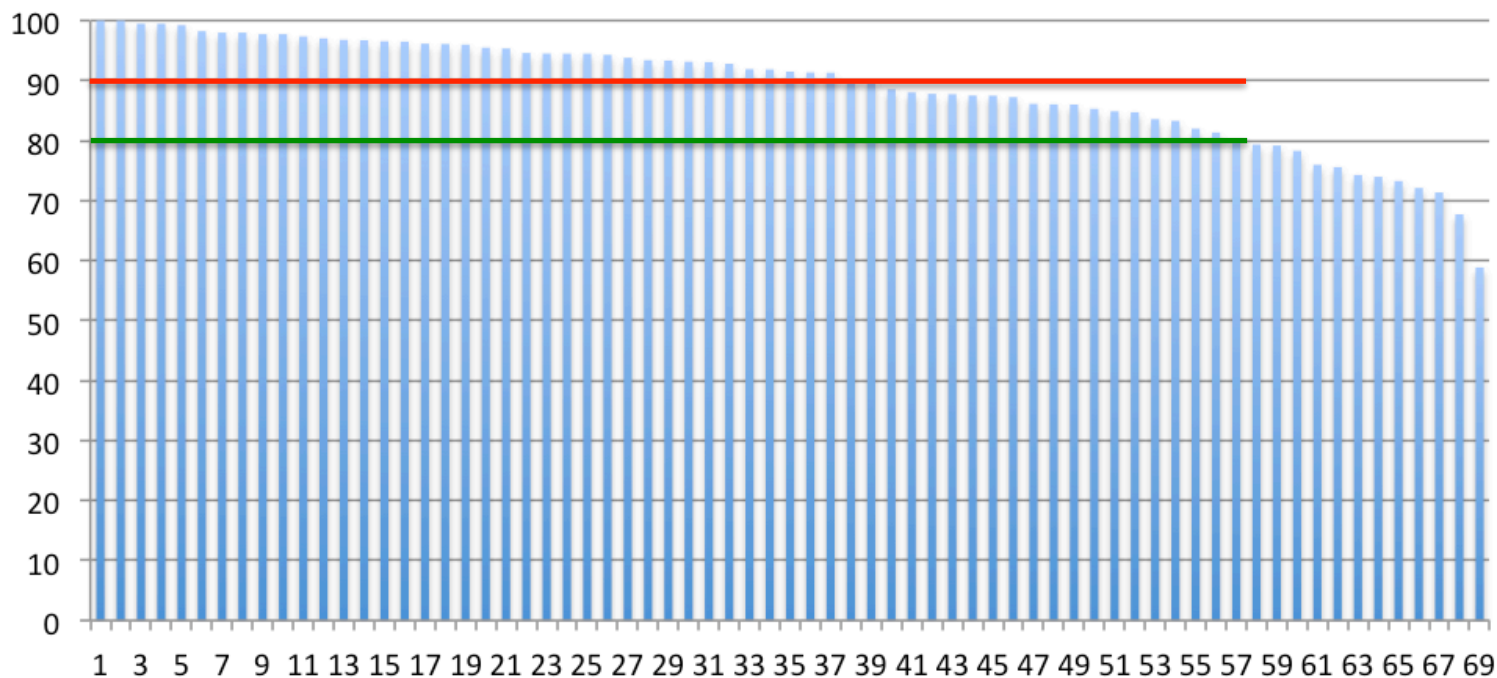


Fall 2012: 2.01 traditional format: **45 students: 10% >90; 50% > 80**

Fall 2013: first run of 2.01 on MITx: **75 students: 50% >90; 87% > 80**

Fall 2015: “steady state” on MITx; **69 students: 56% >90; 85% > 80**

Cumulative 2.01 grades F15



## Costs:

- Initial effort to translate course content to the MITx platform: ODL provides support but faculty leads on content, holds IP.
- (If desired) initial effort to become familiar with the operational details of the platform. Alternatively, rely on support staff.

## Benefits :

- very easy to re-run the course, add/modify content (undergrad TAs in 2.01)
- easy for new faculty to join teaching team and keep curriculum consistent
- freedom from “the classroom clock”. More opportunity to focus on critical course content and rely on online components for prereqs and extensions
- the 21<sup>st</sup> century equivalent to writing a textbook.. that can continually evolve, can be shared and co-authored, personalized updated and expanded



Questions?