Spin fluid and spin nematic states in frustrated quantum magnets

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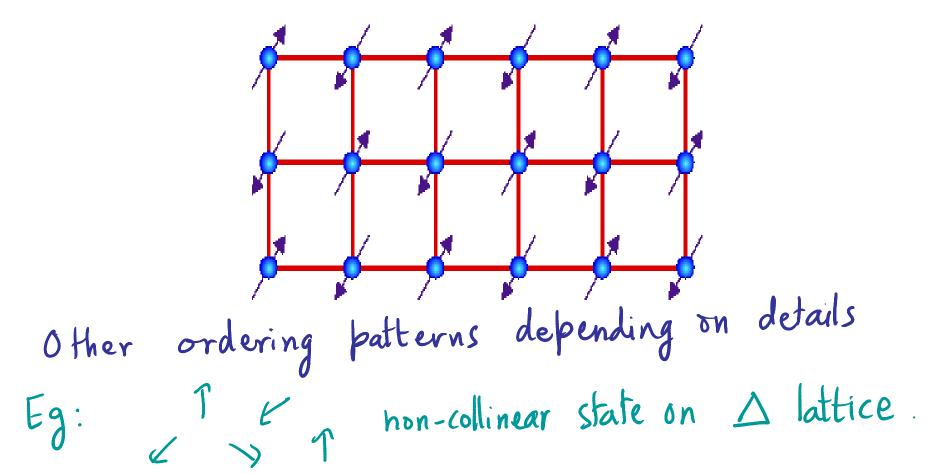
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Quantum magnetism of Mott insulators

Electronic Mott insulators - charges localize below some energy scale "U" Active low energy degree of freedom - electron Shin Fate of local moments at low temperature?? exchange, etc.

Traditional fate – magnetic ordering at low T

Neel ordered state



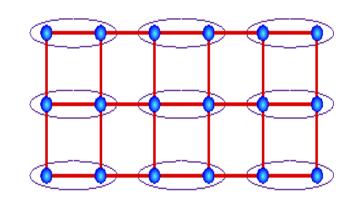
Can quantum fluctuations destroy Neel magnetic ordering at T = 0?

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Yes - well known in d=1.
d>1: Long standing theoretical
 question.
Intense activity in last $20 years.
```

Possible non-Neel phases

QUANTUM PARAMAGNETS

- Simplest: Valence bond solids (spin-Peierls)
- Ordered pattern of valence bonds breaks lattice translation symmetry.
- Elementary spinful excitations have
 S = 1 above spin gap.



 $= (\cancel{p} - \cancel{p})/\sqrt{2}$

Seen in many model calculations.

Are there any genuinely 2d or 3d experimental realizations?

Other ordered non-Neel phases - quantum spin nematics

$$\langle \vec{S} \rangle = 0$$
 but $\langle SS \rangle \neq 0$

=> Spontaneous generation of spin anisobropy without any ordered moment ("Moment-free

(Spontaneous single ion anisotropy)

Where might stabilize a spin nematic?

Eg: S=1 Kagome AF with strong easy axis anisotropy

H =
$$\int \sum_{i=1}^{\infty} S_{i} \cdot S_{i} - D \sum_{i=1}^{\infty} S_{i} \cdot S_{i}$$
 (Damle, TS '06)

$$D \gg J : \langle S \rangle = 0 \text{ but } \langle S_i^{\dagger} \rangle^2 \neq 0$$

Spin liquids and other exotica in quantum magnets

 Traditional quantum magnetism: Ordered ground states (Neel, spin Peierls,)
 Notion of broken symmetry

Modern theory (last 2 decades): Possibility of `spin liquid' states (well-known in d = 1, but also possible in any d).

Eg: Mott insulators with 1 electron/unit cell with no broken symmetry

Excitations with fractional spin (spinons),

Emergent gauge structure, notion of `topological order'

Maturing theoretical understanding - extensive developments in last few years

But where are the spin liquids?

Almost no clear experimental sightings in d > 1 so far.

Hints from theory

- Geometrically frustrated quantum magnets
- "Intermediate" correlation regime

Eg: Mott insulators that are not too deeply into the insulating regime ("weak" Mett insulators)

 More subtle: Intermediate scale physics of doped Mott insulators (in cuprates?)

This talk – focus on specific candidate materials.

Three triangular lattice Mott insulators

1. Cs CuCl - spin-1/2 on anisotropic D lattice Ordered spiral but close to a spin liquid? 2. KET) Cu2 (CN) - "Weak" Mott insulator. A genuine Spin liquid? 3. Ni Gra 254 - Spin-1 on isotropic D lattice Spin liquid or spin nematic?

Very promising candidate for exotica - Cs₂CuCl₄

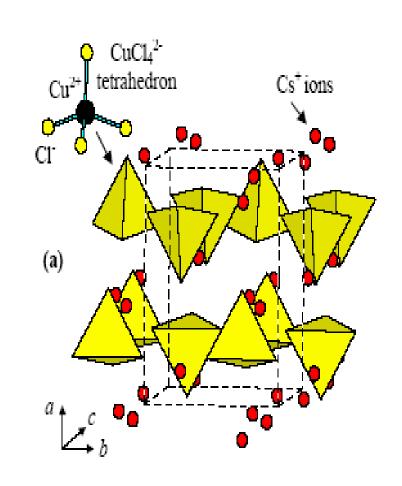
- Transparent layered Mott insulator
- Spin ½ per Cu site on anisotropic triangular lattice

Experiments

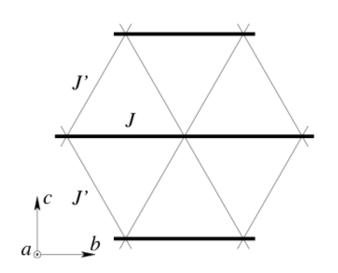
Radu Coldeu's group

Oxford

1996 - present



Known microscopic spin Hamiltonian



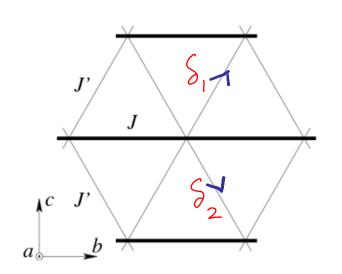
J ≈ 0.375meV

J' ≈J/3

 $J'' \approx 0.045 J$

(weak interlayer exchange)

Known microscopic spin Hamiltonian



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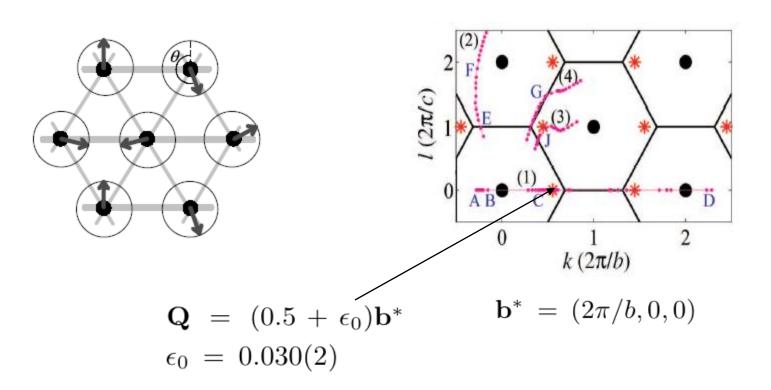
Weak Dzyaloshinski-Moriya interaction along zigzag bonds

$$H_{DM} = -\mathbf{D} \cdot \sum_{\mathbf{r}} \mathbf{S}_{\mathbf{r}} \times (\mathbf{S}_{\mathbf{r}+\boldsymbol{\delta}_1} + \mathbf{S}_{\mathbf{r}+\boldsymbol{\delta}_2})$$

 $D \approx 0.02 meV \approx 0.05 J$

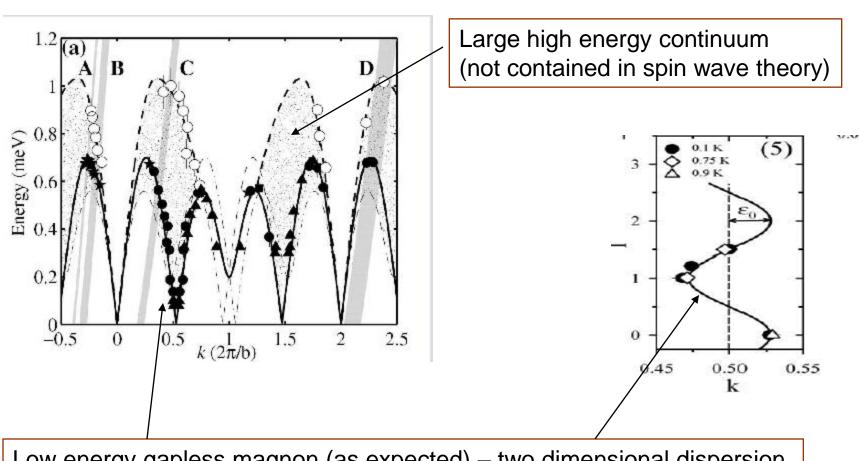
Ordering at low T

Magnetic long range spiral order below T=0.62K with incommensurate wave vector



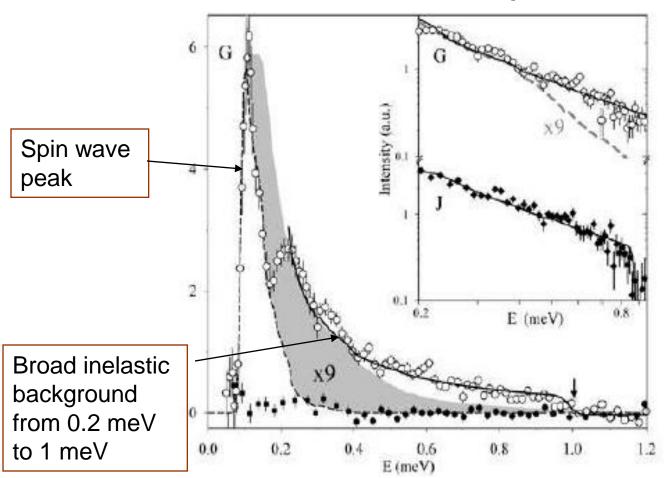
But many unusual phenomena en route!

Spin fluctuation spectrum



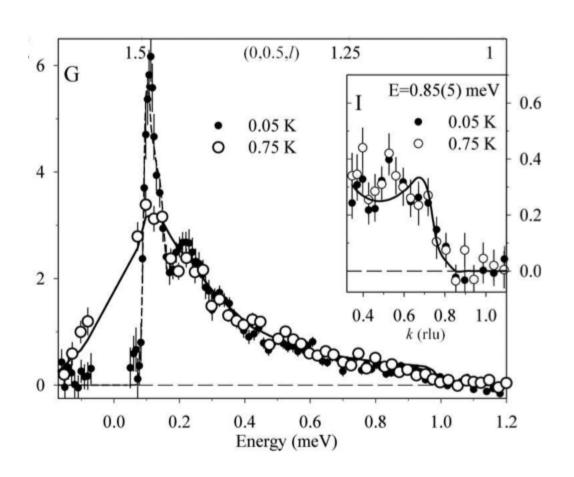
Low energy gapless magnon (as expected) – two dimensional dispersion

Inelastic line shape – failure of spin wave theory



Possibly power law, fit to estimate exponent.

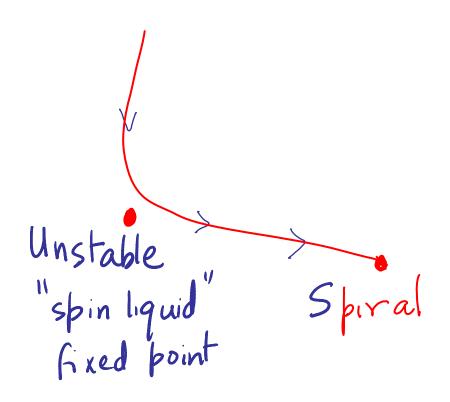
Temperature dependence



Magnon shoots out of broad background on cooling below T_N .

General qualitative similarity to antinodal ARPES in underdoped cuprates.

General viewpoint on the experiments



Unstable fixed point controls broad continuum scattering.

??Nature and description??

General framework:

- 1. Two dimensional but anisotropic
- 2. Spin SU(2) invariant(DM small effect in this energy range)
- 3. Scale invariant?

Candidates (in order of increasing sophistication)

1. Decoupled 1d chains

(Essler, Tsvelik,.....)

Proximate quantum critical point to gapped spin liquid

(Isakov, TS, Kim)

3. `Algebraic spin liquid' (Gapless fermionic spinons coupled to fluctuating gauge field)

(Zhou, Wen)

4. Algebraic vortex liquids

(Alicea, Motrunich, Fisher)

5. Proximate quantum critical point to dimer ordered (spin Peierls) state

(No theory yet!)

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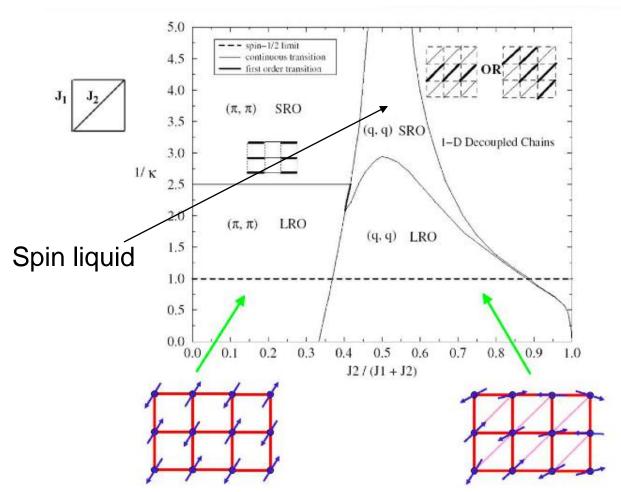
(Alicea, Motrunich, Fisher)

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Chungetal 2001,03

Large-N Phase Diagram - Anisotropic Triangular Lattice

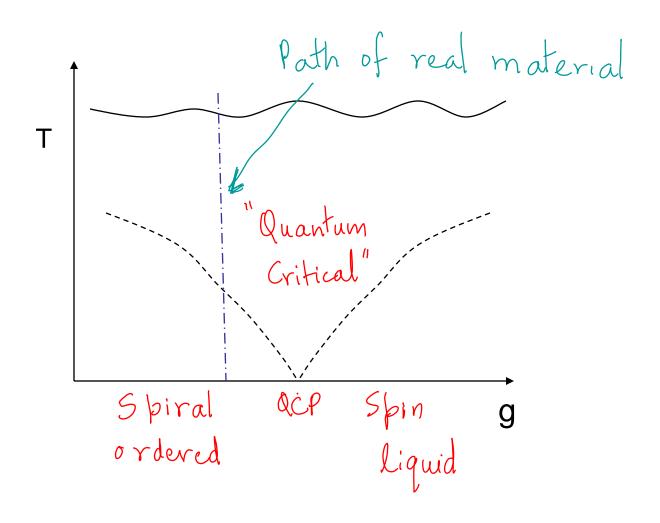


$$\kappa = "2S"$$
 controls quantum fluctuations

$$\mathbf{Q} = (q_x, q_y)$$

magnetic ordering
wave vector

Crossovers near phase boundary to spin liquid



Structure of spiral ordering

$$S:(\underline{r}) \sim \hat{\eta}_{1} \cos(Q \cdot \underline{r}) + \hat{\eta}_{2} \sin(Q \cdot \underline{r})$$

$$\hat{\eta}_{1}^{2} = \hat{\eta}_{2}^{2} = 1 ; \hat{\eta}_{1} \cdot \hat{\eta}_{2} = 0$$

$$\text{Order parameter} = \text{rotation matrix } R$$

$$\in So(3)$$

Topological defects in ordered state

$$SO(3) \sim \frac{SU(2)}{\mathbb{Z}_2} \Rightarrow \text{order parameter}$$
 $Lives in \frac{S^3}{\mathbb{Z}_2}$
 $T_1(\frac{S^3}{\mathbb{Z}_2}) = \mathbb{Z}_2 \Rightarrow \text{point } \mathbb{Z}_2 \text{ vortices}$

Liberating spinons

Chubukov, Sachder, TS 94 Quantum disorder spiral without Isakov, TS, Kim broliferating $\frac{1}{2}$ vortices => redundancy in SU(2) representation of SO(3) matrix unimportant SU(2) matrix $U = \begin{bmatrix} -\overline{b_1} & \overline{z_2} \\ \overline{z_2} & -\overline{c_1} \end{bmatrix}$ (Z1, Z2) = Spin-1/2 Spinons!

Structure of the spin liquid

Paramagnetic phase: Za free 2 gapped (bosonic statistics) Ze vortex survives with gap Effective low energy theory - de confined Zz gauge theory Topologically ordered Zz Spin liquid

Spiral – spin liquid phase transition

Phase transition - condensation of
$$Z_d$$
 $\begin{bmatrix} Z_1 \\ Z_2 \end{bmatrix}$ lives on S^3

Asymptotic critical theory

 $S = \int d^2x \, d^2x$

Scaling of spin fluctuations

Physical spin ~ bilinear of spinons

⇒ Broad inelastic scattering

For
$$q \approx Q$$
, small ω , \top
 $\chi''(q, \omega, \top) \sim \frac{1}{\omega^2 - \gamma} F(\frac{1q - Q}{T}, \frac{\omega}{T})$
 $\eta \approx 1.37$ from Monte-Carlo (large!)

Experiments - hard to measure η

Rough estimate - large $\eta (\approx 0.74)$ qualitatively consistent with theory

Useful future experiments

1. Careful measurement of inelastic line shape for various fixed $q \approx Q$.

2. NMR Relaxation

L ~ T1 ~ T1.37 in quantum critical region

Direct measure of n.

More dramatic consequence -enhanced O(4) symmetry (Isakov, TS, Kim'65)

Under O(4) can rotate
$$\hat{\eta}_1$$
 or $\hat{\eta}_2$ to $\hat{\eta}_3 = \hat{\eta}_1 \times \hat{\eta}_2$ (3rd column of rotation matrix)

$$\Rightarrow \langle \hat{\eta}_3(x) \cdot \hat{\eta}_3(0) \rangle = \langle \hat{\eta}_1(x) \cdot \hat{\eta}_1(0) \rangle = \langle \hat{\eta}_2(x) \cdot \hat{\eta}_2(0) \rangle$$

$$\sim \frac{1}{x^{1+\gamma}} \quad \text{with } \gamma \approx 1-35$$

Microscopics: $\hat{\eta}_3 \sim \text{"vector spin chirality"}$ $\sim \vec{S}(\underline{r}) \times \vec{S}(\underline{r} + \underline{e})$

Detecting vector spin chirality fluctuations -polarized inelastic neutron scattering (Maleyev'95, Isakov,TS,Kim,'05)

Polarization dependent part

- antisymmetric component of spin structure factor ~ (3(00) x 3(x t))

Zero with full SU(2) spin symmetry

Non-Zero due to weak Dzyaloshinski - Moriya D

To 1st order in D, measure vector spin chirality correlations

Expected result in quantum critical regime

For
$$q = Q$$
, $\delta \gg T$,

polarization dependent part

 $R_p(\delta) \sim \frac{1}{7^{2}-1} \frac{5-1}{5-2} (1 \approx 1.37)$

(to linear order in D)

Difficult but doable experiment.

Summary on Cs₂CuCl₄

Concrete version of general idea that Cs₂CuCl₄
 is proximate to a spin liquid

Many testable consequences.

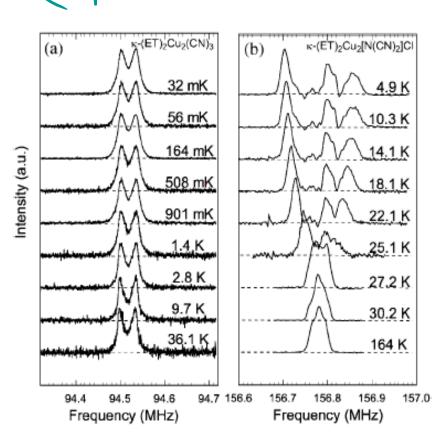
Wish-list for experiments:

- 1. Careful frequency scans at fixed wavevector
- 2. NMR relaxation
- 3. Polarized inelastic neutron

Future theory: Direct second order spiral – dimer transition?

KET) Cu2 (CN) - LONG SOUGHT SPIN LIQUID?

Expt: Kanoda, 2002-present



Weak Mott insulator close to Mott transition.

~ Isotropic D lattice

. No ordering to 32 mK ∠ J≈ 250 K

but $\chi \rightarrow const.$

$$\frac{1}{1}$$
 \rightarrow const.

Promising candidate spin liquid state

Gutzwiller projected Fermi sea PG | Fermi sea (Matrunich '05) remove double occupancy 1/2-filling: Spin wavefunction for particular Spin liquid state.

Rough description: Electrons which have lost their charge "

Thermi Surface of neutral fermionic S=1/2 Spinons.

PRECISE DESCRIPTION

(Metrunich 05

Lee 2 Lee 05)

Effective theory: Fermi sea of spinons coupled to fluctuating U(1) gauge field.

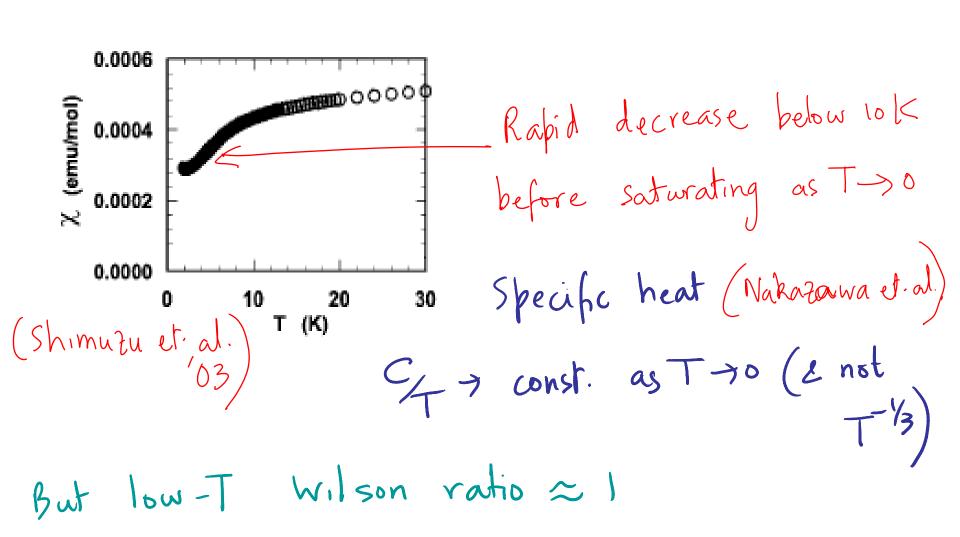
$$H = \int d^2x \quad f^{\dagger} \left(-\left(-i\vec{\nabla} - \vec{a} \right)^2 - \mu \right) f + \left(\vec{\nabla} \times \vec{a} \right)^2$$

e = 11 electric field

Expected properties

X -> const. at low-T C ~ T 2/3 (enhanced by gauge More entropy than in a metal at low-T! Singular 2 kg spin response. Anamolous low-T thermal conductivity 4 ~ T'3

Discrepancy at very low temperature



Instability of the spinon Fermi surface state?

 χ , \subseteq \rightarrow const. in insulator (Lee, Lee, TS) Gabless spinons but no gapless gauge field? Natural route: Pairing (ff) 70 gaps out gauge field but may preserve gapless spinons.

Amperean pairing?

Gauge induced interaction - repulsive for (R -R) fermions but attractive for fermions with 11 momenta (Amperes law)

Mean field theory: Find pairing solution with $\Delta_{\vec{Q}}(\vec{p}) = \langle f(\vec{Q} + \vec{p}) f_{1}(\vec{Q} - \vec{p}) - f_{1}(\vec{Q} - \vec{p}) f_{2}(\vec{Q} - \vec{p}) \rangle + \langle f_{1}(\vec{Q} - \vec{p}) f_{2}(\vec{Q} - \vec{p}) f_{3}(\vec{Q} - \vec{p}) \rangle + \langle f_{1}(\vec{Q} - \vec{p}) f_{3}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) \rangle + \langle f_{1}(\vec{Q} - \vec{p}) f_{3}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) \rangle + \langle f_{1}(\vec{Q} - \vec{p}) f_{3}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) \rangle + \langle f_{1}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) \rangle + \langle f_{1}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) \rangle + \langle f_{1}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec{p}) \rangle + \langle f_{1}(\vec{Q} - \vec{p}) f_{4}(\vec{Q} - \vec$

Ø ∈ maximal curvature points on Fermi Surface

Properties of Amperean paired spin liquid

- 1. $(ff) \neq 0 \Rightarrow U(i)$ gauge field gapped $(get Z_2 \text{ spin liquid})$
- 2. Pairing only in some patches of FS

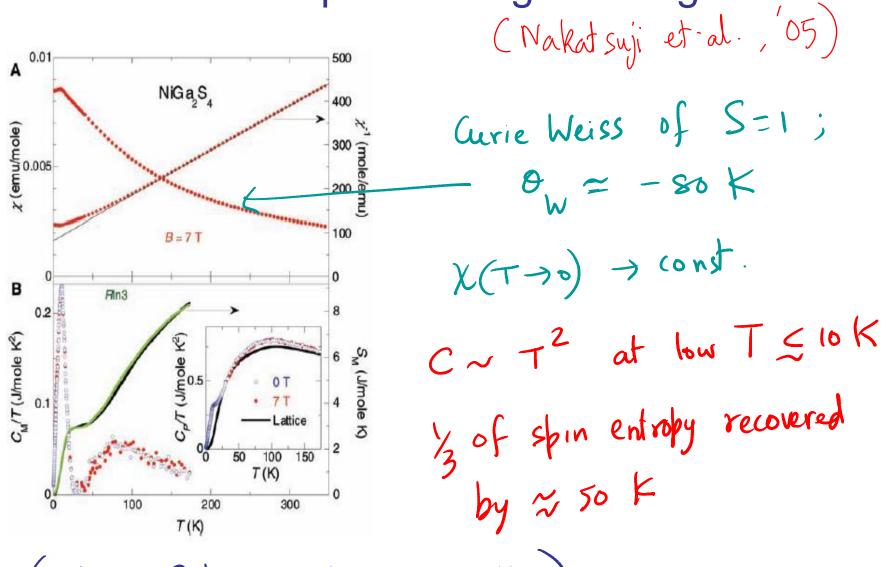
 "gapless" weakly interacting spinons at residual FS"

 =) C~T at low-T.
- 3. Break lattice symmetries in commensurate valence bond solid order coexisting with spin liquid
- 4. KNT like in ordinary metal.

Crucial future experiment

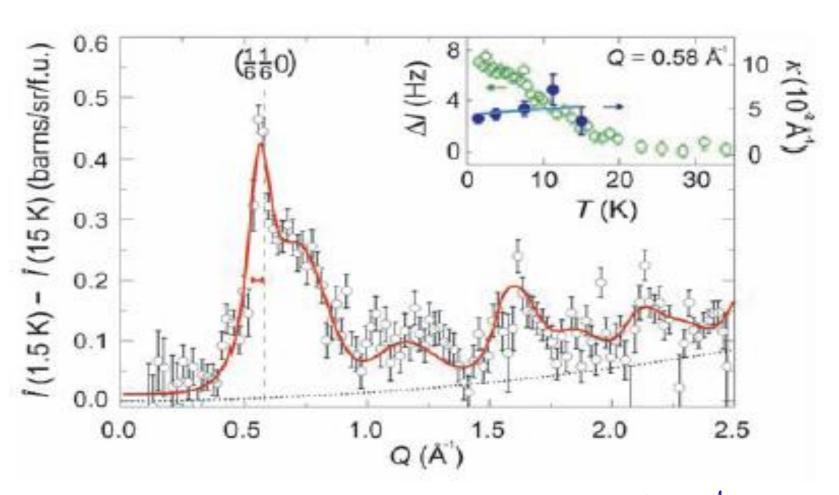
Thermal transport & ~T will be remarkable in an electrical insulator!

(Can distinguish from alternate Scenario of Anderson insulator). NiGa2S4: spin-1 triangular magnet



(Note: Polycrystalline samples)

Powder neutron scattering



No Bragg peak; only short range order!

Quantum spin liquid or nematic?

No obvious (to me!) Spin liquid explanation

Is this a spin nematic?

(5) =0 > No Bragg peaks in neutron expt

$$\left\langle \left\{ S_{\alpha}, S_{\beta} \right\} - 2 \left\{ S_{\alpha\beta} \right\} \right\rangle \neq 0 = 9 \left(n^{\alpha} n^{\beta} - \frac{1}{3} S^{\alpha\beta} \right)$$

=) Broken spin rotations & corresponding Goldstone mode gives T² specific heat.

Specific proposals

Non-collinear nematic (Tsunetsugu, Arikawa) Director na along 3 Ir directions on 3 Sublattices Collinear Ferro-nematic (Lauchli et al., Bhattachargee, Shenoy TS) n uniform independent of site

How to distinguish?

Inelastic neutron scattering: Collinear ferro-nematic: Spins fluctuate in plane Ir to director) anisotropic dynamic susceptibility No single common Non-collinear nematic: plane for all spins.

Summary

 Many interesting new quantum magnets with unusual low temperature physics

 Future – most promising setting to establish the experimental validity of some modern ideas in strong correlation physics (fractionalized quantum liquids, emergent gauge theories, topological order, etc).