

# Angle dependent quasiparticle weight in heavy fermion metals

T. Senthil (MIT)

Pouyan Ghaemi (MIT)

P. Coleman (Rutgers)

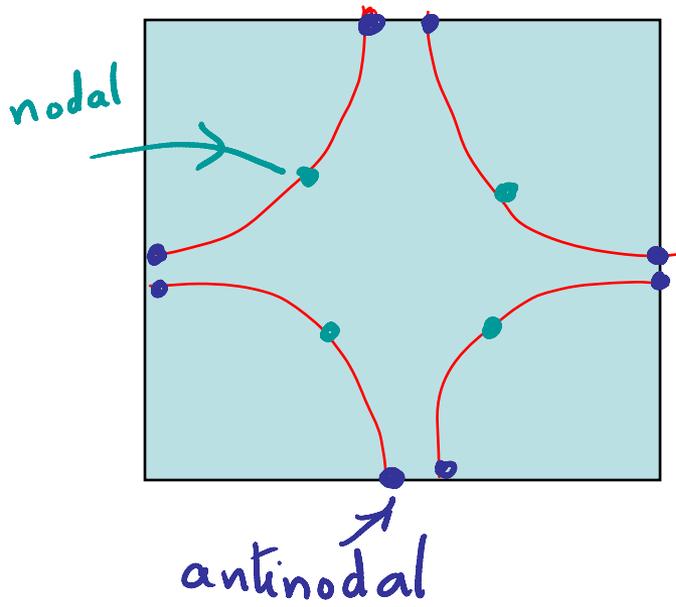


Ghaemi, TS, Phys Rev B '07 and forthcoming .

# Momentum space anisotropy in the cuprate metals

Normal state of cuprates – a non-fermi liquid metal

Differences between different parts of a nominal Fermi surface



Deviation from Fermi liquid  
stronger on moving from nodal  
to antinodal direction.

(Evidence from ARPES and  
transport)

# Strongly correlated metals

Many examples

- Normal state of cuprates
- Heavy electron metal in rare earth intermetallics
- Metals near the Mott transition (eg: organics)

Fermi liquid theory often but not always fails.

# Broad questions

1. Is correlation induced momentum space anisotropy common in correlated metals?
2. How to incorporate correlation effects into a Fermi surface?

1-band Hubbard model: Interesting cluster DMFT calculations (Civelli, Parcollet, Kottiar, Georges, ...)

'04 - '07

## Related simpler question

Momentum dependence of correlation effects in a Fermi liquid metal??

This talk – focus on heavy fermi liquid metals

Simple and general reasoning: strong momentum dependence of quasiparticle spectral weight

# Heavy electron metal: A strongly correlated Fermi liquid

Weakly correlated conduction band coupled to correlated f-band.

- Large effective mass
- Small quasiparticle residue
- Large Fermi surface – localized f-moments dissolve into Fermi sea by Kondo singlet formation.

## Simplified Anderson lattice model for heavy fermi liquids

$$H = \sum_{\mathbf{k}} \epsilon_{\mathbf{k}} c_{\mathbf{k}}^{\dagger} c_{\mathbf{k}} + V \sum_i (c_i^{\dagger} f_{i\alpha} + h.c.) \\ + \sum_{\mathbf{k}} \epsilon_{\mathbf{k}f} f_{\mathbf{k}}^{\dagger} f_{\mathbf{k}} + U \sum_i (n_i^f)^2 - \mu_f \sum_i n_i^f$$

Weak - U limit : Hybridized c and f bands

Fermi volume includes both c and f electrons  
but effective mass not large, and  $Z \sim o(1)$ .

# Strong correlations: Kondo lattice

$\frac{1}{2}$  - filling for f-band

Large  $-U$  limit  $\Rightarrow$  each localized f-orbital  
is singly occupied.

Lattice of localized f-moments coupled to  
c-electrons

$$H = \sum_{\mathbf{k}} \epsilon_{\mathbf{k}} c_{\mathbf{k}}^{\dagger} c_{\mathbf{k}} + J \sum_i \vec{S}_i \cdot c_i^{\dagger} \frac{\vec{\sigma}}{2} c_i$$

$$\vec{S}_i = \text{f-moment}; \quad J \sim o(v^2/U)$$

(N. Read et al, '86)  
Mullis, Lee '86

## Slave particle formulation of Kondo lattice

Write  $\vec{S}_i = f_i^\dagger \frac{\vec{\sigma}}{2} f_i$  with  $f_i^\dagger f_i = 1 \forall i$

Important :  $f_{i\alpha}$  not electrons

- neutral spin- $\frac{1}{2}$  fermions ("spinons")

$$H = \sum_{\mathbf{k}} \epsilon_{\mathbf{k}} c_{\mathbf{k}}^\dagger c_{\mathbf{k}} - J \sum_i (|c_i^\dagger f_i|^2 + h.c.)$$

Constraint :  $f_i^\dagger f_i = 1 \forall i$

# Hybridization mean field theory

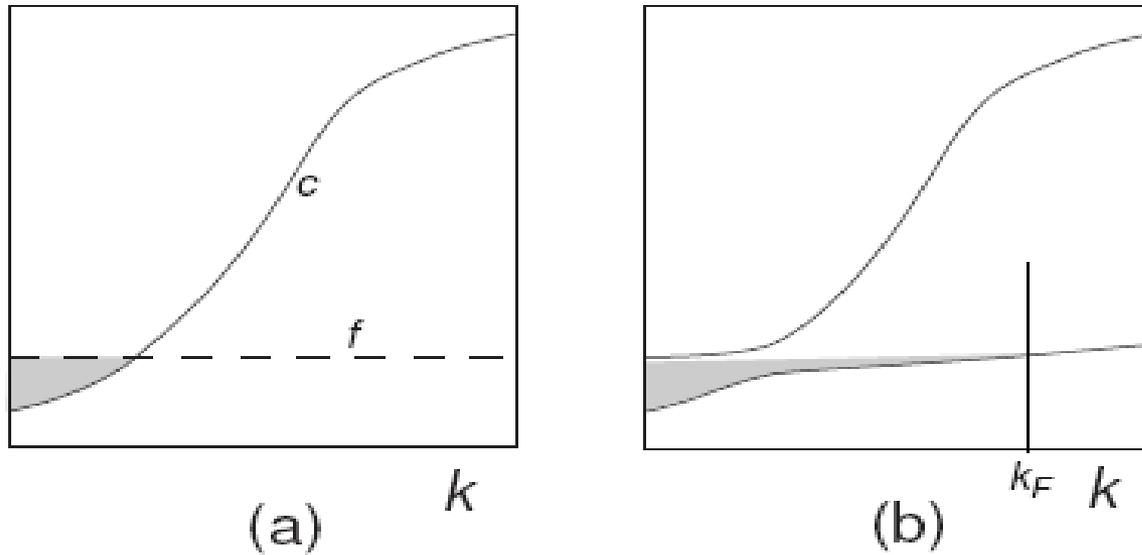
Treat Kondo exchange, constraint in mean field

$$H_{MF} = \sum_{\mathbf{k}} \epsilon_{\mathbf{k}} c_{\mathbf{k}}^{\dagger} c_{\mathbf{k}} + b \sum_{\mathbf{k}} (c_{\mathbf{k}}^{\dagger} f_{\mathbf{k}} + \text{h.c.}) + \mu_f \sum_{\mathbf{k}} f_{\mathbf{k}}^{\dagger} f_{\mathbf{k}}$$

$$b = J \langle f_{\mathbf{k}}^{\dagger} c_{\mathbf{k}} \rangle$$

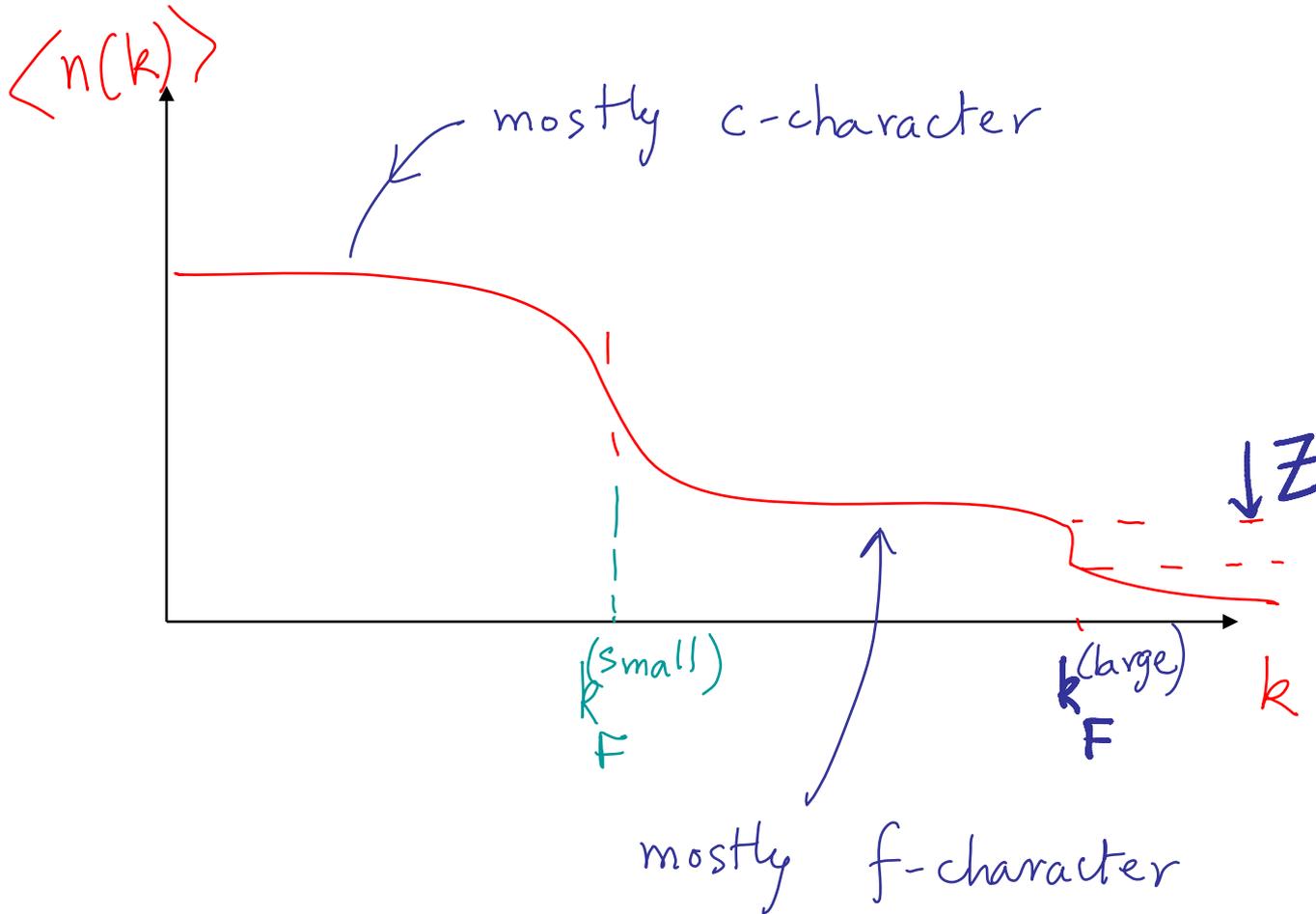
$$\langle f_i^{\dagger} f_i \rangle = 1$$

# Band structure



Theory gives (i) large Fermi surface  
(ii) large quasiparticle mass, etc !

# Momentum distribution

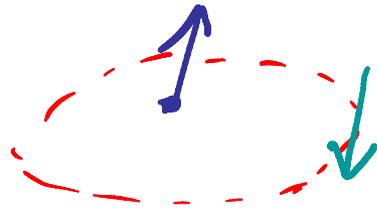


## Comments

1.  $b \sim \langle c^\dagger f \rangle \sim$  amplitude of Kondo singlet
2. Heavy quasiparticles at Fermi surface  
 $\approx f + b c$   
 $\Rightarrow$  Quasiparticle weight  $Z \sim b^2 \sim 0 \left( \frac{m}{m^*} \right) \ll 1$

# Real heavy fermi liquids: Kondo singlets with internal structure

Local moment in f-orbital + c-electron in (say) s-orbital

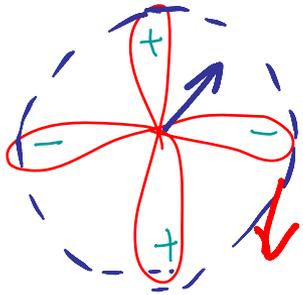


Kondo singlet "molecule" has non-trivial internal orbital structure.

# Higher angular momentum Kondo liquids

Non trivial Fermi surface variation in heavy  
Fermi liquid

Eg: Toy model of d-wave Kondo liquid  
(Ghaemi, TS '07)



Similar theoretical discussion of gapless  
Kondo insulators

- Ikeda, Miyake '96
- Moreno, Coleman '00

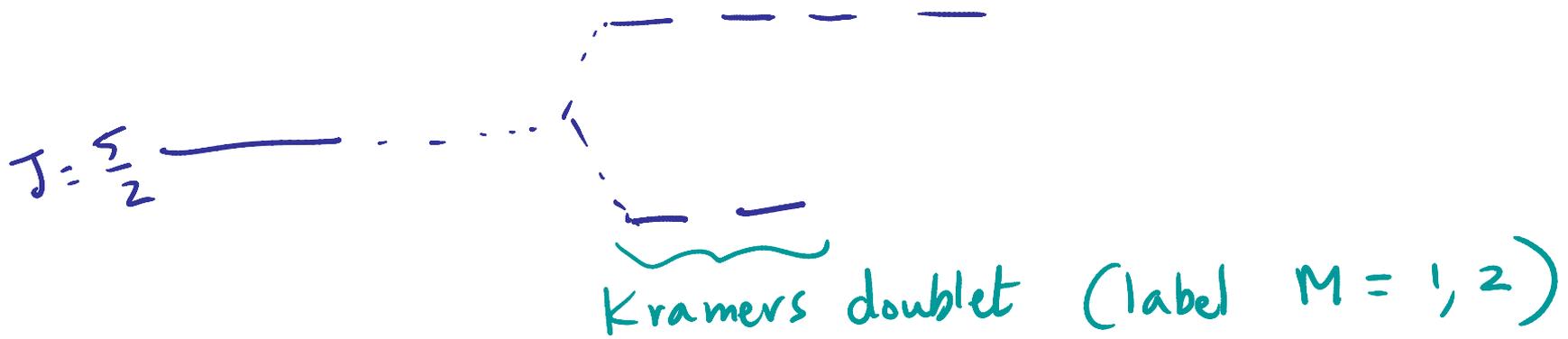
# Illustrate: Kondo lattice model for a cubic Ce-based heavy fermi liquid

Ce  $f'$  ion in cubic environment :

Spin orbit + crystal field  $\Rightarrow$  low energy

Kramers doublet occupied by  $f$ -electron.

$$J = \frac{7}{2}$$



# Kondo lattice model for a cubic Ce-based heavy fermi liquid (cont'd)

$$H = \sum_{\vec{k}\sigma} \epsilon_{\vec{k}} c_{\vec{k}\sigma}^{\dagger} c_{\vec{k}\sigma} + J \sum_{\vec{R}} \sum_{\vec{k}} \sum_{\substack{M\sigma \\ M'\sigma'}} \langle \vec{k} M \vec{R} | \vec{k} M' \vec{R} \rangle f_{M\vec{R}}^{\dagger} c_{\vec{k}\sigma} c_{\vec{k}\sigma'}^{\dagger} f_{M'\vec{R}}$$

$$+ \text{constraint } \sum_M f_{M\vec{R}}^{\dagger} f_{M\vec{R}} = 1$$

$|k M \vec{R}\rangle =$  partial wave centered at site  $\vec{R}$

# Mean field theory: angle dependent hybridization

$$H_{MF} = \sum_{\vec{k}\sigma} c_{\vec{k}\sigma}^\dagger c_{\vec{k}\sigma} + \mu_f \sum_{M\vec{R}} f_{M\vec{R}}^\dagger f_{M\vec{R}} + b \sum_{\vec{k}M\sigma} \left( \langle \vec{k}\sigma | kM \rangle c_{\vec{k}\sigma}^\dagger f_{\vec{k}M} + h.c. \right)$$

Hybridization matrix

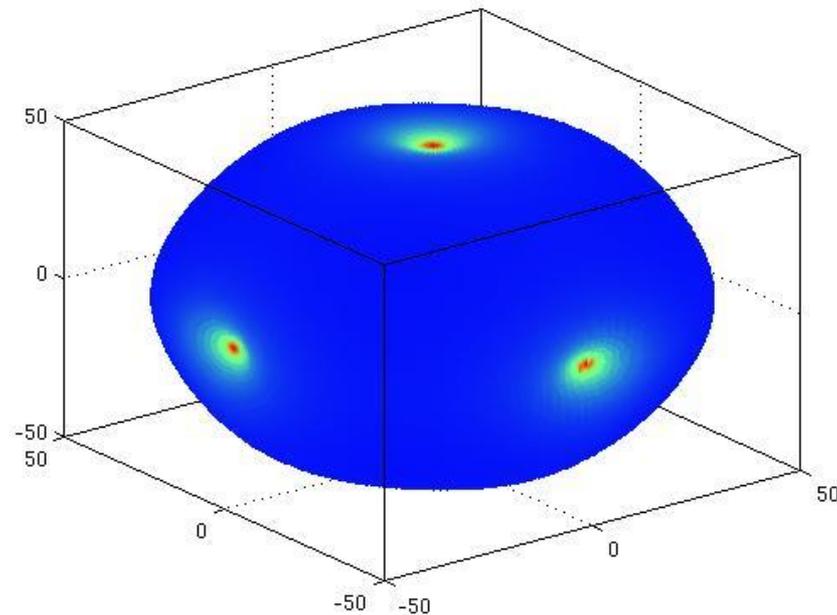
$b \langle \vec{k}\sigma | kM \rangle$  : Strong dependence on  $\vec{k}$ -direction

Vanishes along (100) & related directions.

"Hybridization nodes"

# Fermi surface structure

Along "hybridization nodes" large  $c$ -electron Fermi surface is within original small  $c$ -electron Fermi surface.



## Angle dependence of c-character

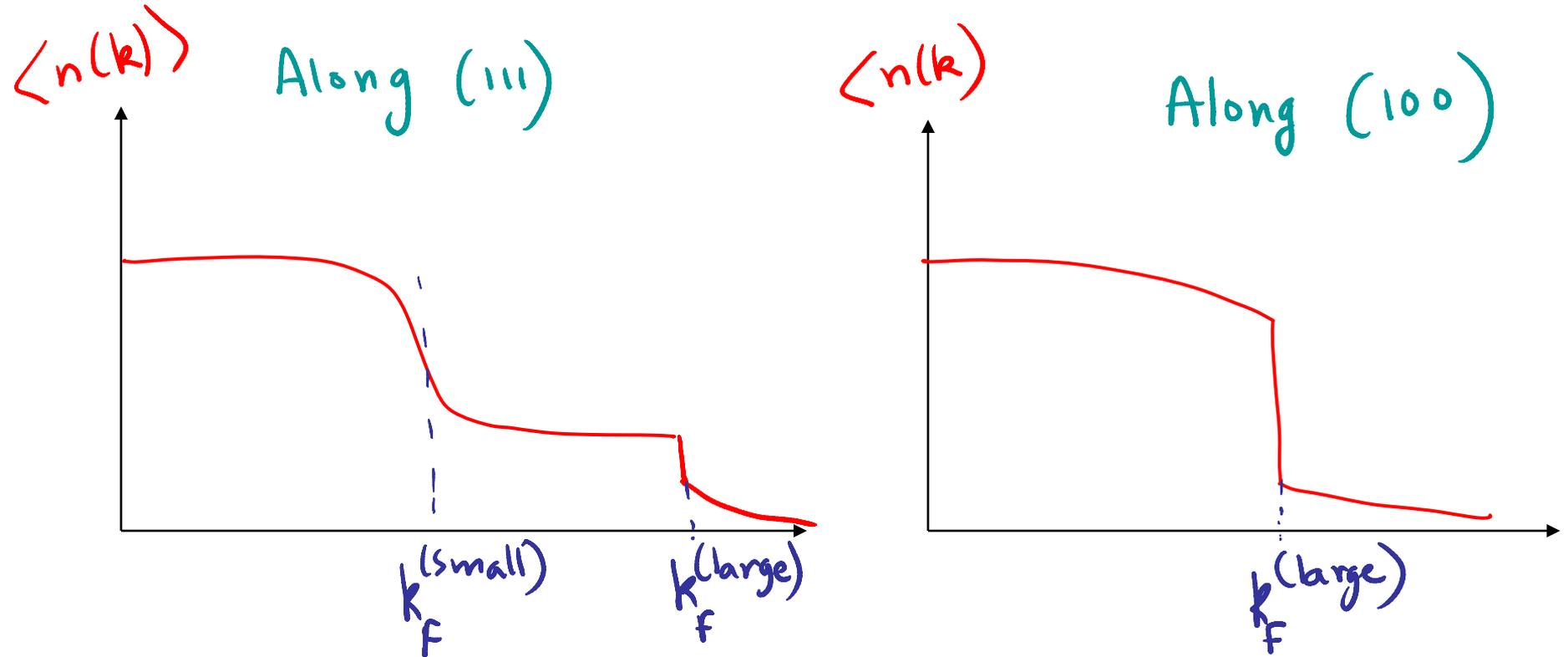
Along hybridization node directions,

quasiparticles essentially c-like

but become essentially f-like further away

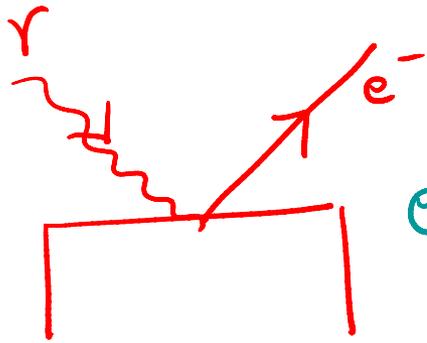
⇒ Strong angle dependence of  
c-character.

# Momentum distribution



Probe in photoemission?

# Photoemission theory for Kondo lattices



For Anderson lattice model,

extracted electron  $\psi_{k\sigma} \sim c_{k\sigma} + \sum_M \alpha_{M\sigma k} f_{kM}$

Strong correlation limit: Changing f-occupation costs energy  $\sim U$

At low energy

$$\psi_{R\sigma} \approx c_{R\sigma} + \frac{V}{U} \sum_{MM'R'} a_{MM'R'} \underbrace{f_{RM} f_{RM'}^+}_{\text{preserves on-site f-occupancy}} c_{R'\sigma}$$

preserves on-site f-occupancy.

# Angle dependent quasiparticle weight

In mean field  $\psi_{\mathbf{k}} \approx c_{\mathbf{k}} + b_{\mathbf{k}} f_{\mathbf{k}}$

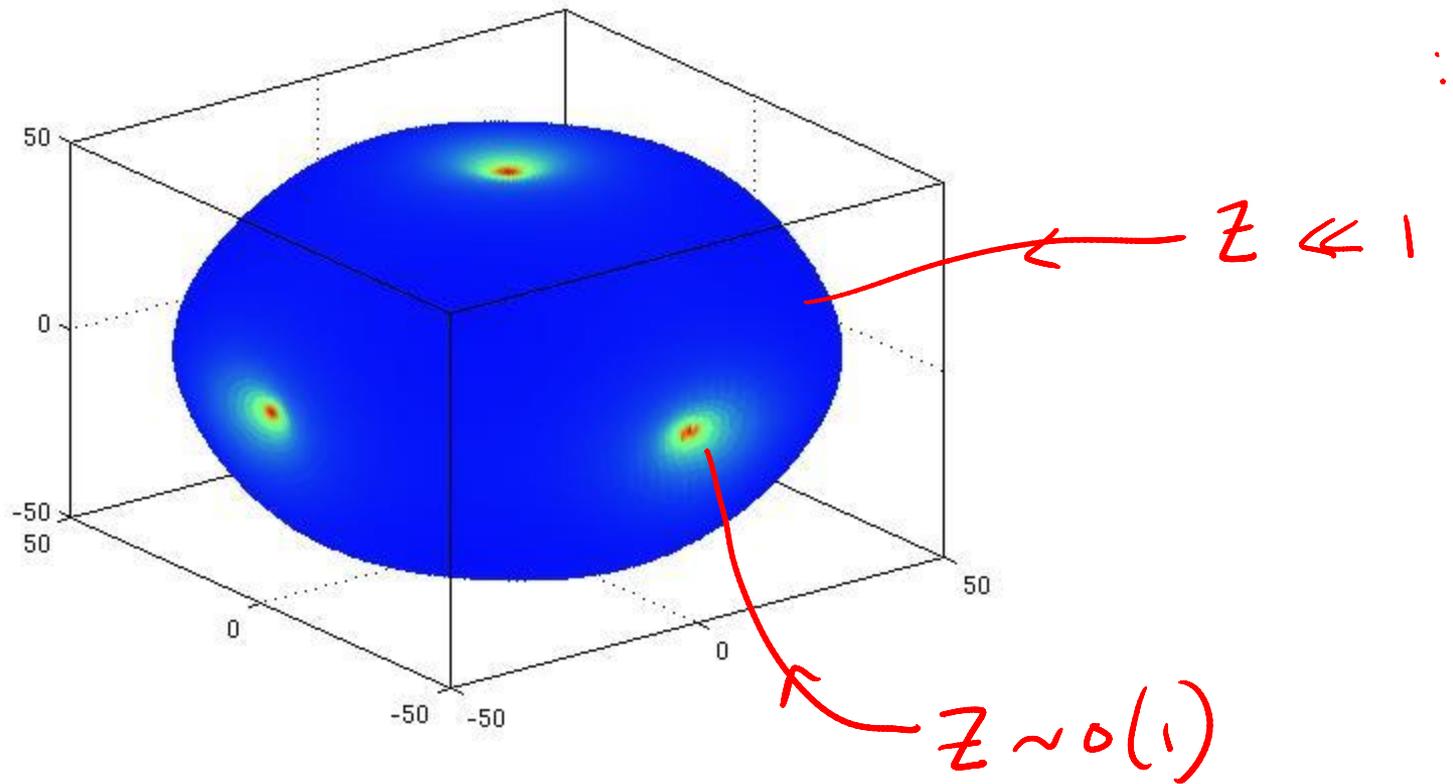
Along hybridization nodes  $\psi_{\mathbf{k}} \approx c_{\mathbf{k}}$

$\Rightarrow Z \sim o(1)$  as quasiparticles  
are c-like

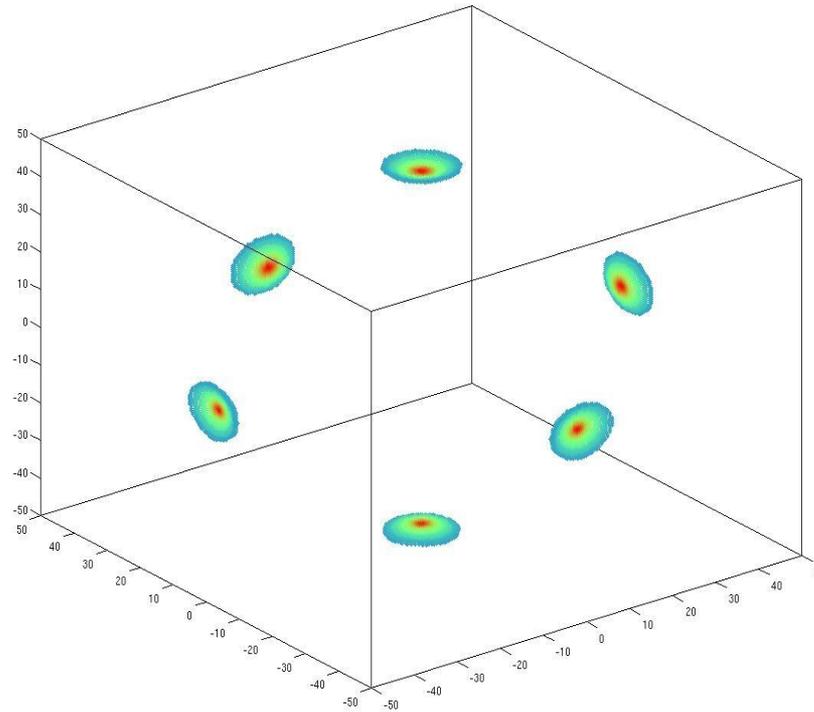
Further away  $Z \sim o(b_{\mathbf{k}}^2) \ll 1$

$\Rightarrow$  Strong angle dependent  $Z$

# Z on the Fermi surface



# Apparent “open” Fermi patches in ARPES



Small  $z$   
regions may  
be missed  
in experiment!

# Tunneling?

Mass enhancement also strongly anisotropic

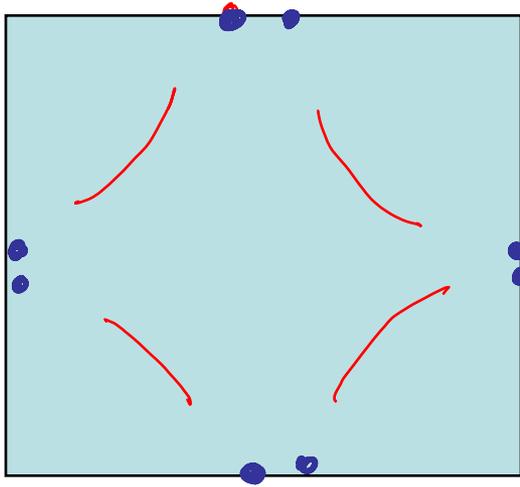
Along (100)  $\frac{m^*}{m_e} \sim 0(1)$

but along (111),  $\frac{m^*}{m_e} \sim \frac{1}{b_k^2} \gg 1$

Tunneling density of states

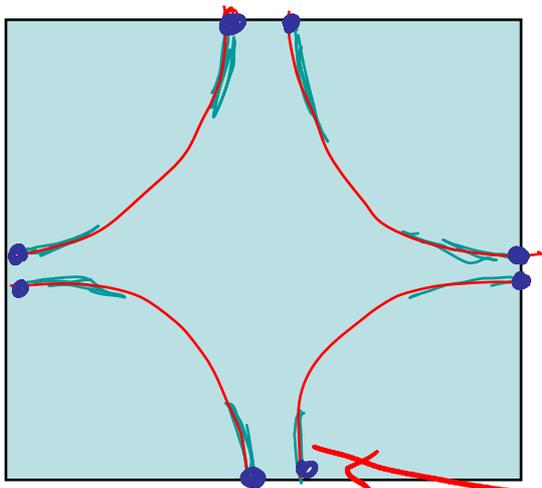
$$\sim \int d\Omega \frac{Z(\Omega)}{\underline{v_f(\Omega)}} \quad \underline{\text{not enhanced.}}$$

# Similar in cuprates?



Underdoped cuprates :

Mysterious gapless Fermi arcs  
in pseudogap normal state .



Could there really be a large  
Fermi surface with  $Z \sim 0(1)$  along  
arcs but small near antinode ?

small  $Z$  ??

## Similar in cuprates?

Heavy fermions: small  $Z$  regions  $\Leftrightarrow$  large effective mass.

Cuprates: Density of states decreases on cooling into pseudogap phase!

In general  $Z \neq \frac{m_e}{m^*}$  ;

$\Rightarrow$  In cuprates, small antinodal  $Z$  with no mass enhancement?

Could the pseudogap phase actually have a **LARGE** Fermi surface with strongly angle dependent low energy electron spectral weight?

Could the pseudogap phase actually have a  
**LARGE** Fermi surface with strongly angle  
dependent low energy electron spectral weight?

Many appealing features !  
Consistency with high field quantum oscillations through  
low-T density wave transition of large Fermi surface .

# Summary

1. Strong angle dependent quasiparticle weight in heavy electron metals due to orbital structure of Kondo singlet.

2. Angle dependent  $Z$  correlated with angle dependent  $m^*$

(Heavy Fermi liquid not uniformly heavy)

## Summary (cont'd)

Possibility of "hybridization nodes":

1. Kondo-Heisenberg models: Vanishing  $Z$  at isolated points on Fermi surface.

Should we call these Fermi liquids?

2. Heavy fermion SC driven by  $f$ -pairing (a'la RVB)

Pairing structure of physical SC order parameter?