

Remarks on Sr_2IrO_4 and its relatives

Fa Wang and T. Senthil, PRL 2011

Iridium oxide materials: various kinds of exotic physics

$\text{Na}_4\text{Ir}_3\text{O}_8$: insulating quantum spin liquid (Okamoto, Takagi et al, 2007)

Sr_2IrO_4 : $J_{\text{eff}} = 1/2$ spin-orbit entangled Mott insulator (B.J. Kim et al, 2008)

Other interesting proposals:

A_2IrO_3 : quantum spin Hall effect? (Shitade, Nagaosa et al, PRL 2009), realization of Kitaev spin liquid? (Jackeli, Khaliullin, PRL 2009)

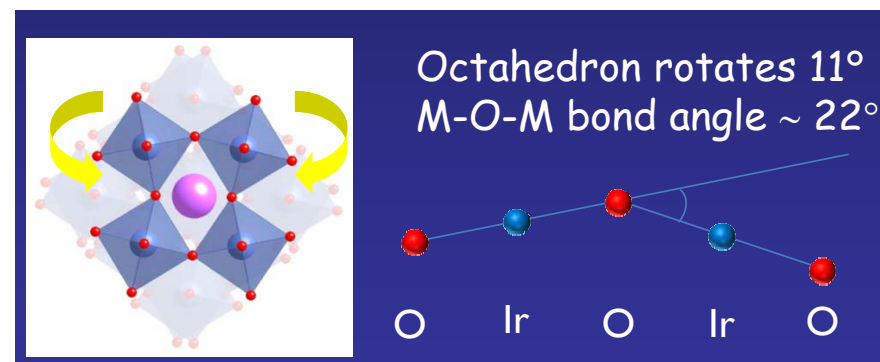
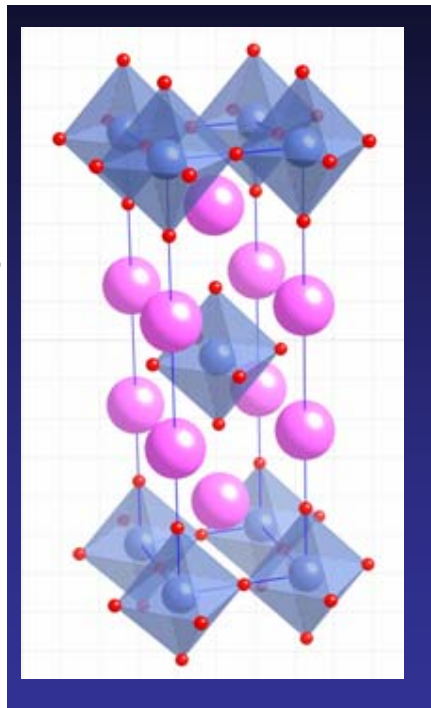
$\text{Ln}_2\text{Ir}_2\text{O}_7$ pyrochlore iridates:

(i) spontaneous anomalous Hall effect (Nakatsuji et al, 2010) for $\text{Ln} = \text{Pr}$;

(ii) other Ln: 3d correlated topological insulator? (Pesin, Balents, Nat Phys 2010), Weyl semi-metals? (Wan, Turner, Vishwanath, Savrasov 2011).

Sr₂IrO₄: preliminaries

K₂NiF₄ structure
similar to La₂CuO₄



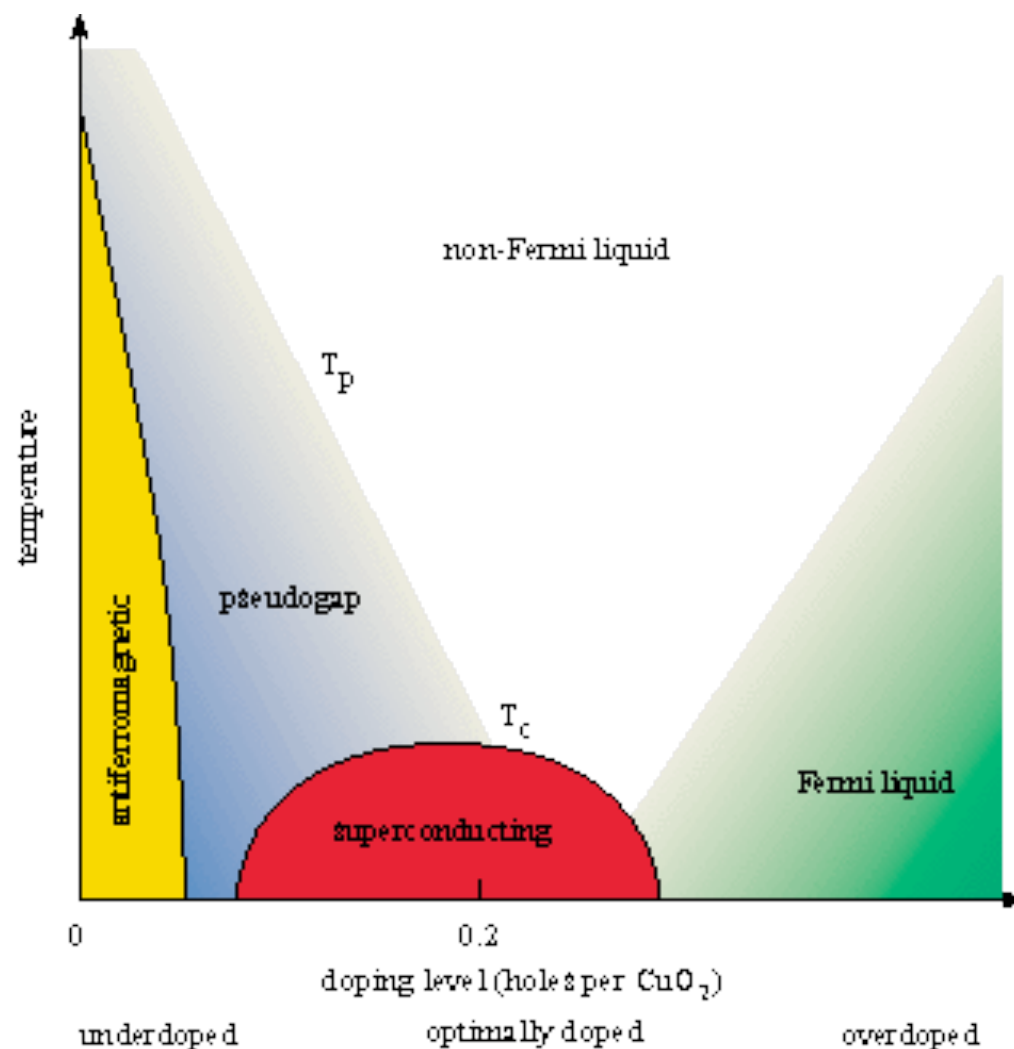
Layers of IrO₂ ;
Ir⁴⁺ ions on a 2d square lattice.
Each Ir surrounded by O octahedra.

Similarity to cuprates noticed in 1990s: M.A.Subramanian,
Gang Cao,

Cuprates are interesting

Still the best high temperature superconductors!

Many other novel broken symmetries found in recent years in underdoped side.



1. Antiferromagnetism

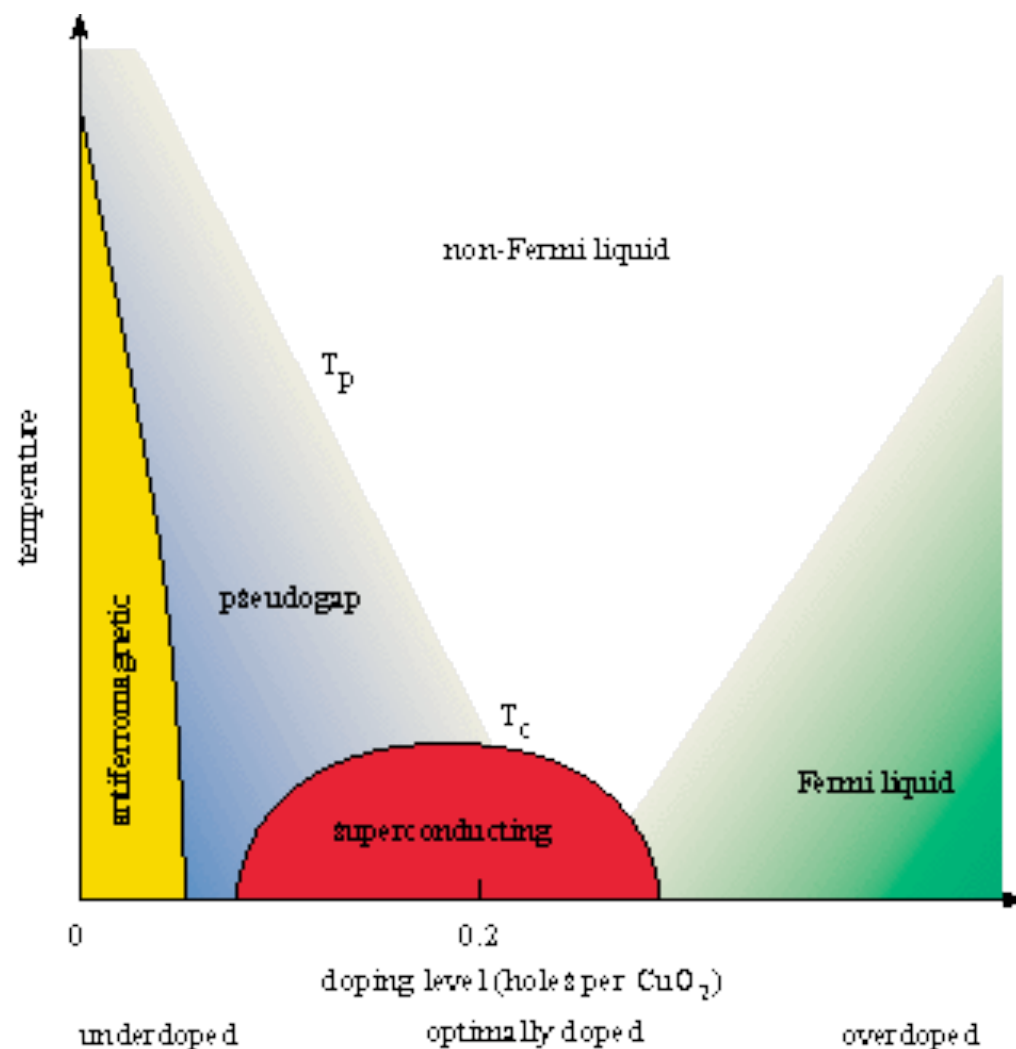
2. Broken translation (stripes)

3. Nematic

4. Broken T-reversal

5. Loop currents (break T-reversal, rotation but preserve combination, translation invariant)

Cuprates are interesting (cont'd)



Apart from high T_c superconductivity/other broken symmetries, cuprates show a number of fascinating and mysterious phenomena.

Eg: pseudogap, strange non-Fermi liquid metal,.....

For some of these the superconductivity is a nuisance that people work hard to get rid of so they can be studied at low-T.

Cuprates are challenging for theory

1. Some understanding of origin and properties of superconductivity, stripes, and some of the other broken symmetries.
2. Very little understanding of how these different orders compete/cooperate.
3. Almost no understanding of essence of pseudogap phenomenon
3. No understanding of strange metal

Do parts of the cuprate story play out elsewhere?

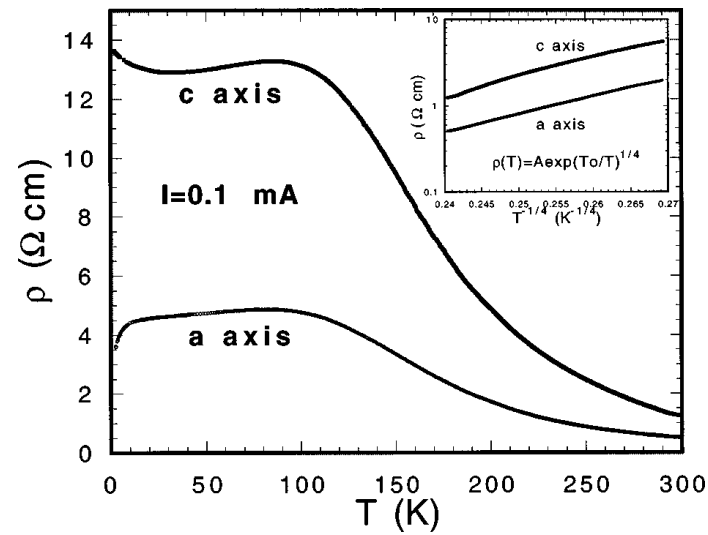
1. Organics: SC proximate to AF Mott insulator, pseudogap in some cases.

2. Pnictides: SC proximate to magnetism in quasi-2d layered square lattice systems, evidence for nematic order but very different microscopically.

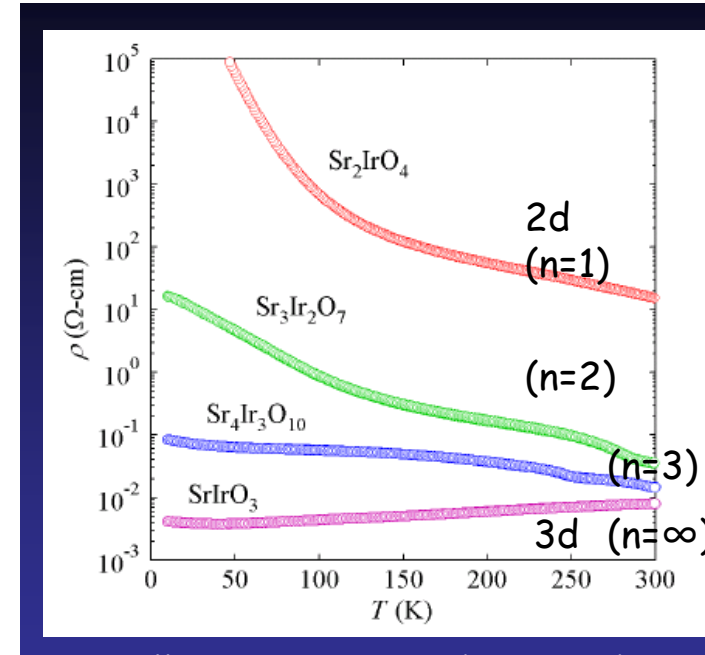
No serious sign of pseudogap, strange metal or (mostly) Mott insulation

3. Iridates ????

Sr₂IrO₄: Mott insulator*



Cao et al, PR B 1998

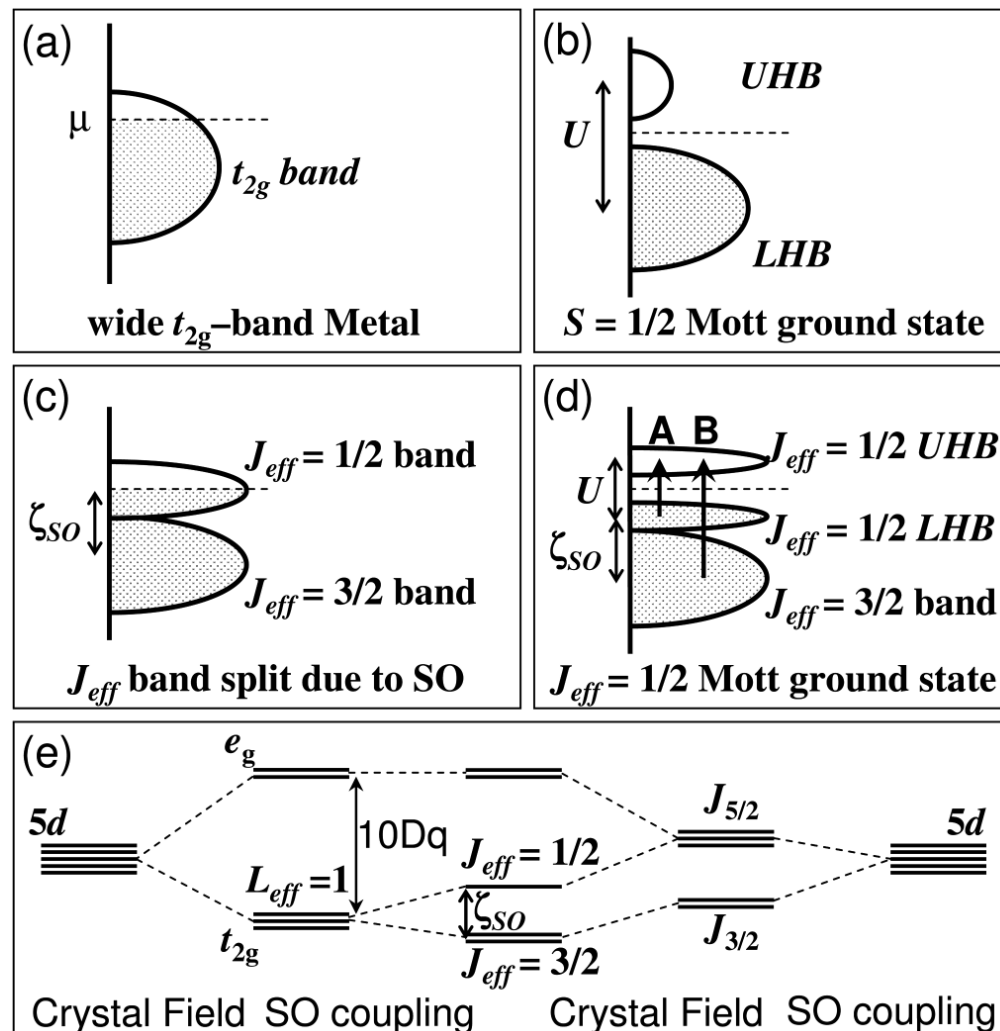


H. Takagi et al, 2008

*Later..how much Mott?

Why a Mott insulator?

Ir 4+ is in a $5d^5$ configuration.



Cubic environment: big t_{2g} - e_g splitting.

SO coupling splits t_{2g} level into $J_{eff} = 1/2$ and $J_{eff} = 3/2$ bands.

$J_{eff} = 1/2$ band is half-filled and narrow
 \Rightarrow moderate U can drive it into a Mott insulator

B. J. Kim et al, PRL 08

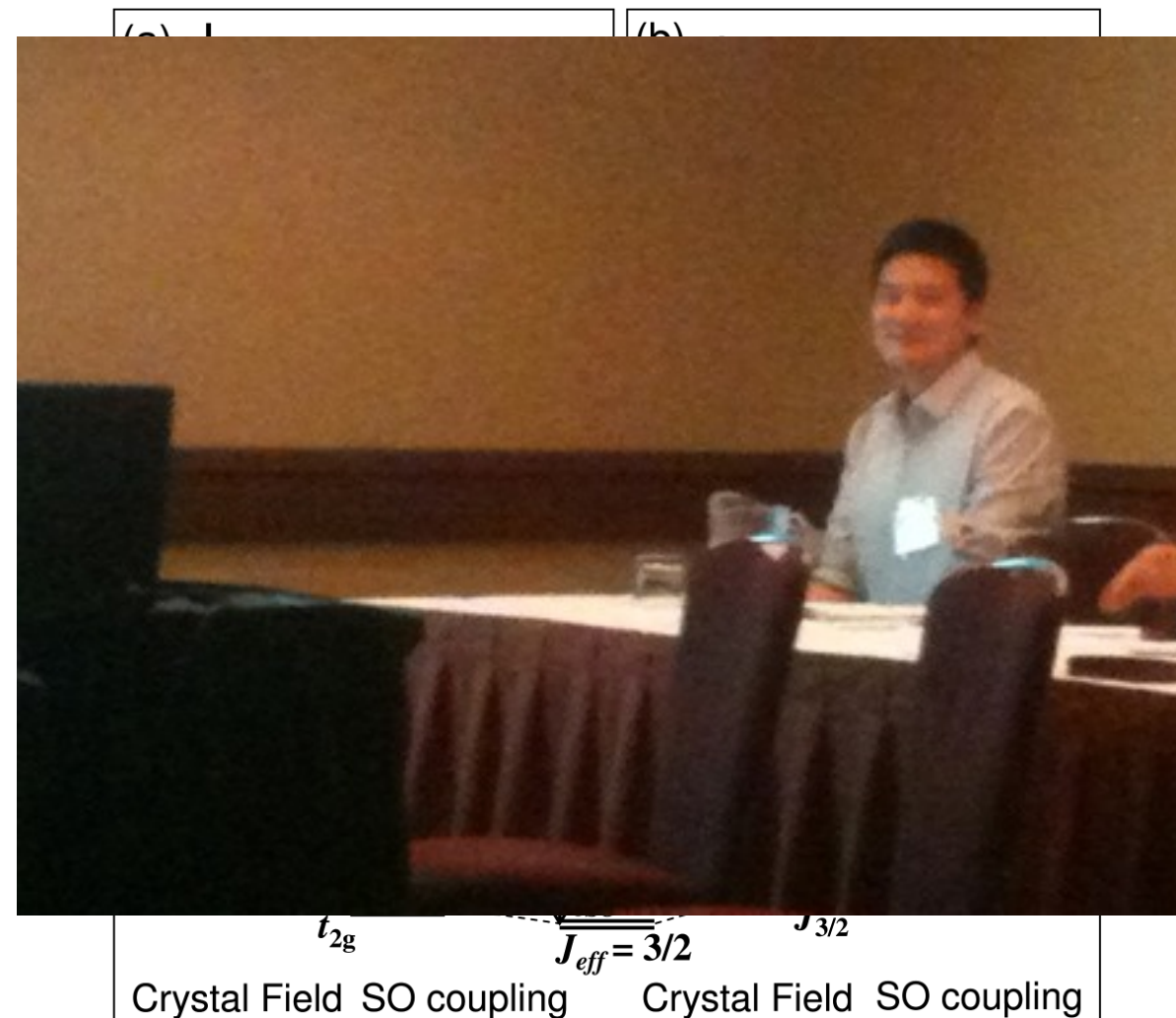
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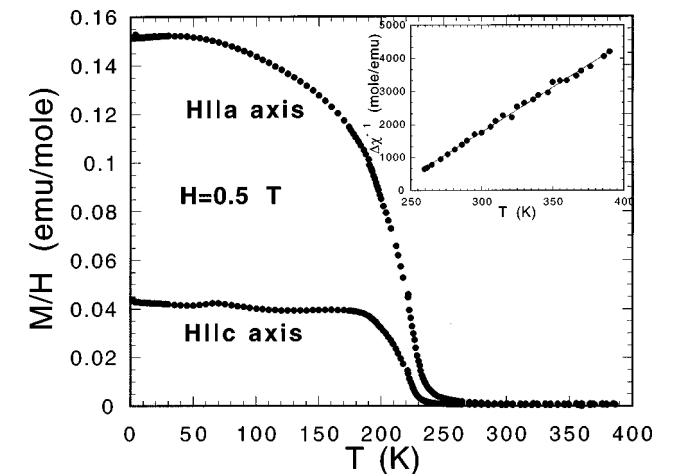


B. J. Kim et al, PRL 08

Spin-orbit entangled Mott insulating magnet

$$J_{eff,+1/2} = \frac{1}{\sqrt{3}} (|xy, +1/2\rangle + |yz, -1/2\rangle + i|zx, -1/2\rangle)$$

$$J_{eff,-1/2} = \frac{1}{\sqrt{3}} (|xy, -1/2\rangle - |yz, +1/2\rangle + i|zx, -1/2\rangle)$$



J_{eff} moments order into a magnetic state below 240 K.

Weak ferromagnetism (from canting of AF moments): $0.7 - 0.14 \mu_B$

Spin-orbital content confirmed by resonant magnetic X-ray diffraction
(B.J. Kim, Takagi et al, Science 2009)

How similar to cuprates??

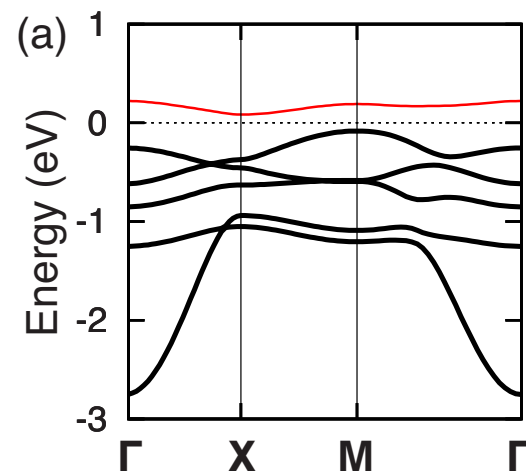
Despite obvious similarities, some worries

1. Different active orbitals
2. Spin anisotropy and related strong spin orbit coupling

Is there a useful effective model which can be compared with, eg, Hubbard model popular for cuprates?

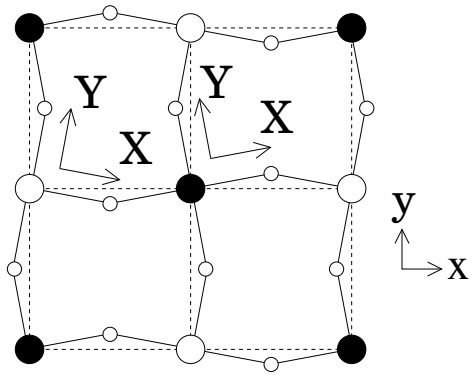
LDA + Spin-Orbit + U bandstructure

Jin, Jaejun Yu, et al, PR B 2009



Fit to obtain tightbinding model (+ U) in
t_{2g} subspace: real orbital diagonal hoppings
(i.e only $xy \rightarrow xy$, $yz \rightarrow yz$, $xz \rightarrow xz$) + on-site
spin-orbit term

Similar result: H. Watanabe et al, PRL 2010



Interpretation of tightbinding model

Wang and TS, 2011

Rotation of oxygen octahedra => must carefully distinguish between local X,Y,Z basis and global x,y,z basis.

Note

1. Crystal field splitting between t_{2g} and e_g is diagonal in local X,Y,Z basis => define t_{2g} orbitals in local orbital basis.
2. If Ir - Ir hopping is mediated by O p-orbitals, symmetry => Ir-Ir hopping diagonal in local orbital basis
3. Global basis for spin $S = 1/2$ => Ir-Ir hopping real.

Conclusion: LDA+SO+U tight-binding fit involves Wannier states with t_{2g} orbitals in local X,Y,Z basis but spin in global basis.

Effective model for $J_{\text{eff}} = 1/2$ states: strategy

Wang and TS, 2011

What are correct $J_{\text{eff}} = 1/2$ states?

Must define both t2g orbitals and spin in local X,Y,Z basis.

$$|J_{\text{eff}}^z = +1/2\rangle = \frac{1}{\sqrt{3}} (+i|XY, \uparrow\rangle - |XZ, \downarrow\rangle + i|YZ, \downarrow\rangle),$$
$$|J_{\text{eff}}^z = -1/2\rangle = \frac{1}{\sqrt{3}} (-i|XY, \downarrow\rangle + |XZ, \uparrow\rangle + i|YZ, \uparrow\rangle).$$

Effective model in $J_{\text{eff}} = 1/2$ subspace:

Start with full tightbinding t2g tightbinding model,

rotate spin from global to local basis, then project onto $J_{\text{eff}} = 1/2$ states.

Effective model for $J_{\text{eff}} = 1/2$ states: result

$$H = - \sum_{\langle jk \rangle, \alpha} (t + i\epsilon_{\alpha} \epsilon_j \bar{t}) d_{j,\alpha}^{\dagger} d_{k,\alpha} - \sum_{\langle\langle jk \rangle\rangle, \alpha} t' d_{j,\alpha}^{\dagger} d_{k,\alpha} \\ - \sum_{\langle\langle\langle jk \rangle\rangle\rangle, \alpha} t'' d_{j,\alpha}^{\dagger} d_{k,\alpha} + U \sum_j d_{j,\uparrow}^{\dagger} d_{j,\uparrow} d_{j,\downarrow}^{\dagger} d_{j,\downarrow}$$

Effective tight-binding parameters $t \approx 0.26\text{eV}$, $t' \approx t/4$, $t'' \approx t/10$.

Imaginary spin-dependent hopping $\bar{t} \approx -t/60$: ignore.

Hubbard $U \approx 2\text{eV}$.

Effective t - t' - t'' - U Hubbard model for $J_{\text{eff}} = 1/2$ band.

Consequence: pseudospin isotropy

At half-filling, expect can describe Mott insulator by usual isotropic pseudospin $J_{\text{eff}} = 1/2$ model

$$H_{AFM} = I \sum_{\langle ij \rangle} \vec{J}_i \cdot \vec{J}_j + \dots \quad (1)$$

Exchange $I \sim 4t^2/U$.

“.....” further neighbor, ring exchange

Similar prior conclusion in spin model limit: Jackeli, Khaliullin 2009

Coupling to external Zeeman field is 'twisted'

Wang, TS, 2011

$$H_B = -\mu_B \sum_i \vec{B} \cdot (\vec{L} + 2\vec{S}) \quad (1)$$

Project to $J_{eff} = 1/2$ states

$$H_B = 2\mu_B (B_X J_X + B_Y J_Y + B_Z J_Z) \quad (2)$$

Subscripts X, Y, Z : components in local basis.

Rotate back to global basis: staggered anisotropic g-tensor.

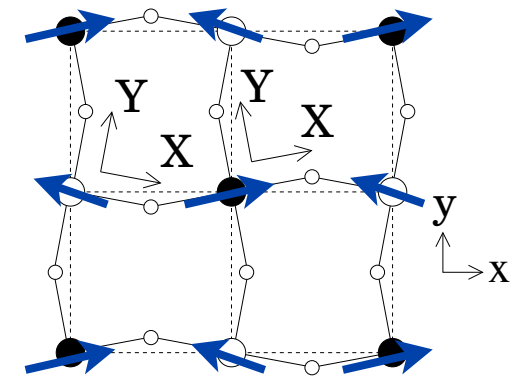
Observable moment \mathbf{M}
related to \mathbf{J} through

$$\begin{pmatrix} M_{j,x} \\ M_{j,y} \\ M_{j,z} \end{pmatrix} = -2\mu_B \begin{pmatrix} \cos \theta & -\epsilon_j \sin \theta & 0 \\ \epsilon_j \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} J_{j,1} \\ J_{j,2} \\ J_{j,3} \end{pmatrix}$$

Twisted magnetic field coupling \Rightarrow anisotropic magnetization even though intrinsic physics is isotropic.

Consequences for magnetism in Sr₂IrO₄

Isotropic pseudospin ordering \Rightarrow observed moment rotates with octahedra rotation.
 \Rightarrow weak ferromagnetism.



$$\text{FM moment} = (\text{AF moment}) \sin \theta$$

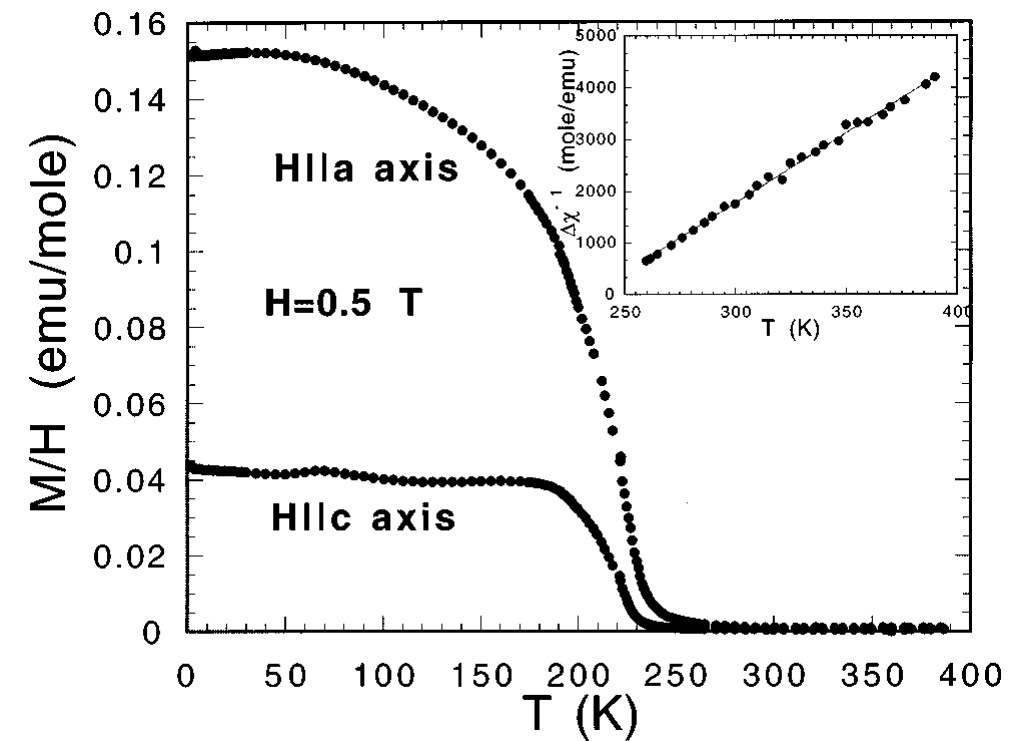
θ = octahedron tilt angle

Known AF moment of $J = 1/2$ Heisenberg model \Rightarrow FM moment $\approx 0.14\mu_B$
similar to experiment.

Consequences for magnetism (cont'd)

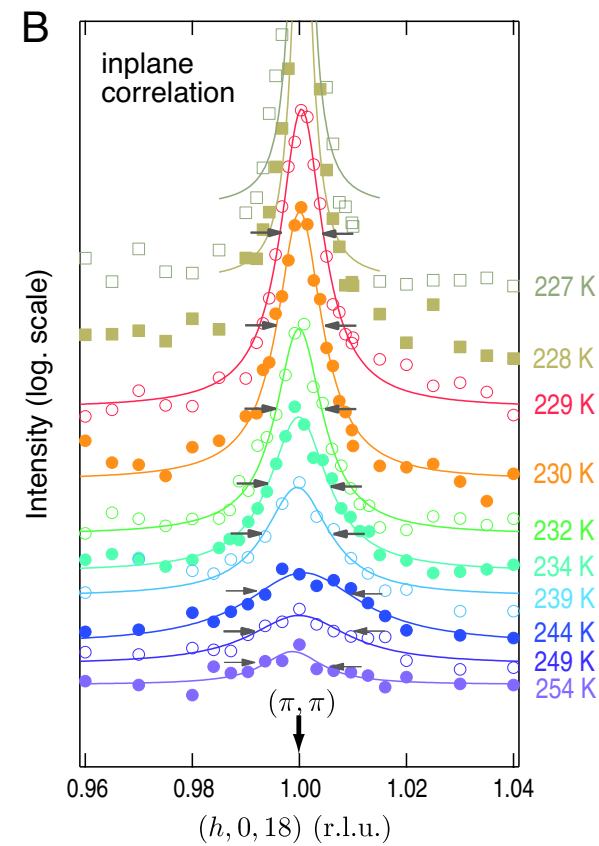
1. Measured susceptibility near $q = 0$ is mixture of uniform and staggered susceptibilities
2. Anisotropy between susceptibility to field along ab-plane versus along c axis.
3. Despite apparent spin anisotropy, spin correlation length above T_N should behave like that of isotropic magnet.

All of these agree with experiment.

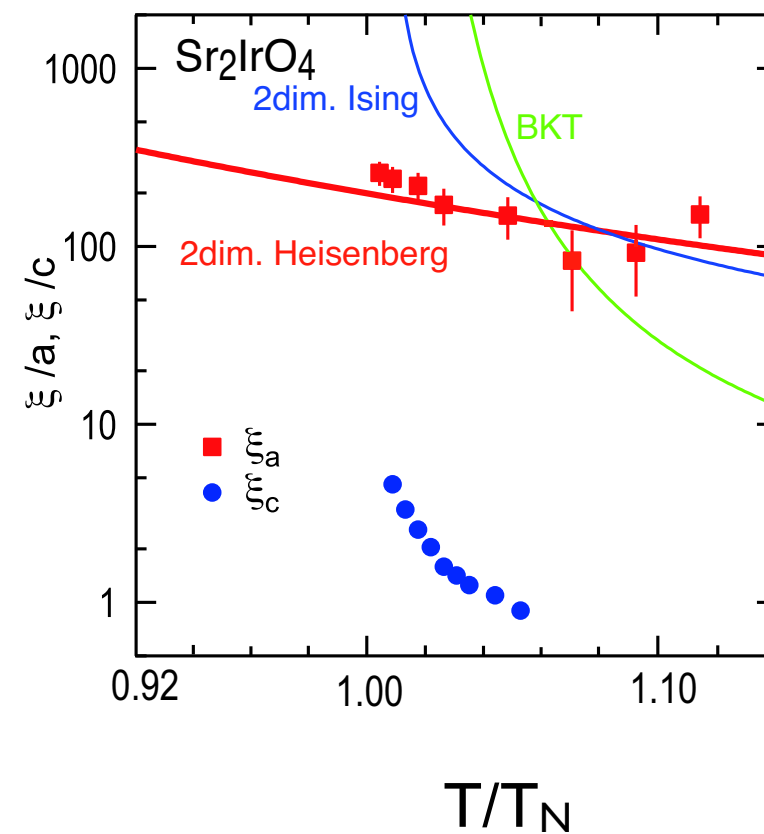


Spin correlation length above T_N

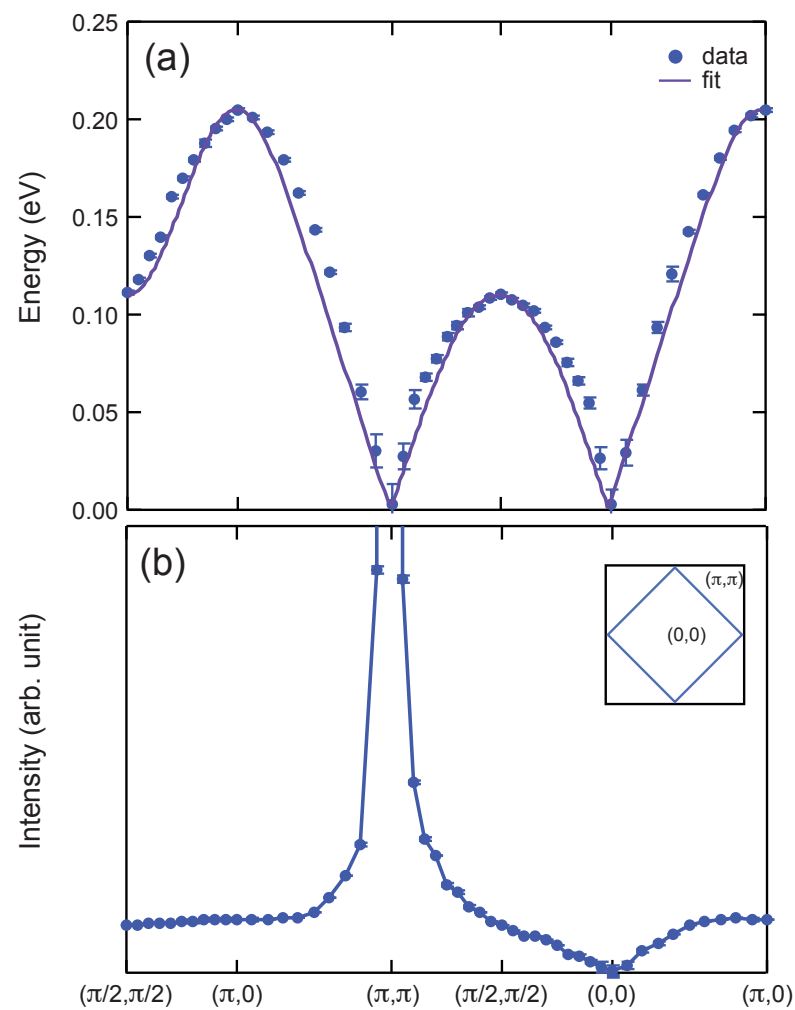
Shigeki Fujiyama, H. Takagi et al, 2012



Diffuse magnetic X-ray
scattering

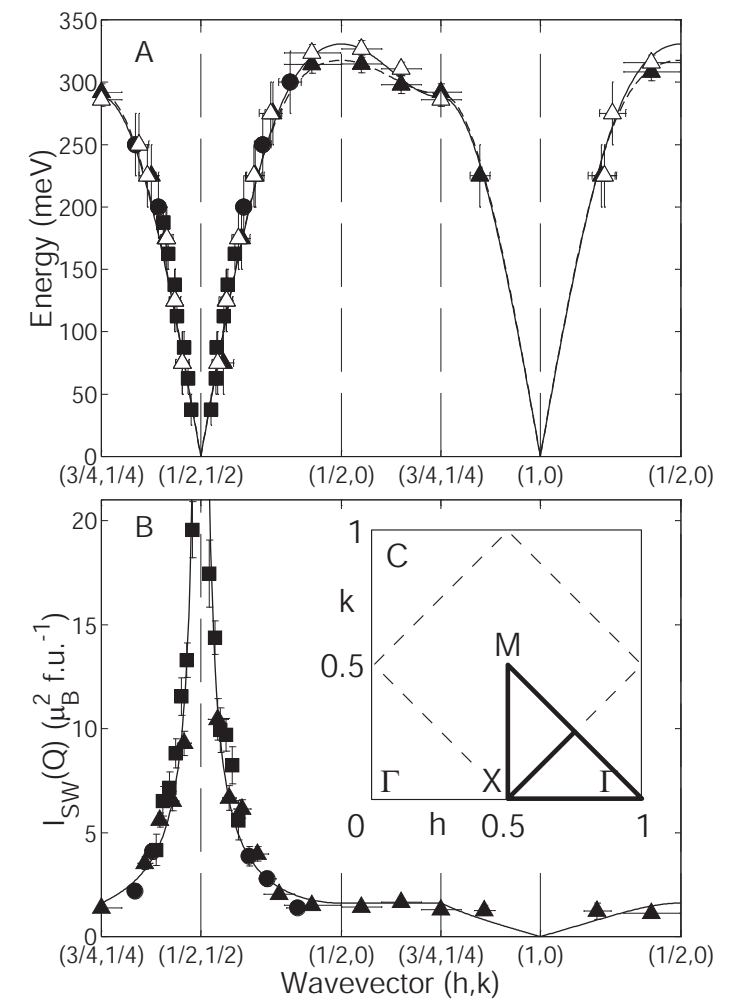


Spin wave dispersion (B.J. Kim) through RIXS



Sr₂IrO₄, Jungho Kim
et al, 2011

Contrast with cuprate



LSCO, Coldea et al, 2001

Compare model to cuprate

Effective isotropic Hubbard model parameters:

$$t \approx 0.2eV, t' \approx \frac{t}{4}, t'' \approx -\frac{t}{10}, U \approx 10t.$$

Similar to cuprate?

1. Roughly same parameter range as cuprate Hubbard model except overall energy scale smaller by ≈ 2 .
2. t'/t positive for iridate - opposite to cuprate

Doped system - superconductivity?

If the doped square lattice 2d Hubbard model is superconducting, can we expect doping the iridate will give a 'high temperature' superconductor?

From comparison to cuprate

(i) $t'/t > 0 \Rightarrow$ Electron doping better than hole doping for iridate
(Example: Replace Sr by La)

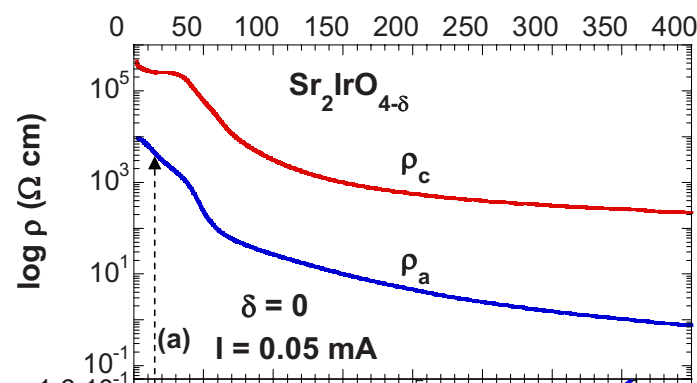
(ii) Overall energy scale smaller by 2 $\Rightarrow T_c$ in range of 50 K???

Differences with cuprates: more coherent c-axis transport?

Interlayer tunneling matrix element in cuprate:
 $(\cos k_x - \cos k_y)^2$ factor which blocks c-axis transport of nodal states.

Iridate: different orbital content implies no suppression of nodal c-axis hopping.

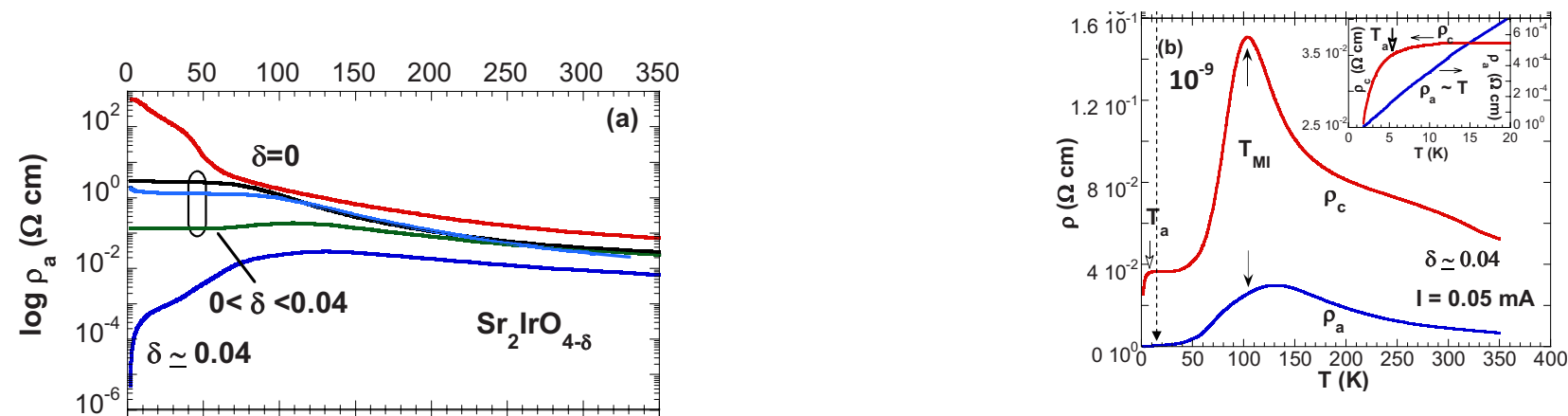
Better c-axis coherence?



Overall resistivity anisotropy of about
100 in undoped insulator

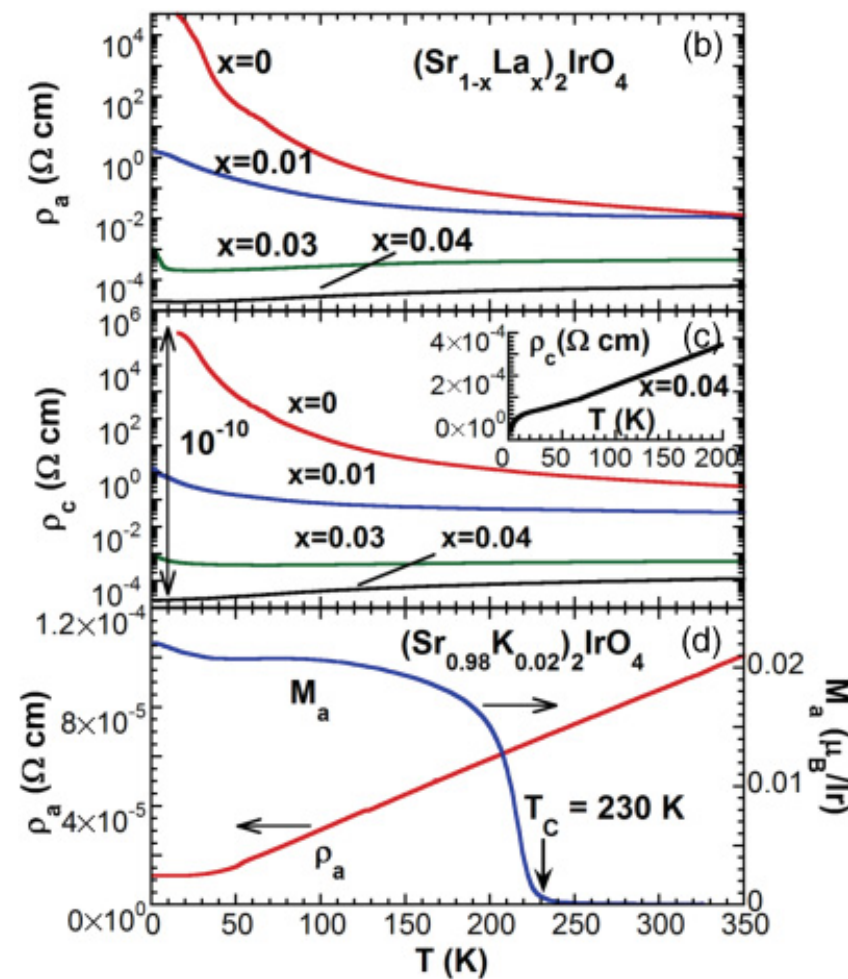
Experimental prospects?

Metal-insulator transition with Oxygen doping



Cornetta, Cao et al, PR B 2010

MIT with La (electron) or K (hole) doping



Will it be possible to dope Sr_2IrO_4 to higher doping levels?

May be try field-effect doping or making oxide interface? ???

Ge, Cao et al, 2011

Some important basic issues to settle

I. Sr_2IrO_4 : Mott or Slater insulator?

Issue raised in recent theory and expt papers. (Arita, Imada et al PRL, 2012; Hsieh et al, 2012)

Naive Slater picture clearly not legitimate:

Insulator above T_N , no Fermi surface nesting.

Almost certainly intermediate U .

Similar issue still being debated in cuprates (eg Millis 2010).

2. Legitimacy of one-band Hubbard description

More serious is whether a one-band description is legitimate at all.

1. Do $J = 3/2$ states start playing a role in doped system?

May be not for electron doped.....

2. Complications due to enlarged unit cell from octahedra rotation
(eg: suggested semimetal in SrIrO_3 (Takagi APS 2012 talk)).

If one-band description breaks down similarity with cuprates can also be expected to break down.....

3. Magnetism in doped Sr-2I4

Fate of magnetic ordering across metal-insulator transition ?

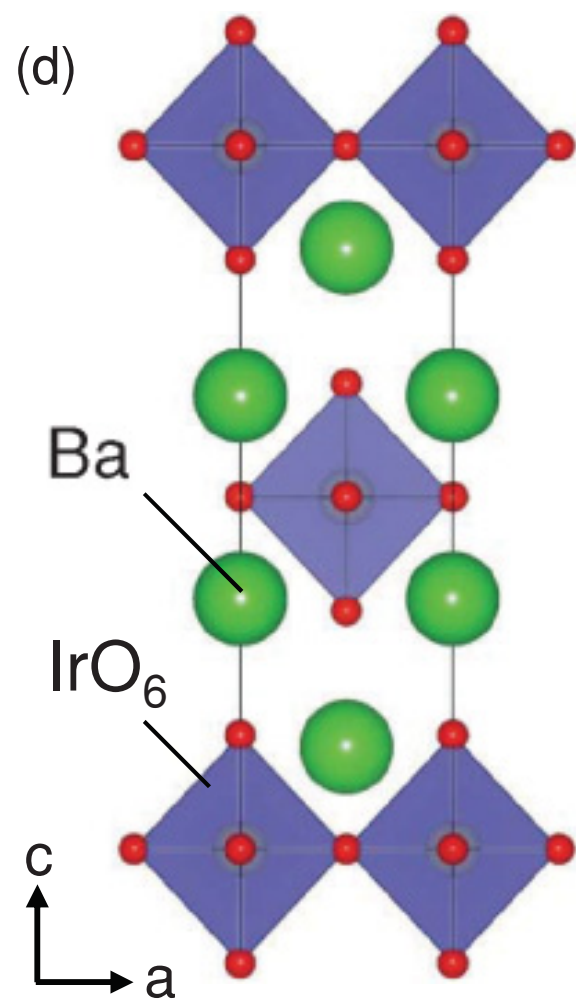
Do long range or at least short range (possibly incommensurate) magnetic correlations persist across MIT?

Resonant X-ray studies of magnetism in doped systems?

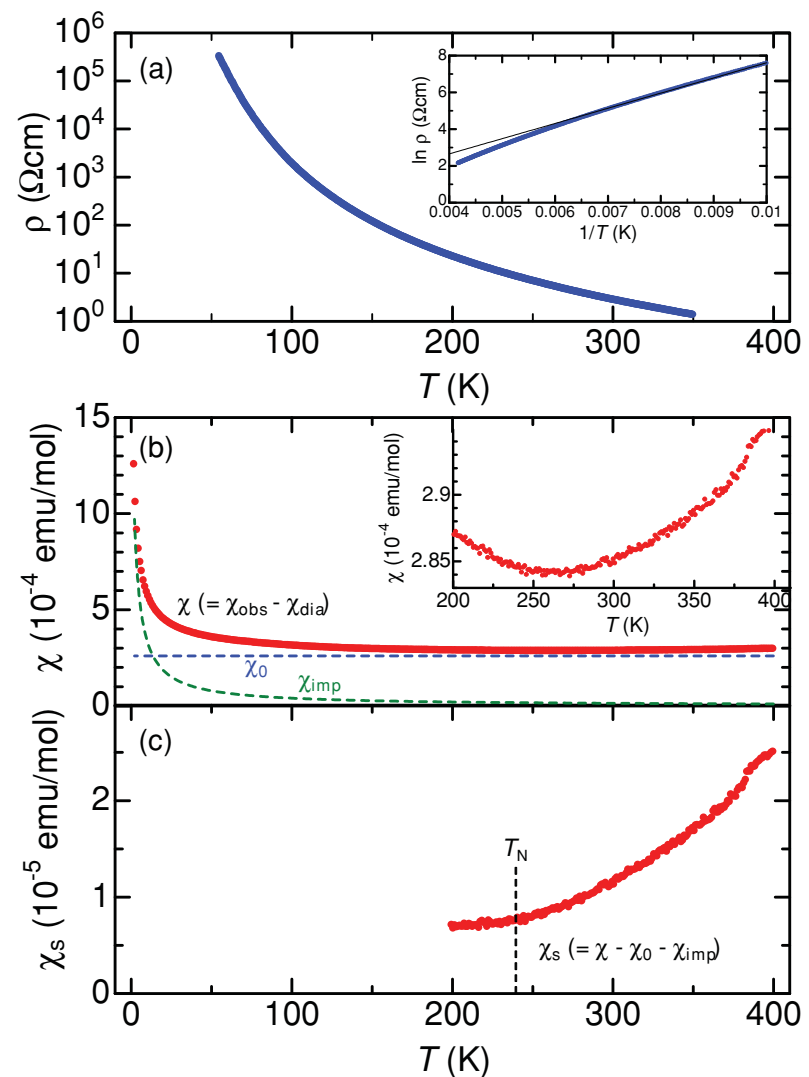
New 214 iridate: Ba₂IrO₄

Same structure as Sr-214 but no rotation of Ir-O octahedra.

Okabe,...Akimitsu et al, 2011

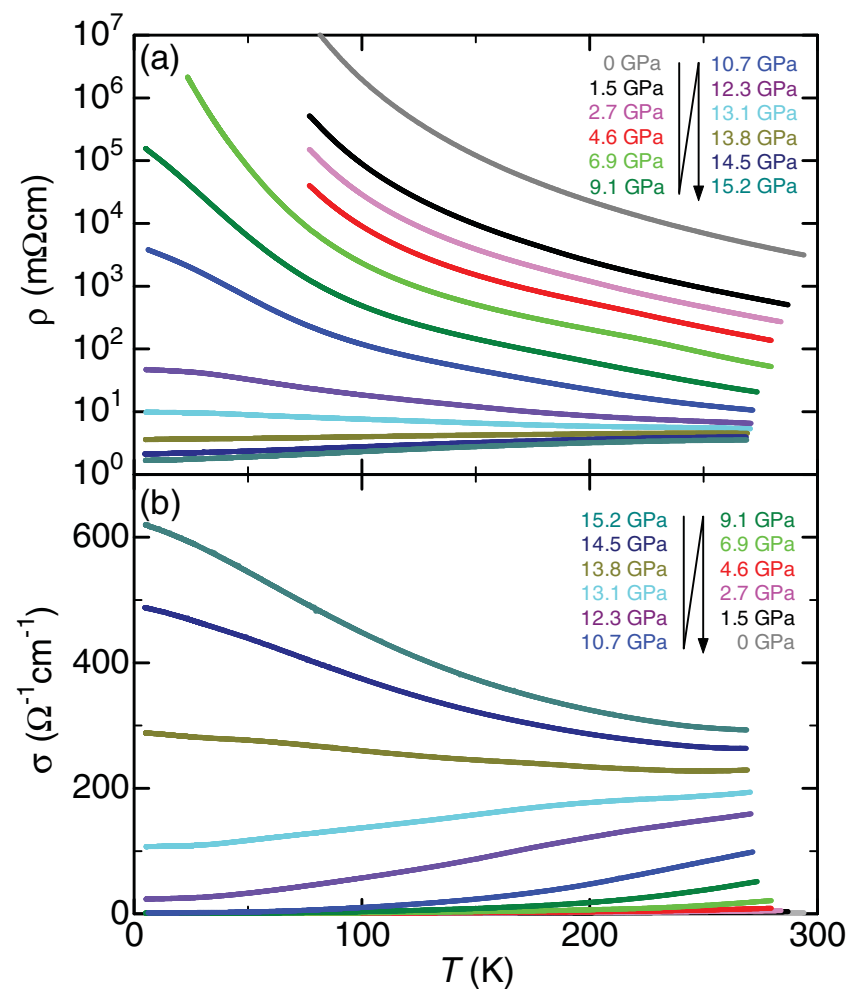


AF seen by muSR



Ba₂IrO₄: Metal-insulator transition under pressure

Okabe,..Akimitsu et al, 2011

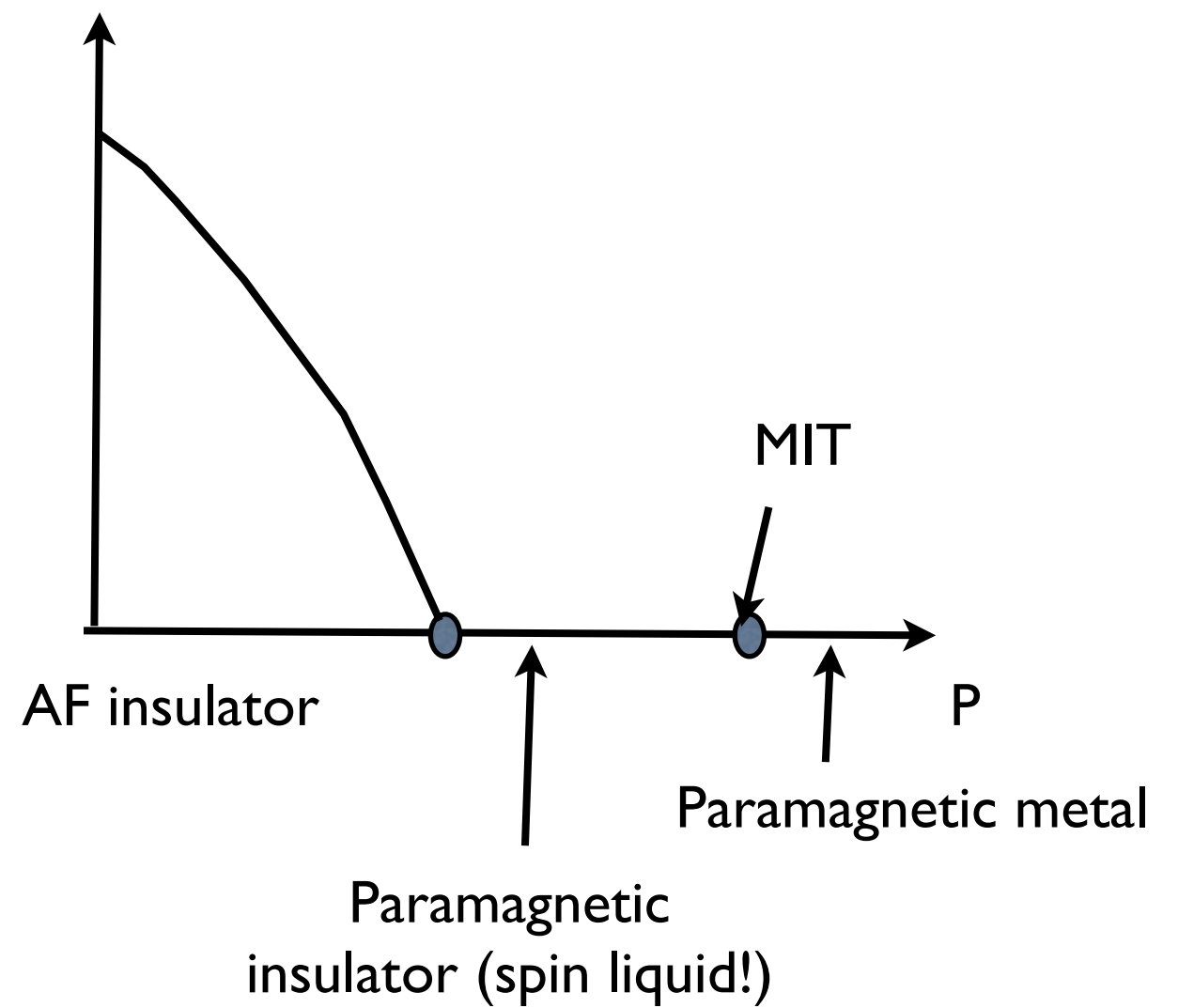
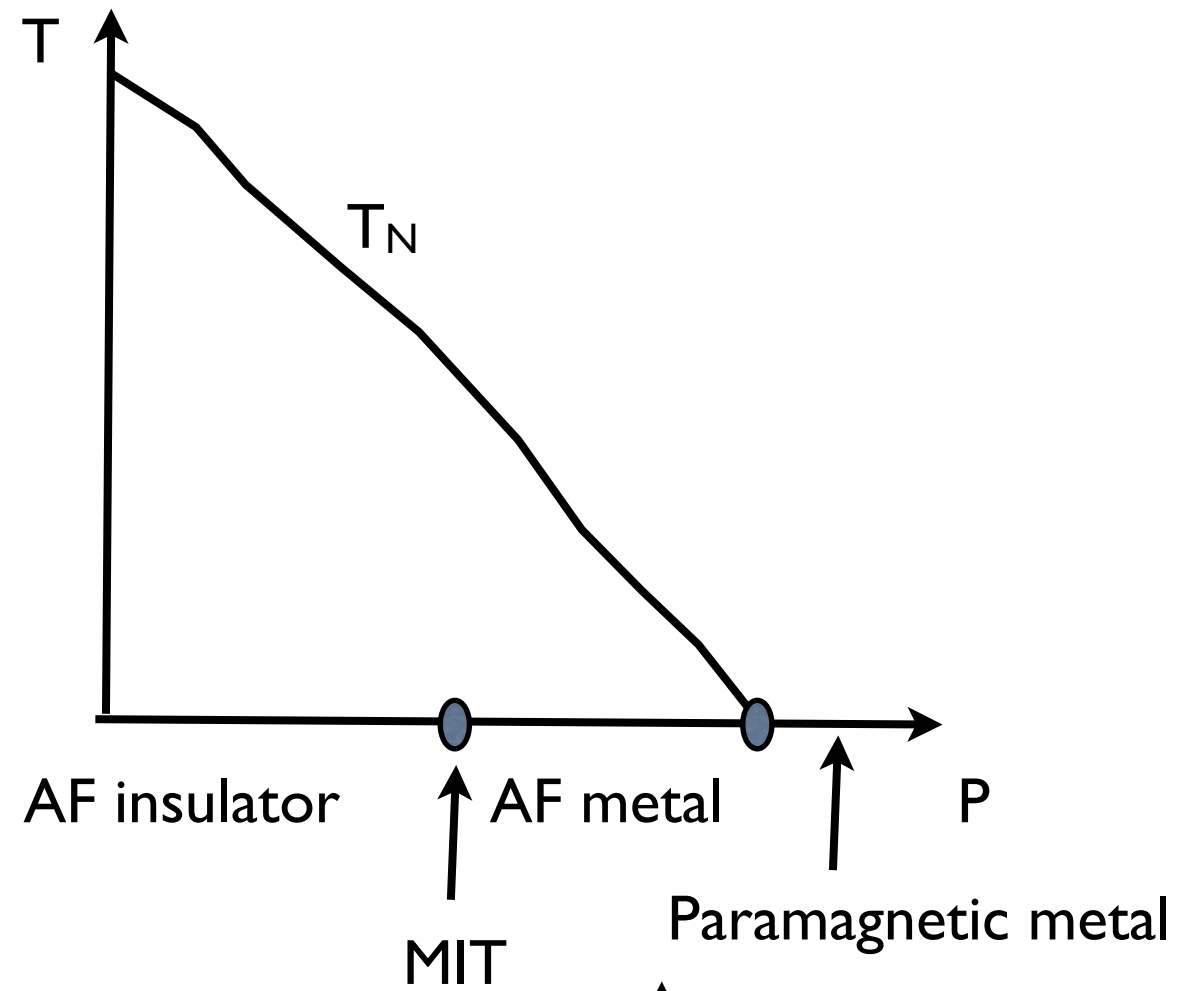


Apparently continuous $T = 0$ metal-insulator transition!

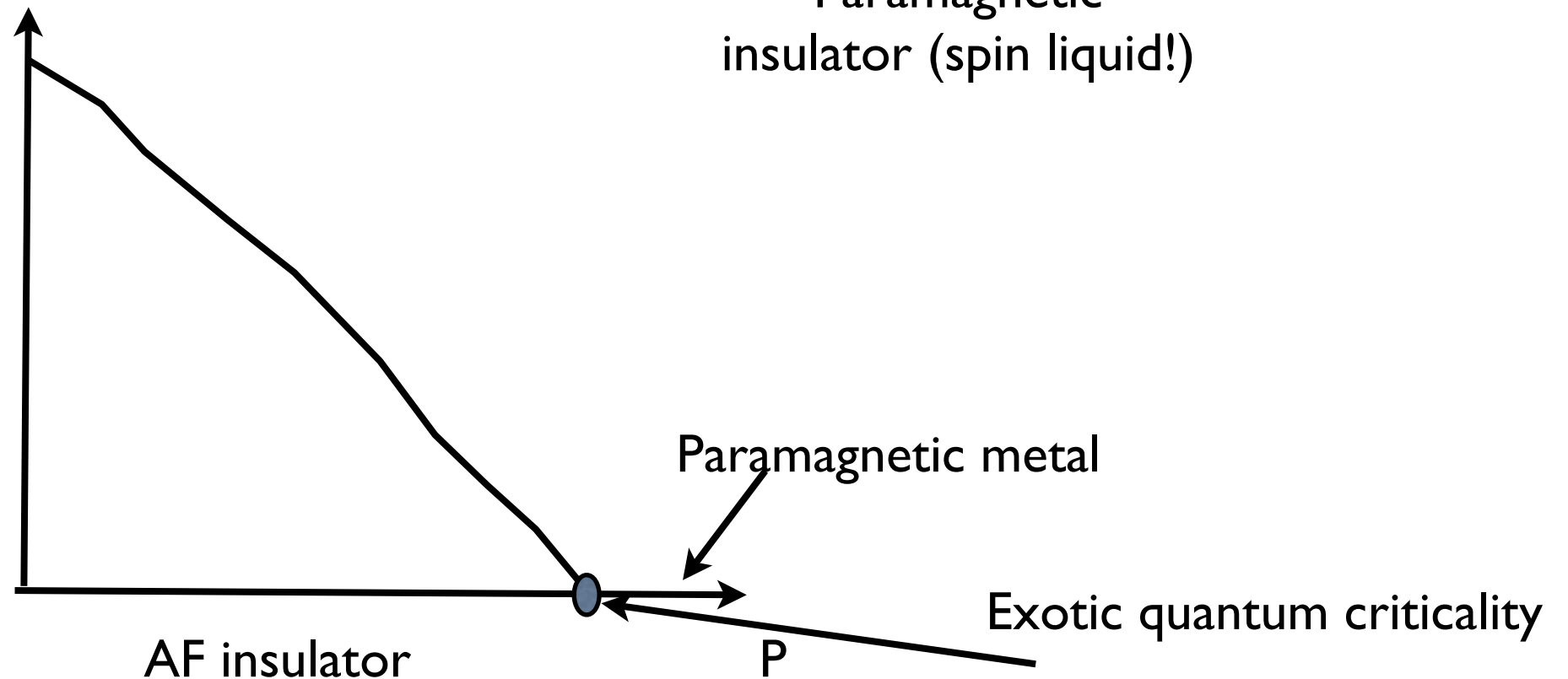
Nice opportunity to study interplay of magnetism and metal-insulator transition.

17O NMR under pressure?

Possibilities



Even more exotic



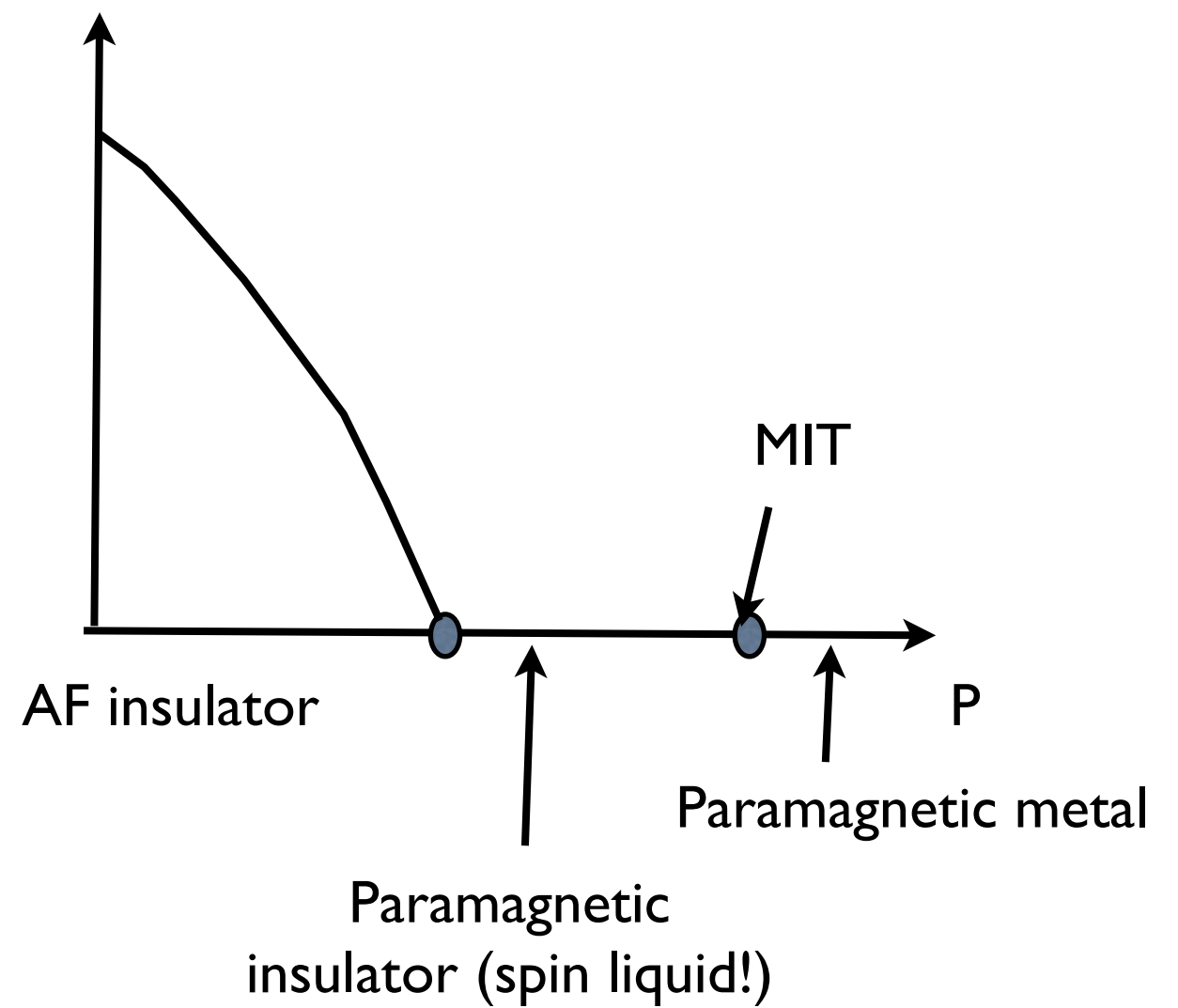
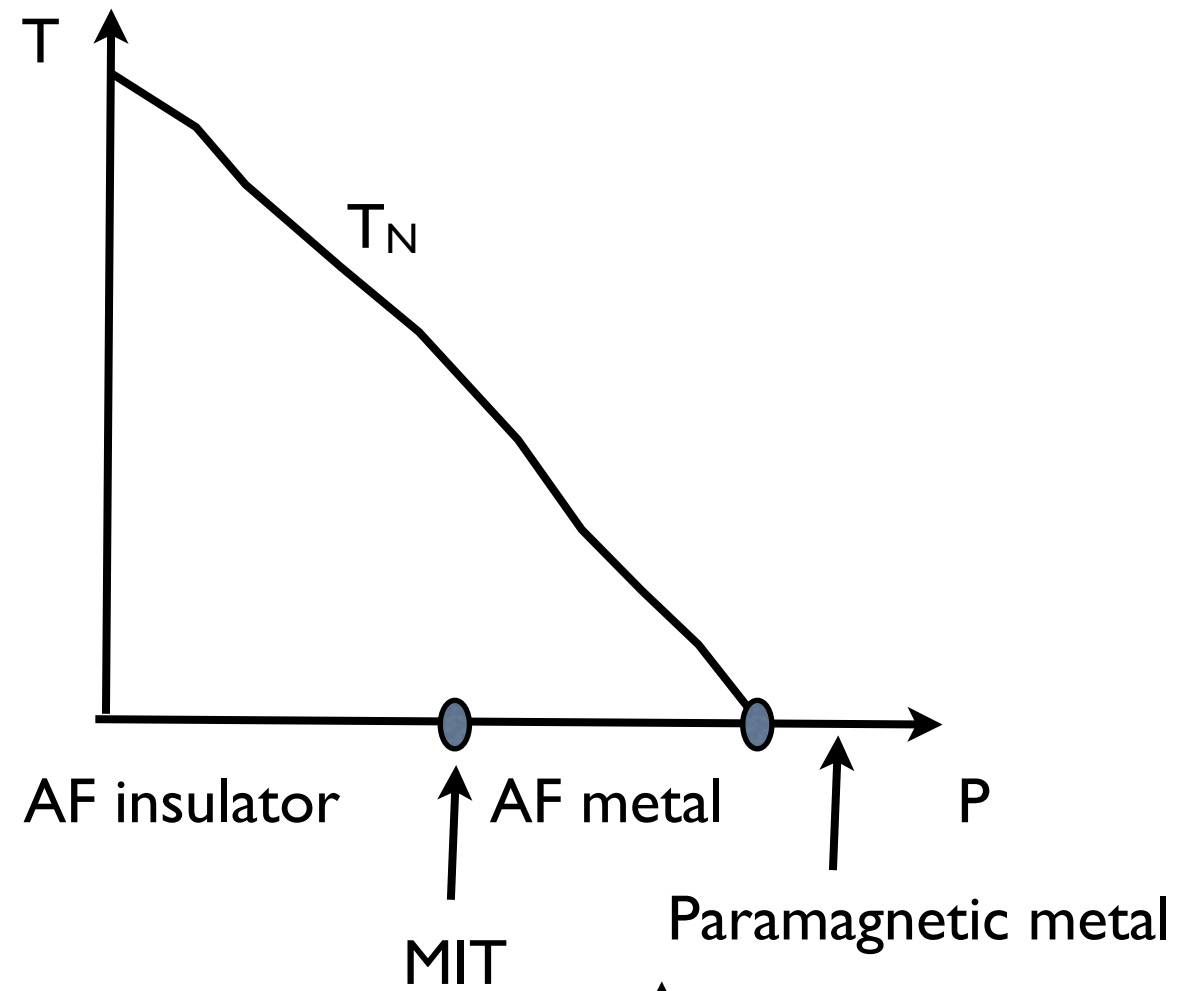
Summary

Sr_2IrO_4 : spin-orbit entangled moments in a Mott insulator
Hubbard model similar to cuprates but smaller overall energy scale.

Ba_2IrO_4 looks very interesting.

Doping: Possible high- T_c superconductor, interesting lessons by comparing with cuprates.

Possibilities



Even more exotic

