

Superconductivity in iridates?  
Remarks on (un)doped Sr<sub>2</sub>IrO<sub>4</sub>  
Fa Wang and T. Senthil, to appear.

026												
Ag												
Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn		
		0.39	5.3							0.9		
Yr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd		
		0.52	9.2	0.92	8.8	0.49				0.56		
Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg		
	6.0	0.09	4.48	0.01	1.70	0.66	0.11			4.16		
Ac												
		Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy		

# Iridium oxide materials: various kinds of exotic physics

$\text{Na}_4\text{Ir}_3\text{O}_8$ : insulating quantum spin liquid (Okamoto, Takagi et al, 2007)

$\text{Sr}_2\text{IrO}_4$ :  $J_{\text{eff}} = 1/2$  spin-orbit entangled Mott insulator (B.J. Kim et al, 2008)

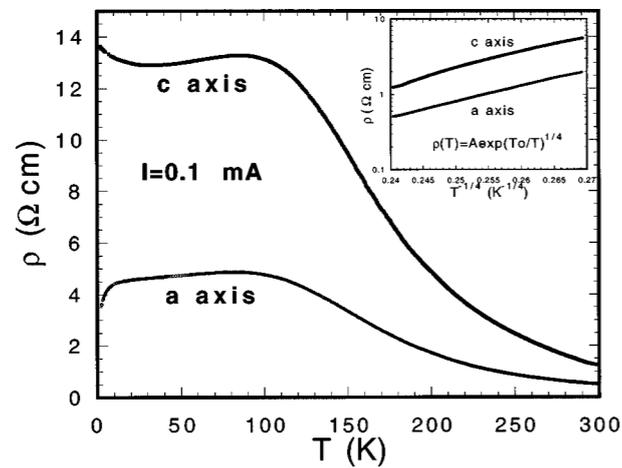
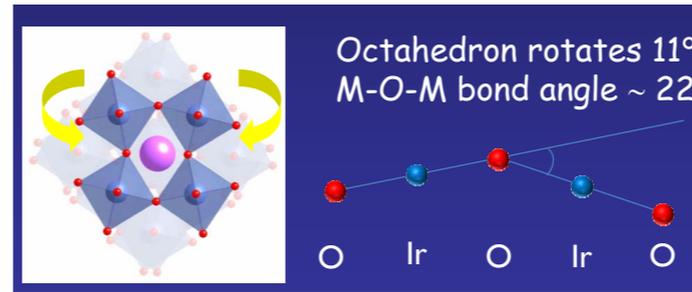
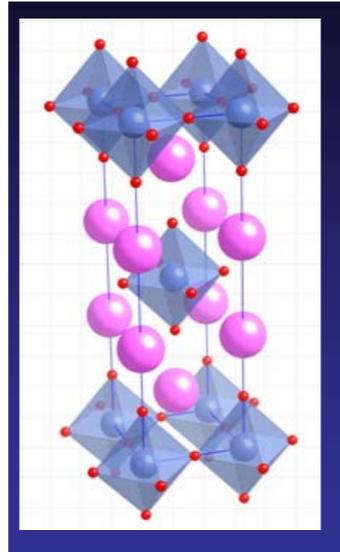
Other interesting proposals:

$\text{A}_2\text{IrO}_3$ : quantum spin Hall effect? (Shitade, Nagaosa et al, PRL 2009), realization of Kitaev spin liquid? (Jackeli, Khaliullin, PRL 2009)

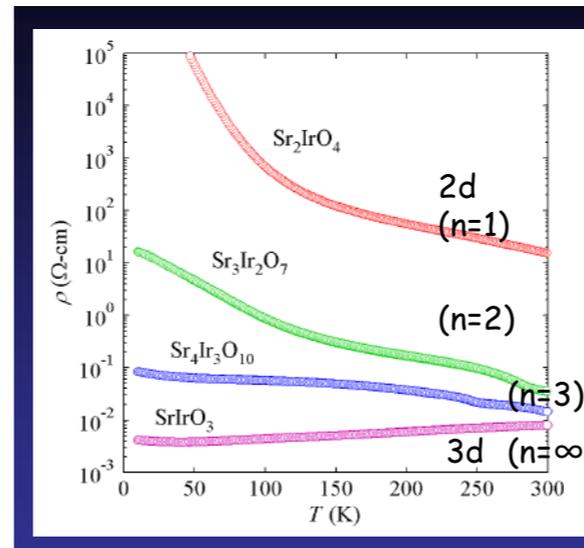
$\text{Ln}_2\text{Ir}_2\text{O}_7$  pyrochlore iridates: 3d correlated topological insulator? (Pesin, Balents, Nat Phys 2010).

# Sr2IrO4: preliminaries

K<sub>2</sub>NiF<sub>4</sub> structure similar to La<sub>2</sub>CuO<sub>4</sub>



Cao et al, PR B 1998



H. Takagi et al, 2008

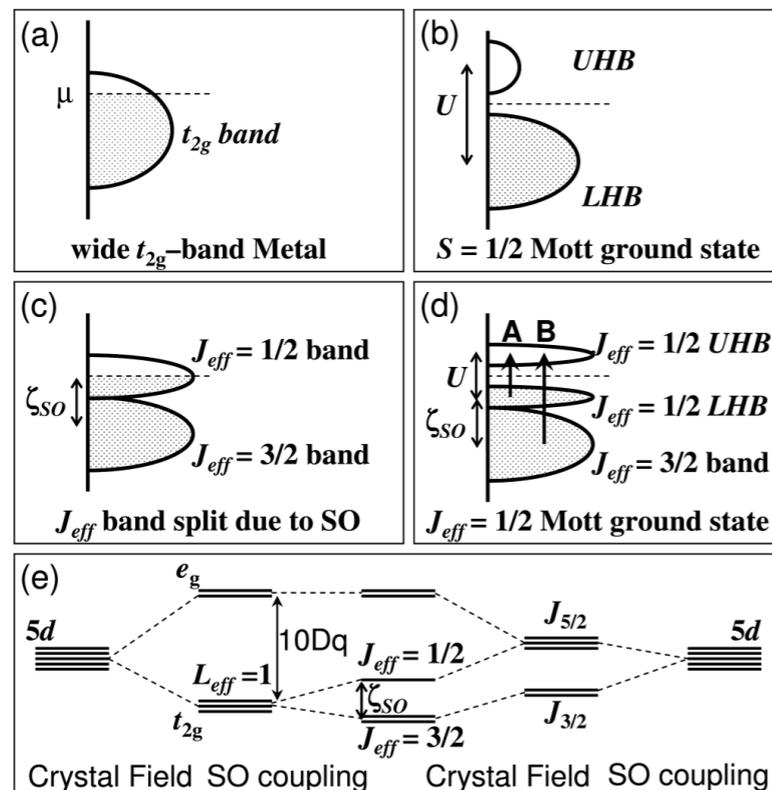
Layers of IrO<sub>2</sub> ;  
Ir<sup>4+</sup> ions on a 2d square lattice.

Each Ir surrounded by  
O octahedra.

Mott insulator

# Why a Mott insulator?

Ir 4+ is in a  $5d^5$  configuration.



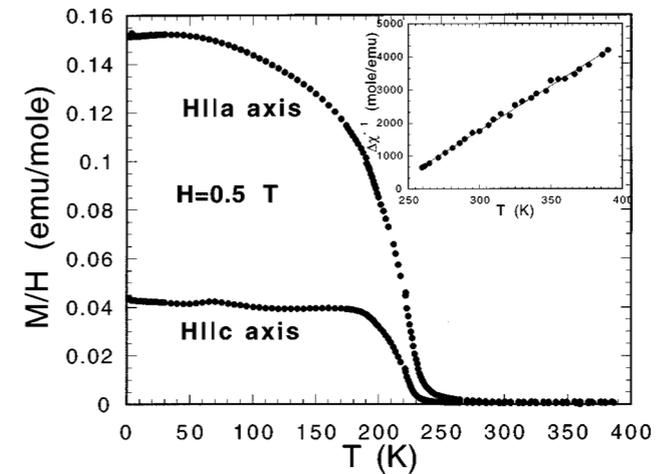
SO coupling splits  $t_{2g}$  level into  $J_{eff} = 1/2$  and  $J_{eff} = 3/2$  bands.

$J_{eff} = 1/2$  band is half-filled and narrow  
 $\Rightarrow$  moderate  $U$  can drive it into a Mott insulator

B. J. Kim et al, PRL 08

# Spin-orbit entangled Mott insulating magnet

$$J_{eff1/2} = \frac{1}{\sqrt{3}} (|xy, \pm 1/2\rangle \pm |yz, \mp 1/2\rangle + i|zx, \mp 1/2\rangle)$$



$J_{eff}$  moments order into a magnetic state below 240 K.

Weak ferromagnetism (from canting of AF moments):  $0.14 \mu_B$

Spin-orbital content confirmed by resonant magnetic X-ray diffraction  
(Takagi et al, Science 2009)

# A microscopic model

Jin, Jaejun Yu, et al, PR B 2009

Tightbinding model for spin-orbit coupled  $t_{2g}$  orbitals projected to  $J_{eff} = \frac{1}{2}$  subspace

Spin dependent nearest neighbor hopping between local  $J_z = \pm\frac{1}{2}$  states.

$$t_0 + i\sigma^z t_1$$

$$t_0 \approx 0.2eV, t_1 \approx -0.04eV$$

Further neighbors  $t' \approx .05eV, t'' \approx -0.02eV$ .

On-site Hubbard  $U \sim 2eV$

Spin model at half-filling:

$$\mathcal{H}_{\text{spin}} = \sum_{\langle ij \rangle} [I_0 \mathbf{J}_i \cdot \mathbf{J}_j + I_1 J_{zi} J_{zj} + \mathbf{D}_{ij} \cdot \mathbf{J}_i \times \mathbf{J}_j]$$

Spin canting explained by Dzyaloshinski-Moriya term

# Mapping to isotropic model

Sublattice dependent  $SU(2)$  spin rotation

$$d_{r\alpha} = \left( e^{i\phi\epsilon_r\sigma^z} \right)_{\alpha\beta} c_{r\beta} \quad (1)$$

gets rid of complex spin dependent hopping.

Rotated basis: Map to isotropic Hubbard model

Wang, TS, 2010

Spin model limit: staggered spin rotation removes anisotropic exchange  
(Jackeli, Khaliullin, PRL 2009, also Shektman et al, PR L 1992 for cuprates)

Explains success of recent fits of high- $T$  spin correlation length to isotropic Heisenberg AF (Fujiyama, Takagi et al, talk at Highly Frustrated Magnetism conference, 2010) with  $J \sim 1000K$ .

# Compare to cuprate

Effective isotropic Hubbard model parameters:

$$t \approx 0.2eV, t' \approx \frac{t}{4}, t'' \approx -\frac{t}{10}, U \approx 10t.$$

Similar to cuprate?

1. Roughly same parameter range as cuprate Hubbard model except overall energy scale smaller by  $\approx 2$ .
2.  $t'/t$  positive for iridate - opposite to cuprate

# Doped system - superconductivity?

If the doped square lattice 2d Hubbard model is superconducting, can we expect doping the iridate will give a 'high temperature' superconductor?

From comparison to cuprate

(i)  $t'/t > 0 \Rightarrow$  Electron doping better than hole doping for iridate  
(Example: Replace Sr by La)

(ii) Overall energy scale smaller by 2  $\Rightarrow$   $T_c$  in range of 50 K???

# Pairing symmetry

In **rotated** basis, expect  $d_{x^2-y^2}$  pairs

$$\Delta \sim \sum_r (d_{r\uparrow}d_{r+x\downarrow} - d_{r\downarrow}d_{r+x\uparrow}) - (x \rightarrow y) \quad (1)$$

In **lab** basis (i.e undo staggered spin rotation)

$$\Delta = \sum_r \cos(\phi) (d_{r\uparrow}d_{r+x\downarrow} - d_{r\downarrow}d_{r+x\uparrow}) - (x \rightarrow y) - i \sum_r \epsilon_r \sin(\phi) (d_{r\uparrow}d_{r+x\downarrow} + d_{r\downarrow}d_{r+x\uparrow}) - (x \rightarrow y) \quad (2)$$

i.e, a mixture of ‘conventional’ d-wave singlet pairing and a d-wave ‘triplet’ centered at  $(\pi, \pi)$ .

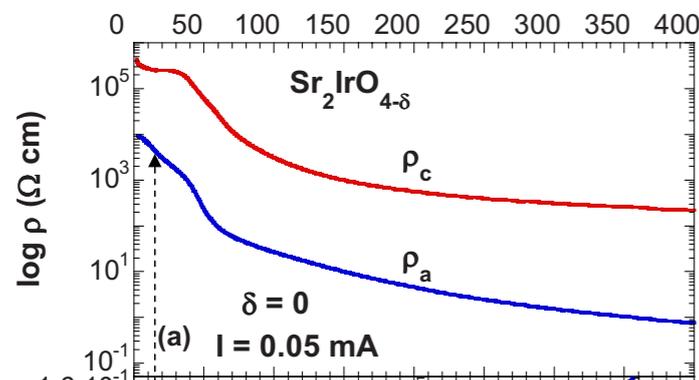
**Note:** despite apparent complex pair wavefunction, **T**-reversal preserved.

# Differences with cuprates: more coherent c-axis transport?

Interlayer tunneling matrix element in cuprate:  
 $(\cos k_x - \cos k_y)^2$  factor which blocks c-axis transport of nodal states.

Iridate: different orbital content implies no suppression of nodal c-axis hopping.

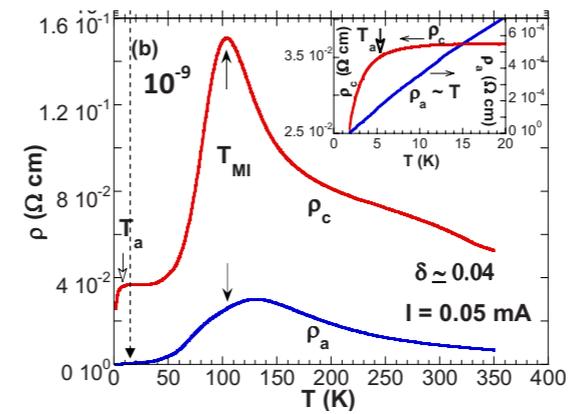
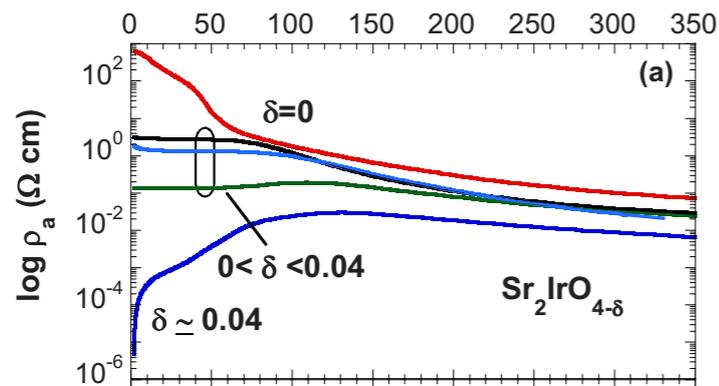
Better c-axis coherence?



Overall resistivity anisotropy of about  
100 in undoped insulator

# Experimental prospects?

## Recent report: Metal-insulator transition with Oxygen doping



Cornetta, Cao et al, PR B 2010

Will it be possible to dope  $\text{Sr}_2\text{IrO}_4$  to higher doping levels?

# Summary

Iridium oxides: spin-orbit coupling enhances importance of correlation effects even with moderate  $U$ .

$\text{Sr}_2\text{IrO}_4$ : spin-orbit entangled moments in a Mott insulator  
Hubbard model similar to cuprates but smaller overall energy scale.

Doping: Possible high- $T_c$  superconductor, interesting lessons by comparing with cuprates.

Other interesting iridate:

$\text{Na}_2\text{IrO}_3$  -  $J_{\text{eff}} = 1/2$  frustrated AF Mott insulator on honeycomb lattice (Singh, Gegenwart, PR B 2010)

Nature yet to be clarified? effects of doping?