

B5

Theory:

$$F = \frac{GmM}{r^2} \quad (\text{Force between } M \text{ and } m)$$

$$\begin{aligned} \tau &= \vec{\ell} \times \vec{F} \\ &= \frac{\ell GmM}{r^2} \quad (\text{Torque due to both mass pairs}) \end{aligned}$$

$$\tau = -K\phi \quad \begin{array}{l} \text{Twisted wire resists torque. Hooke's Law} \\ \phi \equiv \text{angle of twist of wire} \end{array}$$

$$T = 2\pi \sqrt{\frac{I}{K}} \quad \text{Period of torsional pendulum}$$

$$I = \frac{m\ell^2}{2} \quad \text{Moment of Inertia, small masses } m \text{ on rod}$$

$$\theta = 2\phi \quad \text{Reflecting laser from plane mirror.}$$

$$-K\phi = \frac{\ell GmM}{r^2} \quad \text{Equal Torques}$$

$$\phi' = 2\phi \quad \text{Reversed direction of masses. Total deflection}$$

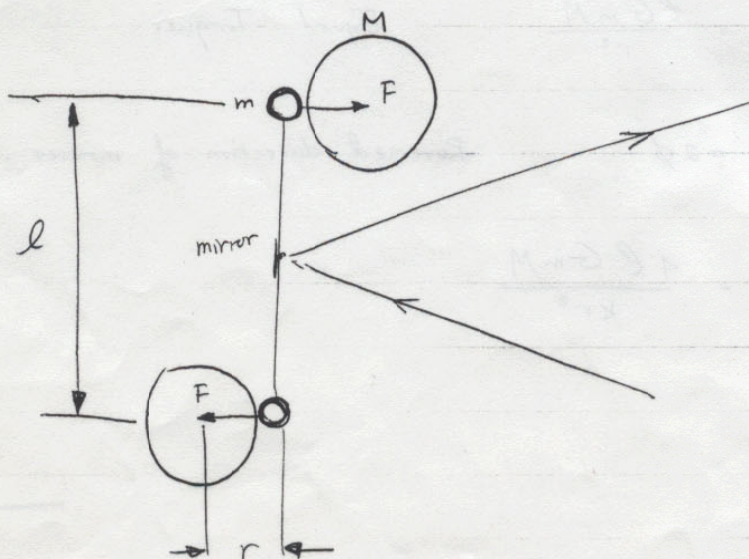
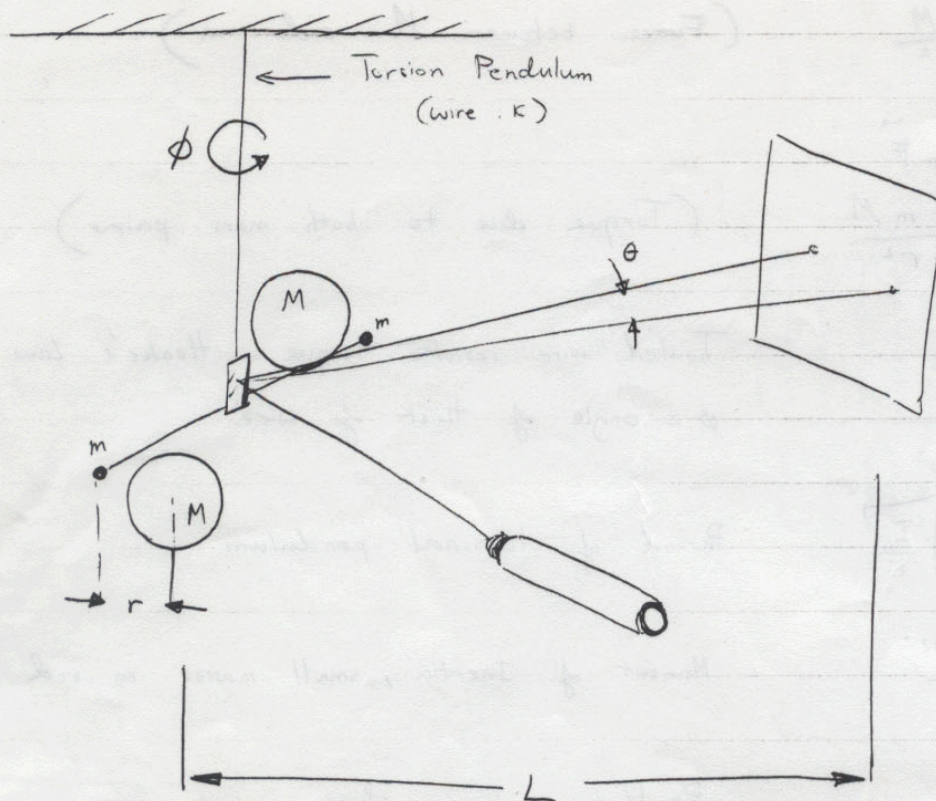
$$\theta = \frac{4\ell GmM}{Kr^2}$$



# Cavendish Exp.

B5

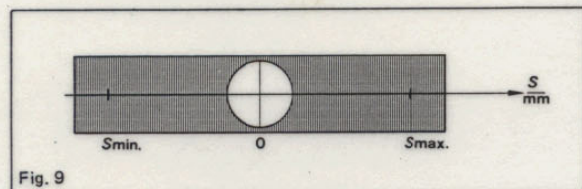
Theory:





### 3.3.2 Zero adjustment

- The gravitation torsion balance must be aligned vertically (see 3.3.1).
- After assembly, the apparatus should have been left for at least one day in adjusted and unlocked state before final zero adjustment, as in the beginning the torsion band always still elongates a little. This will save time.
- At first, remove the large lead balls ③.



Lock the system by means of knurled head screws ⑤ and bring it to oscillation by unlocking.

Watch the light-spot over a longer period (approx. 8 mins.) (Fig. 9). The max. deflections  $S_{min}$  and  $S_{max}$  of the light spot are limited by the small balls touching the casing walls. The effective measuring range lies within these limits.

Mark the two extreme values of the slowly moving light spot left and right on the projection wall (scale). Observe which rest position the system tends to take.

If this rest position deviates greatly from the centre between the above mentioned extremities, turn the torsion head ① through a small angle towards the desired zero point after loosening the lateral knurled head screw ②. Then lock the torsion head again.

Watch the zero again and repeat the procedure until the desired zero position  $S = 0$  is attained.

#### Important Note:

To reduce the time required to perform the zero checks, a small, strong permanent magnet will be very helpful (e. g. the floating magnet from 510 44):

Lead is repelled by magnets due to its diamagnetic properties. Hence, if one of the small lead balls approaches the casing wall, hold the magnet close to it for a short time until the system reverses.

If this is repeated several times, the gravitation torsion balance will quickly come to rest.

When zero adjustment is completed, place the large lead balls on the swivel support ④ left and right. Move the support (as in Fig. 2) carefully until the large balls touch the casing wall.

The light spot will then balance out to its final rest position which is approx.  $0.015 L$  ( $L$  = distance between scale wall and rotary mirror) left from the scale zero.

The unlocked gravitation torsion balance is ready for measurement.

When the ball has moved to the opposite position, the light spot balances out to an equal limit value right from the zero. In mid position of the large balls, the effective gravitational forces compensate each other; the light spot goes to zero position.

The firmly fitted measuring assembly need not be locked. This is only advisable if you cannot prevent unauthorized persons to touch the apparatus.



(Fig. 3)

*Small lead balls*

Mass: each  $m_1 = 0.015$  kg

Ball radius  $r_1 = 6.9$  mm

Distance of center of gravity from the axis of rotation:

$d = 50$  mm

*Large lead balls*

Mass: each  $m_2 = 1.5$  kg

Ball radius:  $r_2 = 32$  mm

Distance of center of gravity between large ball when touching the wall and small ball in mid position:

$s_0 = 46.5$  mm (see Fig. 3)

Period of oscillation of the system:  $T = \text{approx. } 10$  mins.

Logarithmic damping decrement:  $\Delta = \text{approx. } 0.7$ ,

Directional quantity of angle of the torsion band:

$D = \text{approx. } 8.5 \times 10^{-9} \frac{\text{Nm}}{\text{rad}}$

Difference between the light-spot end indications with the large balls turned to the left or to the right:

$S_1 = \text{approx. } 0.03 L$

( $L$ : Distance between scale wall and rotary mirror)

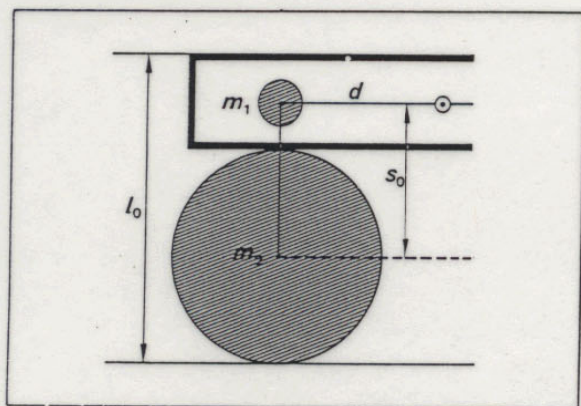


Fig. 3 To determine  $s_0 = \frac{L_0}{2}$ , measure  $L_0$  with a caliper gauge!

### 3 Use

#### 3.1 Additionally required equipment for a solid wall:

**B5**

Cat. No.

1 Stand base, length of sides 28 cm. ....	300 01
1 Pair of levelling screws for 300 01 .....	300 06
2 LEYBOLD multiclips. ....	301 01
or 1 LEYBOLD multiclip (301 01) and	
1 Rotatable clamp (301 03)	
1 Stand rod, bent at an angle, 60 cm long. ....	300 52
1 Lamp housing .....	450 60
1 Lamp, 6 V, 30 W .....	450 51
1 Single-lens condenser with sliding aperture selector .	460 17
1 Voltage source, 6 V, e. g.	
Transformer, 6 V, 30 W. ....	562 76

For faster dying out of the oscillations:

1 Floating magnet .....	510 44
2 Scales, 1 m, with mm-graduation, self-adhesive (Spare Part No. 690 32)	
1 Piece of wire or thread, as thin as possible, approx. 15 cm long	
and/or Adhesive tape, 4 cm long	

#### Assembly aids:

1 Drilling machine	
1 Stone drill	
1 Dowel, 6 mm I. D.	
1 Wood screw, 100 mm long, 6 mm dia.	
1 Screw-driver	
Gypsum	

#### Additional measuring instruments:

1 Precision vernier callipers .....	311 54
1 Time measuring instrument, e. g.	
1 Stop-clock .....	313 05
or	
1 Metronome .....	313 11
or	
1 Electric stop-clock .....	313 04
or	
1 Counter P .....	575 45
or	
1 Electronic stop-clock and relay .....	313 01
or	
1 Digital counter. ....	575 50

#### 3.2 Assembly

Aim: to achieve an experimental assembly which is always ready for use — according to Fig. 2.

##### 3.2.1 Preconditions to be checked:

- There must be a solid wall enabling to suspend a large stand base by its apex borehole at approx. eye-level.
- Above the screw fixture there should be a free space for the carrier tube of at least 30 cm (no breaks, no ceiling).
- It should be possible to mount an at least 0.5 m long scale at a distance of at least 5 m from the site selected for the gravitation torsion balance, at a height of approx.

$\frac{L}{4}$  above the height of the rotary mirror.

(Inclination of light spot  $15^\circ$ ;  $L \tan 15^\circ \approx \frac{L}{4}$ )

The angle of inclination of the light spot and hence the height of the scale may be reduced using a rotatable clamp (301 03) to fasten the lamp.



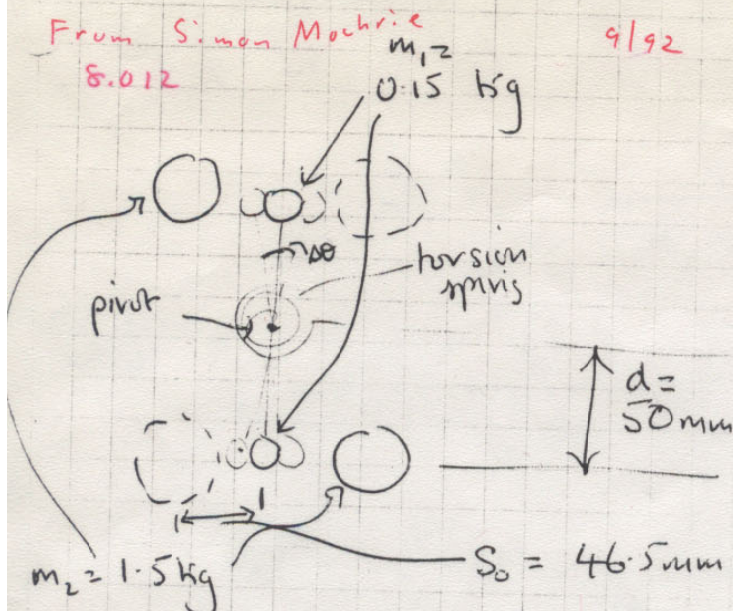
B5

## THE CAVENDISH EXPERIMENT B5

Cavendish Experiment

475

(1)



I ignore  
force between  
small mass &  
distant big ball

↓  
Some significant  
error. see HW.

torsion balance responds as follows

$$\text{Torque} = \text{Force} \times \text{perpendicular distance} = D \frac{1}{2} \Delta \theta$$

$$\text{with } D = 8.5 \times 10^{-9} \text{ m N rad}^{-1}$$

gravitational  
force

$$F \approx \frac{G m_1 m_2}{S_0^2} \times 2$$

$$\text{i.e. } 2 F d = D(\Delta \theta)$$

$$\left( \frac{4 G m_1 m_2}{S_0^2} \right) d = D(\Delta \theta)$$

$$\frac{4}{8.5 \times 10^{-9}} \left( \frac{6.67 \times 10^{-11} (1.5)^2 \times 10^{-2}}{(4.65)^2 \times 10^{-4}} \right) 5 \times 10^{-2} = \cancel{8.5 \times 10^{-9}} (\Delta \theta)$$

$$\frac{4 \times 6.9 \times 5}{8.5} \times 10^{-3} = 16.23 \times 10^{-3} = 0.016 \text{ rads} = 0.9299^\circ = 0.93^\circ$$



35

## THE CAVENDISH EXPERIMENT

B5

or

$$G = \frac{D(\Delta\theta)}{d} \bigg/ \left( \frac{4m_1 m_2}{s_0^2} \right) \quad (2)$$

from  
Simon Machrie

$$= \frac{D s_0^2}{4d m_1 m_2} \Delta\theta$$

$$= \frac{8.5 \times 10^{-9} (4.65)^2 \times 10^{-4}}{4 \times 5 \times 10^{-2} (1.5)^2 \times 10^{-2}} \Delta\theta$$

$$= \frac{8.5 \times (4.65)^2}{\cancel{2 \times 10^{-2}} \times 4.5 \times \cancel{10^{-2}}} \times 10^{-10} \Delta\theta$$

$$= 4.08425 \times 10^{-9} \Delta\theta$$

$$(4.084 \times 10^{-9}) 1.6 \times 10^{-2} = 6.5344 \times 10^{-11}$$



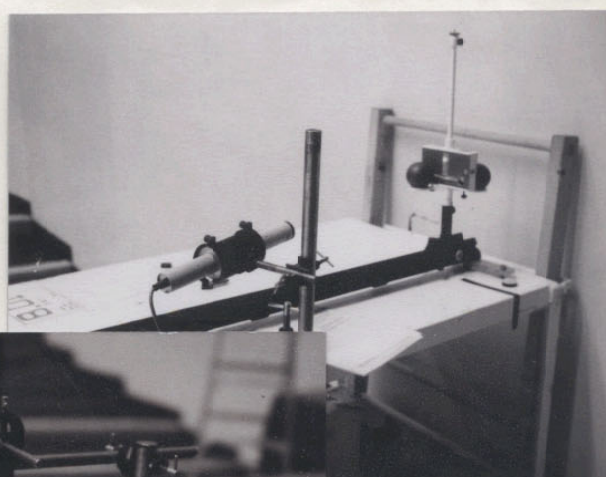
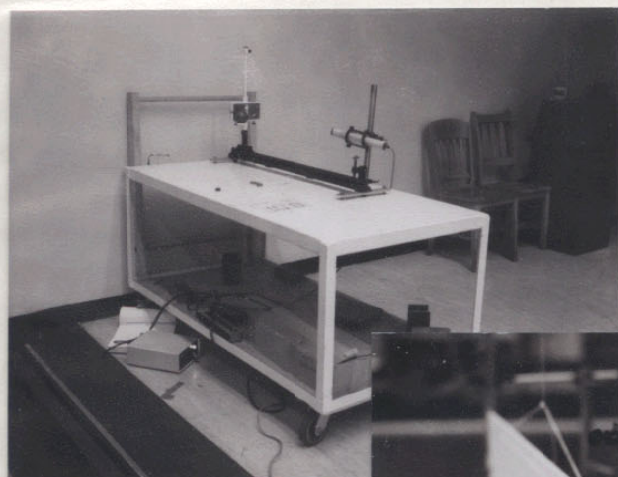
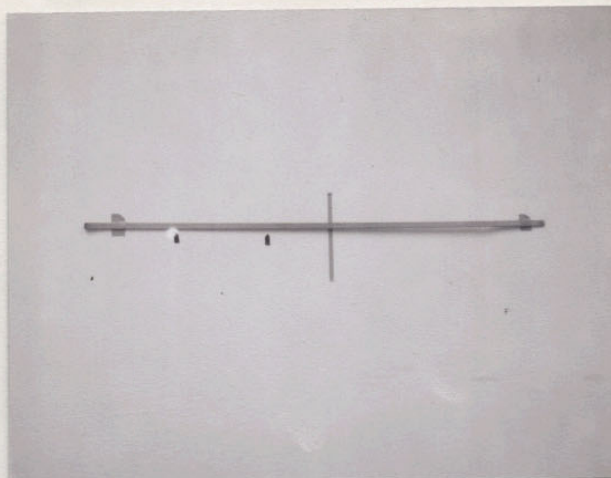
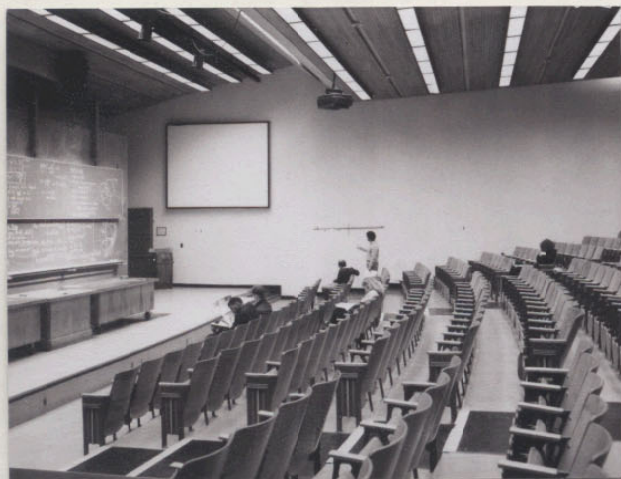
**B5**

## THE CAVENDISH EXPERIMENT

**B5**

### DYNAMICS - Gravitational Forces

A Cavendish apparatus is used for the experimental verification of Newton's law of universal gravitation. The period of oscillation is  $\approx 10$  minutes. There are specific problems using this demonstration in a 50 minute lecture.





**B5**

## THE CAVENDISH EXPERIMENT

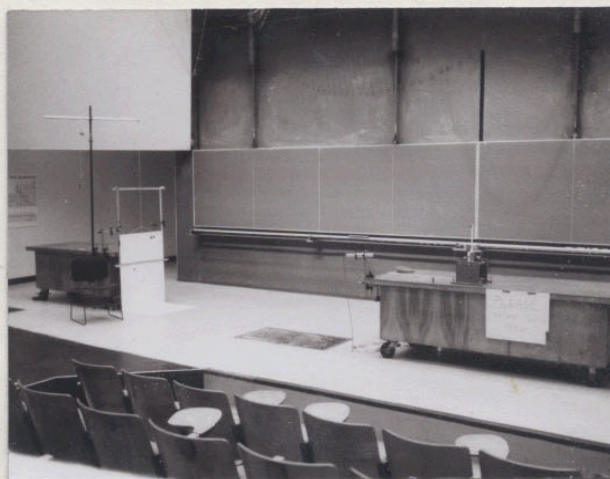
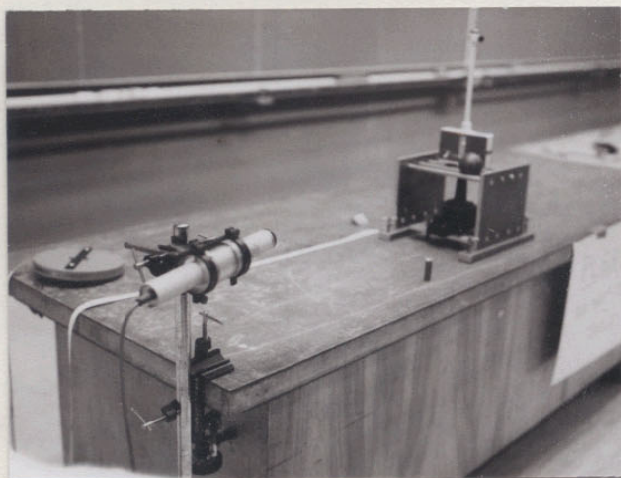
**B5**

### DYNAMICS - Gravitational Forces

This is another way of showing the Cavendish during lecture. The damping is plotted on a movable focore screen used as a scale. The scale is moved up 2cm per minute after the balls are moved.

The distance from the laser to the scale is 5M.

NOTE: Temperature seems to affect the demo.





## Gravitation Torsion Balance

This highly sensitive torsion balance with light-spot reading is used to demonstrate mass attraction and to determine the gravitation constant.

### Measuring principle:

The oscillatory system with long period of oscillation  $T$  and known mass is disturbed in its static equilibrium by the action of gravitational forces of external masses and performs damped oscillations. The active force between the masses may be derived from the motion in time of the oscillation as well as from the new equilibrium position after dying out.

### Examples of Experiments:

- Determining the gravitation constant according to the acceleration method
- Determining the gravitation constant according to the full-deflection method

*Bibliography:* Descriptions of Experiments for 332 10.

### 1 Safety Note

- Suspend the gravitation torsion balance so that it is not accessible to unauthorized persons.

### 2 Standard Equipment, Description, Technical Data

- ① *Metal casing* with glass plate and inner acrylic glass screens to avoid air currents.  
Dimensions: approx. 15 cm x 8 cm x 2.9 cm
- ② *Small lead ball* (2 contained in standard equipment)
- ③ *Large lead ball* (Spare Part No. 68 322, 2 included in standard equipment)
- ④ *Swivel support* for the large balls ③
- ⑤ *Knurled nuts* for locking the torsion balance
- ⑥ *Adjusting ring* for height adjustment of the swivel support ④
- ⑦ *Short rod* for securing to a permanent support, 12 mm dia.
- ⑧ *Concave mirror* for the light-spot indicator, focal length approx. 30 cm
- ⑨ *Torsion band*, made of bronze  
Length: approx. 26 cm  
Cross-section: 0.01 mm x 0.15 mm  
Replacement:  
1 m torsion wire on plastic reel (Spare Part No. 68 320)
- ⑩ *Carrier tube* for torsion band ⑨  
Length: approx. 26 cm
- ⑪ *Torsion head* for zero adjustment
- ⑫ *Knurled head screws* to lock the torsion head ⑪

Furthermore, the standard equipment comprises:  
2 scales, 1 m, with mm-graduation, self-adhesive  
(Spare Part No. 69 032)

### Packing material:

2 metal clamps to protect the apparatus when transporting it (approx. 4 cm wide).

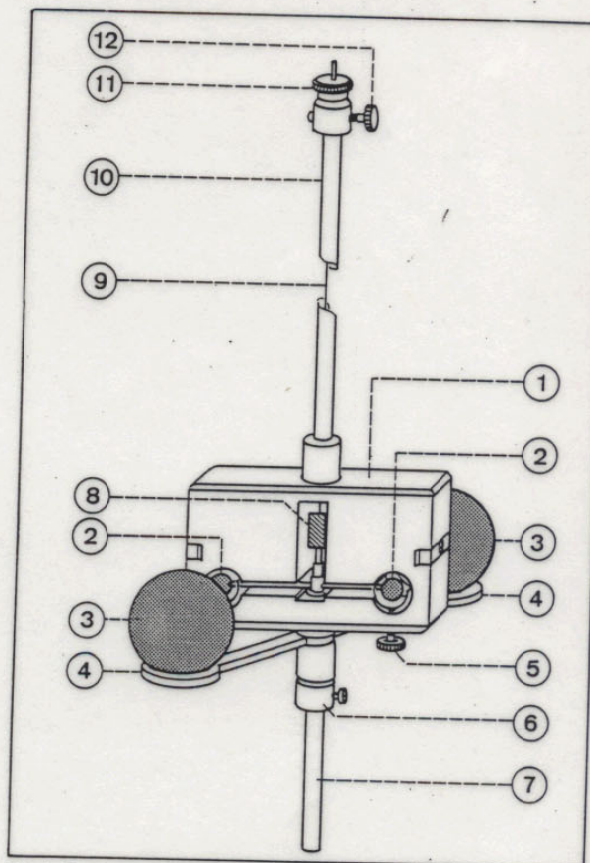


Fig. 1 Standard equipment of gravitation torsion balance (332 10)

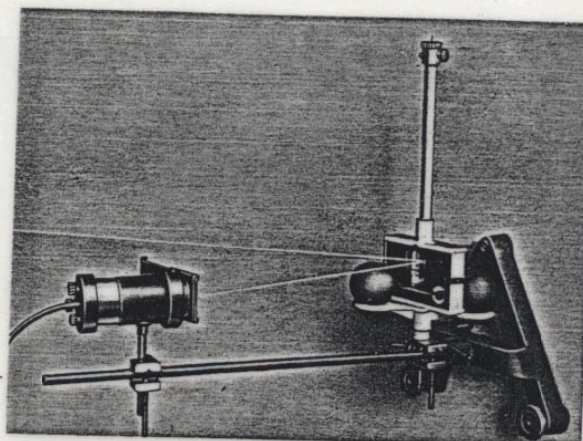


Fig. 2 Ready-to-operate set-up of gravitation torsion balance with additional equipment



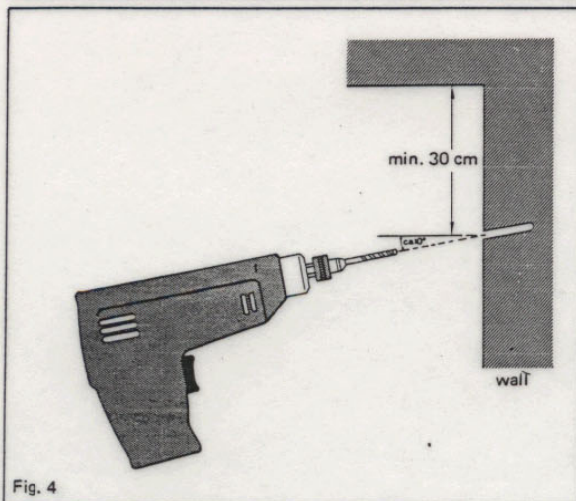


Fig. 4

- Make a hole in the wall using a stone drill (8 mm dia.) holding it at a slightly inclined angle. Observe minimum distance from any corbels of the wall (Fig. 4).

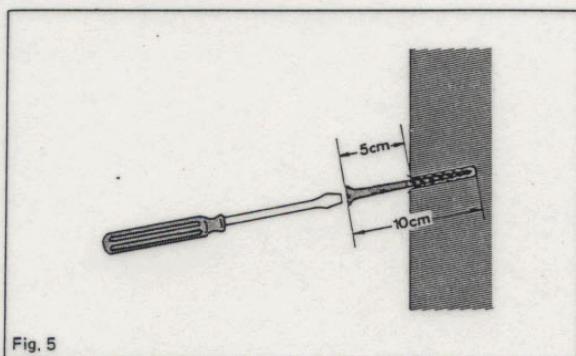


Fig. 5

- Apply a dowel (8 mm dia.) with gypsum and screw in a wood screw (10 cm long) leaving approx. 5 cm (Fig. 5).

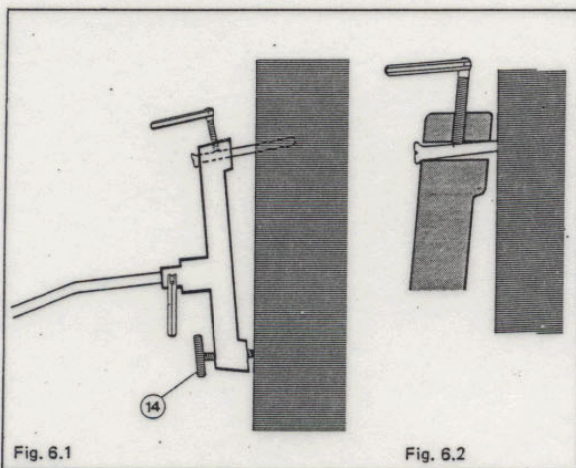


Fig. 6.1

Fig. 6.2

- Suspend a large stand base by its apex borehole and secure it (Figs. 6.1 and 6.2).
- Align the stand base so that it is parallel to the wall using the levelling screws (14), (Figs. 6.1 and 7).  
If the levelling screws should press themselves into the wall, put something solid underneath.

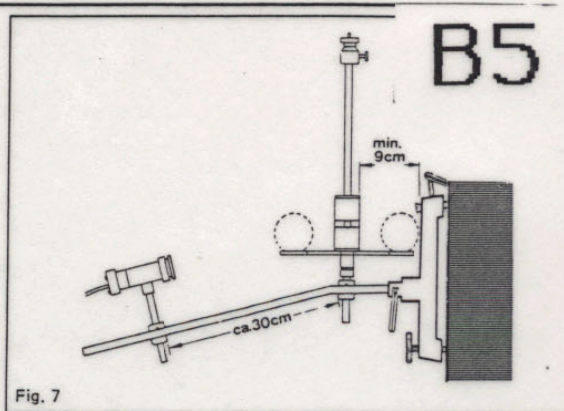


Fig. 7

- Further assembly according to Figs. 7 and 2.

### 3.2.2 Setting up the projection device for the light spot

Mount the condenser to the lamp. Stretch a thin thread over the centre of the large aperture transverse to the sliding diaphragm, or apply adhesive tape so that its edge, which is particularly suitable as a light mark, is positioned accordingly. Produce a sharp image of the light mark on the scale on the opposite wall by shifting the lamp.

Project a vertical image of the lamp filament on the concave mirror by means of the condensor, turning and sliding the lamp insert.

### 3.3 Adjustment instructions

#### 3.3.1 Vertical adjustment of the gravitation torsion balance (Fig. 8)

- Unlock the suspension by loosening the knurled head screws (5).
- Readjust the levelling screws (14) of the stand base (see Fig. 6.1) by turning them until the torsion band is suspended precisely in the axis of boreholes (13).

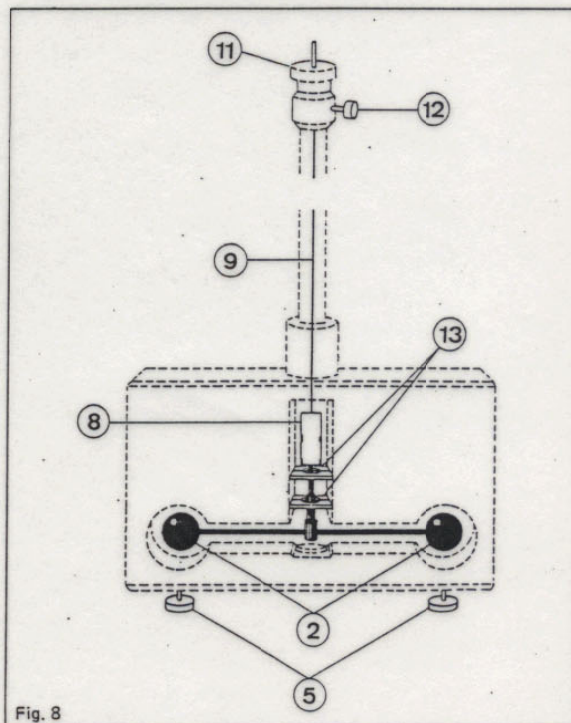
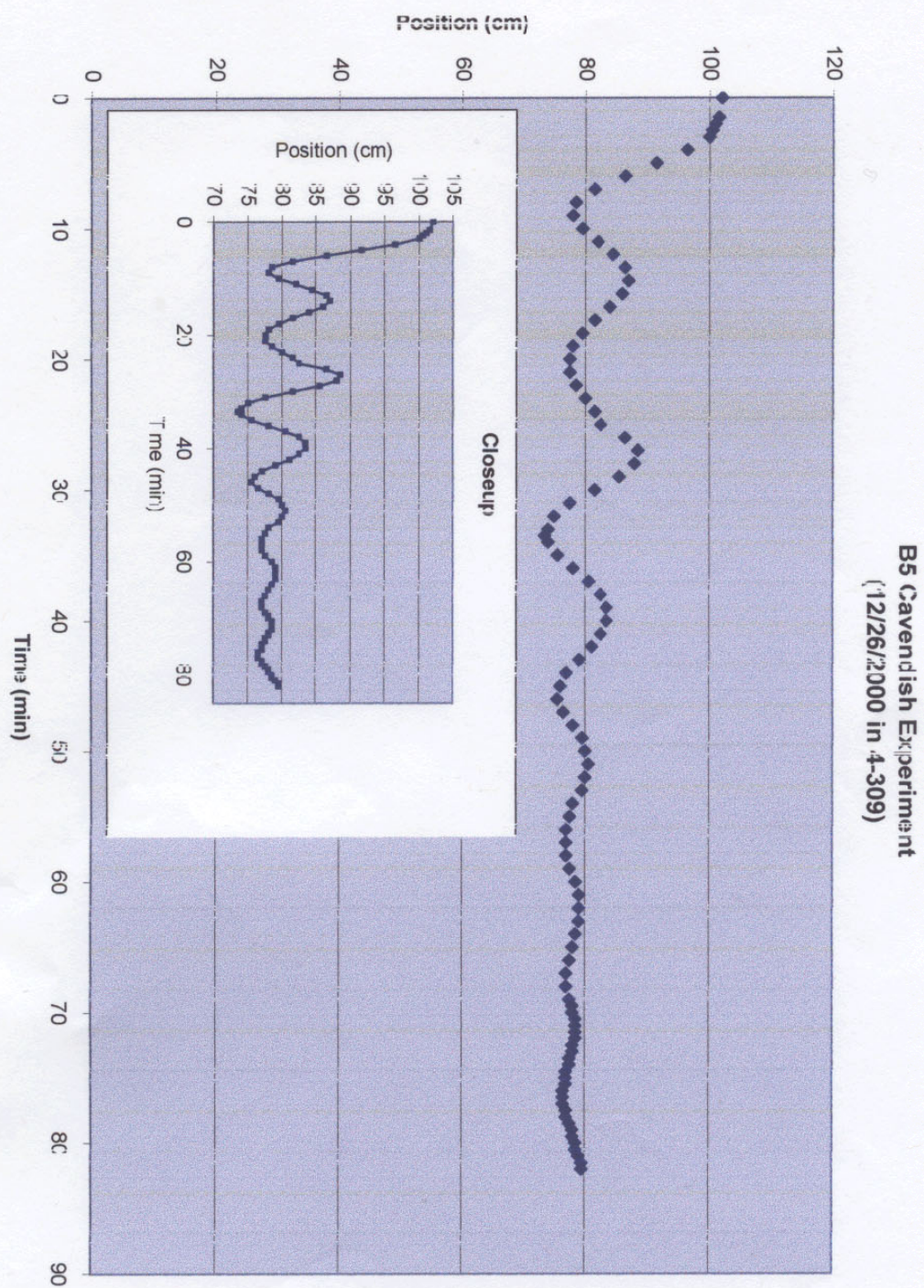


Fig. 8







B5

CAVENDISH

B5

0.015  
1.5  
0.1  
2  
0.0475  
0.7

period 602 seconds Inertia  
lambda 1000 seconds k  
dt 0 seconds pi  
zero 48 mm G  
zerosc 6 mm Angle  
amplitude 55 mm Expected Dx  
Measured Dx  
Ratio Meas./Exp. 72%

0.000078 kg\*m<sup>2</sup>  
8.4969E-09 N\*m/rad  
3.14159265  
6.67E-11 m<sup>3</sup>/(kg\*s<sup>2</sup>)  
0.031 rad  
0.067 m  
0.048 m

mass1  
mass2  
Length  
Distance  
Radius  
Shift

Time	Displacement	Displacement/	Time(sec)	Theory	Zero
12:17	6	0	0.00	-7.00	49.00
12:19	44	38	120.00	32.73	27.75
12:20	74	68	180.00	61.92	36.94
12:21	92	86	240.00	82.79	10.32
12:23	85	79	360.00	79.32	0.10
12:25	44	38	480.00	38.03	0.00
12:27	25	19	600.00	17.82	1.39
12:29	46	40	720.00	39.09	0.82
12:31	73	67	840.00	66.79	0.04
12:33	71	65	960.00	65.44	0.19
12:35	49	43	1080.00	42.90	0.01
12:37	38	32	1200.00	31.45	0.30
12:39	49	43	1320.00	42.82	0.03
12:41	64	58	1440.00	58.15	0.02
12:43	64	58	1560.00	57.70	0.09
12:45	52	46	1680.00	45.41	0.35
12:47	46	40	1800.00	38.93	1.15
12:49	51	45	1920.00	45.00	0.00
12:51	58	52	2040.00	53.47	2.17
12:55	54	48	2280.00	46.69	1.71
13:02	57	51	2700.00	51.68	0.46
13:04	56	50	2820.00	49.31	0.47
13:08	51	45	3060.00	45.76	0.58
13:12	54	48	3300.00	50.02	4.06
13:14	54	48	3420.00	48.76	0.76
13:16	53	47	3540.00	46.83	-0.17
13:19	53	47	3720.00	47.43	0.43
13:20	53	47	3780.00	48.23	1.23

Bolek Wyslowch Fall Term 1993 8.01



**B5****THE CAVENDISH EXPERIMENT****B5****DYNAMICS - Gravitational Forces**

$$r = 4.65 \text{ cm}$$

$$m = 1.5 \text{ kg}$$

$$m = 0.015 \text{ kg}$$

$$l = 10 \text{ cm}$$

$$L = 19.7 \text{ m}$$

$$\Delta s = L\theta$$

$$k = 8.5 \times 10^{-9} \text{ N}\cdot\text{m}/\text{rad}$$

$$T \sim 10 \text{ min}$$

$$\Delta s = \frac{4lLGM}{kr^2}$$

$$= \frac{4 \times 0.10 \times L \times 6.672 \times 10^{-11} \times 0.015 \times 1.5}{8.5 \times 10^{-9} \times (.0465)^2}$$

$$\Delta s = 0.0327L \text{ (m)}$$

$$(\Delta s)_{th} = 64 \text{ cm}$$

$$(\Delta s)_{exp} = 88.5 \text{ cm}$$



## Cavendish Exp.

B5

## Procedure:

Release small lead balls by unscrewing the two holders underneath them. Level lens bench so that the wire of the torsional pendulum does not hit anything. Place the large lead balls on their supports and make sure the wire still does not hit anything. Reflect the laser light off the mirror so that the reflected beam lies on the opposite wall of the lecture hall. Disturb the pendulum so that the small balls oscillate at full amplitude, i.e., so that they gently hit the glass wall on either side of the enclosure. Record that full swing amplitude on the opposite wall by using tape markers. Next, find the center of these two marks on the wall and mark it with a strip of color tape.

The next step is to try to adjust the pendulum, with the large lead balls in the center position, so that its zero point lies as close as possible to the center of the extrema marked earlier. In order to ~~accelerate~~ accelerate the dampening of the pendulum, one can use the small horseshoe magnet to repel the small lead balls in the desired direction. The period of the pendulum is 10 mins. When the pendulum is swinging freely (no magnets) the time between each half-cycle, from one extremum to the other, is very close to 5 min. This can be used to guess when the pendulum will reverse its direction and, therefore, will help in marking the turning points.

→



# Cavendish Exp.

B5

## Procedure (Cont.)

When the pendulum has come to rest, mark the new equilibrium position. This will be the zero for the experiment. Next, turn the lead balls all the way to one side, so that they are (almost) touching the glass wall of the enclosure. This will set the pendulum moving in one direction. Repeat the dampening procedure described earlier to find the new equilibrium position. The pendulum is now ready for class.

At the beginning of class, the lecturer will move the large lead balls completely to the other side and, at the end of the lecture period, will mark the final equilibrium position. He will then measure the distance between the two rest positions corresponding to the large lead balls being one way ~~and~~ on the other and use that to determine the value of  $G$ .



## Cavendish Exp.

B5

## Equipment Needed.

- Cavendish Apparatus
- Lens bench w/ adjustable legs (screws) so that it can be levelled.
- 1 lens holder
- 1 Table clamp
- 1 short rod
- 1 90° clamp
- Laser
- many lead bricks to stabilize the cart
- small horseshoe magnet to dampen rotational pendulum
- 2 meter stick, color tape, duct tape.
- Stopwatch
- Set Up:

Set up Cavendish apparatus and laser on white cart at one end of lecture hall. Direct reflected beam of laser light to opposite wall of lecture hall.



## Cavendish Exp.

B5

$$r = 4.65 \text{ cm} \quad (\text{balls center to center})$$

$$M = 1.5 \text{ kg}$$

$$m = 0.015 \text{ kg}$$

$$l = 10 \text{ cm}$$

$$L = 19.7 \text{ m}$$

$$\Delta s = L \theta$$

$$K = 85 \times 10^{-9} \text{ N-m/rad}$$

$$T \sim 10 \text{ min}$$

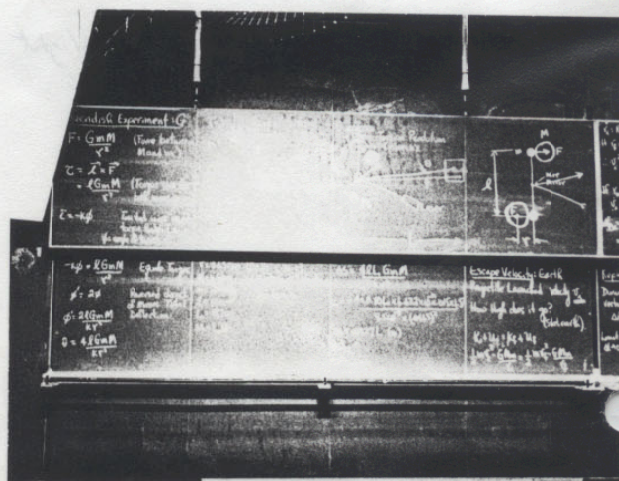
$$\Delta s = \frac{4lLGM}{Kr^2}$$

$$= \frac{4 \times 0.10 \times L \times 6.672 \times 10^{-11} \times 0.015 \times 1.5}{85 \times 10^{-9} \times (.0465)^2}$$

$$\Delta s = 0.0327 L \quad (\text{m})$$

$$(\Delta s)_{Th} = 0.64 \text{ cm}$$

$$(\Delta s)_{exp} = 88.5 \text{ cm}$$





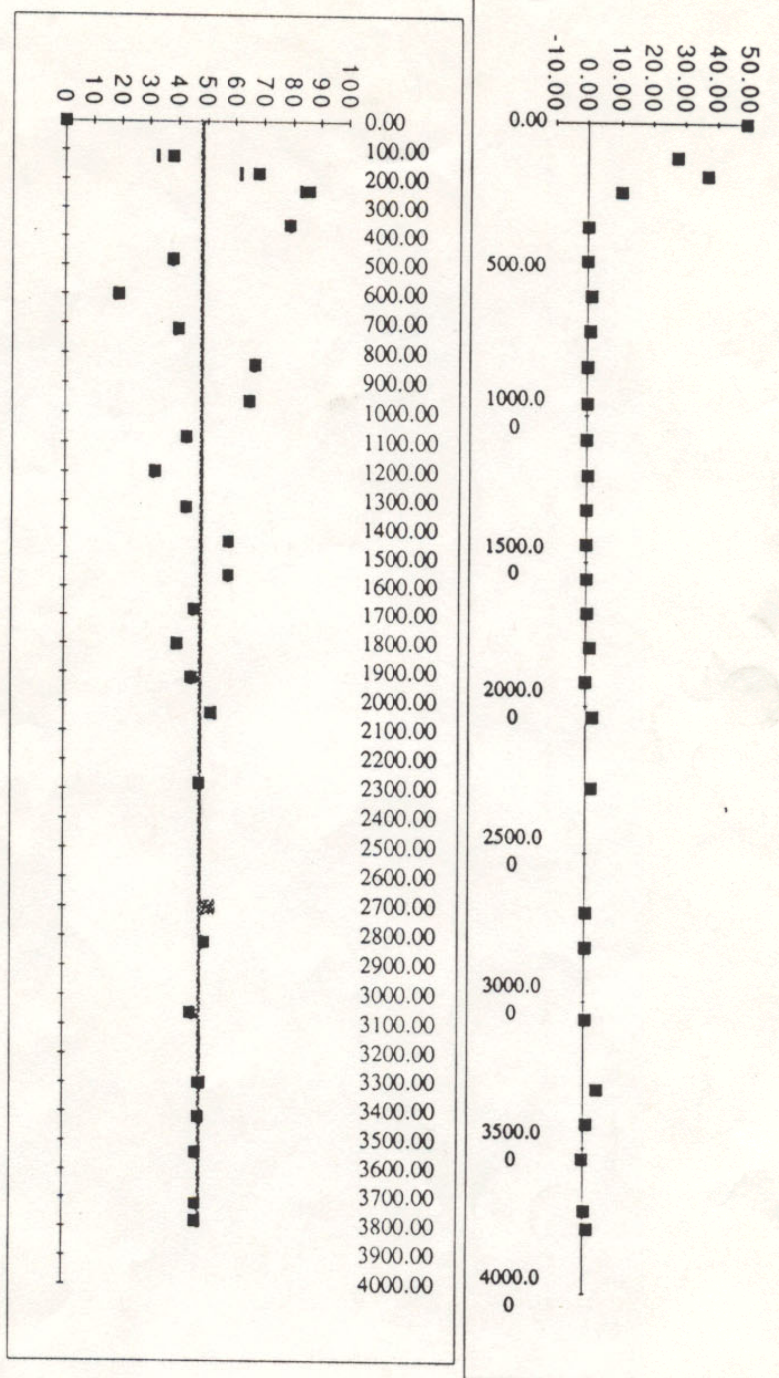
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# CAVENDISH

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Class			
Minutes		45	
Seconds	2700	51.21	
			Difference

3.21





## Gravitation Torsion Balance

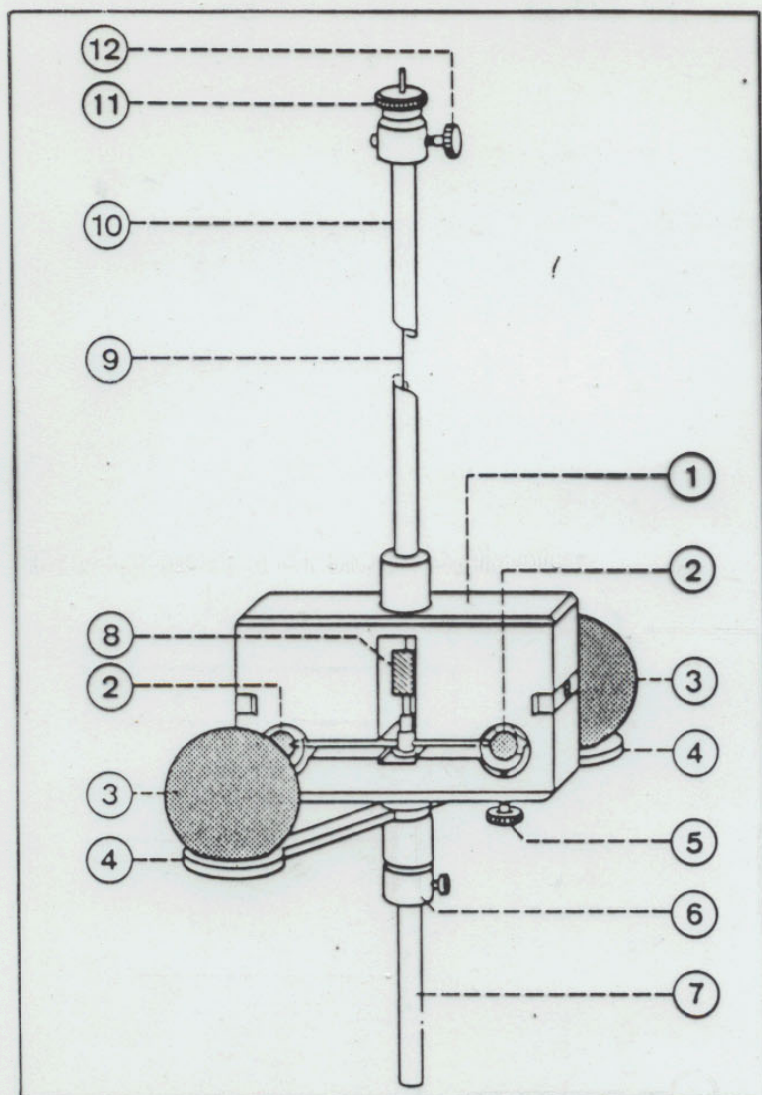


Fig. 1 Standard equipment of gravitation torsion balance (332 10)