1 Arrays and Lists

1.1 Arrays

- **Arrays** are simply matrices generalized to $n$ dimensions where $n$ is any natural number.

- Arrays can be created either by (1) assigning `dim` attributes to an existing vector/matrix or (2) using the `array()` function.

- An $n$-dimensional array can be indexed via `[ , , , ... ]` where there must be $n$ indices separated by commas.

```r
> A <- 1:30
> dim(A) <- c(5,3,2) # turns A into a three-dimensional, 5-by-3-by-2 array
> A <- array(1:30, dim=c(5,3,2)) # equivalent
> A

, , 1

[,1] [,2] [,3]
[1,]  1  6 11
[2,]  2  7 12
[3,]  3  8 13
[4,]  4  9 14
[5,]  5 10 15

, , 2

[,1] [,2] [,3]
[1,] 16 21 26
[2,] 17 22 27
[3,] 18 23 28
[4,] 19 24 29
[5,] 20 25 30

> A[,,2] # returns the second chunk of A
```
A[4,3,1] # returns the (4,3,1) element

[1] 14

- A useful function for arrays (and also for matrices) is \( \text{apply}(x, M, \text{FUN}) \), which invokes another function \( \text{FUN} \) on an array \( x \) along coordinates specified by \( M \).

> apply(A, 3, sum) # returns the sum for each chunk (3rd dimension)

[1] 120 345

> apply(A, 1, mean) # returns the mean of each row

[1] 13.5 14.5 15.5 16.5 17.5

> apply(A, c(2,3), min)

   [,1] [,2]
[1,]  1 16
[2,]  6 21
[3,] 11 26

1.2 Lists

- Lists are one-dimensional data objects composed of possibly heterogeneous elements.

- The elements of a list may themselves be complex data objects, such as lists.

- Each element of a list usually has its own name and can be accessed via the \$ operator.

- The list() function creates a list, whose elements can be given names with arguments of the following form: \text{name} = \text{element}.

> mylist <- list(country = c("Canada","Mexico","USA"), year = 2007, + sales = c(3.2, 4.6, 8.3, 9.9, 2.1, 5), arr = A)

> mylist # shows everything in the list

$country
[1] "Canada" "Mexico" "USA"

$year

$sales
Many functions (e.g. \texttt{lm()}, \texttt{t.test()}) return outputs that have the list format (though their classes are often different, proprietary ones).

\begin{verbatim}
> x <- c(0,1,3,8)
> y <- c(-2,4,3,5)
> fit <- lm(y ~ x)  # The result has a structure similar to a list
> fit$coef

(Intercept)     x
0.6842105 0.6052632

> fit$resid

  1     2     3     4
-2.6842105  2.7105263  0.5000000 -0.5263158
\end{verbatim}

- The \texttt{lapply(x, FUN)} function applies another function \texttt{FUN} on each element in the list \texttt{x}.
- The \texttt{sapply(x, FUN)} function does the same, but the results are suppressed into a vector.

\begin{verbatim}
> lapply(mylist, mean)  # Apply \texttt{mean()} to each element in \texttt{mylist}

$country
[1] NA
\end{verbatim}
2 Functions for Programming

2.1 The function() Function

- You can create your own function with the function() function.
- To define a function, the following syntax is used:

```r
younametest <- function(arg1, arg2){
    body...
}
```

This creates a function named `younametest` which takes `arg1` and `arg2` as its arguments and execute the commands written between the brackets (`body...`).

- A function will return the values specified by the `return()` command within the body. If the body contains no `return`, the last evaluated expression will become the output of the function.
- Arguments can be given default values using the `arg = xxx` specification in the definition.

- Example: Create a function which computes the average of numbers in a numeric vector after omitting the highest and lowest values (which would be useful for figure skating judges).

```r
> mymean <- function(x){
+   highest <- max(x)
+   lowest <- min(x)
+   (sum(x) - highest - lowest) / (length(x) - 2)
+ }
> scores <- c(5.8, 5.9, 5.3, 5.6, 5.4, 5.9, 5.4, 5.2, 5.5, 5.9, 5.8, 4.9)
> mymean(scores)
```

[1] 5.58
• Example Continued: In response to a judging controversy, the International Skating Union decided to use the following (hypothetical) scoring scheme: twelve judges individually award values ranging between 0 and 6, and these values are averaged by randomly selecting nine judges, discarding the highest and lowest values, and averaging the remaining seven.

Let’s create another function for this new scoring system.

```r
> newrule <- function(x){
+   x <- sample(x, 9, replace=F)
+   highest <- max(x)
+   lowest <- min(x)
+   (sum(x) - highest - lowest) / 7
+ }
> newrule(scores)
[1] 5.571429
```

• Now, suppose you’ve found out that the ISU is reconsidering the scoring scheme again. In particular, they want to change the number of values discarded as well as the number of judges sampled. Let’s modify our function so it can take various values for these elements. Also, set the default values of these arguments to the ones currently used.

```r
> newrule2 <- function(x, nsample = 9, ndiscard = 1){
+   x <- sample(x, nsample, replace=F)
+   x <- sort(x) # sort x in the ascending order
+   sum.used <- sum(x[-c(1:ndiscard, (length(x)-ndiscard+1):length(x))])
+   njudges.used <- length(x) - 2*ndiscard
+   sum.used / njudges.used
+ }
> newrule2(scores)
[1] 5.671429

> newrule2(scores, 7, 2) # sample 7 judges, discard the 2 highest & 2 lowest
[1] 5.6
```

2.2 && and ||

• && and || are logical operators indicating “and” and “or”, respectively, and work in the same way as the & and | operators do, except:

1. & and | operate component-wise on vectors, whereas && and || operate on scalar (i.e. single-valued) logical expressions.
2. && evaluates the right-hand expression only if the left-hand one is true, and || only if it is false.

• && (||) is convenient when your right-hand expression will lead to an error if the left-hand expression is false (true).

```r
> x <- "apple" # x is a character string
```

5
> is.numeric(x) & sqrt(x) > 1 # generates an error

> is.numeric(x) && sqrt(x) > 1 # works

[1] FALSE

2.3 The while() Loop

- Instead of the for loop function, the while() and repeat() functions can be also used to perform looping.
- The while() function takes the following syntax:

```
while (condition){
    blah
...
}
```

where the code `blah ...` is repeated as long as the `condition` is met.
- The while() function is especially useful when you do not know ahead of time how many times you will need to repeat the commands.
- Example: Geometric Random Variable. The following code counts how many coin flips are performed until the first “head” occurs.

```
> coin <- "tail" # initialize the coin indicator
> count <- 0 # initialize the counter
> while (coin == "tail"){
+    coin <- sample(c("head","tail"), 1)
+    count <- count + 1
+ }
> count

[1] 1
```

2.4 The repeat Loop

- The repeat function repeats the commands in the body infinitely until exited by the break statement.
- The break statement is often used with conditional statements, such as if.
- The next statement jumps to the next iteration, and also combined with conditional statements within a loop.
- The random variable in the previous example can also be obtained with the repeat() function:
> coin <- "tail"
> count <- 0
> repeat{
+   coin <- sample(c("head","tail"), 1)
+   count <- count + 1
+   if (coin == "head") break
+ }
> count

[1] 2

2.5 Halting Programs via stop()

- The `stop("blah")` function halts execution of a function or script and spits the error message `blah`.
- This is often used when you want to stop your program if something goes wrong.
- Example: We now modify the `newrule2()` function so that it recognizes a silly calculation.

> newrule2(scores, 5, 3) # sample 5 judges, discard...six of them?

[1] 0

> newrule2 <- function(x, nsample = 9, ndiscard = 1){ # Let's modify
+   if (nsample <= 2 * ndiscard) stop("Too few judges sampled!") # added
+   # the rest is the same as before
+   x <- sample(x, nsample, replace=F)
+   x <- sort(x) # sort x in the ascending order
+   sum.used <- sum(x[-c(1:ndiscard, (length(x)-ndiscard+1):length(x))])
+   njudges.used <- length(x) - 2*ndiscard
+   sum.used / njudges.used
+ }
> newrule2(scores, 5, 3) # now spits an error message

2.6 Executing Commands from a File

- Once you have written your program, it is often a good idea to save it as an R script file. The standard extension for R scripts is ".R".
- R scripts in the working directory can be executed anytime by typing `source("yourprogram.R")`.
- This is especially convenient when you have a very long program, or when you want to use your function in more than one program.
- Example: Download `newrule2.R` from Blackboard, which contains the skating scoring function we have created and additional commands. Try running it via the `source()` command. What happened?