

**10.213 Chemical Engineering Thermodynamics  
Spring 2002**

**Problem Set I**

Due Wednesday, April 24, 2002 in lecture

Problem 29

The Redlich-Kwong equation can be written as:

$$P = \frac{RT}{V-b} - \frac{a}{T^{0.5}V(V+b)} \text{ and manipulated to provide that}$$

$$Z = 1 + \frac{b}{V-b} - \frac{a}{RT^{1.5}(V+b)}, \text{ where } a = \frac{0.42748R^2T_c^{2.5}}{P_c} \text{ and } b = \frac{0.08664RT_c}{P_c}.$$

- a) Show that  $\ln \phi = -\ln\left(1 - \frac{b}{V}\right) - \frac{a \ln\left(1 + \frac{b}{V}\right)}{bRT^{1.5}} + Z - 1 - \ln Z$ . As a hint, consider the use of either

$$\frac{G^R}{RT} = \int_0^P (Z-1) \frac{dP}{P} \text{ (eq 6.46) or } \frac{G^R}{RT} = \int_0^P (Z-1) \frac{d\rho}{\rho} + Z - 1 - \ln Z \text{ (eq 6.57) where } \rho = \frac{1}{V}.$$

- b) Determine the fugacity of *n*-butane gas at 500 K and 50 bar using the equation derived in a).  
 c) Determine the fugacity of *n*-butane gas at 500 K and 50 bar using the values of  $H^R = -4.51$  kJ/mol and  $S^R = -6.55$  J/mol-K determined in Example 6.4 for *n*-butane under these conditions (pp 215-216 in SVN&A).  
 d) Determine the fugacity of *n*-butane gas at 500 K and 50 bar using generalized correlations.

Problem 30

The excess Gibbs free energy of a binary liquid mixture at T and P is given by:

$$\frac{G^E}{RT} = (-2.6x_1 - 1.8x_2)x_1x_2$$

- a) Find expression of  $\ln \gamma_1$  and  $\ln \gamma_2$  at T and P.  
 b) Show that when these expressions are combined in accord with Eq 11.95 that the given equation for  $G^E/RT$  is recovered.  
 c) Show that the expressions in a) satisfy the Gibbs-Duhem equation.  
 d) Show that  $(d \ln \gamma_1/dx_1)_{x_1=1} = (d \ln \gamma_2/dx_1)_{x_1=0} = 0$ .  
 e) Plot  $G^E/RT$ ,  $\ln \gamma_1$ , and  $\ln \gamma_2$  as calculated by the given equation for  $G^E/RT$  and by the equations developed in a) vs.  $x_1$ . Label points  $\ln \gamma_1^\infty$  and  $\ln \gamma_2^\infty$  and show their values.  
 f) Plot  $\Delta G/RT$  vs  $x_1$ .  
 g) Does  $\sum(x_i d \gamma_i) = 0$ ? Should it? Hint: consider the definition of the Gibbs-Duhem equation.

### Problem 31

The data tabulated below are experimental values of  $H^E$  for binary liquid mixtures of 1,2-dichloroethane (1) and dimethyl carbonate (2) at 313.15 K and 1 atm

(from R. Francesconi et al. *Int. DATA Ser. A*, Vol. 25, No. 3, p. 225, 1997).

$x_1$	$H^E$ (J/mol)	$x_1$	$H^E$ (J/mol)
0.0426	-23.3	0.5163	-204.2
0.0817	-45.7	0.6156	-191.7
0.1177	-66.5	0.6810	-174.1
0.1510	-86.6	0.7621	-141.0
0.2107	-118.2	0.8181	-116.8
0.2624	-144.6	0.8650	-85.6
0.3472	-176.6	0.9276	-43.5
0.4158	-195.7	0.9624	-22.6

- a) Determine from the data numerical values of the parameters a, b, and c in the correlating equation:

$$H^E = x_1 x_2 (a + b x_1 + c x_1^2)$$

(Hint: consider plotting  $H^E/(x_1 x_2)$  vs.  $x_1$  as a way to determine values of a, b, and c.)

- b) Determine the minimum value of  $H^E$  from the results in part a). At what value of  $x_1$  does this occur?
- c) Determine expressions for  $\bar{H}_1^E$  and  $\bar{H}_2^E$  from the results of part a). Prepare a plot of  $\bar{H}_1^E$  and  $\bar{H}_2^E$  vs.  $x_1$  and discuss its features.
- d) Plot  $\Delta H$  vs.  $x_1$ . What is the relationship between  $\Delta H$  and  $H^E$ ?
- e) Determine values of  $H^E$ ,  $\bar{H}_1^E$ , and  $\bar{H}_2^E$  for  $x_1 = 0$  and  $x_1 = 1$ . For cases where  $H^E = 0$  and either  $\bar{H}_1^E$  or  $\bar{H}_2^E \neq 0$ , explain how  $H^E$  can equal 0 while either  $\bar{H}_1^E$  or  $\bar{H}_2^E$  do not.

### Problem 32.

Steam undergoes an isothermal change in state from 9000 kPa and 400 °C to 300 kPa and 400 °C. Determine *using steam tables*, the ratio of the fugacity in the final state to that in the initial state. (Hint: this question requires only a little bit of calculation, so think first about how to connect fugacities (or rather, fugacity ratios) given the type of data in a steam table.)