## Character Tables

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## Outline

(1) Introduction to Character Tables
(2) The Character Table for $\mathrm{C}_{2 v}$

## What Makes Up a Character Table

Character tables contain information about how functions transform in response to the operations of the group

Five parts of a character table
(1) At the upper left is the symbol for the point group
(2) The top row shows the operations of the point group, organized into classes

B The left column gives the Mulliken symbols for each of the irreducible representations
(4) The rows at the center of the table give the characters of the irreducible representations
(5) Listed at right are certain functions, showing the irreducible representation for which the function can serve as a basis

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## The $C_{2 v}$ Character Table

| $C_{2 v}$ | $E$ | $C_{2}$ | $\sigma_{v}(x z)$ | $\sigma_{v}^{\prime}(y z)$ |  |  |
| :--- | ---: | ---: | ---: | ---: | :--- | :--- |
| $A_{1}$ | 1 | 1 | 1 | 1 | $z$ | $x^{2}, y^{2}, z^{2}$ |
| $A_{2}$ | 1 | 1 | -1 | -1 | $R_{z}$ | $x y$ |
| $B_{1}$ | 1 | -1 | 1 | -1 | $x, R_{y}$ | $x z$ |
| $B_{2}$ | 1 | -1 | -1 | 1 | $y, R_{x}$ | $y z$ |

## Transformation Properties of an $s$ Orbital in $C_{2 v}$ What happens when the $E$ operation is applied?



## Transformation Properties of an $s$ Orbital in $C_{2 v}$

## What happens when the $E$ operation is applied?



- The $E$ operation is a rotation by $360^{\circ}$ about an arbitrary axis


## Transformation Properties of an $s$ Orbital in $C_{2 v}$ The $E$ operation returns the original configuration of the $s$ orbital



- The result of this corresponds to a character of 1


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## Transformation Properties of an $s$ Orbital in $C_{2 v}$ <br> What happens when the $C_{2}$ operation is applied?



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## Transformation Properties of an $s$ Orbital in $C_{2 v}$

## What happens when the $C_{2}$ operation is applied?



- The $C_{2}$ operation is a rotation by $180^{\circ}$ about the $z$ axis


## Transformation Properties of an $s$ Orbital in $C_{2 v}$

 The $C_{2}$ operation returns the original configuration of the $s$ orbital

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## Transformation Properties of an $s$ Orbital in $C_{2 v}$ What happens when the $\sigma_{v}(x z)$ operation is applied?



- The $\sigma_{v}(x z)$ operation is a reflection through the $x z$ plane


## Transformation Properties of an $s$ Orbital in $C_{2 v}$

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## Transformation Properties of an $s$ Orbital in $C_{2 v}$ What happens when the $\sigma_{v}^{\prime}(y z)$ operation is applied?



- The $\sigma_{v}^{\prime}(y z)$ operation is a reflection through the $y z$ plane


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## Transformation Properties of an s Orbital <br> These observations pertain to any central-atom sorbital in any point group

- Consider an s orbital located on a central atom
- An example of a central atom is O in the case of water, or N in the case of ammonia
- Carrying out any operation on a central atom sorbital returns the $s$ orbital in its original configuration
- The central-atom $s$ orbital "belongs to" or "serves as a basis for" the totally symmetric $\left(A_{1}\right)$ irreducible representation
- All the characters of the totally symmetric irreducible representation are 1
- The totally symmetric irreducible representation is always singly degenerate


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## Transformation Properties of a $p_{x}$ Orbital in $C_{2 v}$

 What happens when the $E$ operation is applied?

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- The $E$ operation is a rotation by $360^{\circ}$ about an arbitrary axis


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- The $C_{2}$ operation is a rotation by $180^{\circ}$ about the $z$ axis


## Transformation Properties of a $p_{x}$ Orbital in $C_{2 v}$ The $C_{2}$ operation inverts the phase of the $p_{x}$ orbital



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## Transformation Properties of a $p_{x}$ Orbital in $C_{2 v}$ The $C_{2}$ operation inverts the phase of the $p_{x}$ orbital



- The result of this corresponds to a character of -1


## Transformation Properties of a $p_{x}$ Orbital in $C_{2 v}$

## What happens when the $\sigma_{v}(x z)$ operation is applied?



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## Transformation Properties of a $p_{x}$ Orbital in $C_{2 v}$

## What happens when the $\sigma_{v}(x z)$ operation is applied?



- The $\sigma_{v}(x z)$ operation is a reflection through the $x z$ plane


## Transformation Properties of a $p_{x}$ Orbital in $C_{2 v}$

 The $\sigma_{v}(x z)$ operation does nothing to the phase of the $p_{x}$ orbital

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- The result of this corresponds to a character of 1


## Transformation Properties of a $p_{x}$ Orbital in $C_{2 v}$

 What happens when the $\sigma_{v}^{\prime}(y z)$ operation is applied?

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 What happens when the $\sigma_{v}^{\prime}(y z)$ operation is applied?

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## Transformation Properties of a $p_{x}$ Orbital in $C_{2 v}$

 The $\sigma_{v}^{\prime}(y z)$ operation inverts the phase of the $p_{x}$ orbital

- The result of this corresponds to a character of -1


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## A $p_{x}$ Orbital has $B_{1}$ Symmetry in $C_{2 v}$

- We carried out the operations of $C_{2 v}$ on a central-atom $p_{x}$ orbital
- This generated the following row of characters: $1,-1,1,-1$
- This row of characters in the $C_{2 v}$ character table is labeled $B_{1}$
- Any orbital having these transformation properties in $C_{2 v}$ is said to have $B_{1}$ symmetry


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- The $E$ operation is a rotation by $360^{\circ}$ about an arbitrary axis


## Transformation Properties of a $p_{y}$ Orbital in $C_{2 v}$

The $E$ operation returns the original configuration of the $p_{y}$ orbital


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## What happens when the $E$ operation is applied?



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- The $\sigma_{v}(x z)$ operation is a reflection through the $x z$ plane


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## Symmetry Restrictions on Molecular Orbitals (MOs)

- Only orbitals of the same symmetry may mix
- "Orbitals of the same symmetry" belong to the same irreducible representation
- For the $C_{2 v}$ water molecule, the oxygen $s$ and $p_{z}$ atomic orbitals may contribute to any molecular orbital of $A_{1}$ symmetry, but $p_{x}$ and $p_{y}$ may not
- Any valid molecular orbital must transform according to one of the irreducible representations of the molecular point group


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| :--- | ---: | ---: | ---: | ---: | :--- | :--- |
| $A_{1}$ | 1 | 1 | 1 | 1 | $z$ | $x^{2}, y^{2}, z^{2}$ |
| $A_{2}$ | 1 | 1 | -1 | -1 | $R_{z}$ | $x y$ |
| $B_{1}$ | 1 | -1 | 1 | -1 | $x, R_{y}$ | $x z$ |
| $B_{2}$ | 1 | -1 | -1 | 1 | $y, R_{x}$ | $y z$ |

## The Molecular Orbitals of Water

- Notice that the water HOMO is a pure oxygen $p_{x}$ orbital of $B_{1}$ symmetry
- The hydrogen atoms with their $1 s$ valence orbitals lie in the nodal plane of the oxygen $p_{x}$ orbital
- The two hydrogen $1 s$ orbitals give rise to linear combinations of $A_{1}$ and $B_{2}$ symmetry
- The $\mathrm{O}-\mathrm{H}$ bonding molecular orbitals must likewise be of $A_{1}$ and $B_{2}$ symmetry
- Given that all the irreducible representations of $C_{2 v}$ are singly degenerate, so must be all the MOs of the water molecule
- Click on Link to Water MOs


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- The two hydrogen 1 s orbitals give rise to linear combinations of $A_{1}$ and $B_{2}$ symmetry
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## The Molecular Orbitals of Water

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- Click on Link to Water MOs

