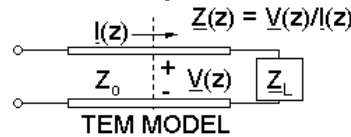
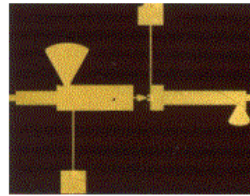


CIRCUIT TRANSFORMATION MAGIC

Printed Microwave Circuits (TEM lines):

- Can contain R's (resistive rectangles)
- Can yield L's and C's (near ω_0)
- Can be resonators for tuning or transformer use
- Can match impedances to maximize power transfer
- Can perform nearly all circuit functions with transistors only
- Has size scale $\sim \lambda/4 \Rightarrow f \gtrsim 1$ GHz



Waveguide Circuits and Systems:

- Can be made lossy
- Can have inductive or capacitive obstacles (L's and C's)
- Can resonate for tuning or transforming
- Can match impedances to maximize power transfer
- Can make circulators (non-reciprocal devices)

Optical Circuits:

Similar to waveguide circuits, but in fibers or free space

L16-1

GAMMA PLANE \leftrightarrow SMITH CHART

TEM Lines:

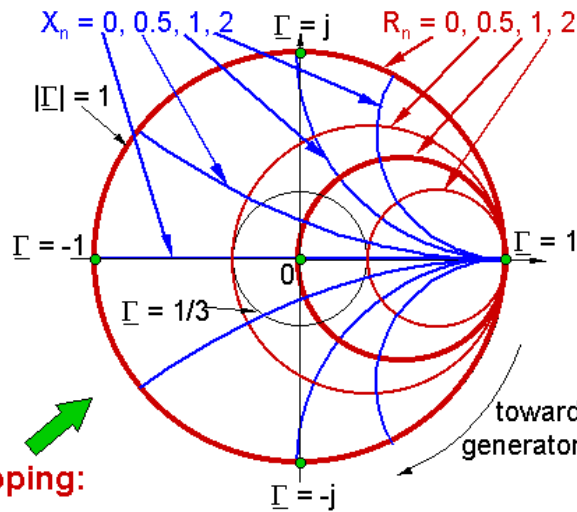
$$\begin{aligned}
 \underline{V}(z) &= \underline{V}_+ e^{-jkz} + \underline{V}_- e^{+jkz} \\
 \underline{I}(z) &= Y_0 [\underline{V}_+ e^{-jkz} - \underline{V}_- e^{+jkz}] \\
 \underline{Z}(z) &= Z_0 (1 + \underline{\Gamma}(z)) / (1 - \underline{\Gamma}(z)) \\
 \underline{\Gamma}(z) &\triangleq (\underline{V}_- / \underline{V}_+) e^{2jkz} = \underline{\Gamma}_L e^{2jkz}
 \end{aligned}$$

$$\underline{Z}_n = \underline{Z}(z) / Z_0 = R_n + jX_n$$

Gamma plane is useful because $\underline{\Gamma}(z) = \underline{\Gamma}_L e^{2jkz}$, which is simply rotation on the plane.

One-to-One Mapping:

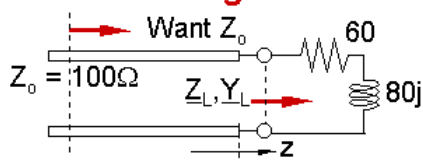
$$\begin{aligned}
 \underline{Z}_n &= (1 + \underline{\Gamma}) / (1 - \underline{\Gamma}) \\
 \underline{\Gamma} &= (\underline{Z}_n - 1) / (\underline{Z}_n + 1)
 \end{aligned}$$



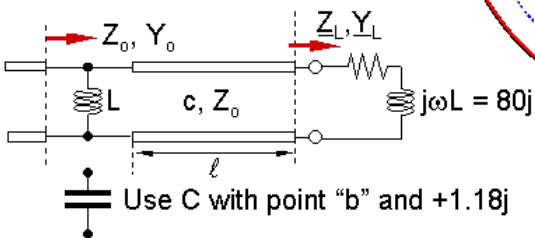
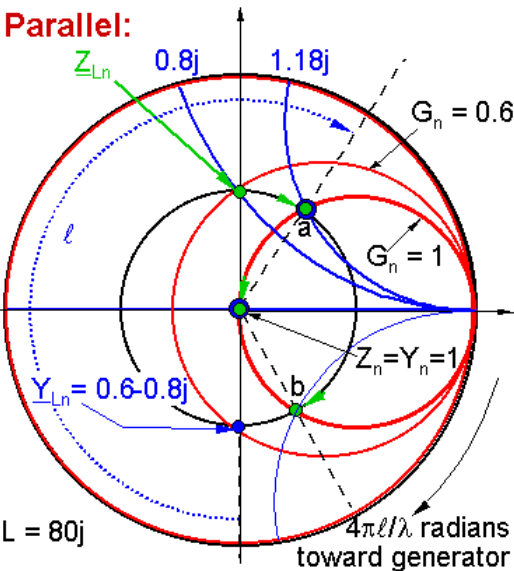
L16-2

MATCHING ADMITTANCES

Reactive Tuning Elements in Parallel:



Find Z_{Ln} on chart, then Y_{Ln} opposite; rotate ℓ to "a" where $G_n = 1$ and add $-1.18j$ admittance to yield $Y_n = Y_0$
 $Y = -1.18jY_0 = 1/j\omega L$
 $\Rightarrow L = Z_0/1.18\omega$



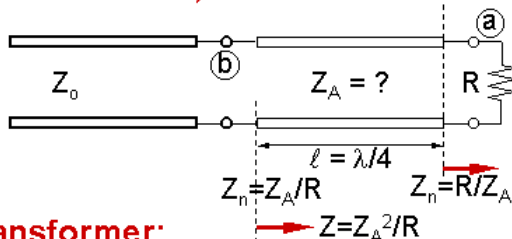
Can match any load!
 (beware resonances)

L16.5

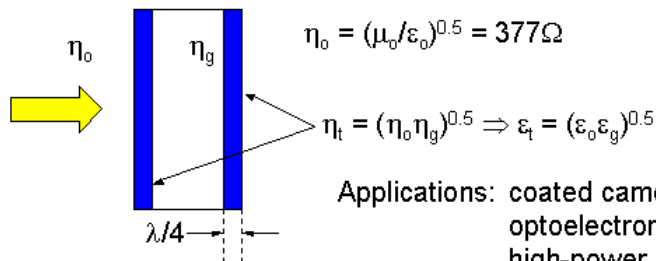
QUARTER-WAVE TRANSFORMER

Matching Real Impedances without L,C:

Let: $\ell = \lambda/4$, then
 Setting: $Z_0 = Z_A^2/R$,
 Yields: $Z_A = (Z_0 R)^{0.5}$



Optical Quarter-Wave Transformer:



$$\eta_0 = (\mu_0/\epsilon_0)^{0.5} = 377\Omega$$

$$\eta_t = (\eta_0 \eta_g)^{0.5} \Rightarrow \epsilon_t = (\epsilon_0 \epsilon_g)^{0.5}$$

Applications: coated camera lenses, glasses, optoelectronic components, high-power lasers, etc.

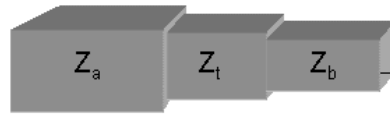
Invented by Prof. Smakula at Leitz

L16.6

MORE QUARTER-WAVE TRANSFORMERS

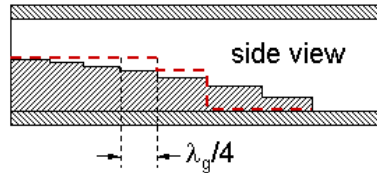
Waveguide Transformers:

Z_0 varies with waveguide sizes
 $Z_t = (Z_a Z_b)^{0.5}$



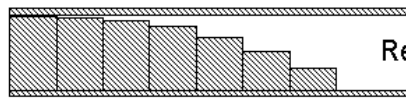
Multi-step Transitions:

Waveguides can have N multiple steps spaced $\lambda/4$ apart



Example, 1:256 Transformer:

For $N = 2$, $Z_a = 1$ ohm, $Z_b = 256$ ohms, and $Z_t = (1 \times 256)^{0.5} = 16$ ohms
 For $N = 4$, $Z_{t1} = (1 \times 16)^{0.5} = 4$ ohms, $Z_{t2} = 16$, $Z_{t3} = (16 \times 256)^{0.5} = 64$
 For $N = 8$, $Z_{t1} = (1 \times 4)^{0.5} = 2$, $Z_{t2} = 4$, (rest are 8, 16, 32, 64, and 128 ohms)



Result is exponential series

L16-7

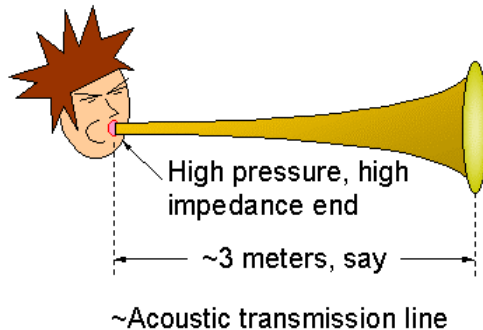
EXPONENTIAL TRANSITIONS AND HORNS

Acoustic Transformers, Exponential Horns:

We use $N \cong 4L/\lambda_g$ sections, where L is the length of the transformer
 In the limit we can smooth the steps to yield an exponential shape

Acoustic Examples:

French horn, trumpet, loudspeakers:



low-pressure,
low-impedance end

$$N = 8 \Rightarrow \lambda_{\max} = 4L/N = 4 \cdot 3/8 = 1.5 \text{ meters}$$

$$f_{\min} = c_s/\lambda = \sim 300/(1.5) = 200 \text{ Hz}$$

L16-8