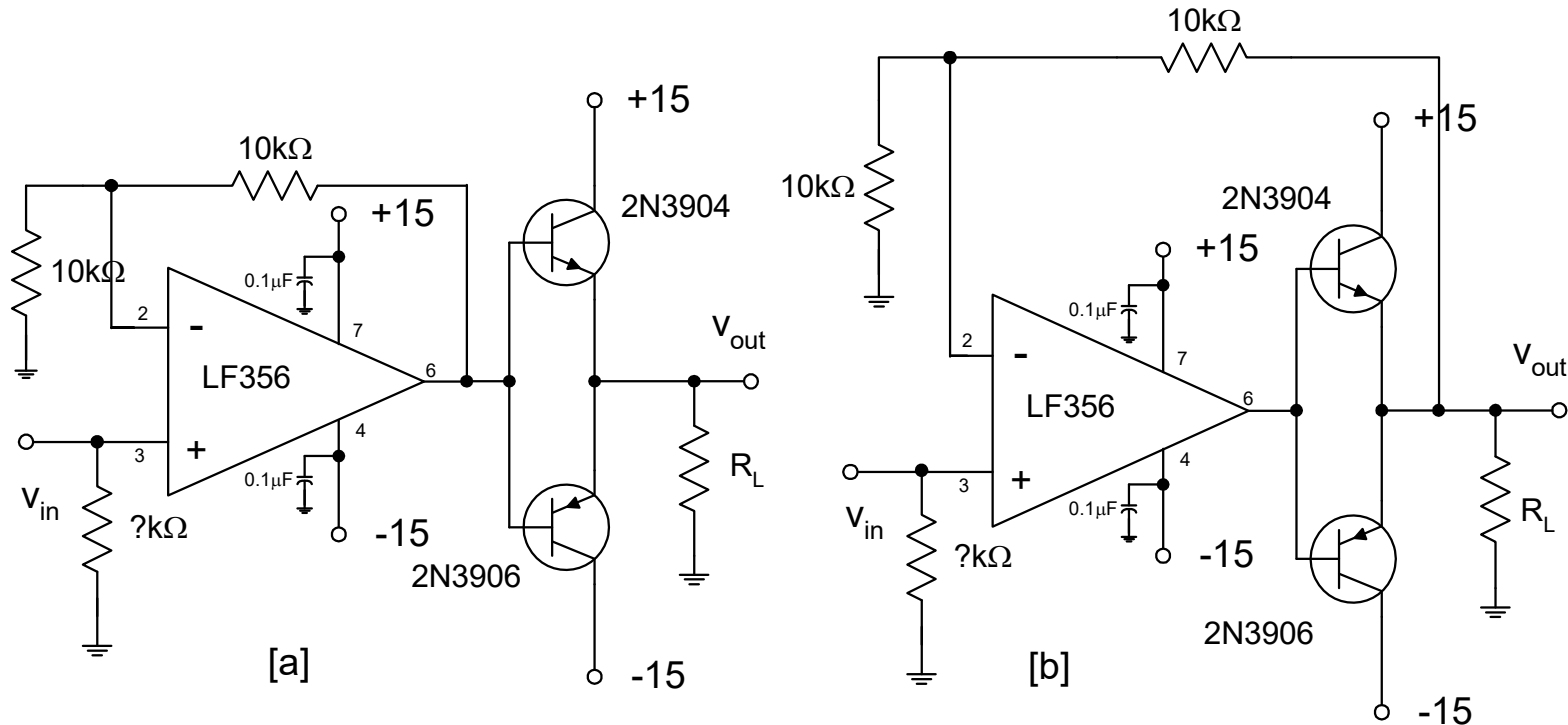




- Amplifiers: Class A, B, AB, D
- Op-amp Application: ECG

Acknowledgements:  
Ron Roscoe

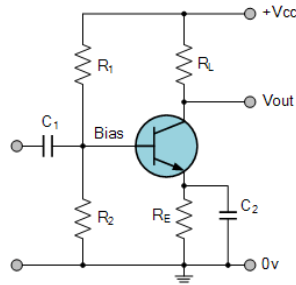
# Crossover Distortion (hole)



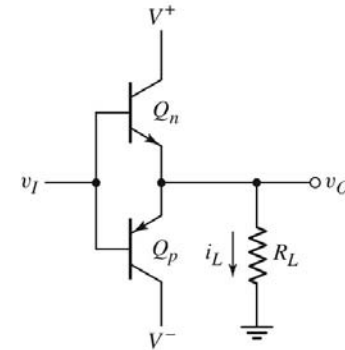
Why is [b] better?

# Amplifier Classification

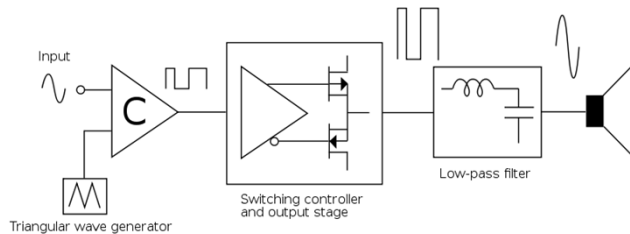
- Class A: output transistors are biased with a quiescent current – common emitter



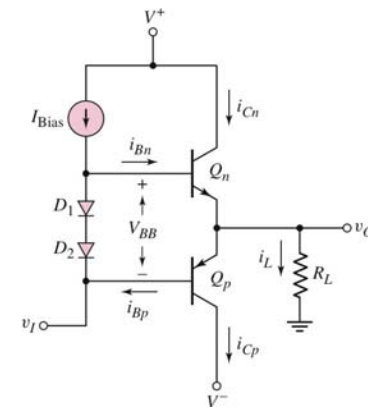
- Class B: output transistors conduct for only one half of each sine wave input - push pull



- Class D: output transistors are switched on/off with PWM\*

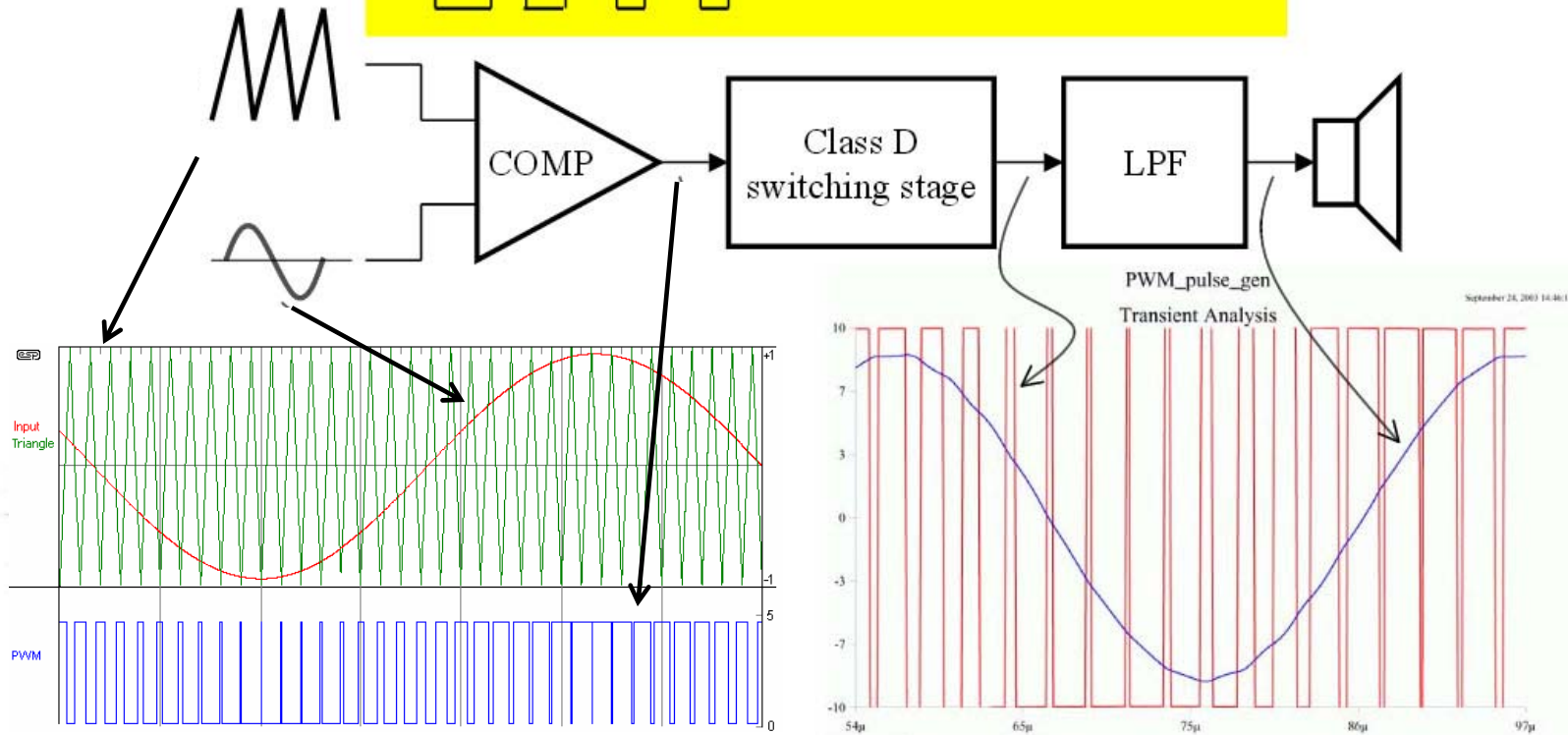
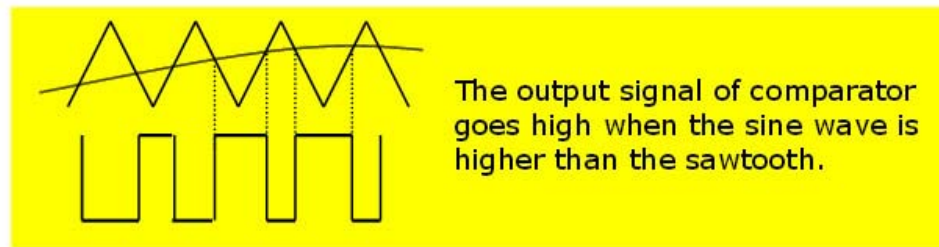


- Class AB: output transistors are biased at a small quiescent current

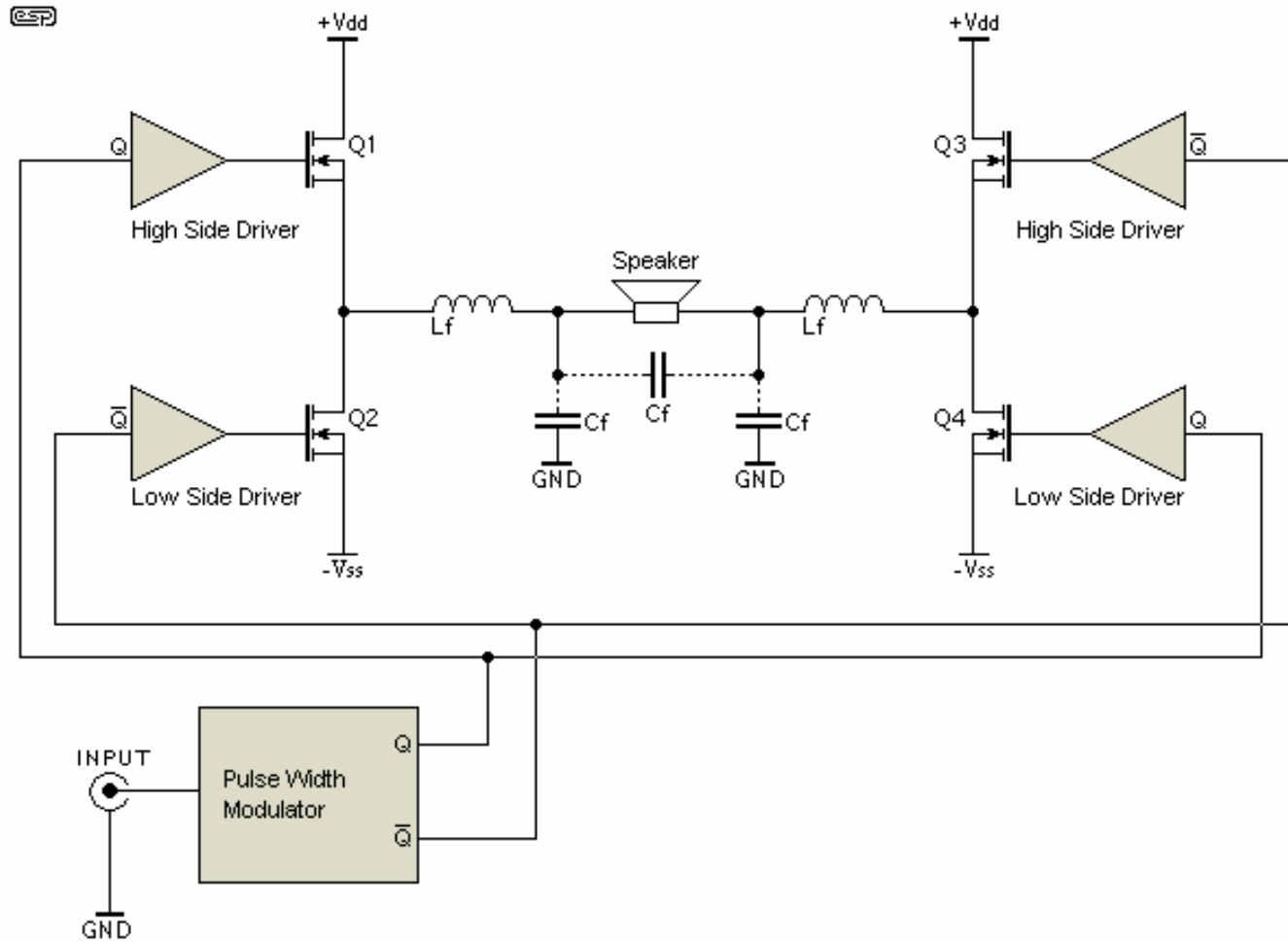


\* [http://upload.wikimedia.org/wikipedia/commons/thumb/4/4c/Pwm\\_amp.svg/800px-Pwm\\_amp.svg.png](http://upload.wikimedia.org/wikipedia/commons/thumb/4/4c/Pwm_amp.svg/800px-Pwm_amp.svg.png)

## Basic PWM Operation

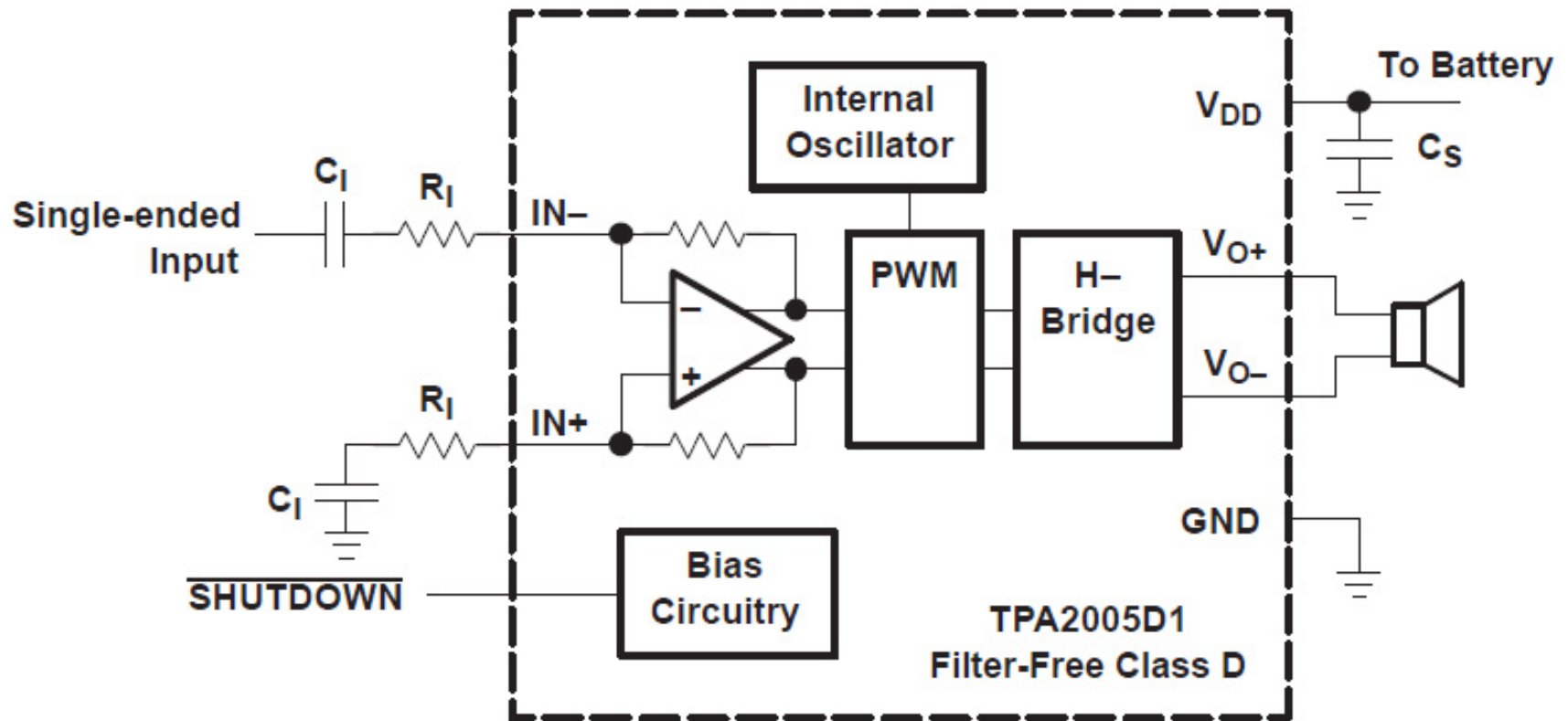


# Class D Output Stage\*

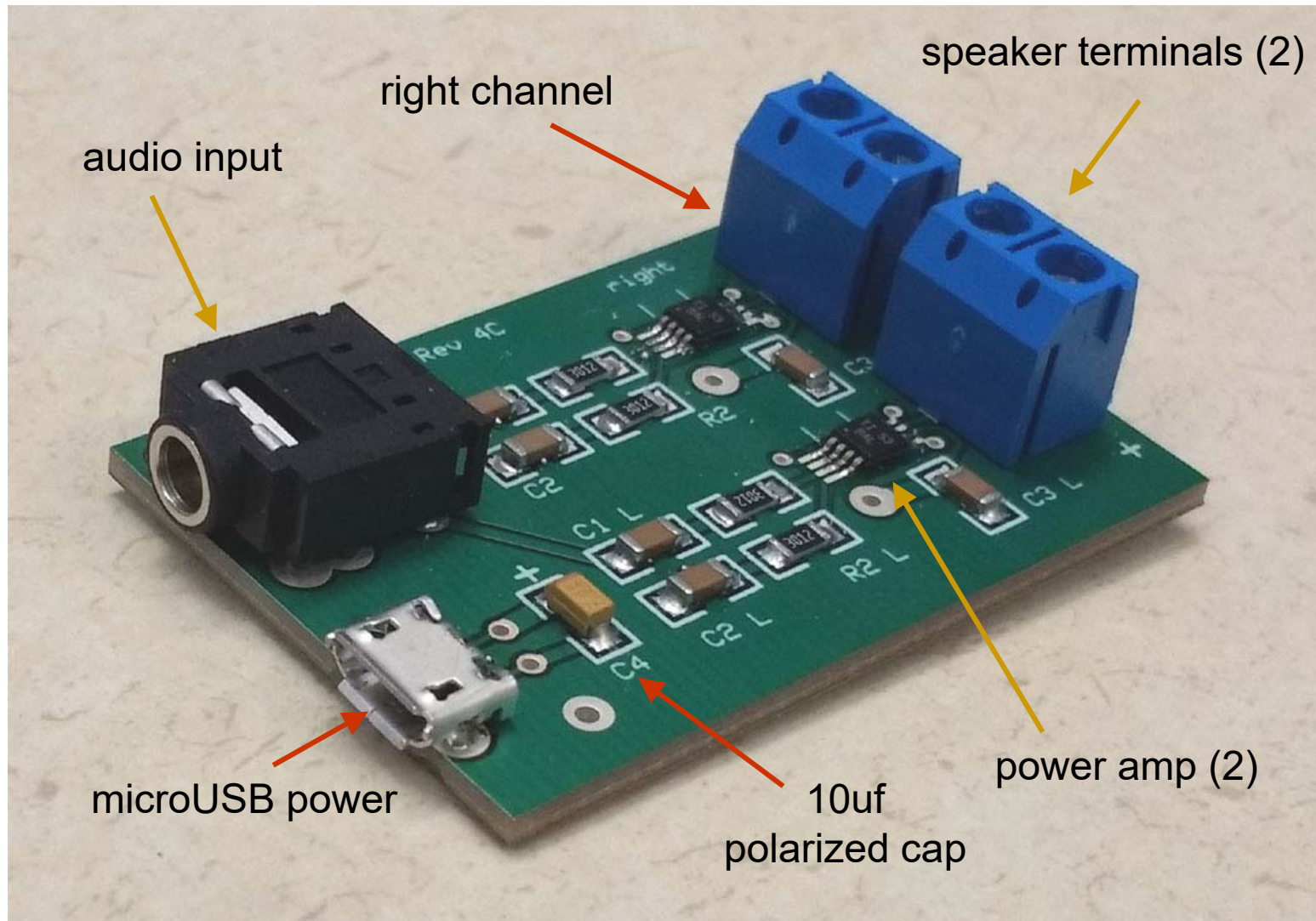


\*[sound.westhost.com/pwm.htm](http://sound.westhost.com/pwm.htm)

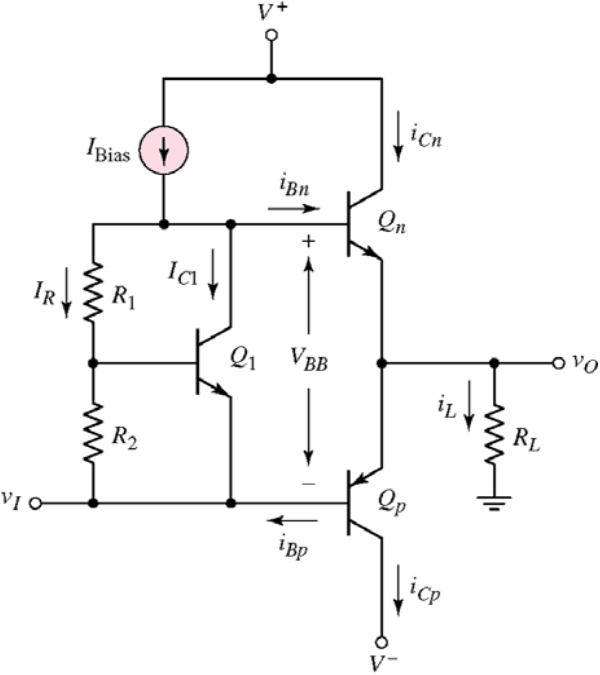
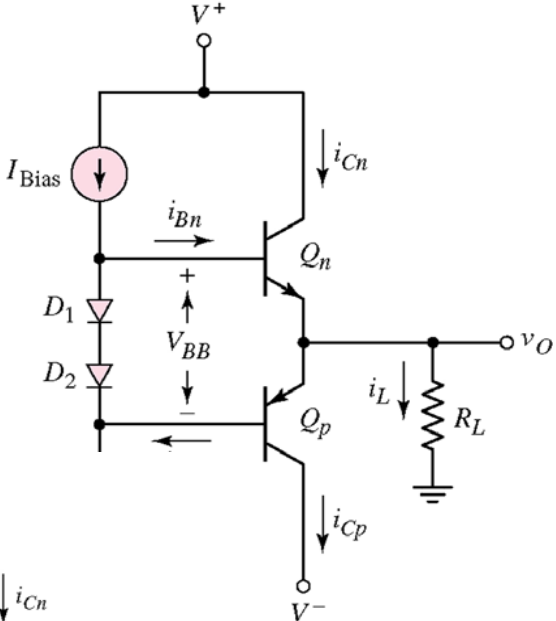
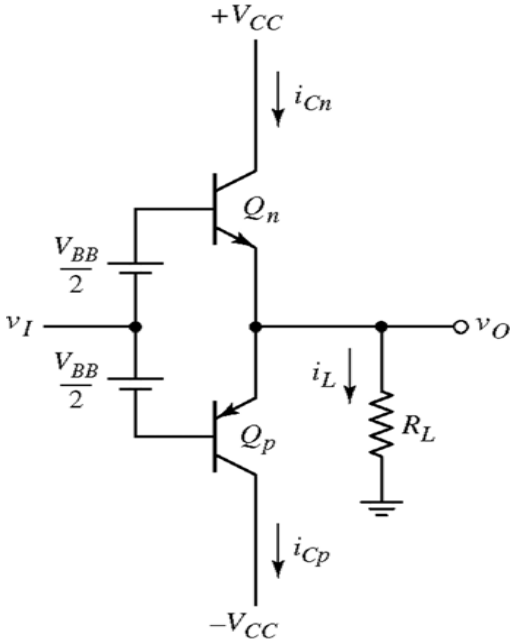
# TPA2005 – Integrated Class D Amplifier Surface Mount



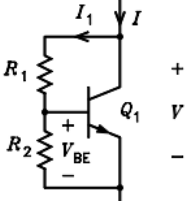
# USB Power Amplifier



# Class AB Biasing

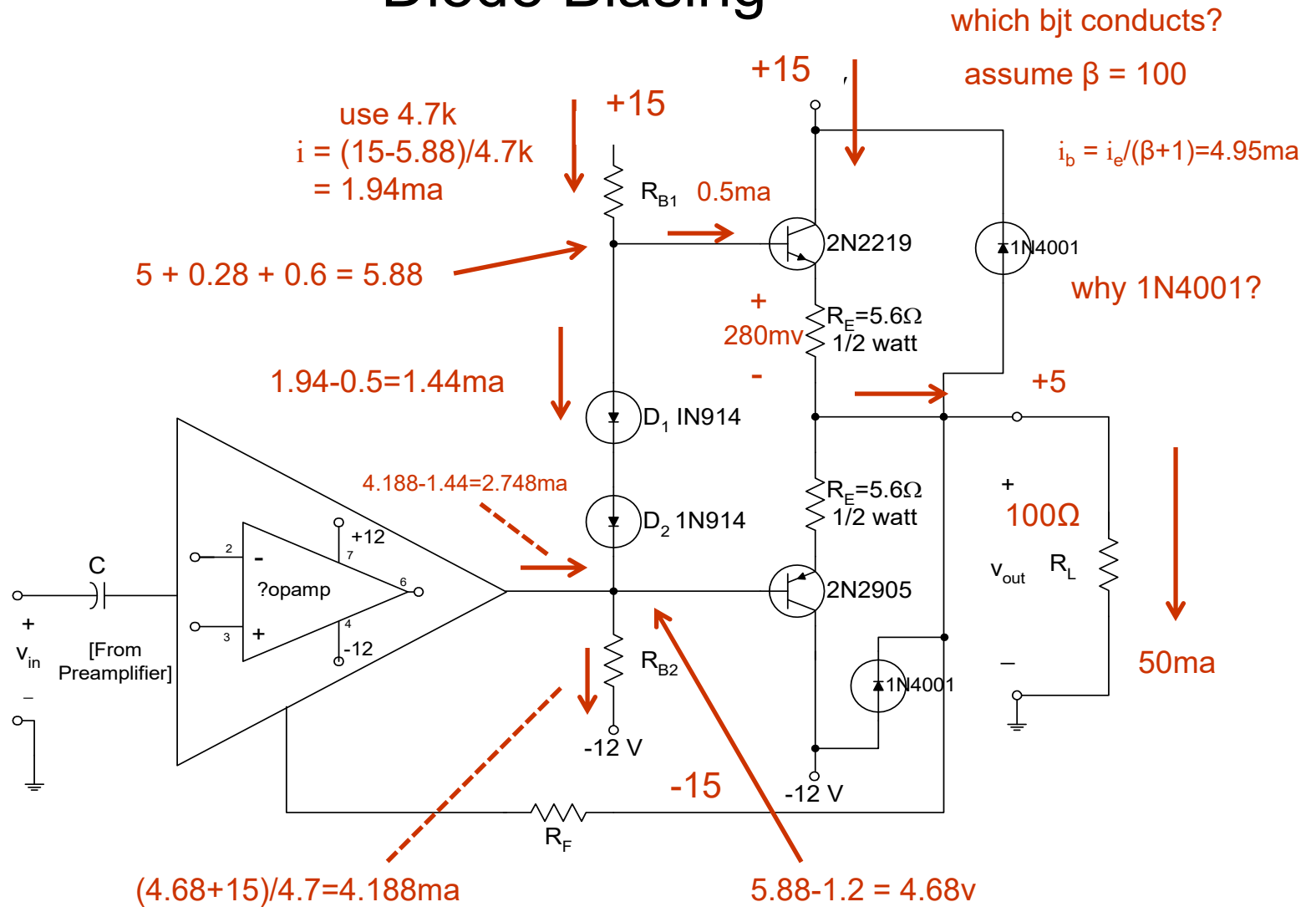


$$V = \frac{(R_1 + R_2)}{R_2} V_{BE}$$





# Diode Biasing



# Cardiac Electrophysiology

- Contraction of the heart results from depolarization and polarization (change in voltage) of myocardial cells.
- Sinoatrial (SA) node acts as pacemaker initiates atrial depolarization.
- Electrical signal propagates to the ventricles by the atrioventricular (AV) node through a specialized conducting tissue, the Bundle of His.
- Voltage sensed by electrodes on skin surface typically 0.5 - 2.0 millivolts.

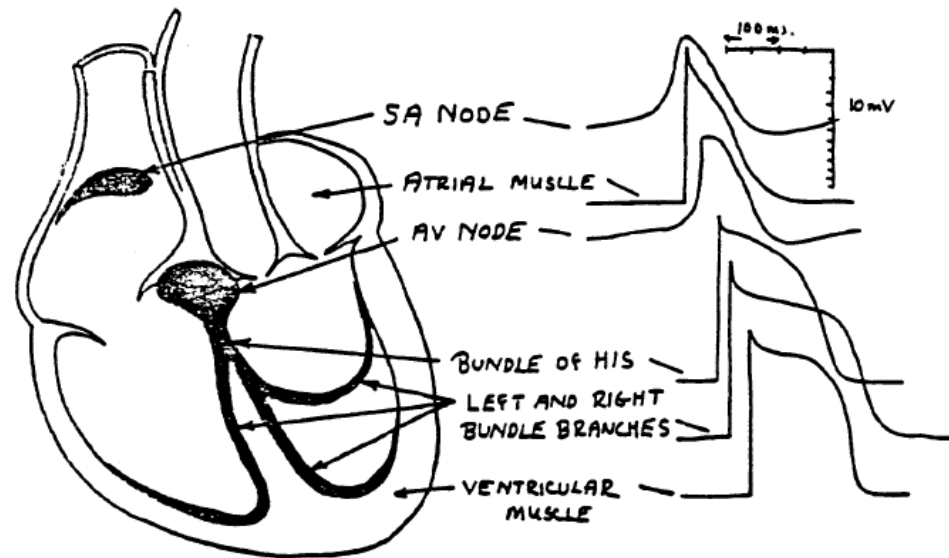


Diagram  
from 6.022

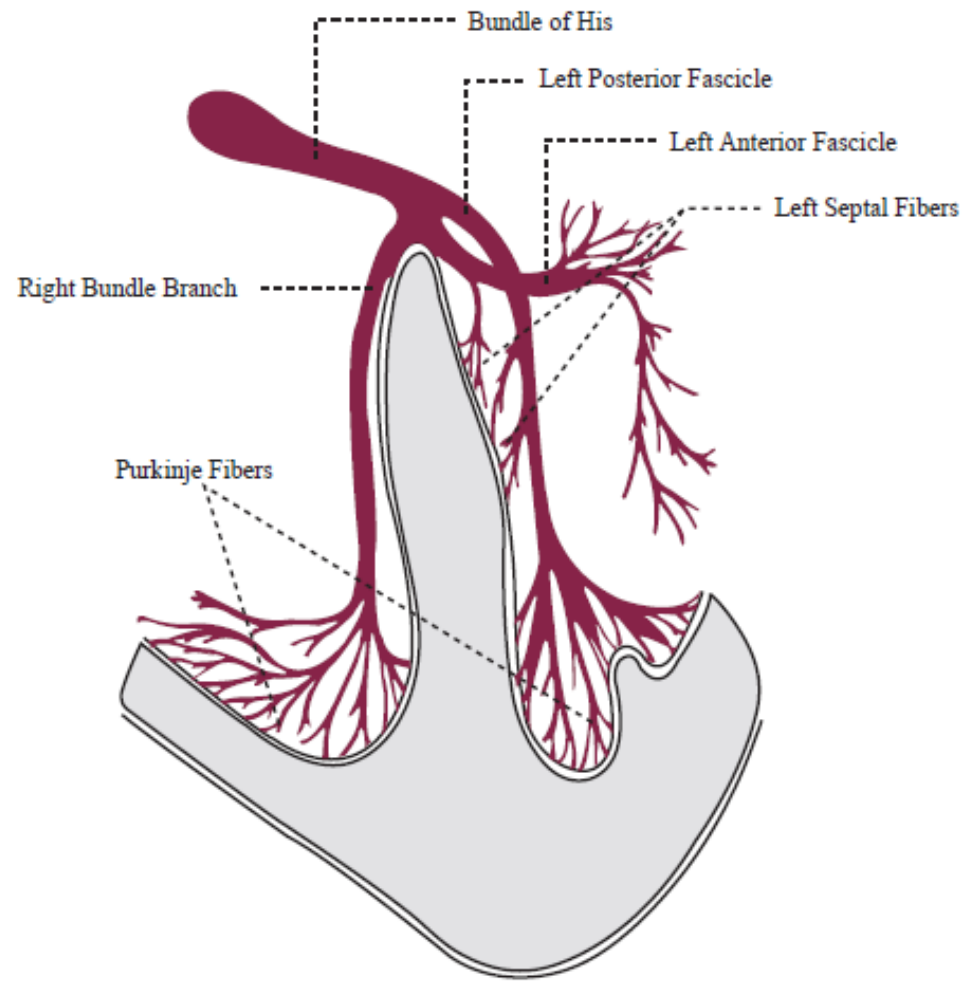
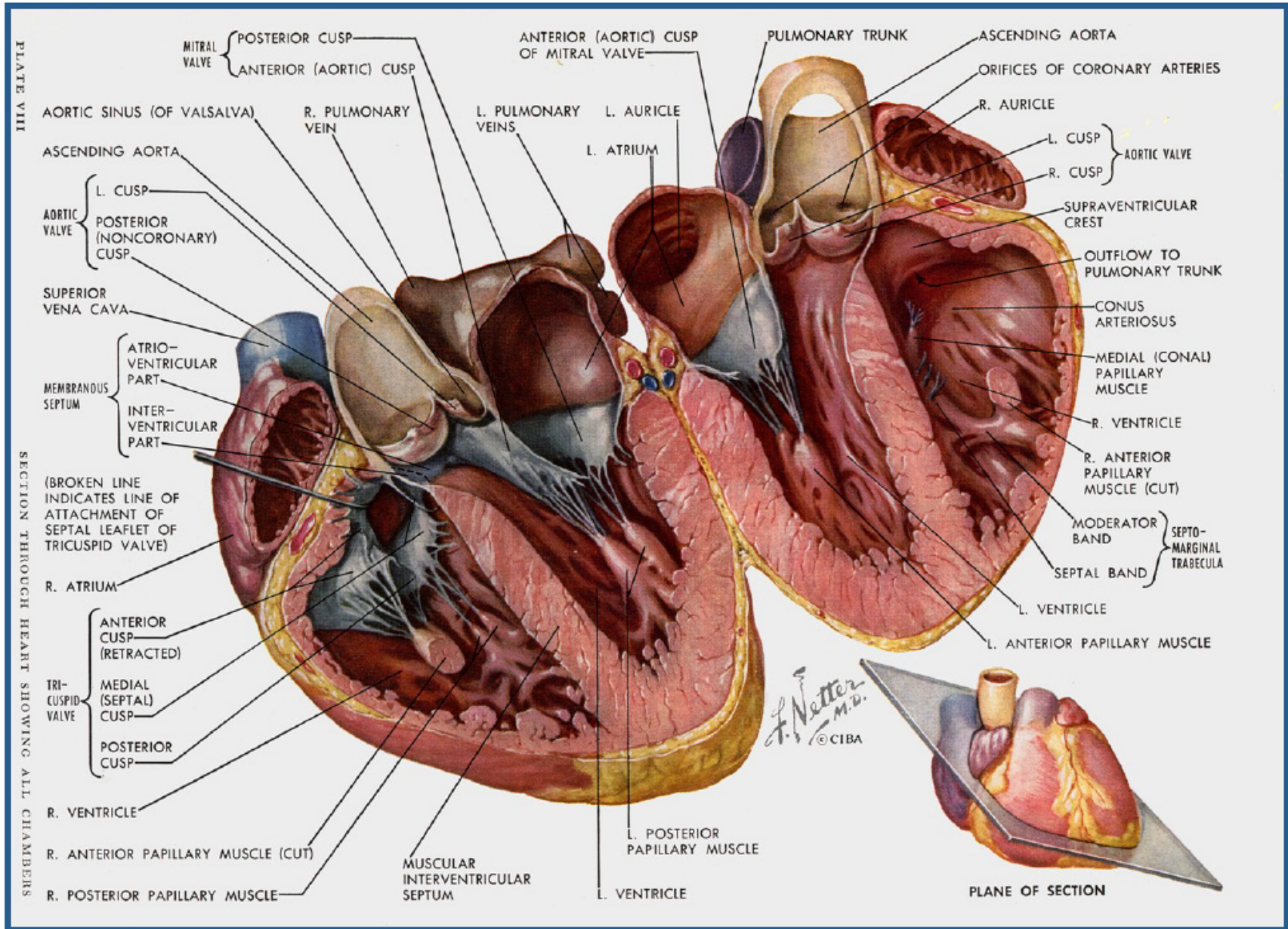


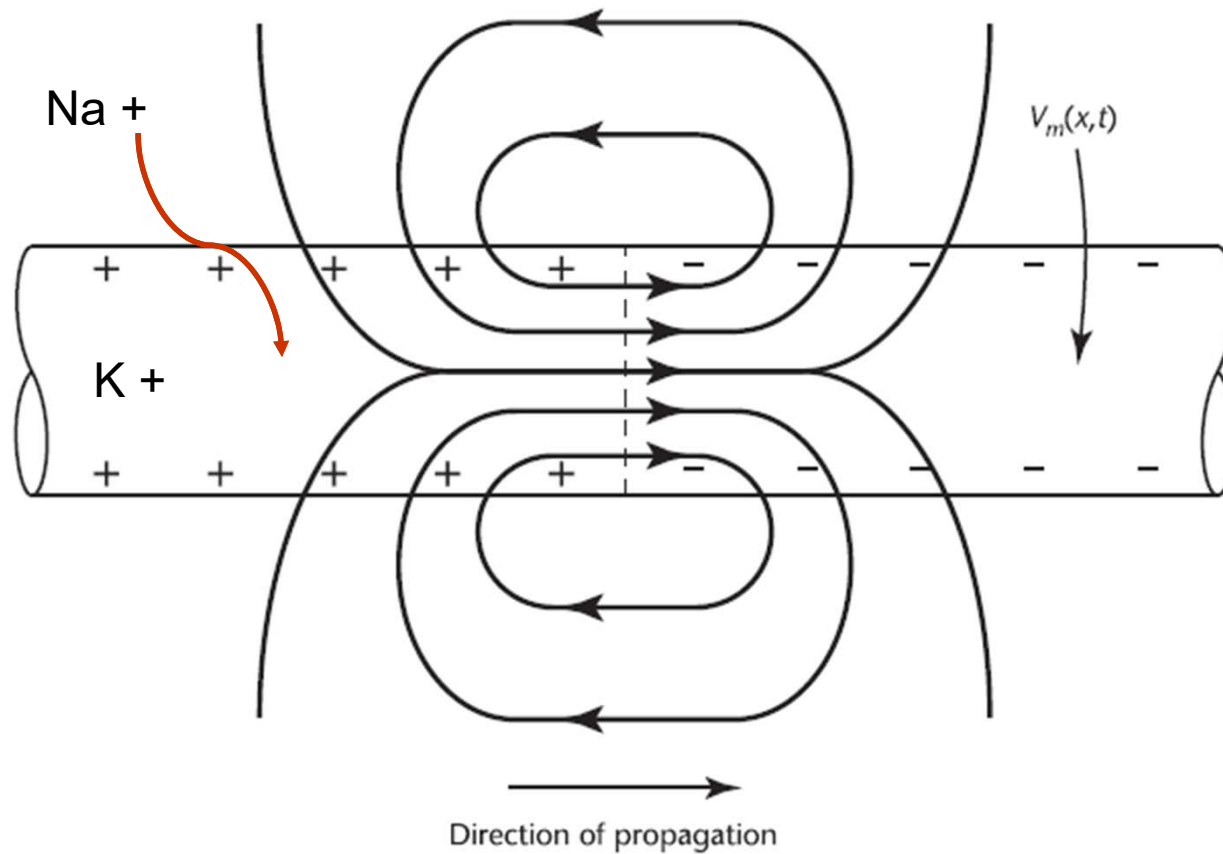
Figure by MIT OCW. After M. J. Goldman, *Principles of Clinical Electrocardiography*. 8th ed (1973), p. 37.



# “Electric Current” in the Body

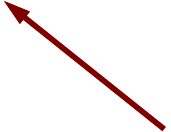
- A cell normally is polarized (excess of  $\text{Na}^+$  in the extracellular space; excess of  $\text{K}^+$  intracellular space);
- Movement of ions leads to easing of electrochemical gradients, causing a lessening of the magnitude of polarization (i.e., depolarization).
- Key points:
  - Current is propagated through the myocardium;
  - Current does not refer to movement of electrons, but rather movement of ions;
  - Movement of ions causes a “current dipole” – movement of dipoles throughout myocardium

# Dipole Field In Myocardial Cell



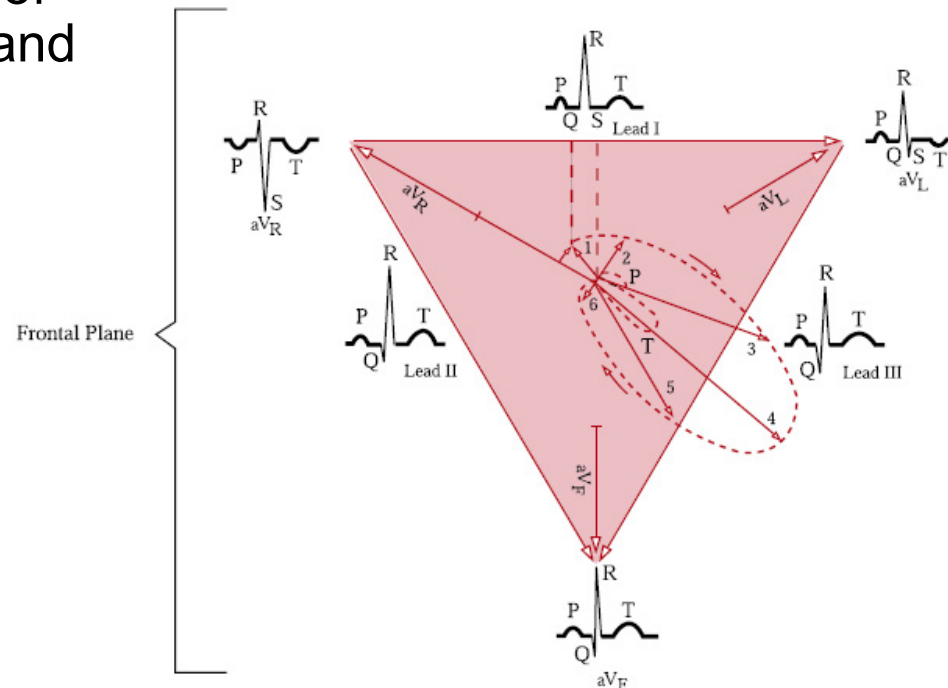
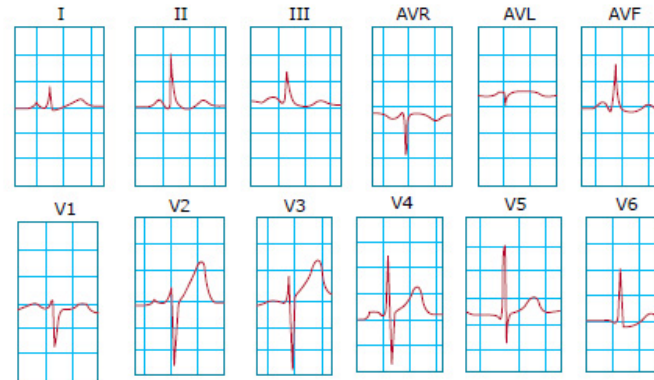
**Figure 1.2** The dipole field due to current flow in a myocardial cell at the advancing front of depolarization.  $V_m$  is the transmembrane potential. (From: [2]. © 2004 MIT OCW. Reprinted with permission.)

# Terminology

- Surface potential – the electric potential energy at a point arising from the surface charge
  - ECG Lead – difference in the surface potential at two points. Uses 10 electrodes.
  - 12 leads place on body & orientation
    - Right to Left,
    - Superior to Inferior,
    - Anterior to Posterior
    - RA = right arm; LA = left arm, LL = left foot
  - Bipolar limb leads (frontal plane):
    - Lead I: RA (-) to LA (+) (Right Left, or lateral)
    - Lead II: RA (-) to LL (+) (Superior Inferior)
    - Lead III: LA (-) to LL (+) (Superior Inferior)
  - Augmented unipolar limb leads (frontal plane):
    - Lead aVR: RA (+) to [LA & LL] (-) (Rightward)
    - Lead aVL: LA (+) to [RA & LL] (-) (Leftward)
    - Lead aVF: LL (+) to [RA & LA] (-) (Inferior)
  - Unipolar (+) chest leads (horizontal plane):
    - Leads V1, V2, V3: (Posterior Anterior)
    - Leads V4, V5, V6: (Right Left, or lateral)
- 

# Medical Grade ECG

- Medical grade ECG uses 6 or 10 monitoring electrodes.
- Three lead ECG circuit used to show a ECG signal and demonstration operation of instrumentation op-amp and low pass filter.

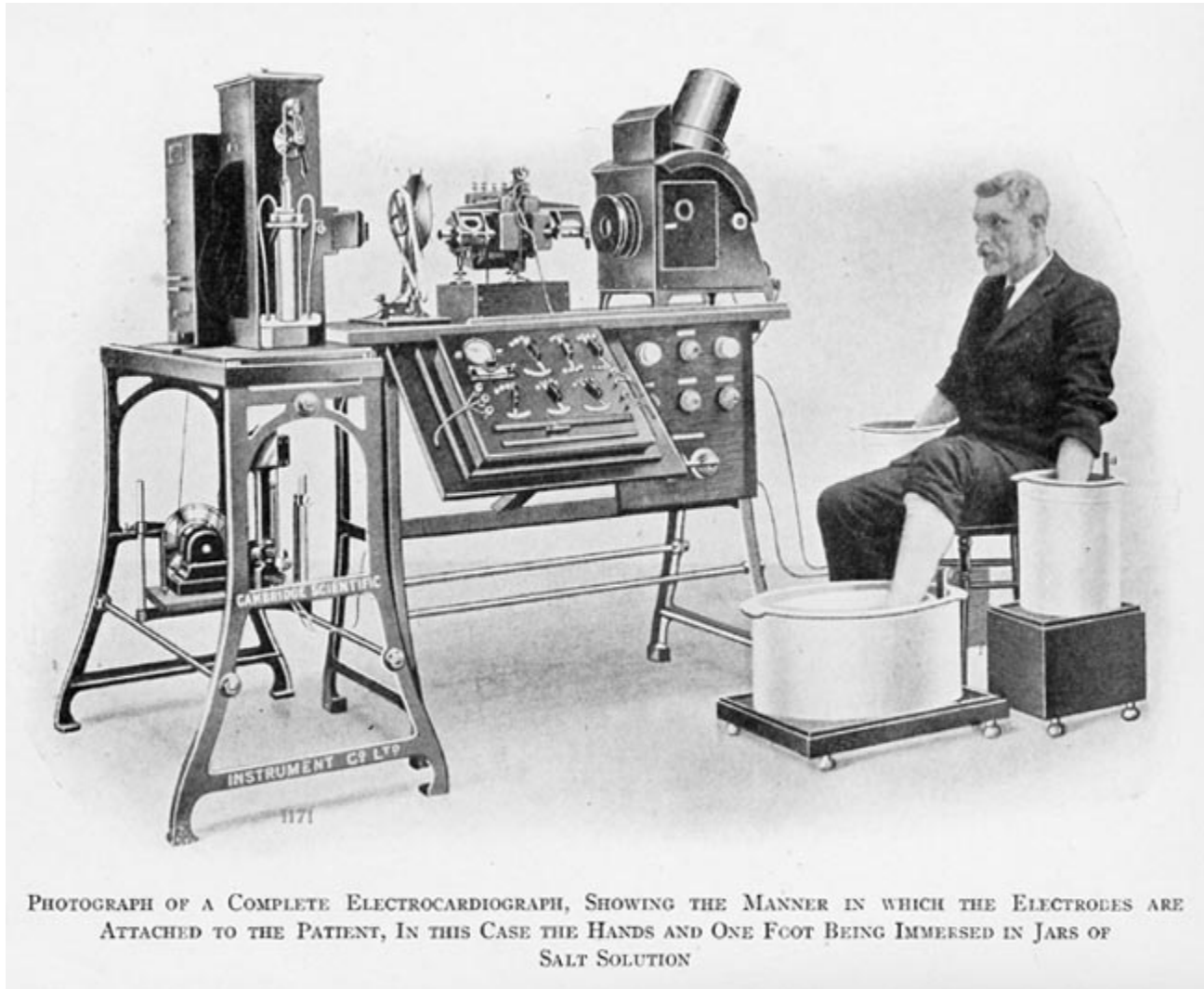




# ECG Measurement

- Human tissue is electrically conductive; necessary for muscle control
- Place electrodes at multiple points on the body.
  - Electrode is metal contact with conductive gel and an adhesive backing.
  - Hand lotion and KY jelly are conductive
- Measure potential difference (voltage) between two points.

The Nobel Prize Medicine 1924 Willem Einthoven  
"discovery of the mechanism of the electrocardiogram"





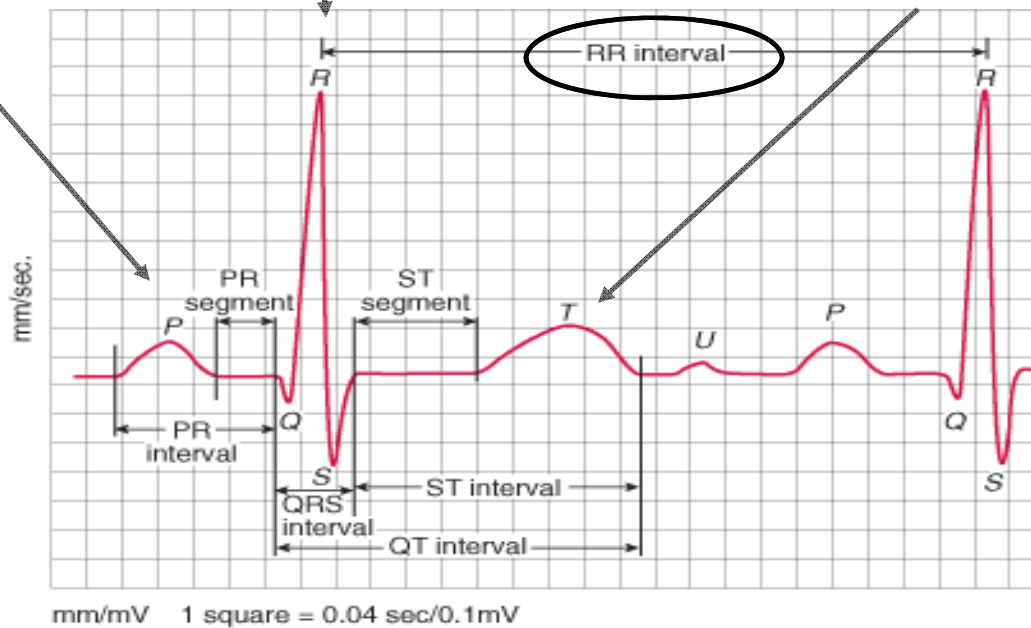
**Goldfinger**

# ECG Characteristics

QRS complex: ventricular contraction

P wave: atrial contraction

T wave: ventricular recovery  
repolarization



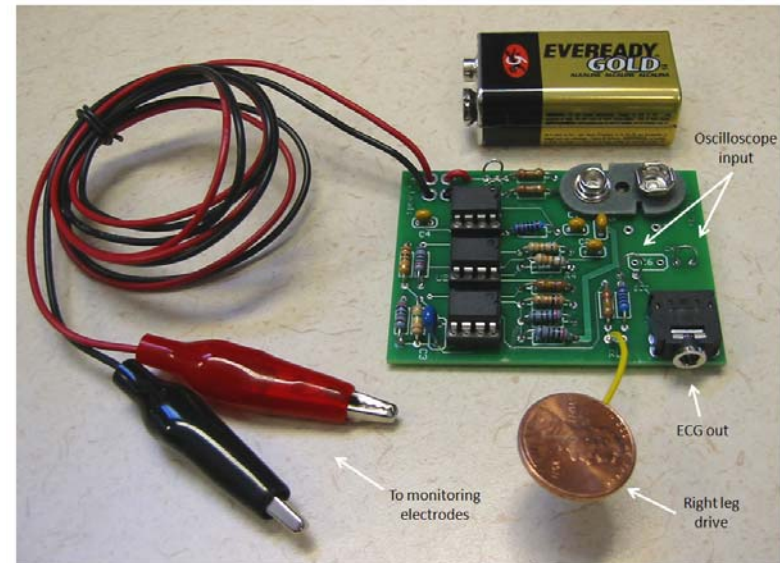
# Functional ECG Design - Uninspired

- Dual supply op-amp, instrumentation amplifier
- Oscilloscope display
- Data export for MATLAB analysis
- Or AD interface to PC

# ECG Circuit Design Goals

- Powered by 9V battery for safety
- Use inexpensive commercial parts
- Use thru hole two layer PCB
- Display ECG (lead 1) signal
- Direct attach to PC for demonstration and analysis

Used in 6.03 lab



# Where is my ECG?

## Skin Signal Composition

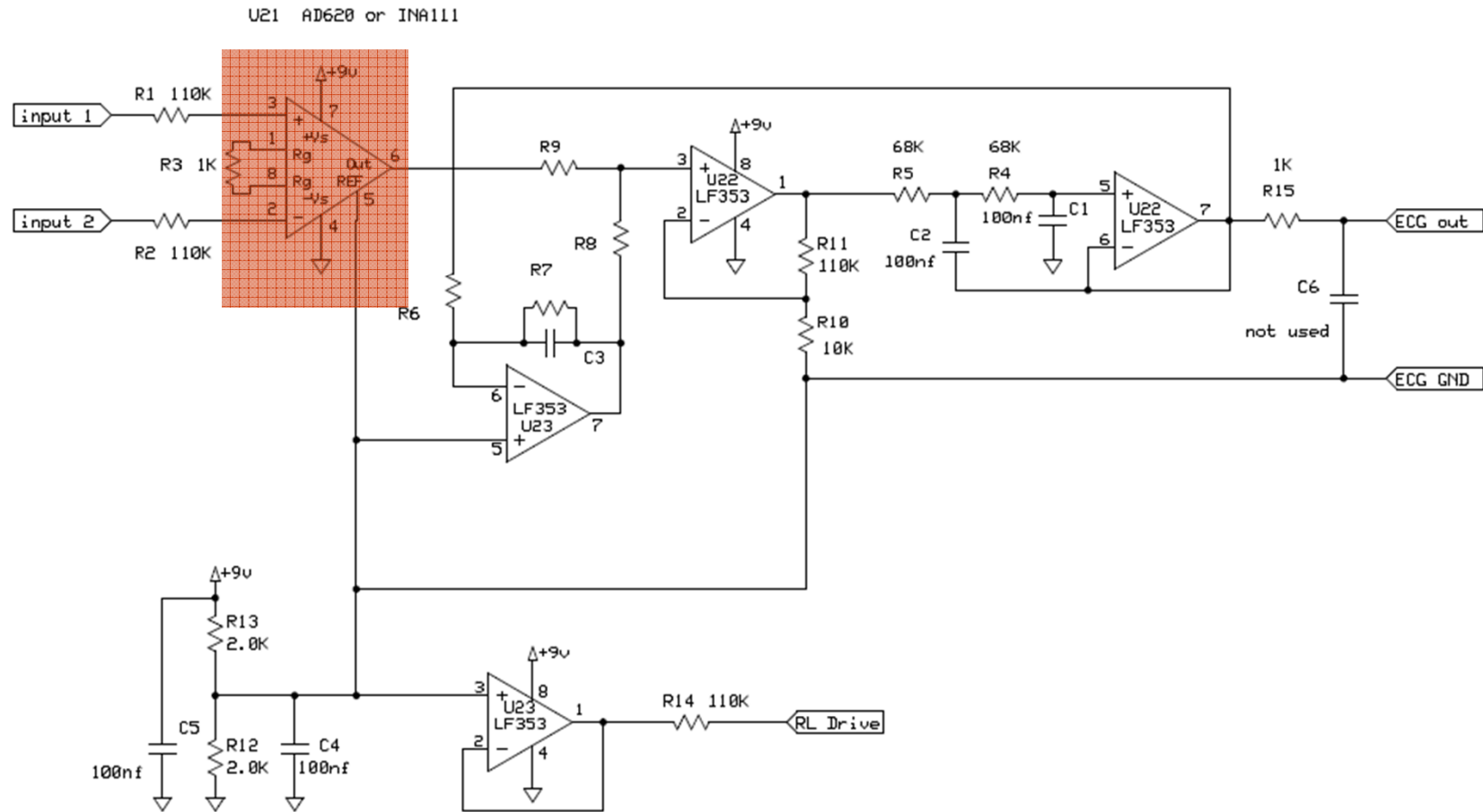
- Electromagnetic interference (EMI) and other noise pickup. Common mode and differential mode noise
- 50-60hz ac line noise
- ECG Heart signal ~ 1mv
- DC offset (signals originate from different parts of the body) ~ up to 500mv

# ECG Signal Processing Steps

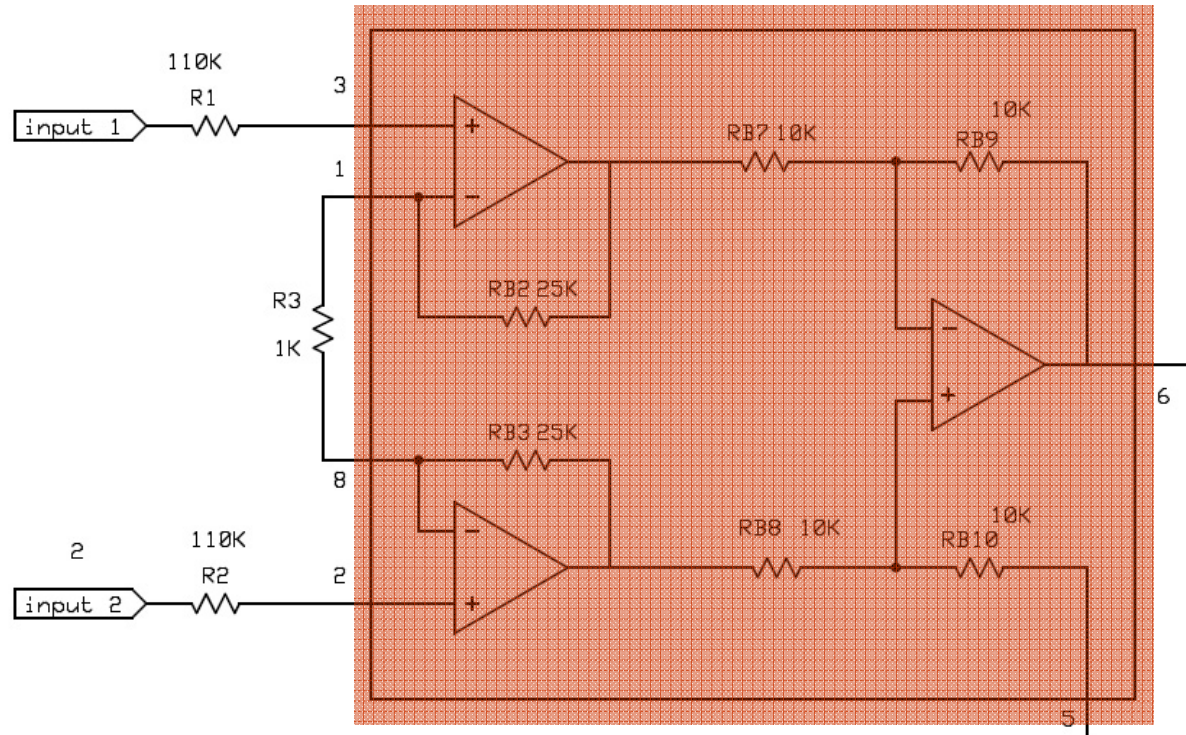
- Amplify signal from electrodes
- Remove common mode noise, amplify signal
- Remove noise above 23hz with low pass filter
- Apply bias for single supply operation and improve common mode rejection
- Compensate for DC offset



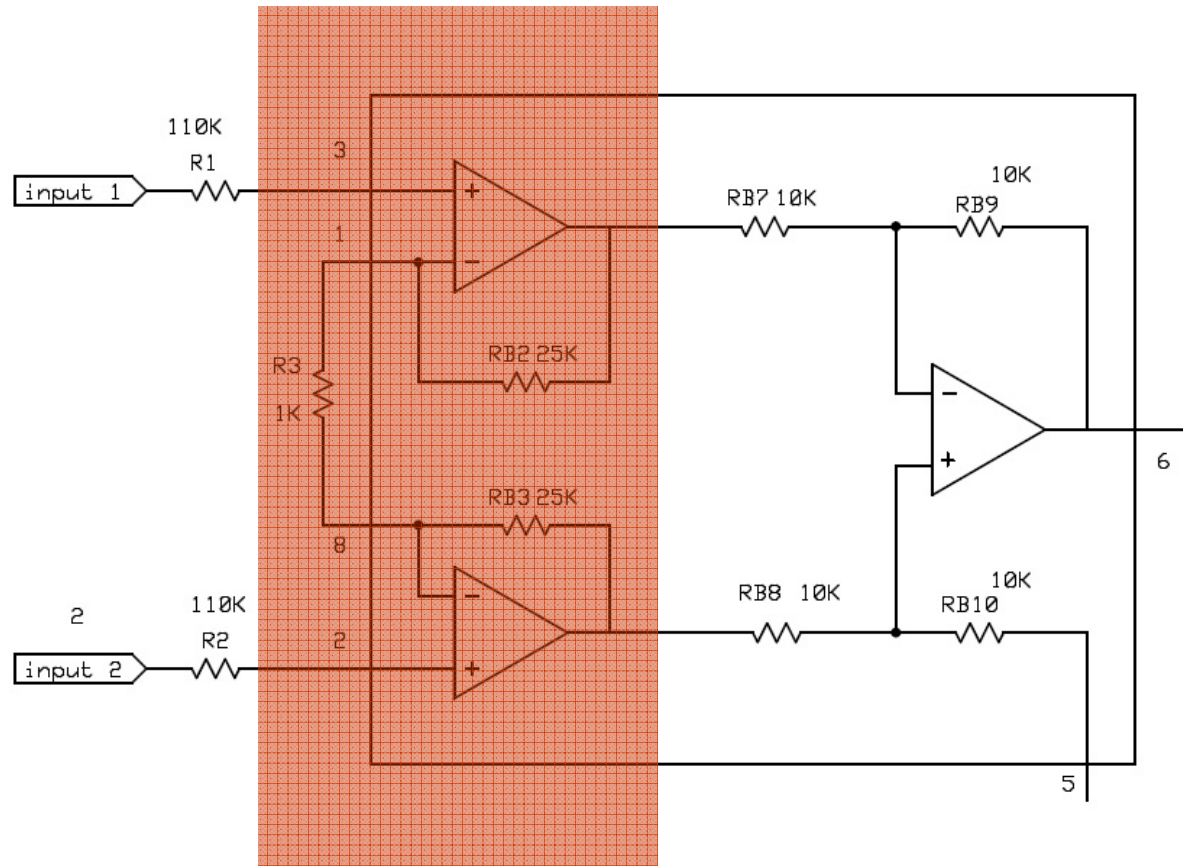
# ECG Board



# 1NA 111 Instrumentation Amplifier

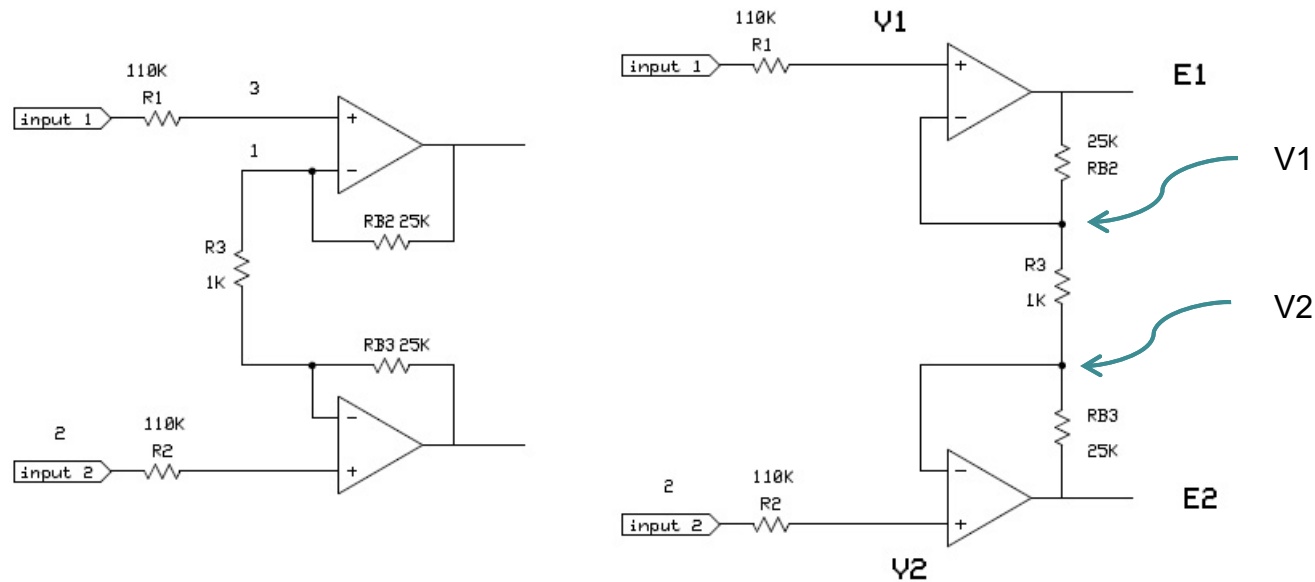


# 1NA 111 Instrumentation Amplifier



# Instrumentation Op Amp Front End

Equivalent circuits – differential mode signal

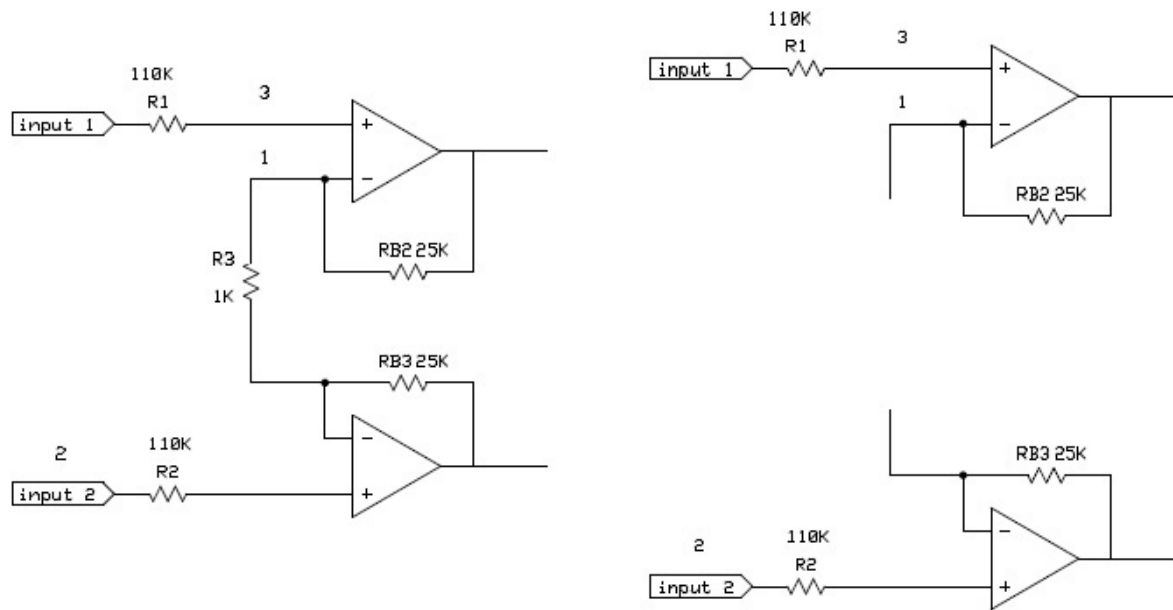


$$i_{R3} = \frac{V1 - V2}{1k} \quad (E1 - E2) = i_{R3} (RB2 + R3 + RB3)$$

$$(E1 - E2) = \frac{(V1 - V2)}{R3} (RB2 + R3 + RB3) = (V1 - V2) \left(1 + \frac{2RB}{R3}\right) \quad \text{Gain} = 51$$

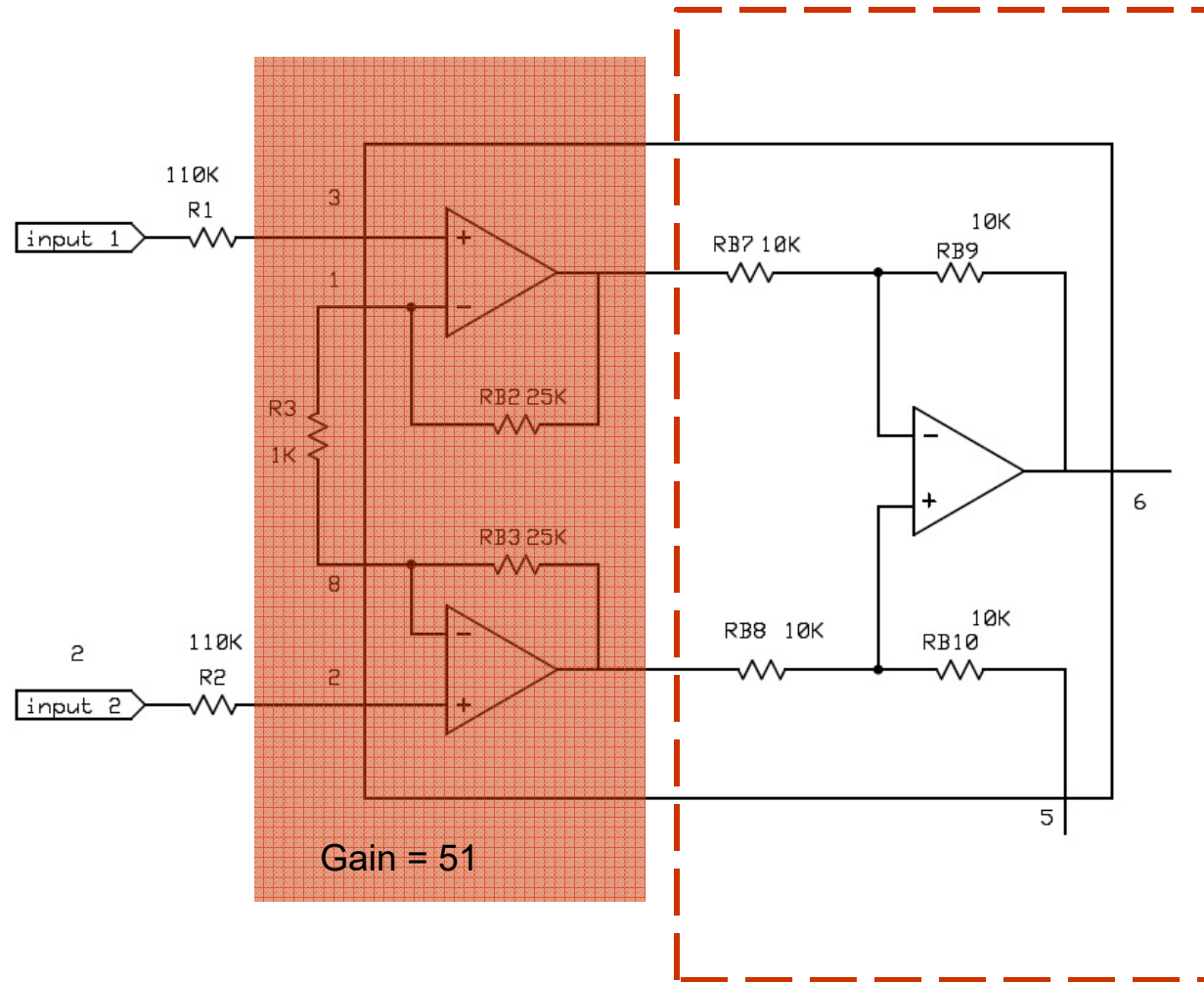
# Instrumentation Op Amp Front End

Equivalent circuits – Common mode signal

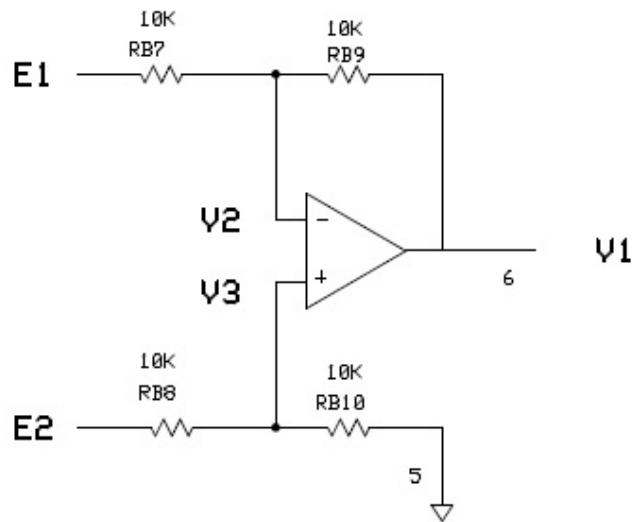


Common mode gain = 1

# 1NA 111 Instrumentation Amplifier



# Elimination of Common Mode Noise



$$V2 = V3$$

$$V3 = E2 \times \frac{RB10}{RB8 + RB10}$$

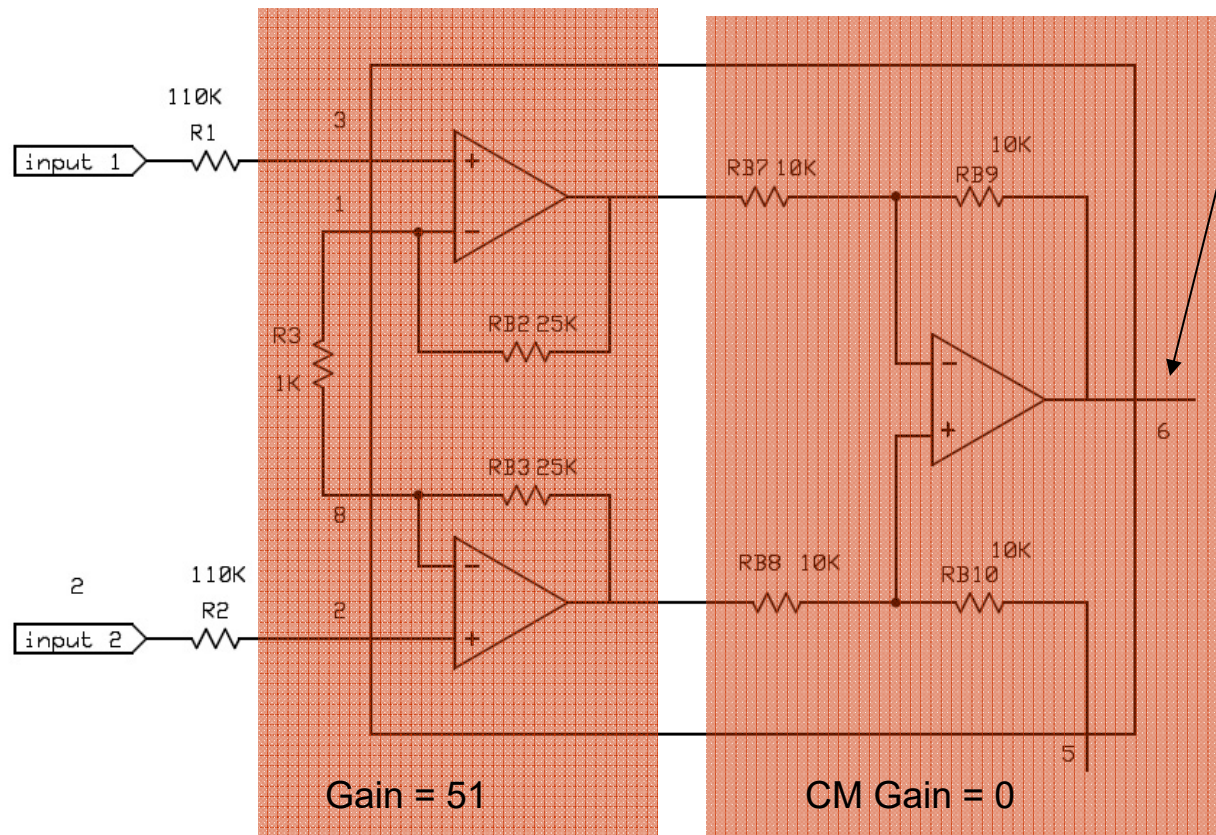
$$V2 = E1 \left( \frac{RB9}{RB7 + RB9} \right) + V1 \left( \frac{RB7}{RB7 + RB9} \right)$$

$$RB7 = RB8 = RB9 = RB10 = 10K$$

$$V1 = (E2 - E1)$$

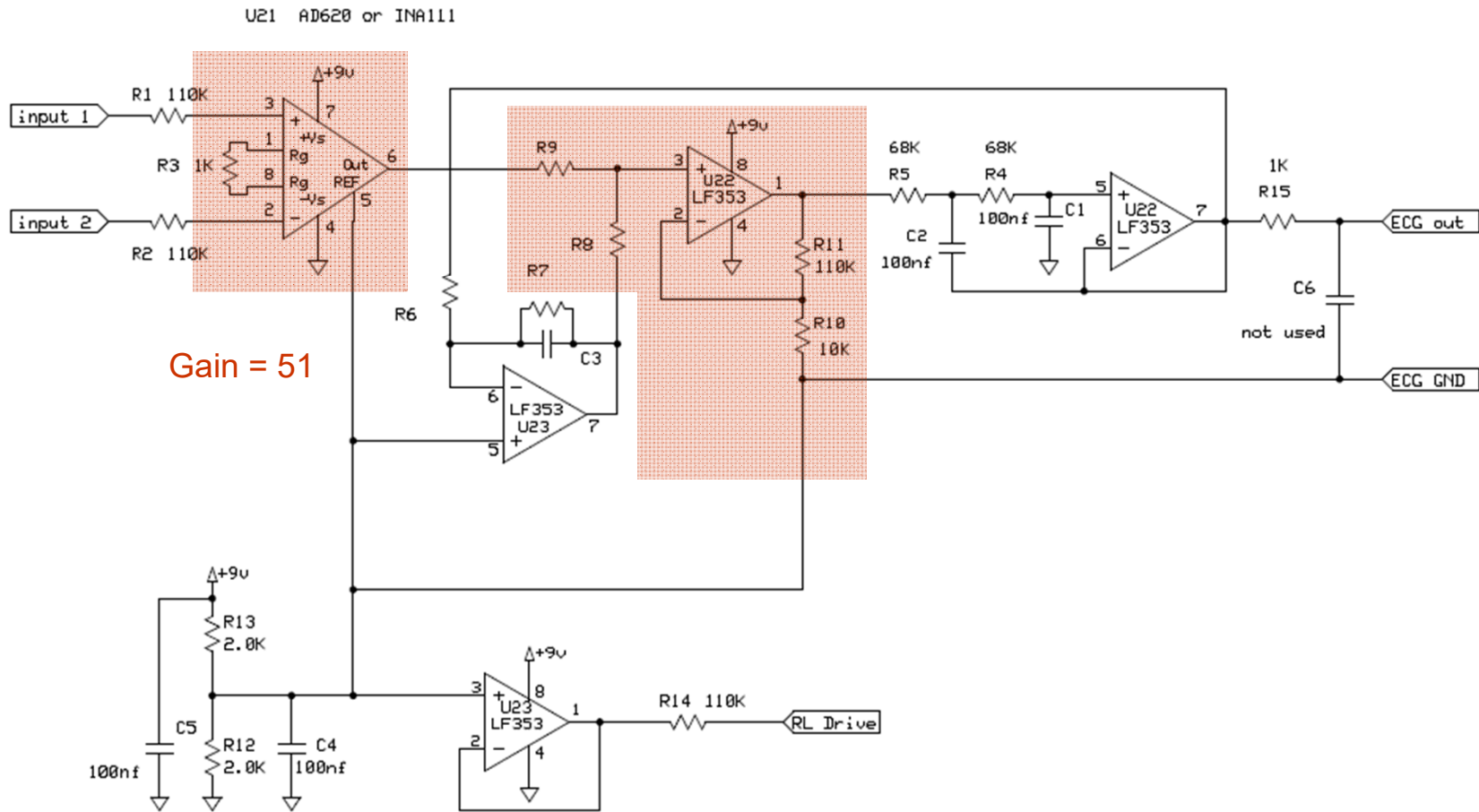
# 1NA111 Instrumentation Amplifier

common mode noise removed  
difference amplifier

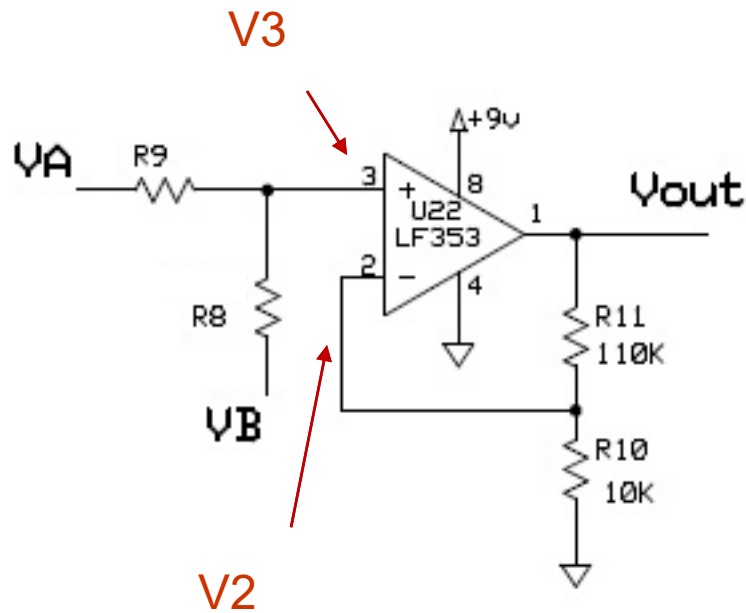




# ECG Board



# Adder Circuit

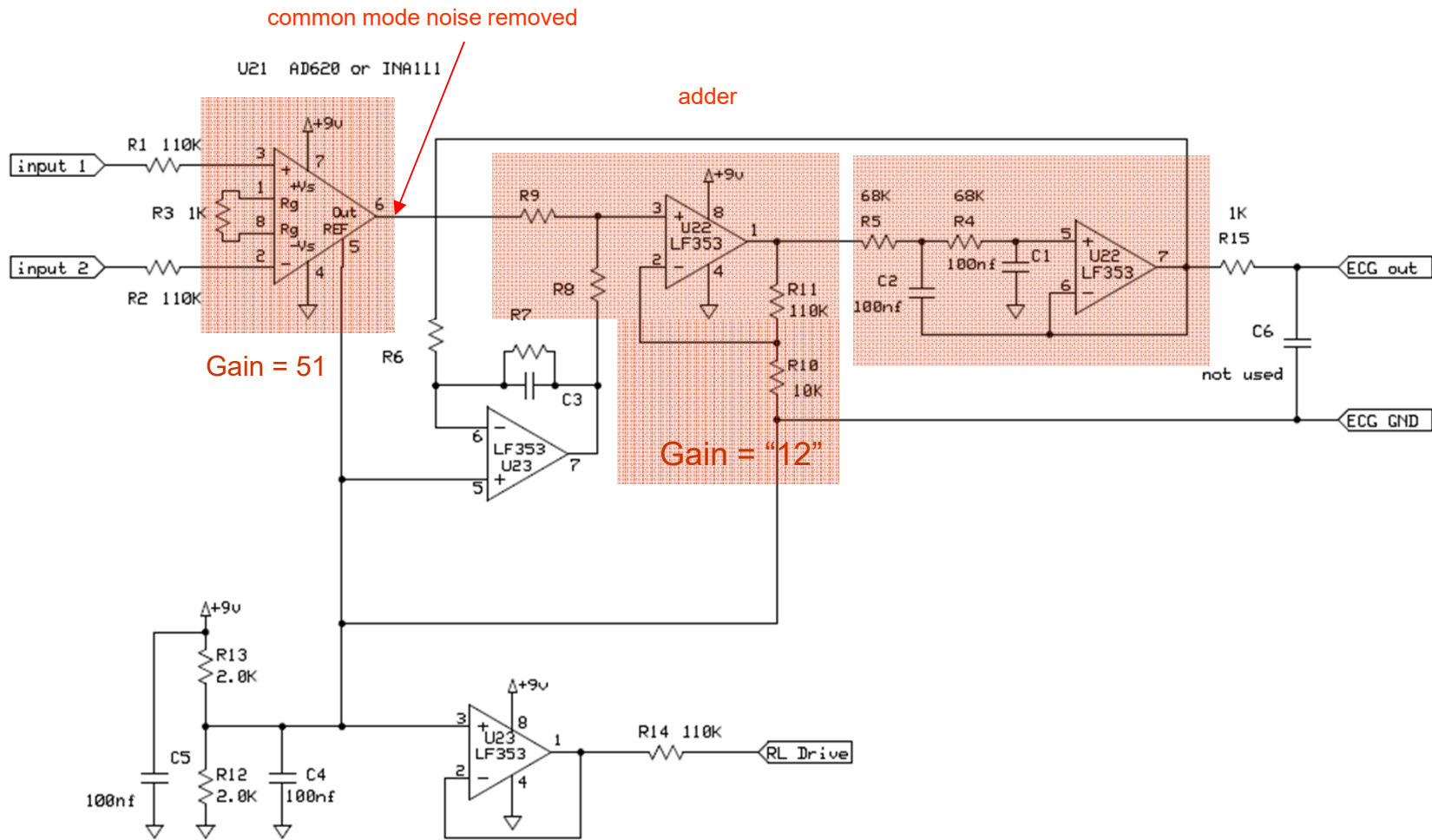


$$V3 = VA\left(\frac{R8}{R8 + R9}\right) + VB\left(\frac{R9}{R8 + R9}\right)$$

$$V2 = Vout\left(\frac{R10}{R10 + R11}\right)$$

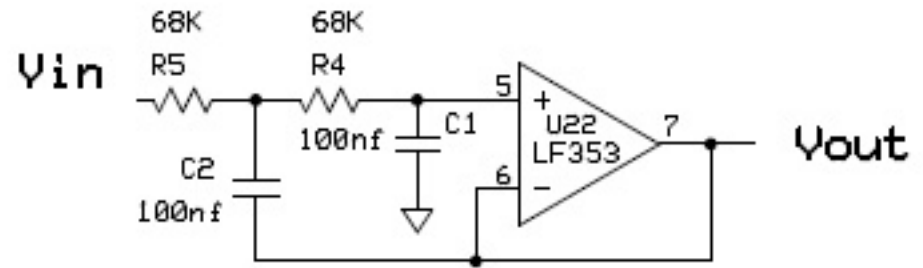
$$Vout = \left( VA\left(\frac{R8}{R8 + R9}\right) + VB\left(\frac{R9}{R8 + R9}\right) \right) \left( \frac{R10 + R11}{R10} \right)$$

# ECG Board



# Elimination of High Frequency Noise

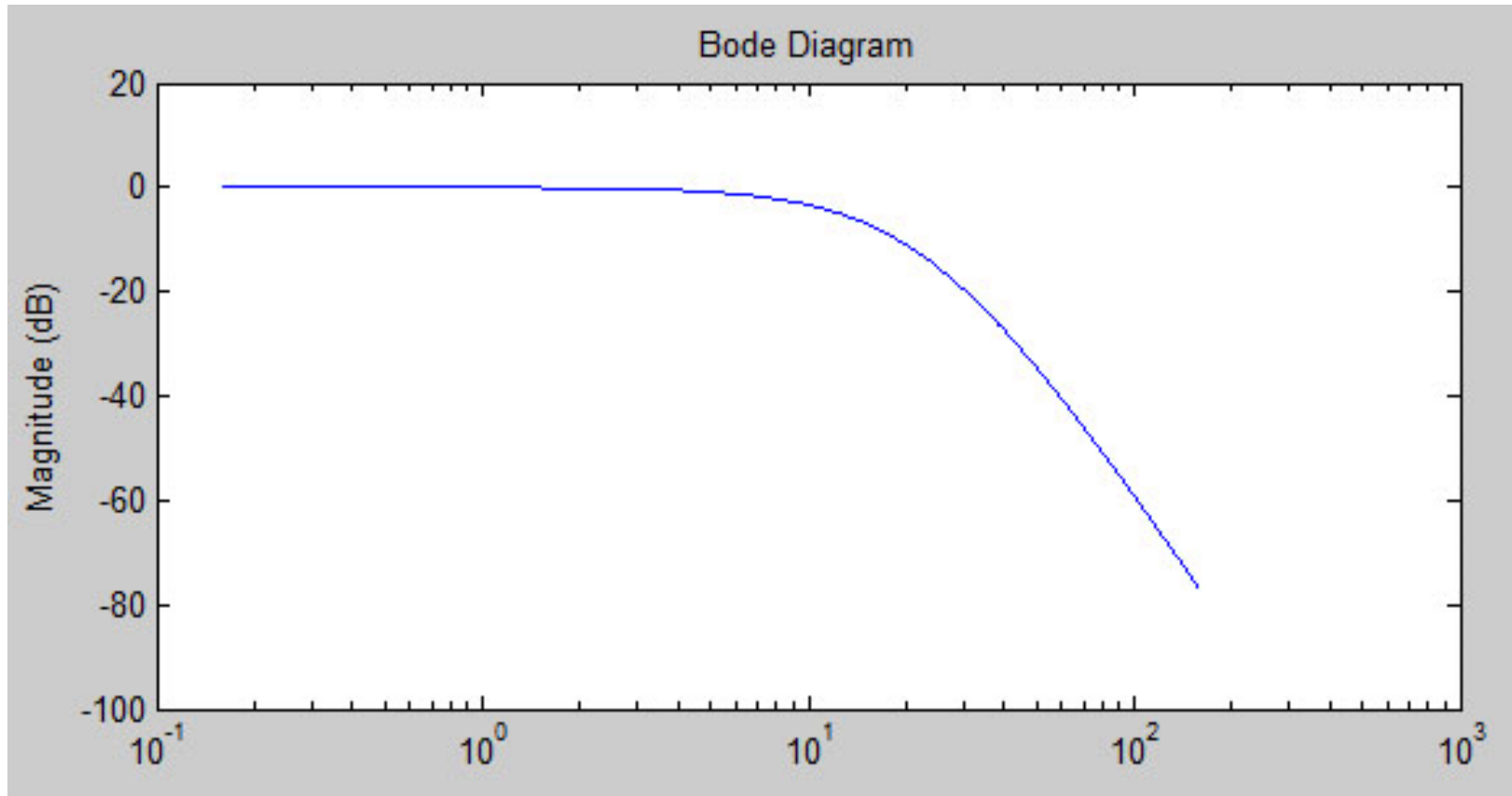
- Use low pass filter (LPF). Sallen-Key filter is a second order filter. (A second order filter attenuates by a factor of one fourth for every doubling of frequency.)
- For low frequencies, C1, C2 are open circuit – op amp feeds signal through.
- For high frequencies, C1, C2 act as shorts.



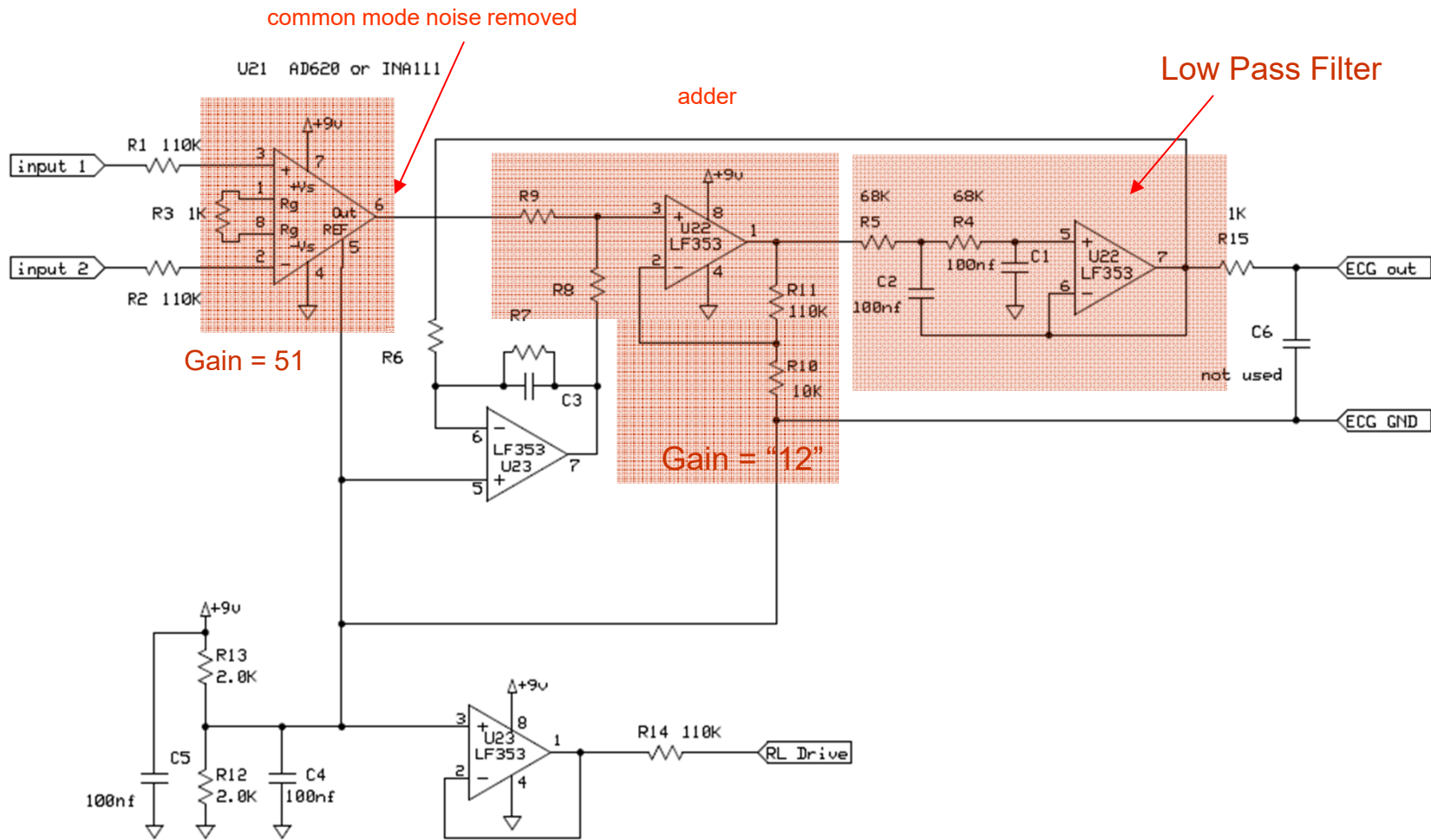
$$f_c = \frac{1}{2\pi RC}$$

$$\begin{aligned} R5 &= R4 = 68K \\ C1 &= C2 = 100nf \\ f_c &= 23.4 \text{ Hz} \end{aligned}$$

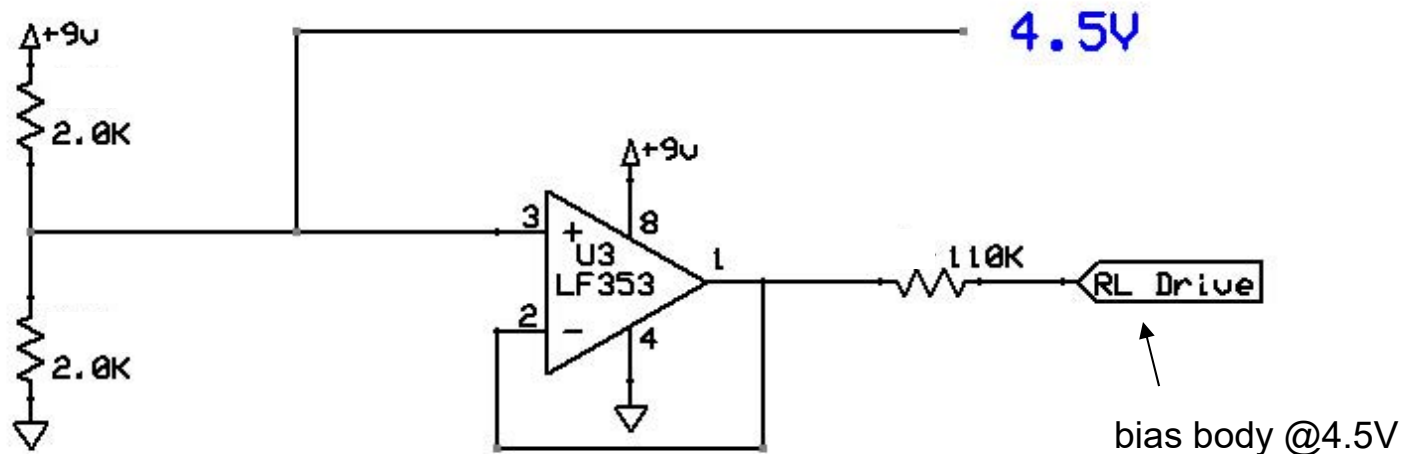
# Sallen Key Bode Diagram



# ECG Board

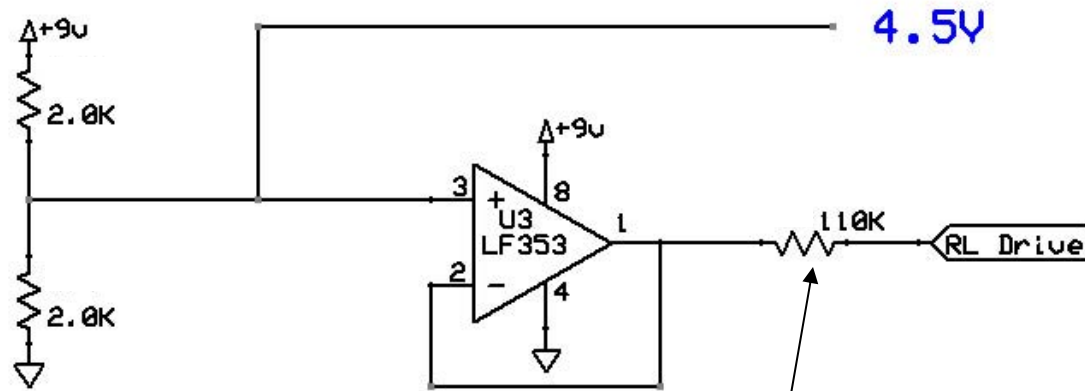


## Operation from 9V source Right Leg Drive



- LF353 (but not all op amps) need a plus/minus voltage source
- Set the reference voltage (typically ground) to 4.5V.
- Op amps sees +4.5 and -4.5
- Improves CMRR by shunting noise to “ground”

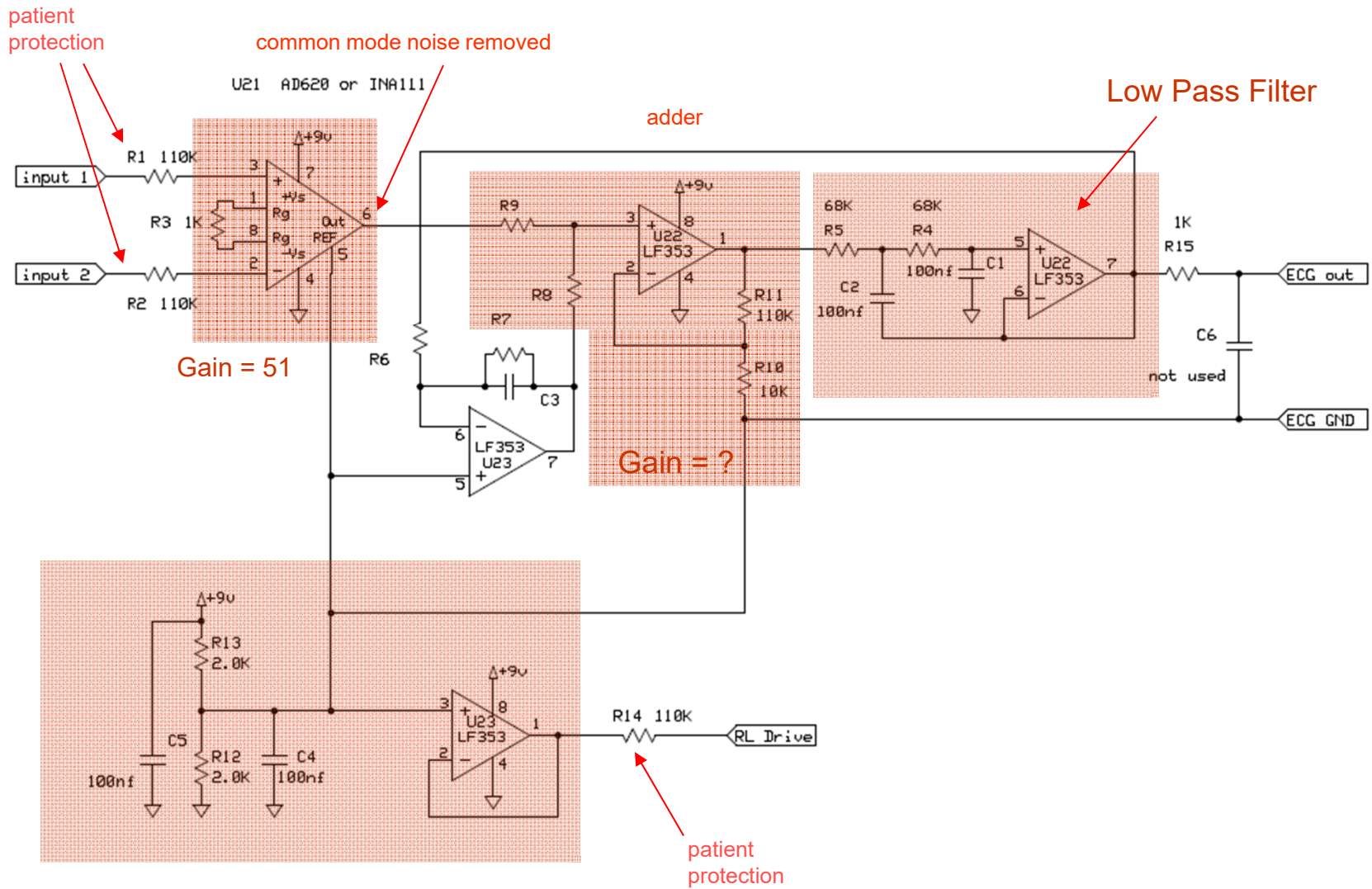
# Patient Protection



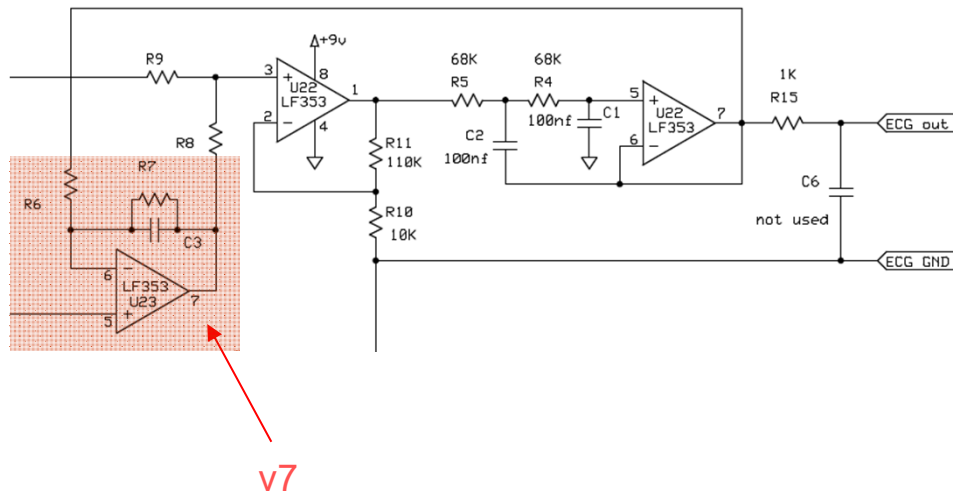
- Use 9V battery
- 110K resistor in series with all leads connecting to patient



# ECG Board



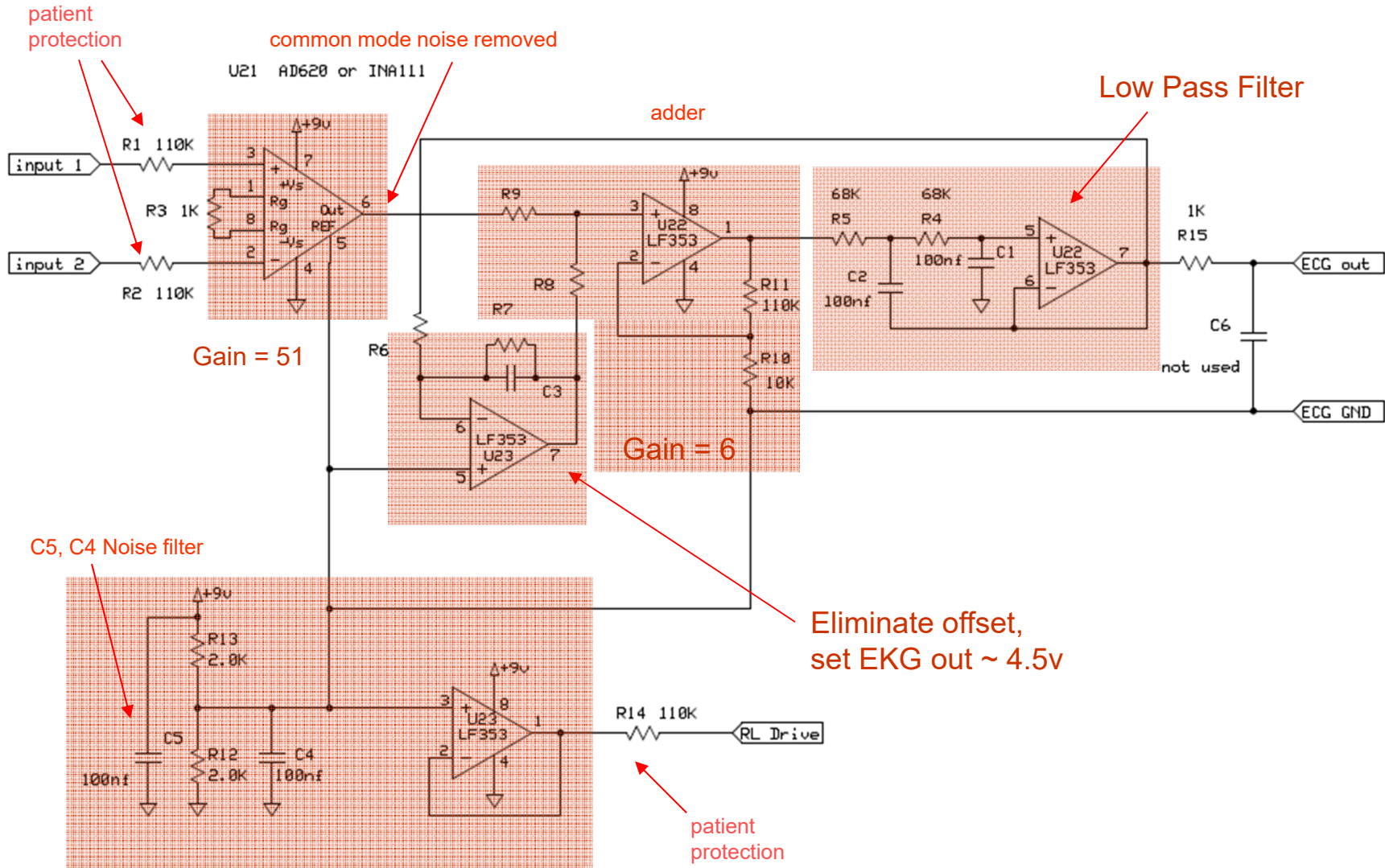
# Elimination of DC Offset\*



v7 added to amplified ECG signal to maintain  $ECG_{out}$  at 4.5 V

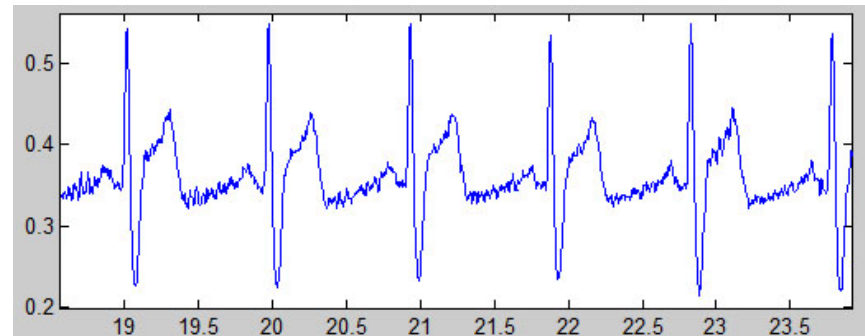
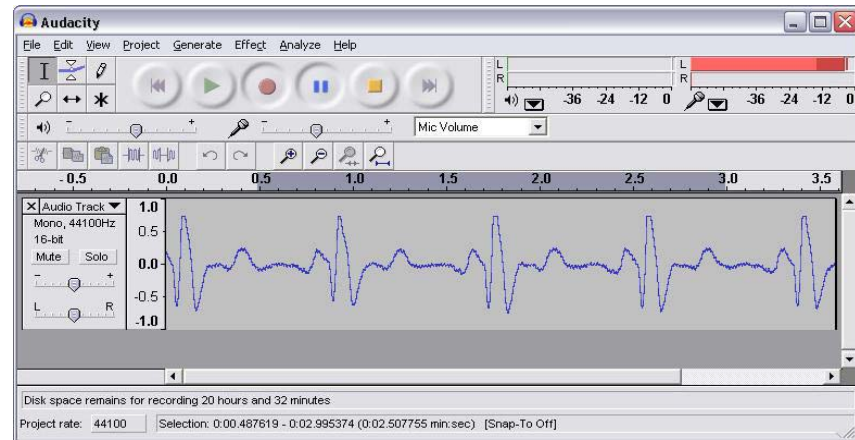
- This block, a LPF, integrates the output voltage over time and compensates for any DC offset
- Determine transfer function
- Select R6, R7 and C3 values.

# ECG Board



# Displaying ECG

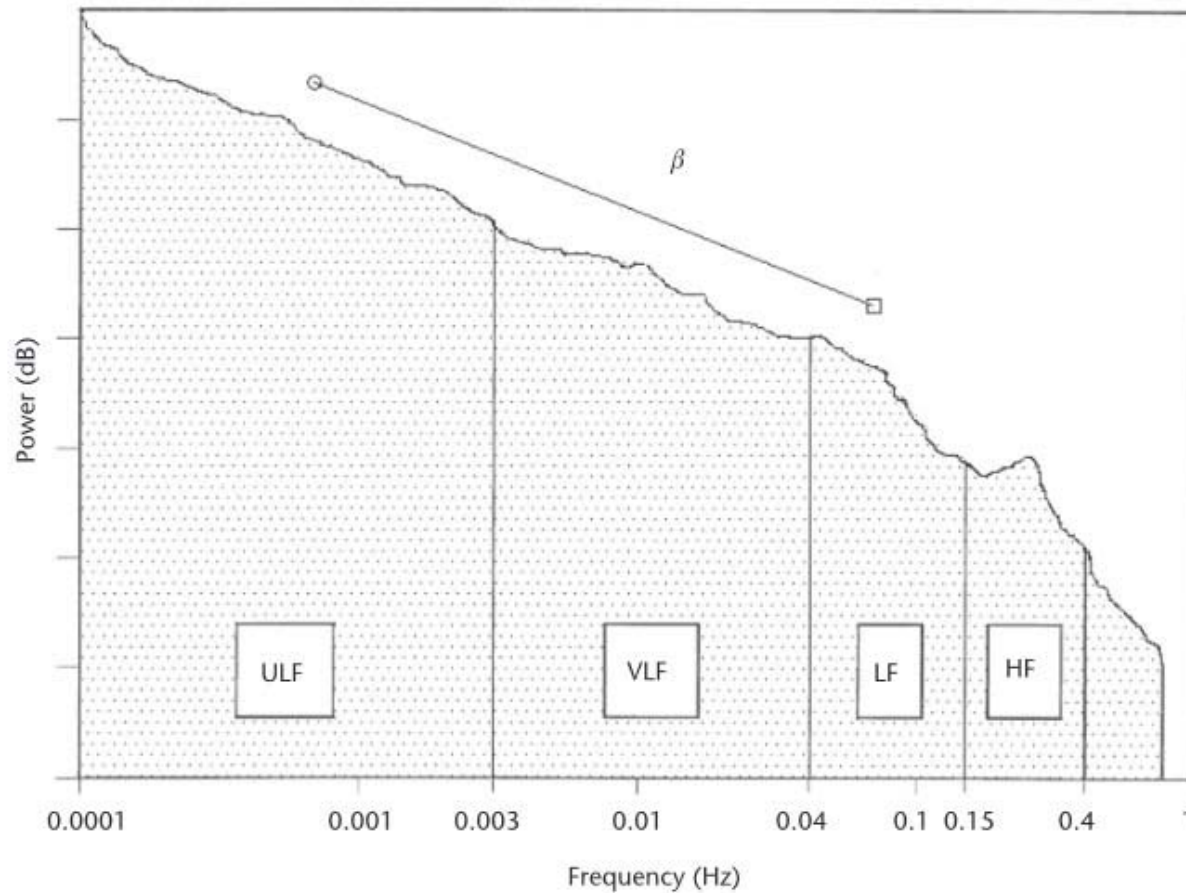
- PC audio uses AC-97 chip with 20 bit A-D converter (DAC) for microphone/line input.
- Display using Audacity, open source recording/editing software with ECG as microphone input
- Display using MATLAB



# ECG Variability Analysis

- Time domain analysis – Time series
  - NN series: beat to beat interval also called RR series.
  - SDNN: standard deviation of NN interval
  - RMSSD: root mean square of successive differences
  - NN50: number of NN pairs differing by 50ms
- Frequency domain analysis – power spectral density
  - Frequency bands
    - High frequency (HF) 0.15-0.4 Hz
    - Low frequency (LF) 0.04-.015 Hz
    - Very low frequency (VLF) 0.0033-.04 Hz

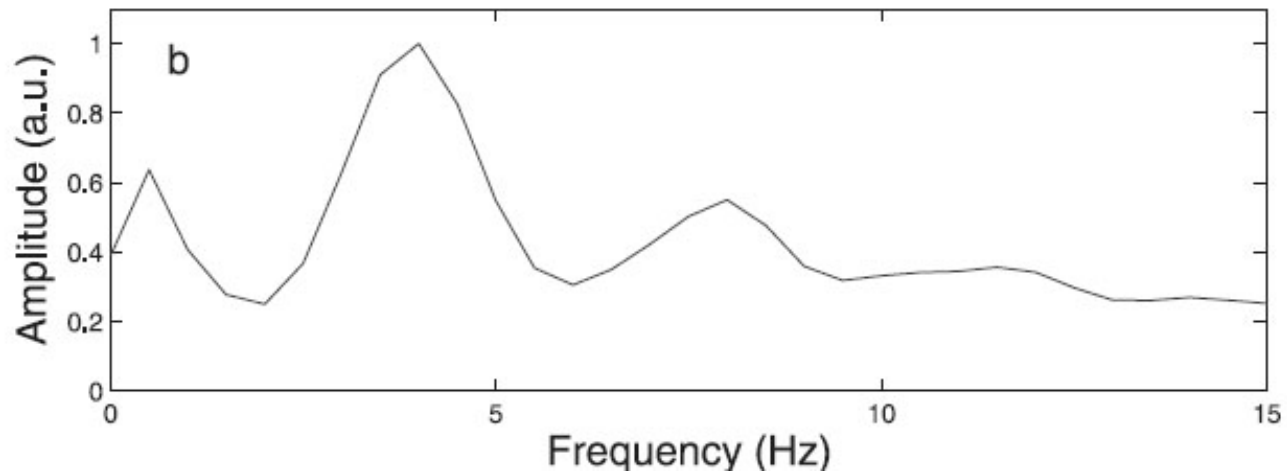
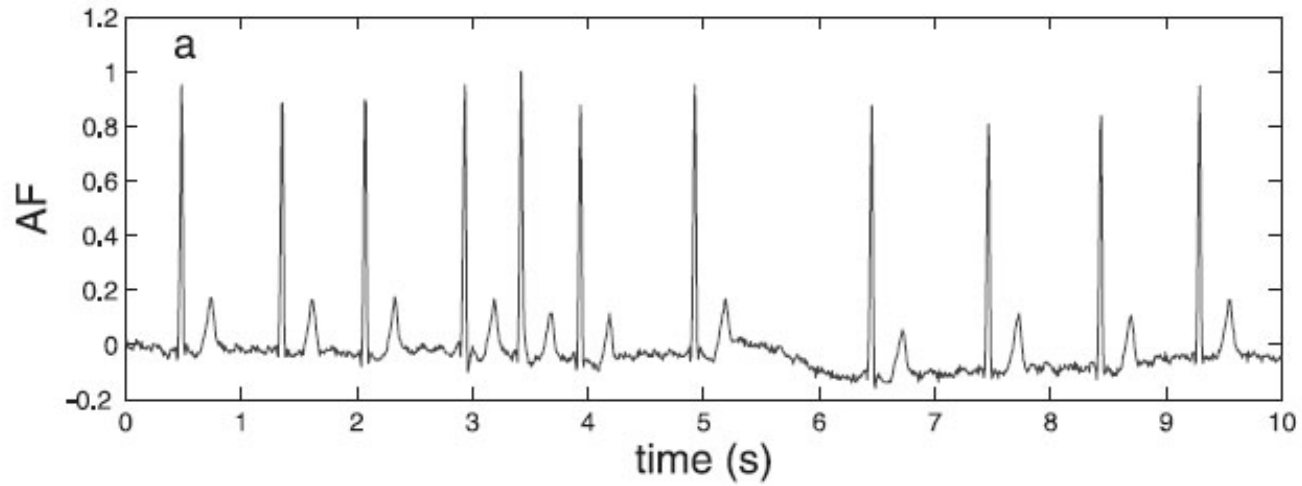
# ECG PSD - Frequency Domain



PSD: Power spectral density

# ECG\*

Atrial  
Fibrillation



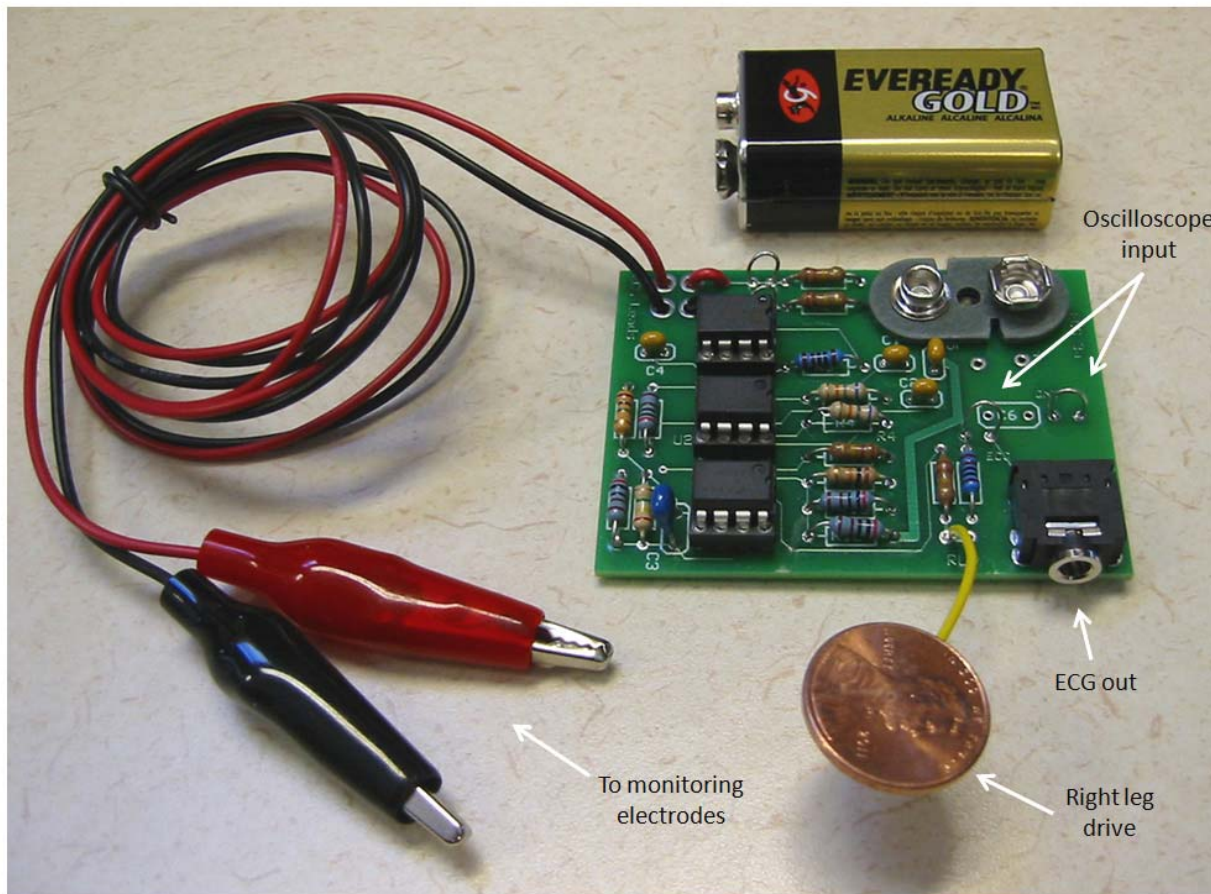
\* Clifford, Gari ECG Book

6.101 Spring 2020

Lecture 8

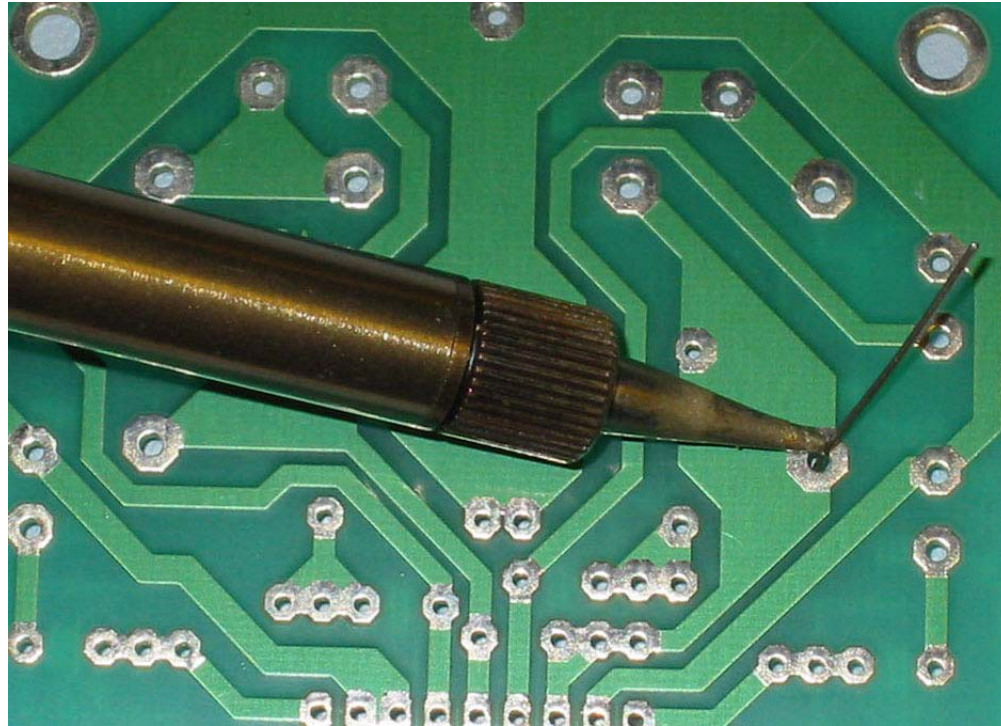
47

# Lab Exercise



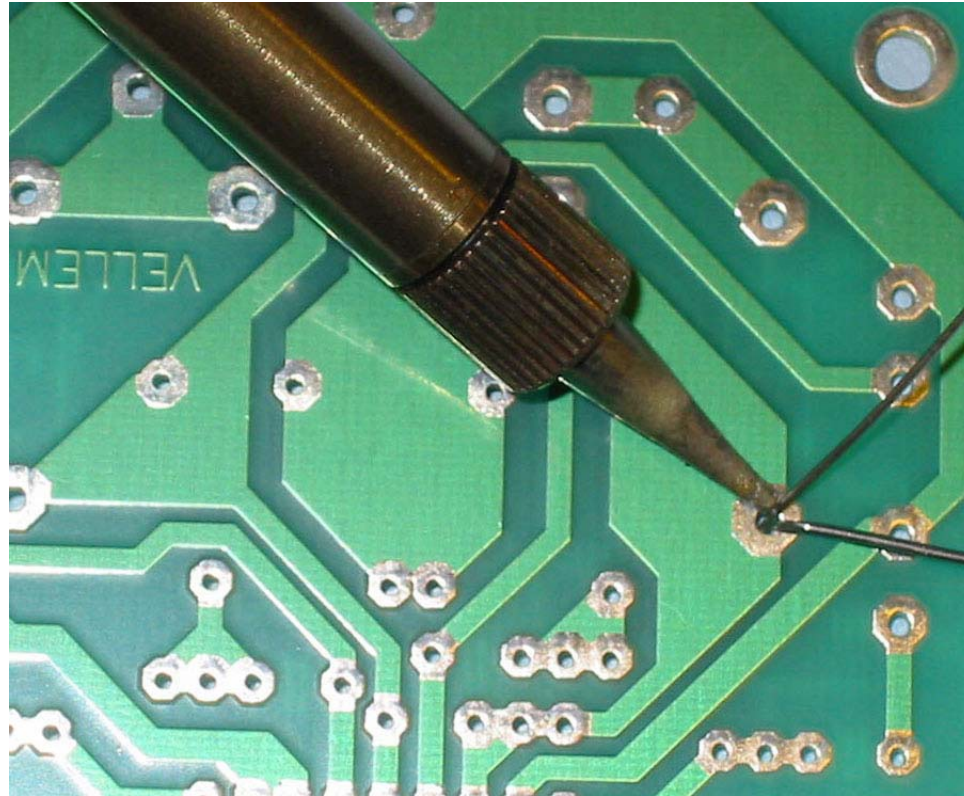
- Build ECG circuit
- Display ECG waveform on oscilloscope
- Perform MATLAB analysis
- Follow lab write up carefully!





*Turn on exhaust fan*

Apply heat to the circuit board but ok to initially melt a little bit of solder on the iron to improve heat conduction.



Apply solder to the component, not to the soldering.

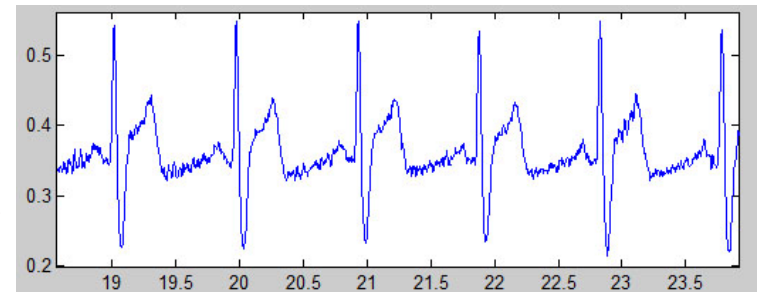
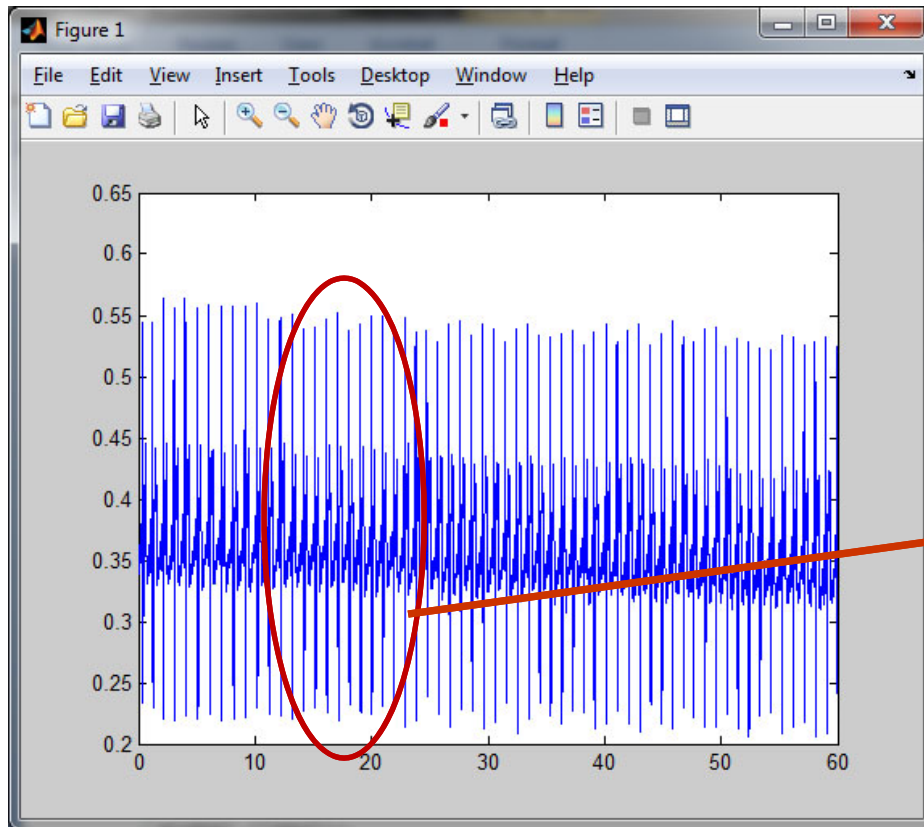
# ECG Exercise

- Sample ECG for 60 sec using MATLAB script; using your laptop or Win7 PC in 38-530
- Store data using save command
  - `save(FILENAME)` stores all variables from the current workspace in a MATLAB formatted binary file (MAT-file) called FILENAME.
  - `load(FILENAME)` restores saved variables.
- Calculate average heart rate in a 60 second interval.

# ECG Acquisition

```
%%  
recObj = audiorecorder(1000,16, 1);  
% 1000 sample rate, 16 bits, 1 channel  
  
record_time = 5;  
disp('Start ECG.')recordblocking(recObj, record_time);  
disp('End of Recording.');  
% Store data in double-precision array.  
myECG = getaudiodata(recObj);  
  
% create x axis in 1/1000 interval  
t = [0:1/1000:record_time-1/1000];  
  
% Plot the waveform.  
plot(t,myECG);  
% label x axis in seconds  
xlabel ('sec');  
%%  
save('mydata')
```

# ECG Figures



# Useful MATLAB commands

- `title ('ECG 60 seconds')` % set title of graph
- `xlabel ('time ms')`, `ylabel...`
- `save(FILENAME)` stores all variables from the current workspace in a MATLAB formatted binary file (MAT-file) called FILENAME.
- `length(X)` returns the length of vector X.
- `[peaks, loc]= findpeaks(v)` % gives peaks and location of peaks
- `diff_data = diff(X)`, for a vector X, is  $[X(2)-X(1), X(3)-X(2) \dots X(n)-X(n-1)]$
- `mean(X)` is the mean value of the elements in X
- `linspace(X1, X2, N)` generates N points between X1 and X2.

# Built-in Matlab function "findpeaks".

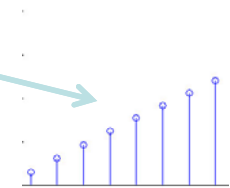
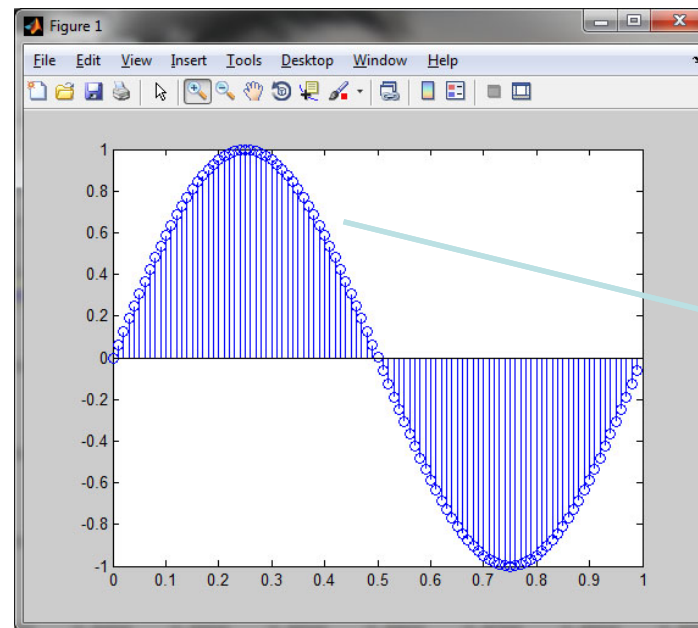
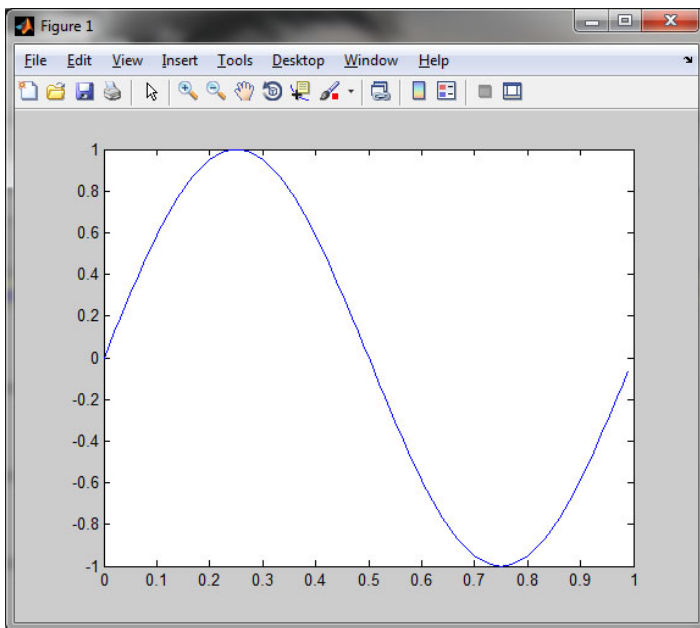
`[pks,locs]= findpeaks (X)` returns the indices "locs" at which the peaks occur as well as the value of the peaks "pks"

`findpeaks` also allows the user to specify the minimum peak height (MinPeakHeight) and the minimum peak distance (MinPeakDistance). For example:

```
[peaks,locs] = findpeaks(myECG, ' MinPeakHeight ',MPH)
                %enter a value for MPH
```

# MATLAB example $\sin(x)$

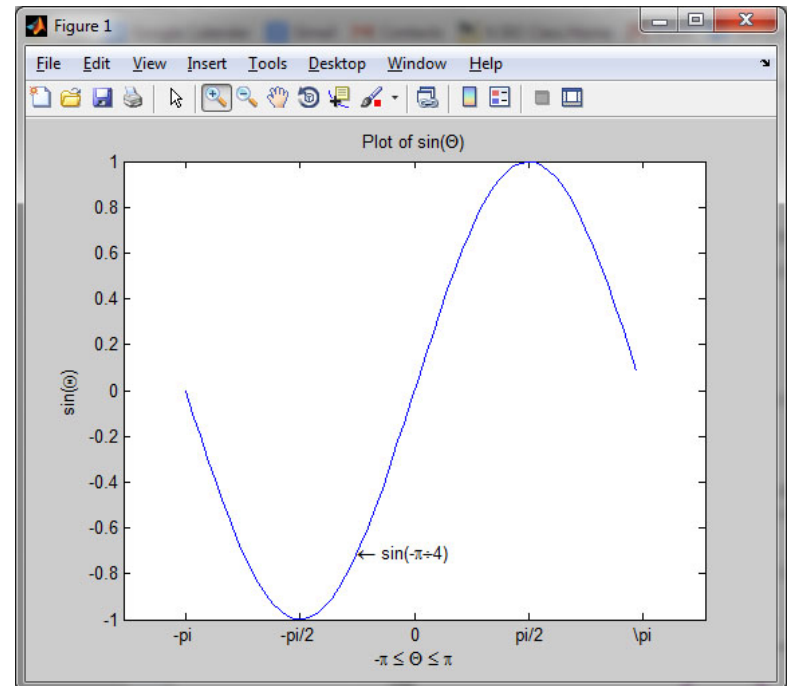
```
>> t=[0:1/100:1-1/100]; % create t from 0 to .99, 100 values  
>> x=sin(2*pi*t);  
>> plot(t, x);  
>> stem(t,x);  
>> shg
```





# MATLAB plot commands

- Example  $y = \sin(x)$   
`x = -pi:.1:pi; % -pi < x < pi in .1 increments`  
`y = sin(x);`  
`plot(x,y)`  
`set(gca,'XTick',-pi:pi/2:pi) % gca = graphics current axis; label x axis in pi/2 increment`  
`set(gca,'XTickLabel',{'-pi','-pi/2','0','pi/2','pi'}) % label the x axis`
- add axis labels and draw an arrow that points to the location on the graph where  $y = \sin(-\pi/4)$ :  
`xlabel('-\pi \leq \Theta \leq \pi')`  
`ylabel('sin(\Theta)')`  
`title('Plot of sin(\Theta)')`  
`text(-pi/4,sin(-pi/4),'\leftarrow sin(-\pi\div4)',`  
`'HorizontalAlignment','left')`



## A Matlab Cheat-sheet (MIT 18.06, Fall 2007)

### Basics:

save 'file.mat' save variables to *file.mat*  
 load 'file.mat' load variables from *file.mat*  
 diary on record input/output to file *diary*  
 diary off stop recording  
 whos list all variables currently defined  
 clear delete/undefine all variables  
 help command quick help on a given *command*  
 doc command extensive help on a given *command*

### Defining/changing variables:

$x = 3$  define variable  $x$  to be 3  
 $x = [1\ 2\ 3]$  set  $x$  to the  $1 \times 3$  row-vector (1,2,3)  
 $x = [1\ 2\ 3];$  same, but don't echo  $x$  to output  
 $x = [1;2;3]$  set  $x$  to the  $3 \times 1$  column-vector (1,2,3)  
 $A = [1\ 2\ 3\ 4; 5\ 6\ 7\ 8; 9\ 10\ 11\ 12];$   
 set  $A$  to the  $3 \times 4$  matrix with rows 1,2,3,4 etc.  
 $x(2) = 7$  change  $x$  from (1,2,3) to (1,7,3)  
 $A(2,1) = 0$  change  $A_{2,1}$  from 5 to 0

### Arithmetic and functions of numbers:

$3*4, 7+4, 2-6, 8/3$  multiply, add, subtract, and divide numbers  
 $3^7, 3^{(8+2i)}$  compute 3 to the 7th power, or 3 to the  $8+2i$  power  
 $\text{sqrt}(-5)$  compute the square root of  $-5$   
 $\text{exp}(12)$  compute  $e^{12}$   
 $\text{log}(3), \text{log}_{10}(100)$  compute the natural log (ln) and base-10 log ( $\log_{10}$ )  
 $\text{abs}(-5)$  compute the absolute value  $|-5|$   
 $\text{sin}(5*\text{pi}/3)$  compute the sine of  $5\pi/3$   
 $\text{besselj}(2,6)$  compute the Bessel function  $J_2(6)$

### Arithmetic and functions of vectors and matrices:

$x * 3$  multiply every element of  $x$  by 3  
 $x + 2$  add 2 to every element of  $x$   
 $x + y$  element-wise addition of two vectors  $x$  and  $y$   
 $A * y$  product of a matrix  $A$  and a vector  $y$   
 $A * B$  product of two matrices  $A$  and  $B$   
 $x * y$  not allowed if  $x$  and  $y$  are two column vectors!  
 $x .* y$  element-wise product of vectors  $x$  and  $y$   
 $A^3$  the square matrix  $A$  to the 3rd power  
 $x^3$  not allowed if  $x$  is not a square matrix!  
 $x.^3$  every element of  $x$  is taken to the 3rd power  
 $\text{cos}(x)$  the cosine of every element of  $x$   
 $\text{abs}(A)$  the absolute value of every element of  $A$   
 $\text{exp}(A)$   $e$  to the power of every element of  $A$   
 $\text{sqrt}(A)$  the square root of every element of  $A$   
 $\text{expm}(A)$  the matrix exponential  $e^A$   
 $\text{sqrtm}(A)$  the matrix whose square is  $A$

### Transposes and dot products:

$x.', A.'$  the transposes of  $x$  and  $A$   
 $x', A'$  the complex-conjugate of the transposes of  $x$  and  $A$   
 $x' * y$  the dot (inner) product of two *column* vectors  $x$  and  $y$   
 $\text{dot}(x,y), \text{sum}(x.*y)$  ...two other ways to write the dot product  
 $x * y'$  the *outer* product of two *column* vectors  $x$  and  $y$

### Constructing a few simple matrices:

$\text{rand}(12,4)$  a  $12 \times 4$  matrix with uniform random numbers in  $[0,1)$   
 $\text{randn}(12,4)$  a  $12 \times 4$  matrix with Gaussian random (center 0, variance 1)  
 $\text{zeros}(12,4)$  a  $12 \times 4$  matrix of zeros  
 $\text{ones}(12,4)$  a  $12 \times 4$  matrix of ones  
 $\text{eye}(5)$  a  $5 \times 5$  identity matrix  $I$  ("eye")  
 $\text{eye}(12,4)$  a  $12 \times 4$  matrix whose first 4 rows are the  $4 \times 4$  identity  
 $\text{linspace}(1.2, 4.7, 100)$  row vector of 100 equally-spaced numbers from 1.2 to 4.7  
 $7:15$  row vector of 7,8,9,...,14,15  
 $\text{diag}(x)$  matrix whose diagonal is the entries of  $x$  (and other elements = 0)

### Portions of matrices and vectors:

$x(2:12)$  the 2nd to the 12th elements of  $x$   
 $x(2:\text{end})$  the 2nd to the last elements of  $x$   
 $x(1:3:\text{end})$  every third element of  $x$ , from 1st to the last  
 $x(:)$  all the elements of  $x$   
 $A(5,:)$  the row vector of every element in the 5th row of  $A$   
 $A(5,1:3)$  the row vector of the first 3 elements in the 5th row of  $A$   
 $A(:,2)$  the column vector of every element in the 2nd column of  $A$   
 $\text{diag}(A)$  column vector of the diagonal elements of  $A$

### Solving linear equations:

$A \setminus b$  for  $A$  a matrix and  $b$  a column vector, the solution  $x$  to  $Ax=b$   
 $\text{inv}(A)$  the inverse matrix  $A^{-1}$   
 $[L,U,P] = \text{lu}(A)$  the LU factorization  $PA=LU$   
 $\text{eig}(A)$  the eigenvalues of  $A$   
 $[V,D] = \text{eig}(A)$  the columns of  $V$  are the eigenvectors of  $A$ , and the diagonals  $\text{diag}(D)$  are the eigenvalues of  $A$

### Plotting:

$\text{plot}(y)$  plot  $y$  as the  $y$  axis, with 1,2,3,... as the  $x$  axis  
 $\text{plot}(x,y)$  plot  $y$  versus  $x$  (must have same length)  
 $\text{plot}(x,A)$  plot columns of  $A$  versus  $x$  (must have same # rows)  
 $\text{loglog}(x,y)$  plot  $y$  versus  $x$  on a log-log scale  
 $\text{semilogx}(x,y)$  plot  $y$  versus  $x$  with  $x$  on a log scale  
 $\text{semilogy}(x,y)$  plot  $y$  versus  $x$  with  $y$  on a log scale  
 $\text{fplot}(@(\text{x}) \dots \text{expression}, [a,b])$   
 plot some expression in  $x$  from  $x=a$  to  $x=b$   
 $\text{axis equal}$  force the  $x$  and  $y$  axes of the current plot to be scaled equally  
 $\text{title}('A Title')$  add a title  $A Title$  at the top of the plot  
 $\text{xlabel}('blah')$  label the  $x$  axis as *blah*  
 $\text{ylabel}('blah')$  label the  $y$  axis as *blah*  
 $\text{legend}('foo', 'bar')$  label 2 curves in the plot *foo* and *bar*  
 $\text{grid}$  include a grid in the plot  
 $\text{figure}$  open up a new figure window

# ECG Project Ideas

- Transmit ECG wirelessly
  - RF (AM, FM)
  - Laser beam
- Display ECG using galvanometer or TFT Teensy
- Add sound, alarm
- 2014 Project Video
  - Send ECG via fiber optic cable
  - Display heart rate via analog meter
  - Set alarms
  - Output tone proportional to heart rate