# 6.1800 Spring 2024

Lecture #18: Isolation

what do we want from isolation, and how do we get it?

## 6.1800 in the news

## How the Solar Eclipse Will Impact Electricity Supplies

This April's total solar eclipse will present a unique challenge to power grid operators because of the decline in solar power generation

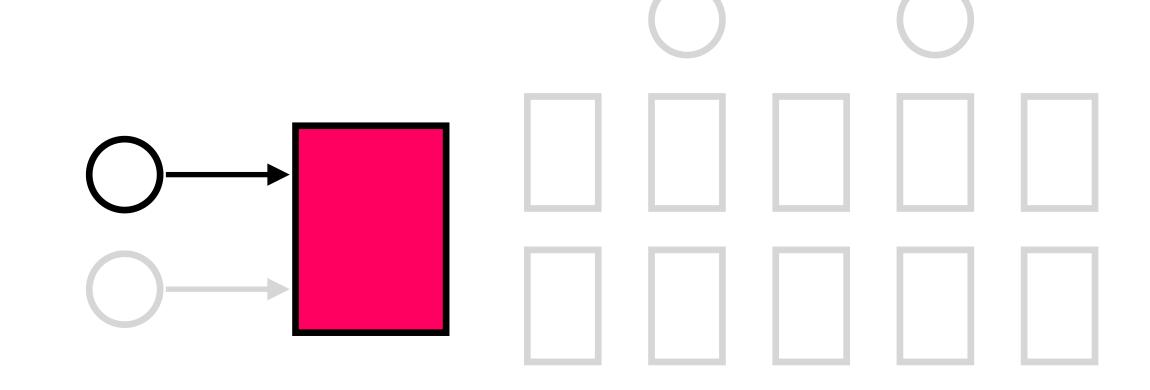
BY VAHE PEROOMIAN & THE CONVERSATION US

To plan for an eclipse, electrical system operators need to figure out how much the energy production will drop and how much power people will draw from the reserves. On the day of the 2017 total solar eclipse, for example, solar power generation in the U.S. <u>dropped 25%</u> below average.

Because solar power production falls quickly during the eclipse's peak, grid operators may need to tap into reserves at a rate that may strain the <u>electrical transmission lines</u>. To try to keep things running smoothly, grid operators will rely on local reserves and minimize power transfer <u>between grids</u> during the event. This should lessen the burden on transmission lines in local grids and prevent temporary blackouts.



our goal is to build **reliable systems from unreliable components**. we want to build systems that serve many clients, store a lot of data, perform well, all while keeping availability high



**transactions** — which provide **atomicity** and **isolation** — make it easier for us to reason about failures

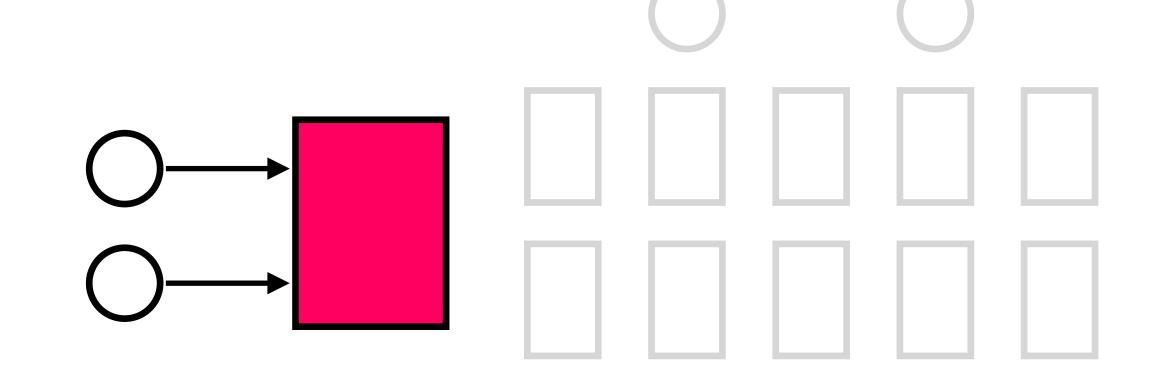
our job in lecture is to understand how a system *implements* these two abstractions. how do our systems guarantee atomicity? how do they guarantee isolation?

atomicity: provided by logging, which gives better performance than shadow copies\* at the cost of some added complexity

\* shadow copies are used in some systems

isolation: we don't really have this yet (coarse-grained locks perform poorly; fine-grained locks are difficult to reason about)

our goal is to build **reliable systems from unreliable components**. we want to build systems that serve many clients, store a lot of data, perform well, all while keeping availability high



**transactions** — which provide **atomicity** and **isolation** — make it easier for us to reason about failures

our job in lecture is to understand how a system *implements* these two abstractions. how do our systems guarantee atomicity? how do they guarantee isolation?

atomicity: provided by logging, which gives better performance than shadow copies\* at the cost of some added complexity

\* shadow copies are used in some systems

isolation: provided by two-phase locking

goal: run transactions T1, T2, ..., TN concurrently, and have it "appear" as if they ran sequentially

what does this even mean?

when we run two transactions concurrently, we'll always run the steps of a single transaction in order (e.g., T1.1 before T1.2). but we might interleave steps of T2 in between steps of T1.

naive approach: actually run them sequentially, via (perhaps) a single global lock

goal: run transactions T1, T2 concurrently, and have it "appear" as if they ran sequentially

```
T1.1 read(x)
T1.2 tmp = read(y)
T1.3 write(y, tmp+10)
T2.1 write(x, 20)
T2.2 write(y, 30)
T1.1 read(x)
T2.1 write(x, 20)
T1.2 tmp = read(y)
T2.2 write(y, 30)
T1.3 write(y, tmp+10)

result: x=20; y=30
result: x=20; y=40
```

let's look at a few different schedules of T1 and T2 (this is not an exhaustive list)

```
T1.1 read(x)
T2.1 write(x, 20)
                                                                                  T1.1 read(x)
                                                                                  T2.1 write(x, 20)
T1.1 read(x)
                                         T2.1 write(x, 20)
T2.2 write(y, 30)
                                        T1.2 \text{ tmp} = \text{read}(y)
                                                                                  T2.2 write(y, 30)
T1.2 \text{ tmp} = \text{read}(y)
                                        T2.2 write(y, 30)
                                                                                 T1.2 \text{ tmp} = \text{read}(y)
T1.3 write(y, tmp+10)
                                        T1.3 write(y, tmp+10)
                                                                                  T1.3 write(y, tmp+10)
result: x=20; y=40
                                                                                  result: x=20; y=40
                                         result: x=20; y=10
```

goal: run transactions T1, T2 concurrently, and have it "appear" as if they ran sequentially

```
T1.1 read(x)
T1.2 tmp = read(y)
T1.3 write(y, tmp+10)
T2.1 write(x, 20)
T2.1 write(x, 20)
T2.1 write(x, 20)
T2.2 tmp = read(y)
T2.2 write(y, 30)
T1.3 write(y, tmp+10)

result: x=20; y=30
result: x=20; y=40
```

let's look at a few different schedules of T1 and T2 (this is not an exhaustive list)

```
T1.1 read(x)
T2.1 write(x, 20)
                                                                                  T1.1 read(x)
                                                                                  T2.1 write(x, 20)
T1.1 read(x)
                                         T2.1 write(x, 20)
T2.2 write(y, 30)
                                        T1.2 \text{ tmp} = \text{read}(y)
                                                                                  T2.2 write(y, 30)
T1.2 \text{ tmp} = \text{read}(y)
                                        T2.2 write(y, 30)
                                                                                 T1.2 \text{ tmp} = \text{read}(y)
T1.3 write(y, tmp+10)
                                        T1.3 write(y, tmp+10)
                                                                                  T1.3 write(y, tmp+10)
result: x=20; y=40
                                                                                  result: x=20; y=40
                                         result: x=20; y=10
```

it seems like the middle schedule is out; x=20; y=10 is not possible in either of our serialized schedules

goal: run transactions T1, T2 concurrently, and have it "appear" as if they ran sequentially

```
T1.1 read(x)
T1.2 tmp = read(y)
T1.3 write(y, tmp+10)
T2.1 write(x, 20)
T2.1 write(x, 20)
T2.1 write(x, 20)
T2.2 write(y, 30)
T1.3 write(y, tmp+10)

result: x=20; y=30
T1 reads x=0; y=0
T1 reads x=20; y=30
T1 reads x=20; y=30
```

let's look at a few different schedules of T1 and T2 (this is not an exhaustive list)

```
T1.1 \text{ read}(x)
T2.1 write(x, 20)
                                                                                T1.1 read(x) // x=0
                                                                                T2.1 write(x, 20)
T1.1 read(x)
                                        T2.1 write(x, 20)
T2.2 write(y, 30)
                                        T1.2 \text{ tmp} = \text{read}(y)
                                                                                T2.2 write(y, 30)
T1.2 \text{ tmp} = \text{read}(y)
                                       T2.2 write(y, 30)
                                                                                T1.2 \text{ tmp} = \text{read}(y) // y=30
T1.3 write(y, tmp+10)
                                                                                T1.3 write(y, tmp+10)
                                        T1.3 write(y, tmp+10)
result: x=20; y=40
                                        result: x=20; y=10
                                                                                result: x=20; y=40
```

but take a closer look at the third schedule; in the first step, T1.1 reads x=0, and in the fourth step, T1.2 reads y=30. those two reads together aren't possible in either sequential schedule. is that okay?

### it depends.

there are many ways for multiple transactions to "appear" to have been run in sequence; we say there are different notions of **serializability**. what type of serializability you want depends on what your application needs.

conflicts: two operations conflict if they operate on the same object and at least one of them is a write

```
conflicts

T1.1 read(x) and T2.1 write(x, 20)
T1.2 tmp = read(y) and T2.2 write(y, 30)
T1.3 write(y, tmp+10) and T2.2 write(y, 30)
```

in any schedule, two conflicting operations A and B will have an order: either A is executed before B, or B is executed before A. we'll call this the **order** of the conflict (in that schedule).

```
T1.1 read(x)

T1.2 tmp = read(y)

T1.3 write(y, tmp+10)

T2.1 write(x, 20)

T2.2 write(y, 30)

T3.2 write(y, 30)

T3.3 write(y, 10)

T3.4 read(x) -> T2.1 write(x, 20)

T3.5 tmp = read(y) -> T2.2 write(y, 30)

T3.6 write(y, 10)

T3.7 write(y, 10)

T3.8 write(y, 10)

T3.9 write(y, 30)
```

conflicts: two operations conflict if they operate on the same object and at least one of them is a write

```
conflicts

T1.1 read(x) and T2.1 write(x, 20)

T1.2 tmp = read(y) and T2.2 write(y, 30)

T1.3 write(y, tmp+10) and T2.2 write(y, 30)
```

in any schedule, two conflicting operations A and B will have an order: either A is executed before B, or B is executed before A. we'll call this the **order** of the conflict (in that schedule).

```
T2.1 write(x, 20)
T1.1 \text{ read}(x)
                                order of conflicts
                                                                                                          order of conflicts
                                                                      T2.2 write(y, 30)
T1.2 \text{ tmp} = \text{read}(y)
                                 T1.1 \rightarrow T2.1
                                                                                                            T2.1 -> T1.1
                                                                      T1.1 read(x)
T1.3 write(y, tmp+10)
                                 T1.2 -> T2.2
                                                                                                            T2.2 -> T1.2
                                                                      T1.2 \text{ tmp} = \text{read}(y)
T2.1 write(x, 20)
                                 T1.3 \rightarrow T2.2
                                                                                                            T2.2 \rightarrow T1.3
                                                                      T1.3 write(y, tmp+10)
T2.2 write(y, 30)
```

notice that, if we execute T1 and T2 serially, then in the ordering of the conflicts we see either *all* of T1's operations occurring first, or *all* of T2's operations occurring first

conflicts: two operations conflict if they operate on the same object and at least one of them is a write

```
conflicts

T1.1 read(x) and T2.1 write(x, 20)

T1.2 tmp = read(y) and T2.2 write(y, 30)

T1.3 write(y, tmp+10) and T2.2 write(y, 30)
```

in any schedule, two conflicting operations A and B will have an order: either A is executed before B, or B is executed before A. we'll call this the **order** of the conflict (in that schedule).

```
T1.1 read(x)
T2.1 write(x, 20)
                               order of conflicts
                                                                                                          order of conflicts
                                                                      T2.1 write(x, 20)
T1.1 \text{ read}(x)
                                 T2.1 -> T1.1
                                                                                                            T1.1 \rightarrow T2.1
                                                                      T2.2 write(y, 30)
T2.2 write(y, 30)
                                 T2.2 -> T1.2
                                                                                                            T2.2 -> T1.2
                                                                      T1.2 \text{ tmp} = \text{read}(y)
T1.2 \text{ tmp} = \text{read}(y)
                                 T2.2 \rightarrow T1.3
                                                                                                            T2.2 \rightarrow T1.3
                                                                      T1.3 write(y, tmp+10)
T1.3 write(y, tmp+10)
```

on the left schedule, the order of conflicts is the same as if we had run T2 entirely before T1; on the right schedule, the order of conflicts isn't the same as either serial schedule

a schedule is **conflict serializable** if the order of all of its conflicts is the same as the order of the conflicts in some sequential schedule.

```
conflicts

T1.1 read(x) and T2.1 write(x, 20)

T1.2 tmp = read(y) and T2.2 write(y, 30)

T1.3 write(y, tmp+10) and T2.2 write(y, 30)
```

this schedule is conflict serializable

```
T1.1 read(x)

T2.1 write(x, 20)

T2.2 write(y, 30)

T1.2 tmp = read(y)

T1.3 write(y, tmp+10)

order of conflicts

T1.1 -> T2.1

T2.2 -> T1.2
```

this schedule is **not** conflict serializable

a schedule is **conflict serializable** if the order of all of its conflicts is the same as the order of the conflicts in some sequential schedule.

```
conflicts

T1.1 read(x) and T2.1 write(x, 20)

T1.2 tmp = read(y) and T2.2 write(y, 30)

T1.3 write(y, tmp+10) and T2.2 write(y, 30)
```

we can express the order of conflicts more succinctly with a **conflict graph**: there is an edge from  $T_i$  to  $T_j$  if and only if  $T_i$  and  $T_j$  have a conflict between them and the first step in the conflict occurs in  $T_i$ 

```
T2.1 write(x, 20) conflict graph
T1.1 read(x)
T2.2 write(y, 30)
T1.2 tmp = read(y)
T1.3 write(y, tmp+10)
```

```
this schedule is conflict serializable
```

```
T1.1 read(x)

T2.1 write(x, 20)

T2.2 write(y, 30)

T1.2 tmp = read(y)

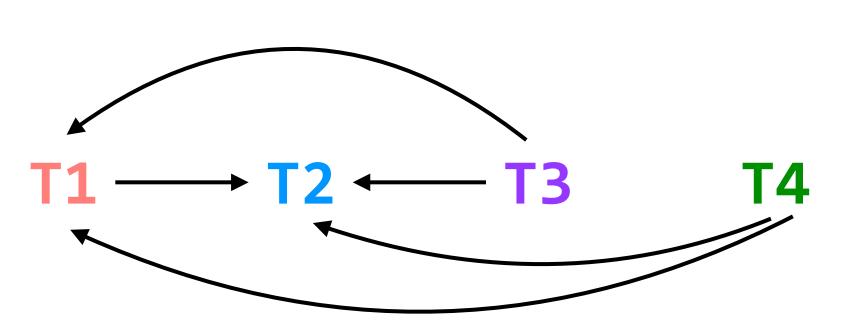
T1.3 write(y, tmp+10)
```

this schedule is **not** conflict serializable

#### interlude: practice with conflict graphs

```
T1
                                                                   T4
                       T2
                                             T3
begin
                                             begin
                       begin
                                                                   begin
T1.1 read(x)
                       T2.1 write(x, 20)
                                            T3.1 read(y)
                                                                   T4.1 read(y)
                                                                   commit
T1.2 write(y, 10)
                       T2.2 write(y, 30)
                                             T3.2 write(z, 40)
commit
                       commit
                                             commit
```

```
T1.1 read(x)
T2.1 write(x, 20)
T3.1 read(y)
T4.1 read(y)
T1.2 write(y, 10)
T2.2 write(y, 30)
T3.2 write(z, 40)
```



## what is the conflict graph for this schedule?

a schedule is **conflict serializable** if the order of all of its conflicts is the same as the order of the conflicts in some sequential schedule.

this schedule is conflict serializable

```
conflicts

T1.1 read(x) and T2.1 write(x, 20)

T1.2 tmp = read(y) and T2.2 write(y, 30)

T1.3 write(y, tmp+10) and T2.2 write(y, 30)
```

this schedule is **not** conflict serializable

we can express the order of conflicts more succinctly with a **conflict graph**: there is an edge from  $T_i$  to  $T_j$  if and only if  $T_i$  and  $T_j$  have a conflict between them and the first step in the conflict occurs in  $T_i$ 

```
T2.1 write(x, 20) conflict graph

T1.1 read(x)

T2.1 write(x, 20)

T2.2 write(y, 30)

T2 \rightarrow T1

T1.2 tmp = read(y)

T1.3 write(y, tmp+10)

T1.1 read(x)

T2.1 write(x, 20)

T2.2 write(y, 30)

T2 \rightarrow T1

T1.3 write(y, tmp+10)
```

a schedule is conflict serializable if and only if it has an acyclic conflict graph

a schedule is **conflict serializable** if the order of all of its conflicts is the same as the order of the conflicts in some sequential schedule.

```
conflicts

T1.1 read(x) and T2.1 write(x, 20)
T1.2 tmp = read(y) and T2.2 write(y, 30)
T1.3 write(y, tmp+10) and T2.2 write(y, 30)
```

## our goal (in lecture) is to run transactions concurrently, but to produce a schedule that is conflict serializable

how does a system do that? one way might be to generate all possible schedules and check their conflict graphs, and run one of the schedules with an acyclic conflict graph, but this will take some time

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

```
T1
begin
T1.1 read(x)
T1.2 tmp = read(y)
T1.3 write(y, tmp+10)
commit
```

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

```
begin
acquire(x.lock)
acquire(y.lock)
T1.1 read(x)
T1.2 tmp = read(y)
T1.3 write(y, tmp+10)
release(x.lock)
release(y.lock)
commit
```

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

```
begin
acquire(x.lock)
T1.1 read(x)
acquire(y.lock)
T1.2 tmp = read(y)
T1.3 write(y, tmp+10)
release(x.lock)
release(y.lock)
commit
```

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

```
T1
begin
acquire(x.lock)
T1.1 read(x)
acquire(y.lock)
release(x.lock)
T1.2 tmp = read(y)
T1.3 write(y, tmp+10)
release(y.lock)
commit
```

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

2PL still gives us options for where we place the locks

```
begin
acquire(x.lock)
T1.1 read(x)
release(x.lock)
acquire(y.lock)
T1.2 tmp = read(y)
T1.3 write(y, tmp+10)
release(y.lock)
commit
```

we can't do this; it breaks the third rule of 2PL

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

if we release locks after commit, that is technically *strict* two-phase locking

2PL still gives us options for where we place the locks

```
T2
                          begin
begin
                          acquire(x.lock)
acquire(x.lock)
                          T2.1 write(x, 20)
T1.1 read(x)
                          acquire(y.lock)
acquire(y.lock)
                          T2.2 write(y, 30)
T1.2 \text{ tmp} = \text{read}(y)
                          commit
T1.3 write(y, tmp+10)
                          release(x.lock)
commit
                          release(y.lock)
release(x.lock)
release(y.lock)
```

notice that with this approach to 2PL, we will effectively force these two transactions to run serially. we'll address that in a few slides!

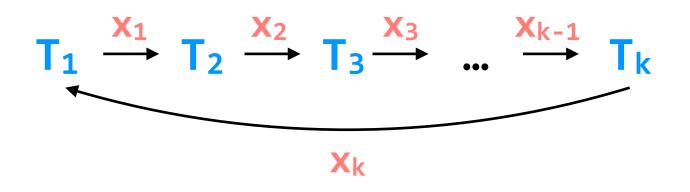
there are some lingering issues related to possible deadlocks and performance; we'll deal with those, but let's first try to understand why 2PL produces a conflict-serializable schedule

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

#### 2PL produces a conflict-serializable schedule

(equivalently, 2PL produces a conflict graph without a cycle)

proof: suppose not. then a cycle exists in the conflict graph



T<sub>1</sub> acquires x<sub>1</sub>.lock
T<sub>2</sub> acquires x<sub>1</sub>.lock

T<sub>2</sub> acquires x<sub>2</sub>.lock
T<sub>3</sub> acquires x<sub>2</sub>.lock

T<sub>k</sub> acquires x<sub>k</sub>.lock
T<sub>1</sub> acquires x<sub>k</sub>.lock

to cause the conflict, each pair of conflicting transactions must have some shared variable that they conflict on

in the schedule, each pair of transactions needs to acquire a lock on their shared variable

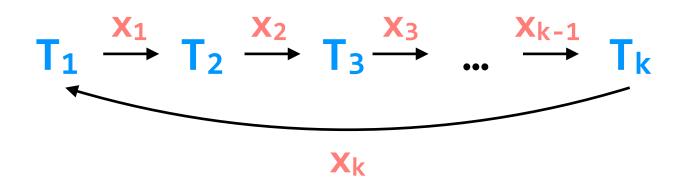
the order of the conflict tells us which transaction acquired the lock first

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

#### 2PL produces a conflict-serializable schedule

(equivalently, 2PL produces a conflict graph without a cycle)

proof: suppose not. then a cycle exists in the conflict graph



T<sub>1</sub> acquires x<sub>1</sub>.lock

T<sub>1</sub> releases x<sub>1</sub>.lock

T<sub>2</sub> acquires x<sub>1</sub>.lock

T<sub>2</sub> acquires x<sub>2</sub>.lock

T<sub>3</sub> acquires x<sub>2</sub>.lock

\_

T<sub>k</sub> acquires x<sub>k</sub>.lock

T<sub>1</sub> acquires x<sub>k</sub>.lock

to cause the conflict, each pair of conflicting transactions must have some shared variable that they conflict on

in the schedule, each pair of transactions needs to acquire a lock on their shared variable

the order of the conflict tells us which transaction acquired the lock first

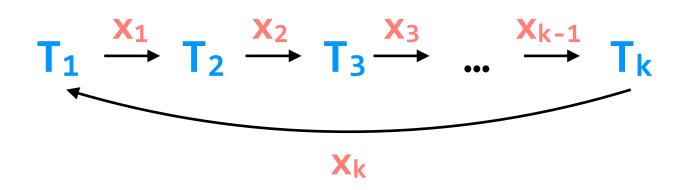
in order for the schedule to progress, T<sub>1</sub> must have released its lock on x<sub>1</sub> before T<sub>2</sub> acquired it

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

#### 2PL produces a conflict-serializable schedule

(equivalently, 2PL produces a conflict graph without a cycle)

proof: suppose not. then a cycle exists in the conflict graph



T<sub>1</sub> acquires x<sub>1</sub>.lock

T<sub>1</sub> releases x<sub>1</sub>.lock

T<sub>2</sub> acquires x<sub>1</sub>.lock

T<sub>2</sub> acquires x<sub>2</sub>.lock

T<sub>3</sub> acquires x<sub>2</sub>.lock

•••

T<sub>k</sub> acquires x<sub>k</sub>.lock
T<sub>1</sub> acquires x<sub>k</sub>.lock

to cause the conflict, each pair of conflicting transactions must have some shared variable that they conflict on

in the schedule, each pair of transactions needs to acquire a lock on their shared variable

the order of the conflict tells us which transaction acquired the lock first

in order for the schedule to progress, T<sub>1</sub> must have released its lock on x<sub>1</sub> before T<sub>2</sub> acquired it

contradiction: this is not a valid 2PL schedule

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

#### problem: 2PL can result in deadlock

```
T2
                          begin
begin
                          acquire(x.lock)
acquire(x.lock)
                          T2.1 write(x, 20)
T1.1 read(x)
                          acquire(y.lock)
acquire(y.lock)
                          T2.2 write(y, 30)
T1.2 \text{ tmp} = \text{read}(y)
                          commit
T1.3 write(y, tmp+10)
                          release(x.lock)
commit
                          release(y.lock)
release(x.lock)
release(y.lock)
```

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

```
problem: 2PL can result in deadlock
```

```
T2
                          begin
begin
                          acquire(y.lock)
acquire(x.lock)
                          T2.1 write(y, 30)
T1.1 read(x)
                          acquire(x.lock)
acquire(y.lock)
                          T2.2 write(x, 20)
T1.2 \text{ tmp} = \text{read}(y)
T1.3 write(y, tmp+10)
                          commit
                          release(x.lock)
commit
                          release(y.lock)
release(x.lock)
release(y.lock)
```

for example, suppose T2 wrote to y before x

one solution to this problem is a global ordering on locks; but we hate that! a better solution is to take advantage of atomicity and abort one of the transactions

- 1. each shared variable has a lock
- 2. before **any** operation on a variable, the transaction must acquire the corresponding lock
- 3. after a transaction releases a lock, it may **not** acquire any other locks

#### problem: performance

```
T2
                          begin
begin
                          acquire(x.lock)
acquire(x.lock)
                          T2.1 write(x, 20)
T1.1 read(x)
                          acquire(y.lock)
acquire(y.lock)
                          T2.2 write(y, 30)
T1.2 \text{ tmp} = \text{read}(y)
                          commit
T1.3 write(y, tmp+10)
                          release(x.lock)
commit
                          release(y.lock)
release(x.lock)
```

release(y.lock)

with reader-/writer- locks

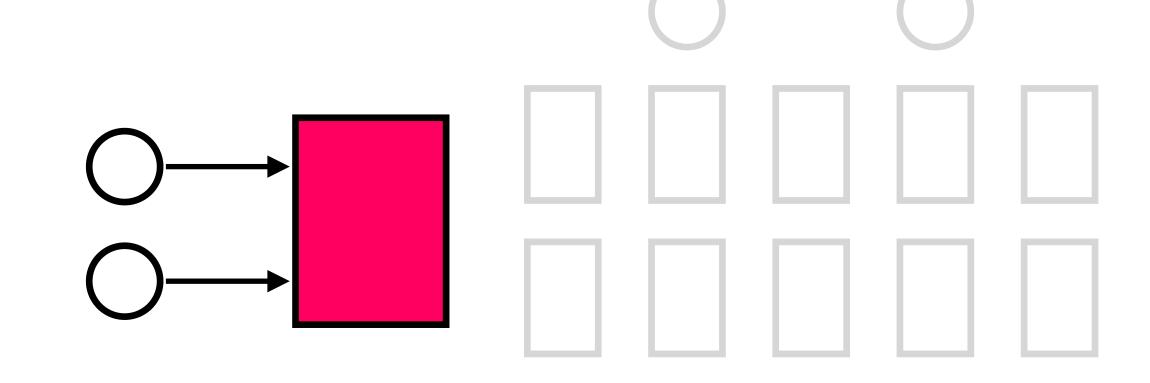
- each shared variable has two locks: one for reading, one for writing
- 2. before **any** operation on a variable, the transaction must acquire the appropriate lock
- 3. multiple transactions can hold reader locks for the same variable at once; a transaction can only hold a writer lock for a variable if there are *no* other locks held for that variable
- 4. after a transaction releases a lock, it may **not** acquire any other locks

#### problem: performance

```
T1
                            T2
begin
                            begin
acquire(x.reader_lock)
                            acquire(x.writer_lock)
T1.1 read(x)
                            T2.1 write(x, 20)
acquire(y.reader_lock)
                            acquire(y.writer_lock)
T1.2 \text{ tmp} = \text{read}(y)
                            T2.2 write(y, 30)
acquire(y.writer_lock)
                            commit
                            release(x.writer_lock)
T1.3 write(y, tmp+10)
                            release(y.writer_lock)
commit
release(x.reader_lock)
release(y.reader_lock)
release(y.writer_lock)
```

we will often release reader locks before the commit

our goal is to build **reliable systems from unreliable components**. we want to build systems that serve many clients, store a lot of data, perform well, all while keeping availability high



**transactions** — which provide **atomicity** and **isolation** — make it easier for us to reason about failures

our job in lecture is to understand how a system *implements* these two abstractions. how do our systems guarantee atomicity? how do they guarantee isolation?

atomicity: provided by logging, which gives better performance than shadow copies\* at the cost of some added complexity

\* shadow copies are used in some systems

isolation: provided by two-phase locking

different types of **serializability** allow us to specify precise what we want when we run transactions in parallel. **conflict-serializability** is a relatively strict form of serializability.

**two-phase locking** allows us to generate conflictserializable schedules. we can improve its performance by allowing concurrent reads via reader- and writer- locks.

2PL does not produce every possible conflict-serializable schedule — that's okay! the claim is only that the schedules it does produce are conflict-serializable