

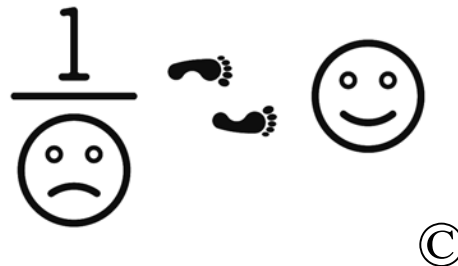
Precision Machine Design

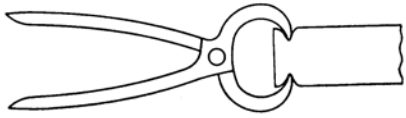
Topic 2

*FUN*daMENTAL Principles

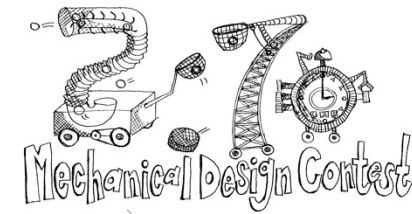
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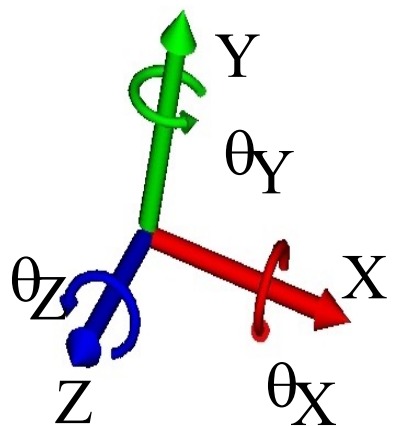
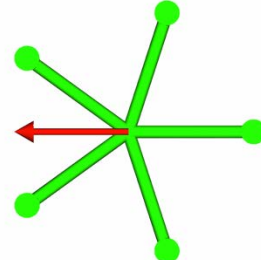
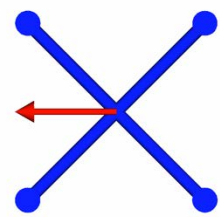
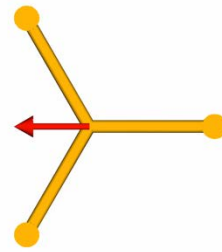
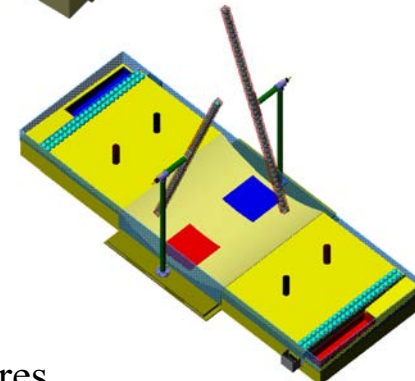
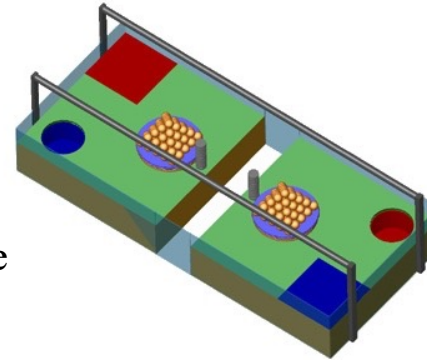


FUNda**MENTAL** Principles



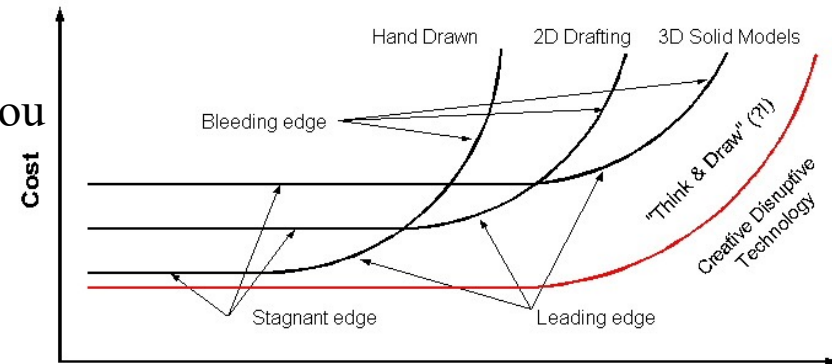
Topics

- Occam's Razor
- Newton's Laws
- Conservation of Energy
- Saint-Venant's Principle
- Golden Rectangle
- Abbe's Principle
- Maxwell & Reciprocity
- Self-Principles
- Stability
- Symmetry
- Parallel Axis Theorem
- Accuracy, Repeatability, Resolution
- Sensitive Directions & Reference Features
- Structural Loops
- Preload
- Centers of Action
- Exact Constraint Design
- Elastically Averaged Design
- Stick Figures

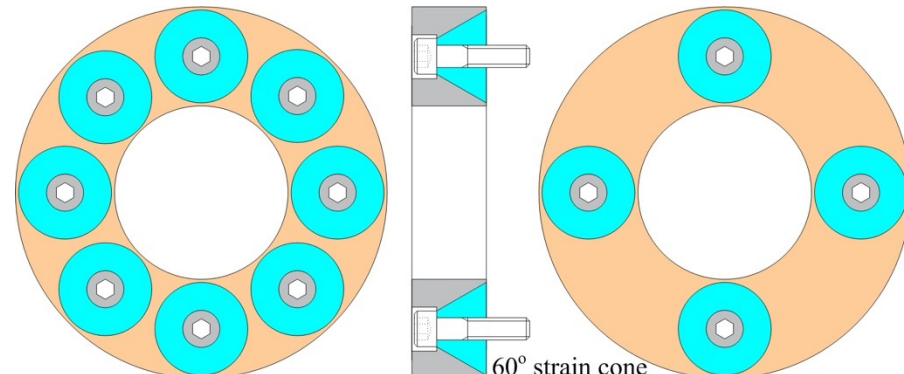
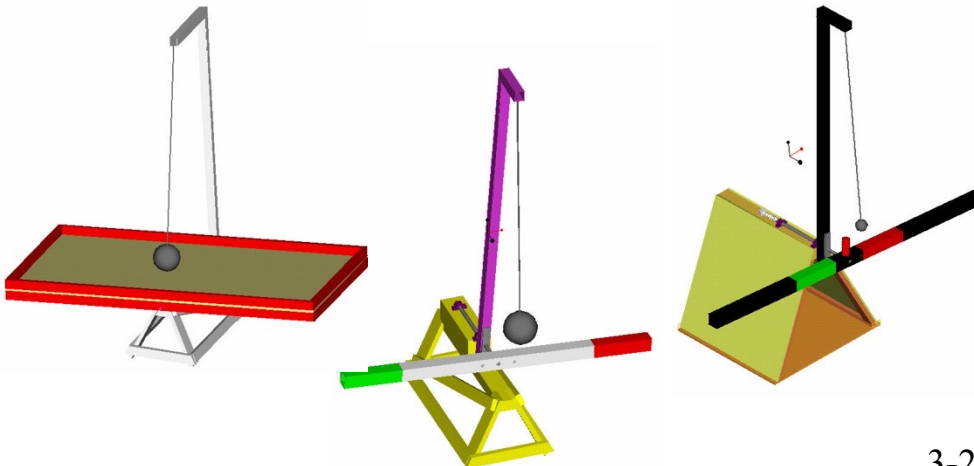


Occam's Razor

- William of Occam (Ockham) (1284-1347) was an English philosopher and theologian
 - Ockham stressed the Aristotelian principle that *entities must not be multiplied beyond what is necessary* (see Maudslay's maxims on page 1-4)
 - “The medieval rule of parsimony, or principle of economy, frequently used by Ockham came to be known as **Ockham's razor**. The rule, which said that *plurality should not be assumed without necessity* (or, in modern English, *keep it simple, stupid*), was used to eliminate many pseudo-explanatory entities” (<http://wotug.ukc.ac.uk/parallel/www/occam/occam-bio.html>)
 - **A problem should be stated in its most basic and simplest terms**
 - **The simplest theory that fits the facts of a problem is the one that should be selected**
 - **Limit Analysis can be used to check ideas**
- Use fundamental principles as catalysts to help you
 - Keep It Super Simple (KISS)
 - Make It Super Simple (MISS)
 - “Silicon is cheaper than cast iron” (Don Blomquist)



Performance



Newton's Laws

- Invaluable design catalysts that can help launch many an idea!
 - (The only real “law” perhaps is 300,000 km/second!)
- Conservation of linear momentum
 - If no force is applied, then momentum is constant
- Conservation of angular momentum
 - If no torque is applied to a body about an axis, angular momentum is constant about that axis
 - A force coincident with an axis does not apply torque about that axis

See *Projectile_motion.xls*

Sir Isaac Newton (1642 - 1727)
Isaac probably would have LOVED snowboarding!

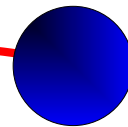
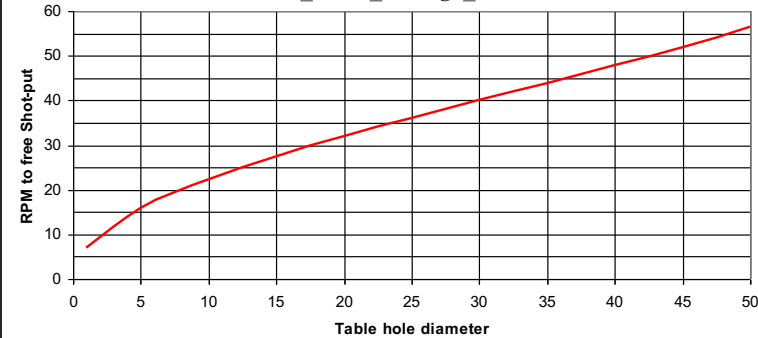
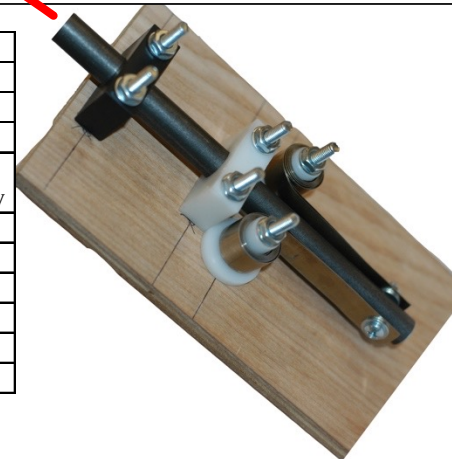
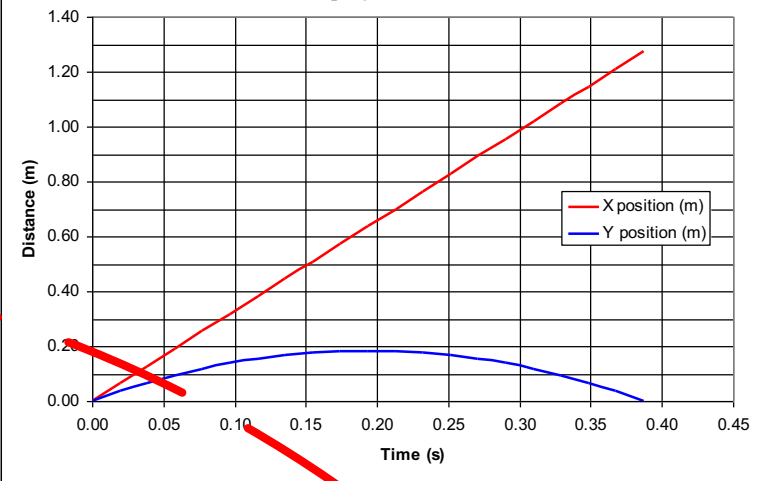


Table Speed to Free Shot-puts
Table_rotate_dislodge_ball.xls



Projectile trajectory
projectile.xls

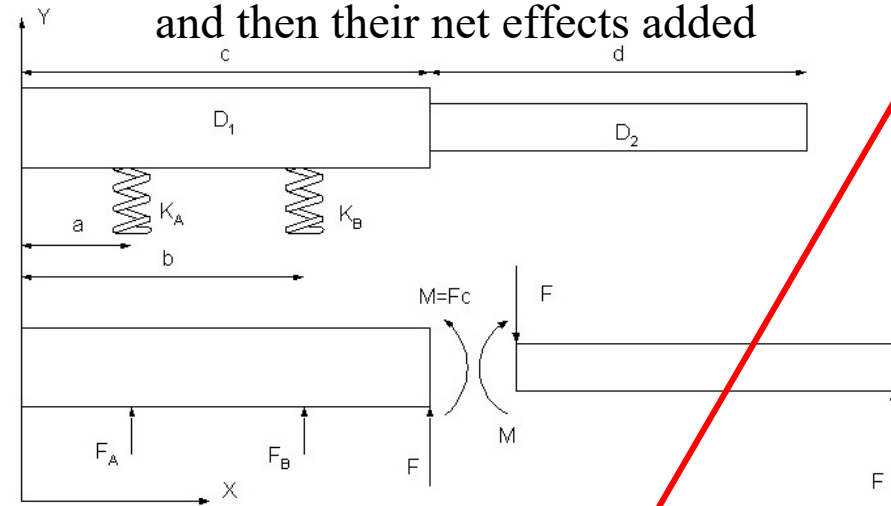


Power budget estimate.xls										
Power & energy budget for individual moves, total (S) for simultaneous moves, and cumulative										
Last modified 9/01/03 by Alex Slocum										
Enters numbers in BOLD , Results in RED						Power (Watts)			Energy (N-m)	
Axis	Move #	Force (N)	Velocity (m/s)	Distance (m)	Efficiency, net system	Move	Battery dissipation	Σ power for move #	Energy for move	Σ Energy
Drive to pucks	1	3	0.2	1	29%	2.10	8.30		52.0	52.0
Lower arm	1	0.5	0.5	0.04	29%	0.88	8.30	11.28	0.7	52.8
Scoop	2	3	0.2	0.02	29%	2.10	3.00	5.10	0.5	53.3
Raise arm	3	3	0.2	0.05	29%	2.10	3.00	5.10	1.3	54.5
Drive to goal	4	2	0.2	0.5	29%	1.40	3.00	4.40	11.0	65.6
Dump pucks	5	0.1	0.5	0.05	29%	0.18	3.00	3.18	0.3	65.9

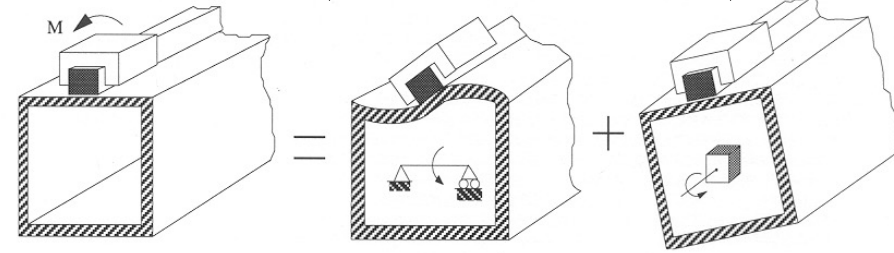
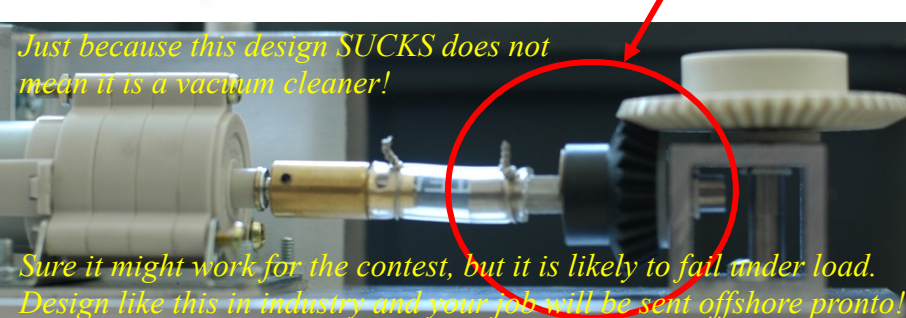
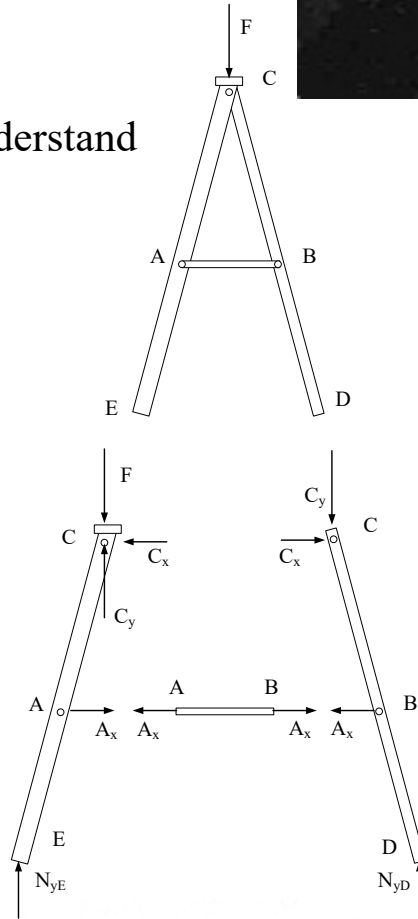
Newton: *Free Body Diagrams & Superposition*



- *Free body diagrams* are a graphical representation of Newton's third law
 - They allow a designer to show **components** and their relationship to each other with respect to forces transmitted between them
 - Invaluable for properly visualizing loads on **components**
 - In order to properly constrain a **component**, one has to understand how it is loaded and constrained
- *Superposition* allows a complex load to be broken up into **components** each of which can be applied one at a time, and then their net effects added



What supports the other end of the shaft to which the gear is attached? How will the gear-tooth radial forces be resisted? A simple FBD of every component can be a critical design synthesis catalyst. FDBs are critical to helping identify how to properly support components! (in a few pages, Saint-Venant will...)



Conservation of Energy

- What goes in must come out:

$$\eta_{\text{efficiency}} \times E_{\text{energy in}} = E_{\text{energy out}}$$

$$E = F_{\text{force out (N)}} \times d_{\text{distance out (m)}}$$

$$E = \Gamma_{\text{torque (or moment) (N-m)}} \times \alpha_{\text{distance (radians)}}$$

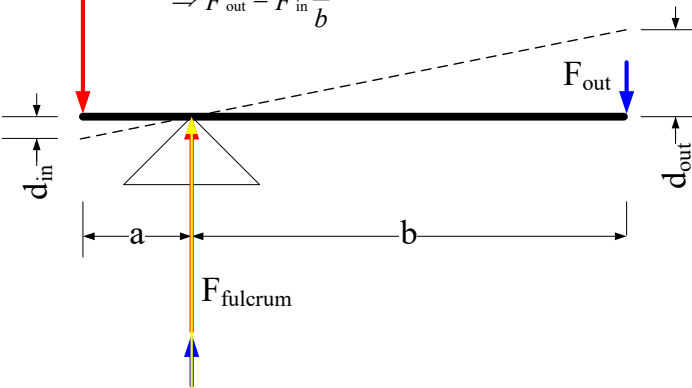
Assume F_{in} and d_{in} are known inputs; find F_{out} and d_{out} :

$$F_{\text{in}} \times d_{\text{in}} = F_{\text{out}} \times d_{\text{out}} \Rightarrow 1 \text{ equation and 2 unknowns}$$

$$\Rightarrow \frac{d_{\text{in}}}{a} = \frac{d_{\text{out}}}{b} \Rightarrow \text{geometric compatability (small angles)}$$

$$F_{\text{in}} \Rightarrow d_{\text{out}} = d_{\text{in}} \frac{a}{b} \Rightarrow \text{use in the first equation}$$

$$\Rightarrow F_{\text{out}} = F_{\text{in}} \frac{a}{b}$$



Force and Moment Equilibrium (Newton's First Law):

Assume F_{in} is a known input; find F_{out} and F_{fulcrum}

$$\sum F_y = 0 \Rightarrow -F_{\text{in}} - F_{\text{out}} + F_{\text{fulcrum}} = 0 \Rightarrow 1 \text{ equation and 2 unknowns}$$

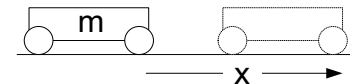
$$\sum M_A = 0 \Rightarrow F_{\text{in}} \times a = F_{\text{out}} \times b \Rightarrow 1 \text{ equation and 1 unknown}$$

$$\Rightarrow F_{\text{out}} = F_{\text{in}} \frac{a}{b} \Rightarrow \text{use in the first equation}$$

$$\Rightarrow F_{\text{fulcrum}} = F_{\text{in}} + F_{\text{out}} = F_{\text{in}} \left(1 + \frac{a}{b} \right)$$

For a machine of mass m to move a distance x under constant acceleration in time t :

$$x = \frac{at^2}{2} \quad v = at \quad F = ma \quad P = \frac{Fv}{\eta_{\text{efficiency}}}$$



Solving for the power consumed

$$a = \frac{2x}{t^2} \quad v = \frac{2x}{t} \quad F = \frac{2xm}{t^2} \quad P = \frac{4mx^2}{\eta_{\text{efficiency}} t^3}$$

If the percent weight of the vehicle over the drive wheels is β , then the minimum coefficient of friction between the drive wheels and the ground is:

$$\mu_{\text{minimum}} = \frac{F}{mg\beta}$$

[See Power_to_Move.xls](#)

Assume Γ_{in} and α_{in} are known inputs ($\alpha_{\text{in}} = \pi$); find Γ_{out} and α_{out} :

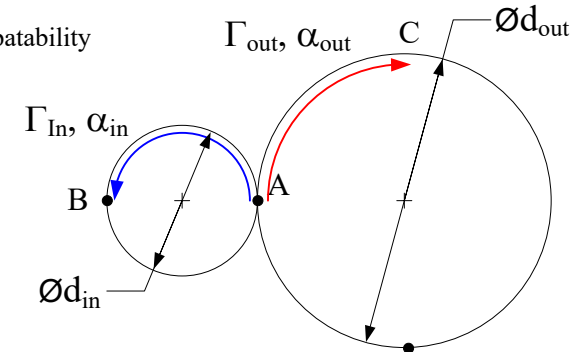
$$\Gamma_{\text{in}} \times \alpha_{\text{in}} = \Gamma_{\text{out}} \times \alpha_{\text{out}} \Rightarrow 1 \text{ equation, 2 unknowns}$$

$$\Rightarrow \pi \frac{d_{\text{in}}}{2} = \alpha_{\text{out}} \frac{d_{\text{out}}}{2} \Rightarrow \text{geometric compatability}$$

$$\Rightarrow \Gamma_{\text{in}} \times \pi = \Gamma_{\text{out}} \times \pi \frac{d_{\text{in}}}{d_{\text{out}}}$$

$$\Rightarrow \Gamma_{\text{out}} = \Gamma_{\text{in}} \frac{d_{\text{out}}}{d_{\text{in}}}$$

[See Spurgears.xls](#)



Assume torque applied to screw is Γ_{in} over one revolution ($\alpha_{\text{in}} = 2\pi$)

Lead ℓ is defined as distance nut travels in one screw revolution

$$\Gamma_{\text{in}} \times 2\pi \times \eta_{\text{efficiency}} = F_{\text{out}} \times \ell \Rightarrow 1 \text{ equation, 1 unknown}$$

$$\Rightarrow F_{\text{out}} = \frac{2\pi\eta\Gamma_{\text{in}}}{\ell}$$

[See Screwforce.xls](#)





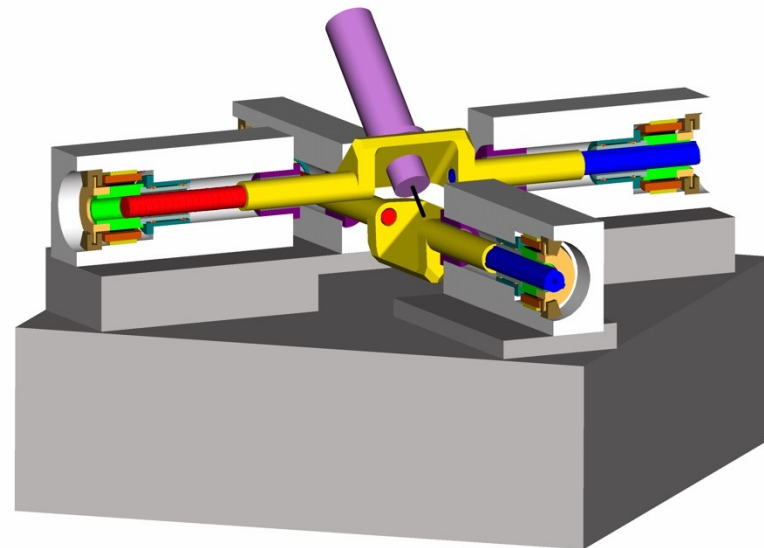
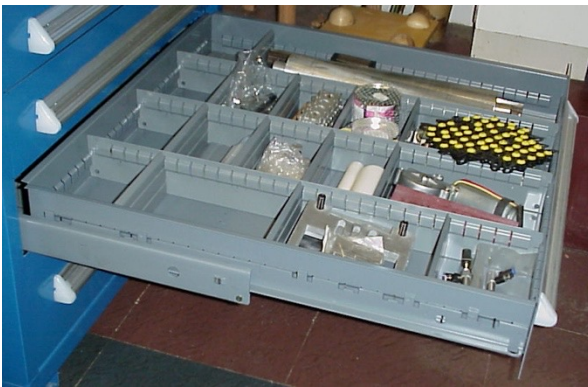
Saint-Venant's Principle

- Saint-Venant did research in the theory of elasticity, and often relied on the assumption that local effects of loading do not affect global strains
 - e.g., bending strains at the root of a cantilever are not influenced by the local deformations of a point load applied to the end of a cantilever
- The engineering application of these observations are profound for the development of conceptual ideas and initial layouts of designs:
 - To NOT be affected by local deformations of a force, be several characteristic dimensions away
 - How many seats away from the sweaty person do you want to be?
 - Several can be interpreted as 3-5
 - To have control of an object, apply constraints over several characteristic dimensions
 - These are just initial layout guidelines, and designs must be optimized using closed-form or finite element analysis



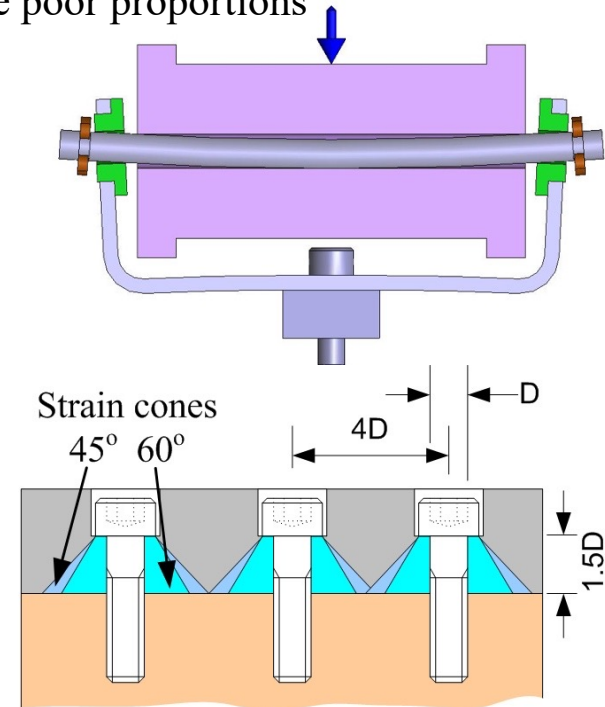
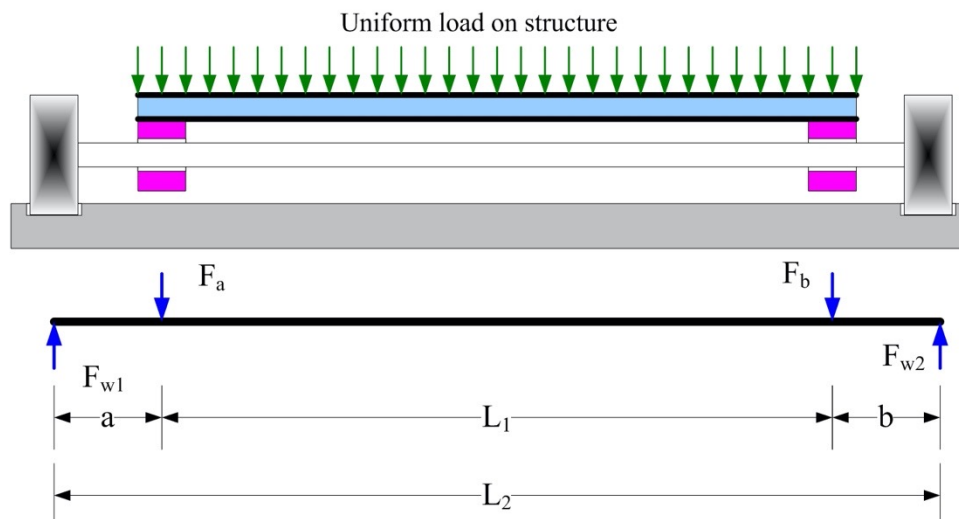
Barré de Saint-Venant
1797-1886

• One of the most powerful principles in your drawer of **FUNdaMENTALS**

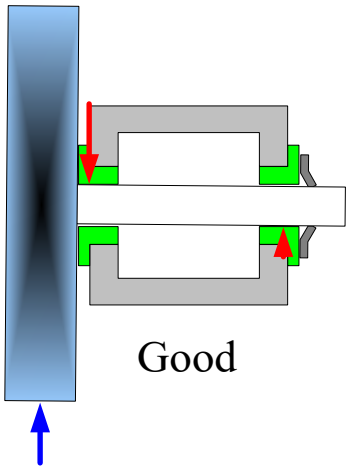
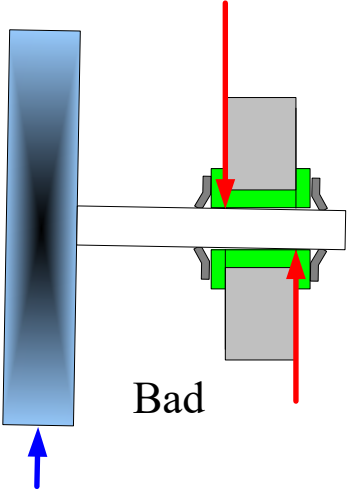
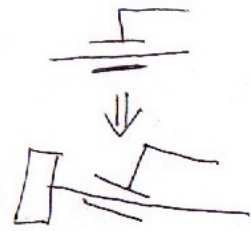


Saint-Venant's Principle: *Structures*

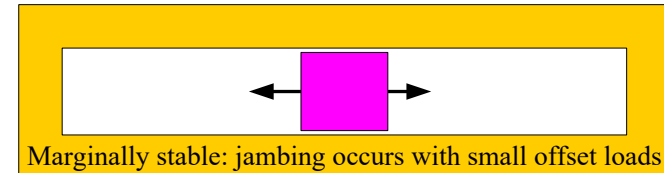
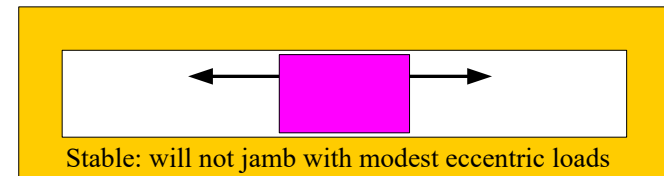
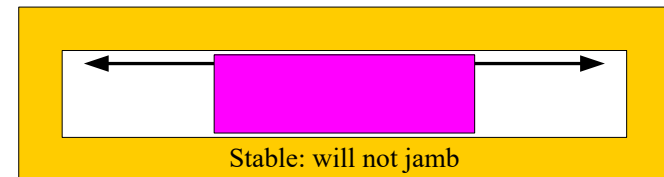
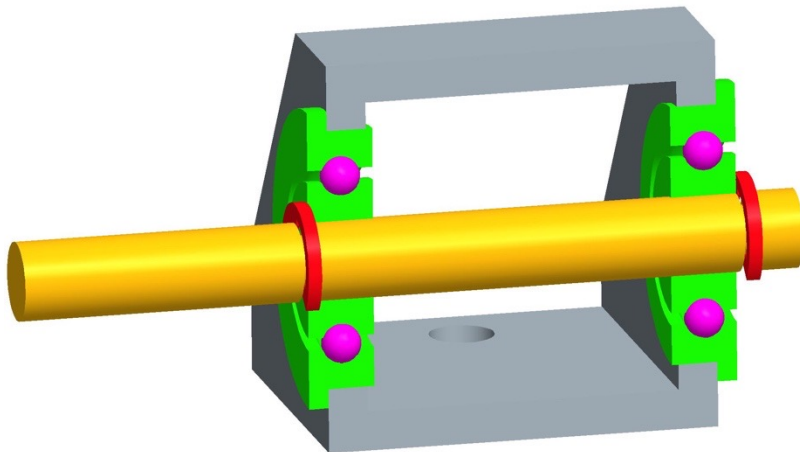
- To NOT feel something's effects, be several characteristic dimensions away!
 - If a plate is 5 mm thick and a bolt passes through it, you should be 3 plate thicknesses away from the bolt force to not cause any warping of the plate!
 - Many bearing systems fail because bolts are too close to the bearings
 - Beware the strain cone under a bolt that deforms due to bolt pressure!
 - Strain cones should overlap in the vicinity bearings to prevent wavy deformations
 - BUT check the design's functional requirements, and only use as many bolts as are needed!
- To DOMINATE and CONTROL something, control several characteristic dimensions
 - If a column is to be cantilevered, the anchor region should be 3 times the column base area
 - Too compliant machines (lawn furniture syndrome) often have poor proportions
 - Diagonal braces can be most effective at stiffening a structure



Saint-Venant's Principle: *Bearings*

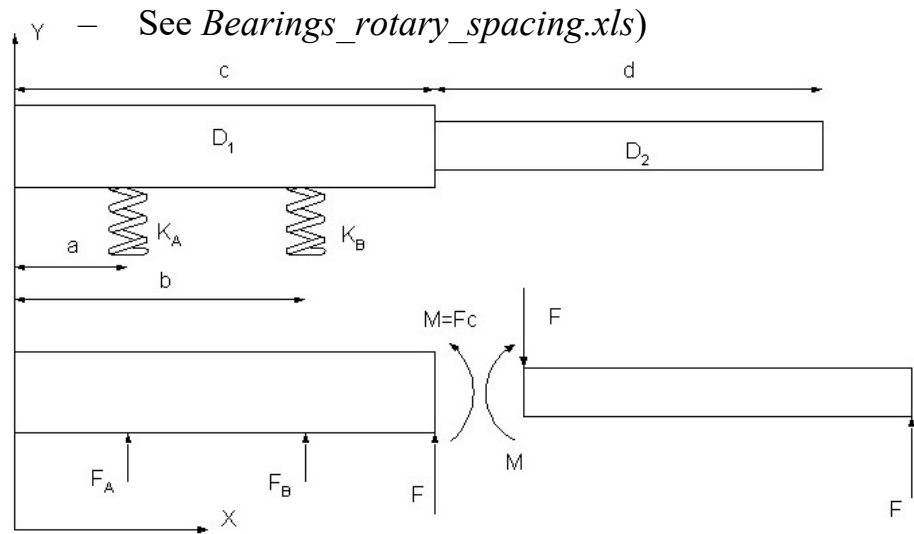


- Saint-Venant: *Linear Bearings*:
 - Make friction (μ) low and $L/D > 1$, 1.6:1 very good, 3:1 awesome
 - Every year some students try $L/D < 1$ and their machines jam!
 - Wide drawers guided at the outside edges can jamb
 - Wide drawers guided by a central runner do not!
 - If $L/D < 1$, actuate both sides of the slide!
- Saint-Venant: *Rotary Bearings*:
 - $L/D > 3$ if the bearings are to act to constrain the shaft like a cantilever
 - IF $L/D < 3$, BE careful that slope from shaft bending does edge-load the bearings and cause premature failure
 - For sliding contact bearings, angular deformations can cause a shaft to make edge contact at both ends of a bearing
 - This can cause the bearing to twist, seize, and fail
 - Some shaft-to bearing bore clearance must always exist

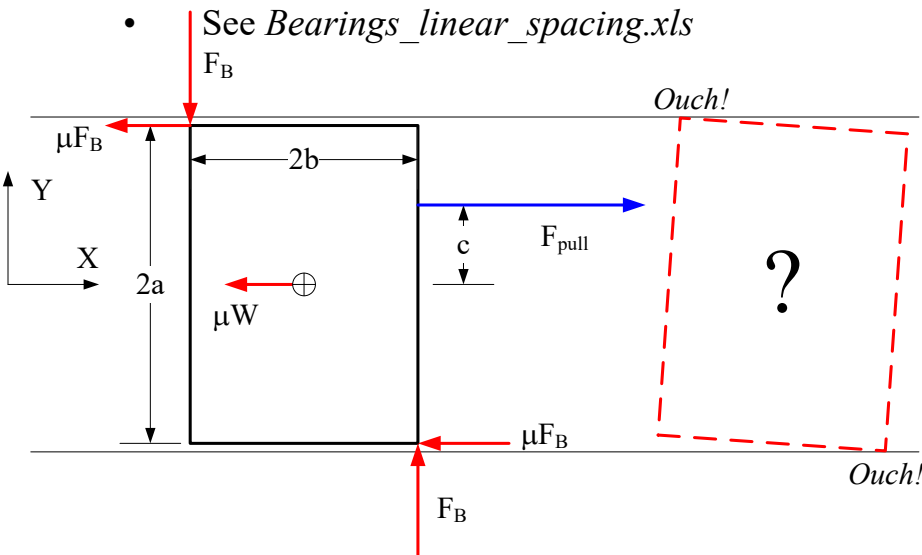


Saint-Venant's Principle: *Bearings*

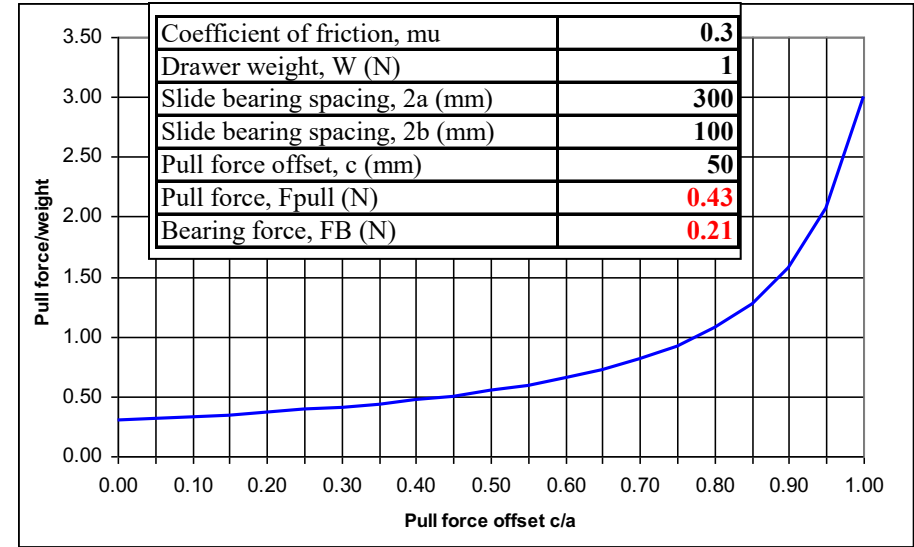
- Model of a shaft supported by bearings: Minimize the deflection of the ends of the beam



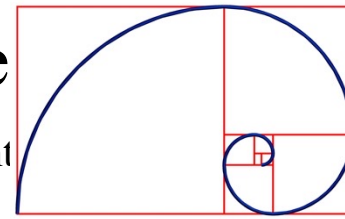
- Model of the effect of bearing width, friction, and length spacing on the actuation force (drawer jamming)



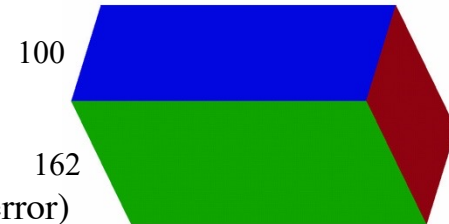
Design Parameters		Values
a (mm)		50
b (mm)		20
c (mm)		250
d (mm)		100
Diameter, D 1 (mm)		15
Diameter, D 2 (mm)		10
Bearing radial spring constant, KA (N/mm)		2.00E+02
Bearing radial spring constant, KB (N/mm)		2.00E+02
Modulus, E (N/mm^2)		6.70E+04
Tip force, F (N)		10.00
Moment of inertia, I 1 (mm^4)		2.49E+03
Moment of inertia, I 2 (mm^4)		4.91E+02
Spring force, FA (N)		-110.00
Spring force, FB (N)		100.00
End deflection of just D 2 segment (mm)		1.01E-01
End slope of just D 2 segment (rad)		1.52E-03
Ratio (deflection left end)/(deflection right end)		-0.103
Position along beam: 0, a, (a+b)/2, b, c, (c+d)	deflection (mm)	slope (rad)
	0	-1.20E+00 3.51E-02
	50	5.53E-01 3.54E-02
	35	2.39E-02 3.52E-02
	20	-5.03E-01 3.51E-02
	250	7.91E+00 3.78E-02
	350	1.17E+01 3.93E-02
Bearing gap closure (for sliding contact bearing supports)		
Bearing width, wb (mm)		5.00
Diametral clearance loss at first bearing (a) (mm)		0.177
Diametral clearance loss at first bearing (b) (mm)		0.176



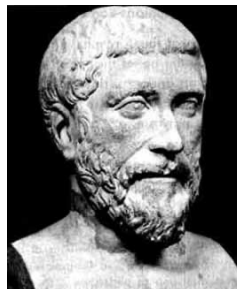
The Golden Rectangle



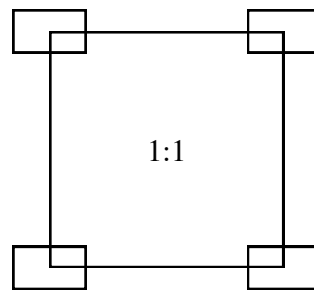
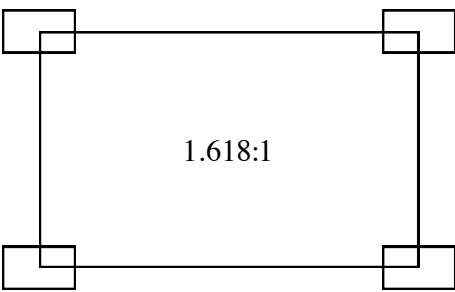
- The proportions of the *Golden Rectangle* are a natural starting point for preliminary sizing of structures and elements
 - Golden Rectangle*: A rectangle where when a square is cut from the rectangle, the remaining rectangle has the same proportions as the original rectangle: $a/b = 1/(a/b - 1)$
 - See and study *Donald in Mathmagic Land*!
 - Try a *Golden Solid*: 1: 1.618: 2.618, & the diagonal has length $2a = 3.236$
 - Example: Bearings:
 - The greater the ratio of the longitudinal to latitudinal (length to width) spacing:
 - The smoother the motion will be and the less the chance of walking (yaw error)
 - First try to design the system so the ratio of the longitudinal to latitudinal spacing of bearing elements is about 2:1
 - For the space conscious, the bearing elements can lie on the perimeter of a golden rectangle (ratio about 1.618:1)
 - The minimum length to width ratio should be 1:1
 - To minimize yaw error
 - Depends on friction too



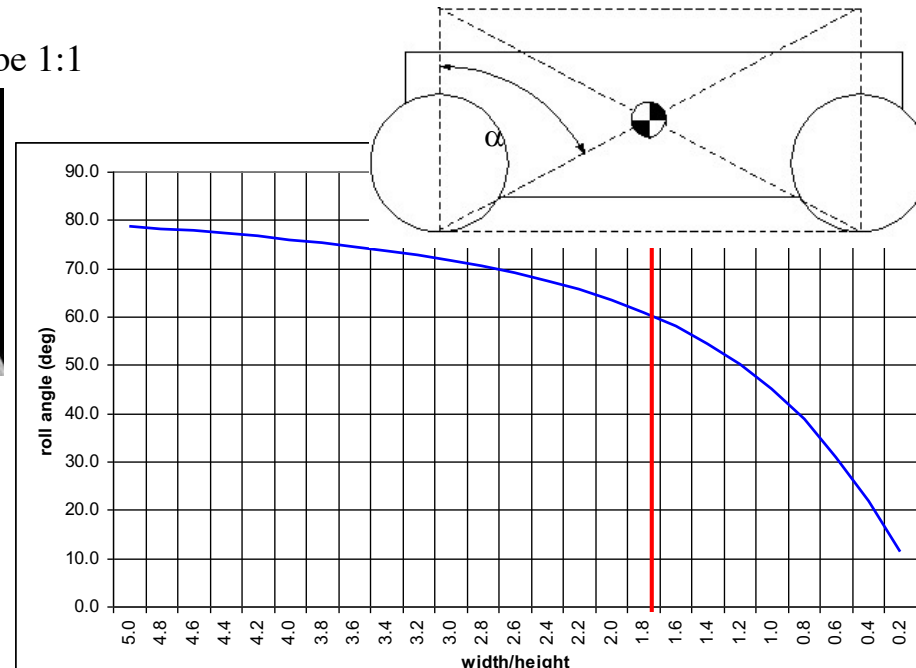
Pythagoras of Samos
569 BC-475 BC



<http://www-gap.dcs.st-and.ac.uk/~history/Mathematicians/Pythagoras.html>



3-10

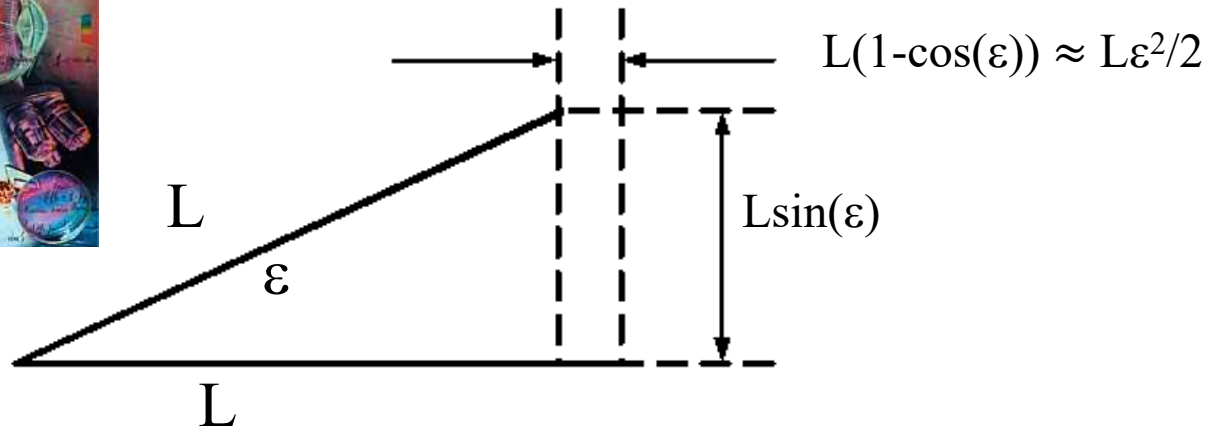


Abbe's Principle

- In the late 1800s, Dr. Ernst Abbe (1840-1905) and Dr. Carl Zeiss (1816-1888) worked together to create one of the world's foremost precision optics companies: Carl Zeiss, GmbH (<http://www.zeiss.com/us/about/history.shtml>)
- The Abbe Principle (*Abbe errors*) resulted from observations about measurement errors in the manufacture of microscopes:
 - *If errors in parallax are to be avoided, the measuring system must be placed coaxially with the axis along which the displacement is to be measured on the workpiece*
 - Strictly speaking, the term *Abbe error* only applies to measurement errors
- When an angular error is amplified by a distance, e.g., to create an error in a machine's position, the strict definition of the error is a *sine* or *cosine* error

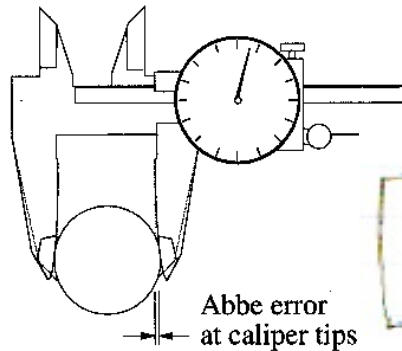
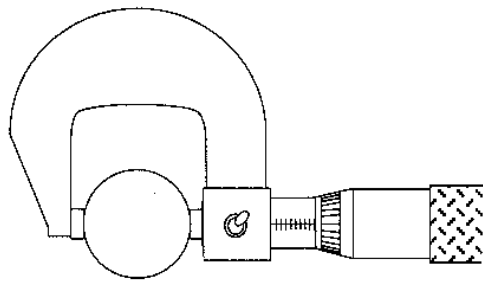


From www.zeiss.com



Abbe's Principle: *Locating Components*

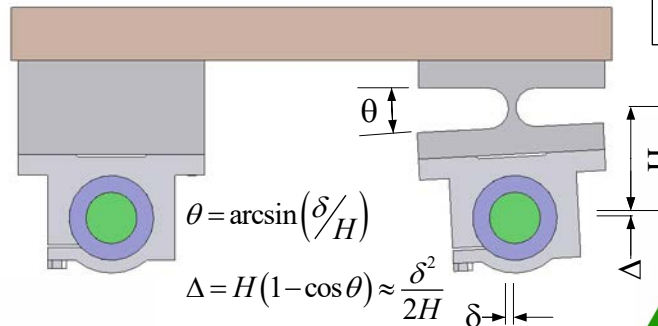
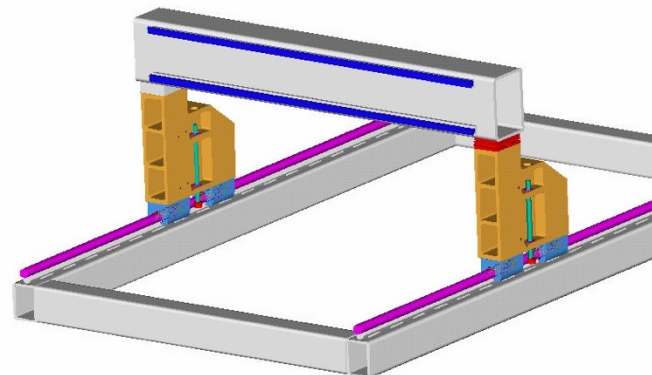
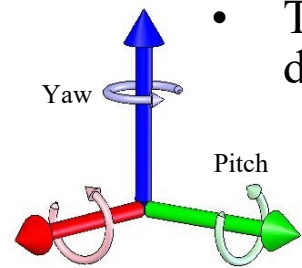
- Geometric: Angular errors are amplified by the distance from the source
 - Measure near the source, and move the bearings and actuator near the work!
- Thermal: Temperatures are harder to measure further from the source
 - Measure near the source!



On Brown & Sharpe's vernier caliper: "It was the first practical tool for exact measurements which could be sold in any country at a price within the reach of the ordinary machinist, and its importance in the attainment of accuracy for fine work can hardly be overestimated"

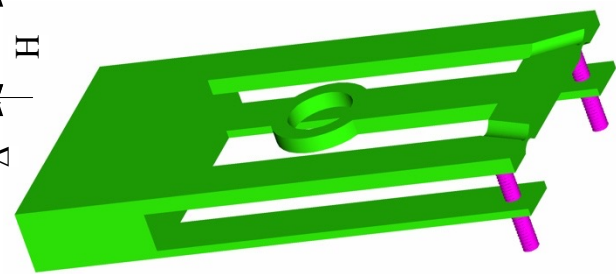
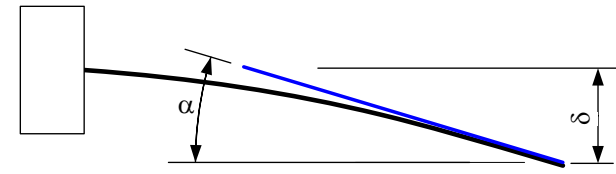


- Thinking of Abbe errors, and the system FRs is a powerful catalyst to help develop DPs, where location of motion axes is depicted schematically
 - Example: Stick figures with arrows indicating motions are a powerful simple means of depicting *strategy* or *concepts*



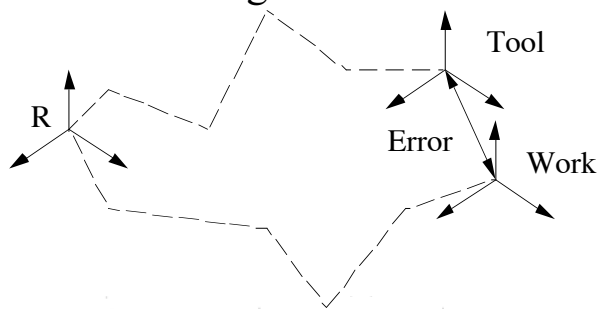
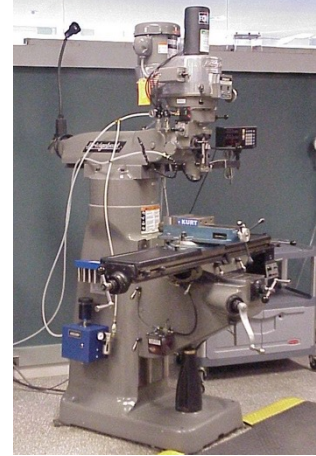
$$\theta = \arcsin\left(\frac{\delta}{H}\right)$$

$$\Delta = H(1 - \cos \theta) \approx \frac{\delta^2}{2H}$$



Abbe's Principle: *Cascading Errors*

- A small angular deflection in one part of a machine quickly grows as subsequent layers of machine are stacked upon it...
 - A component that tips on top of a component that tips...
 - *If You Give a Mouse a Cookie...* (great kid's book for adults!)
- Error budgeting keeps tracks of errors in cascaded components
 - Designs must consider not only linear deflections, but angular deflections and their resulting *sine errors*...

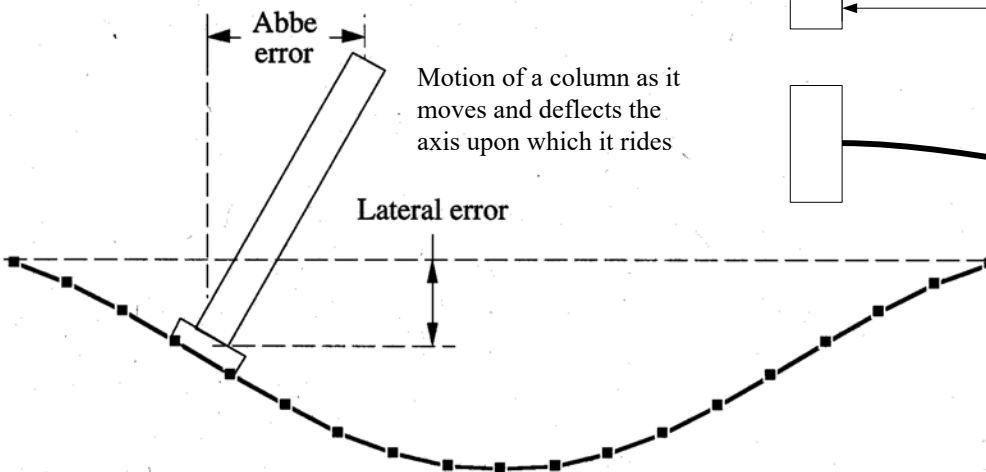
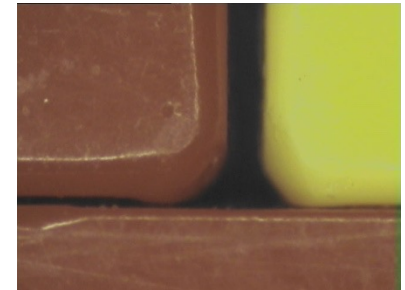
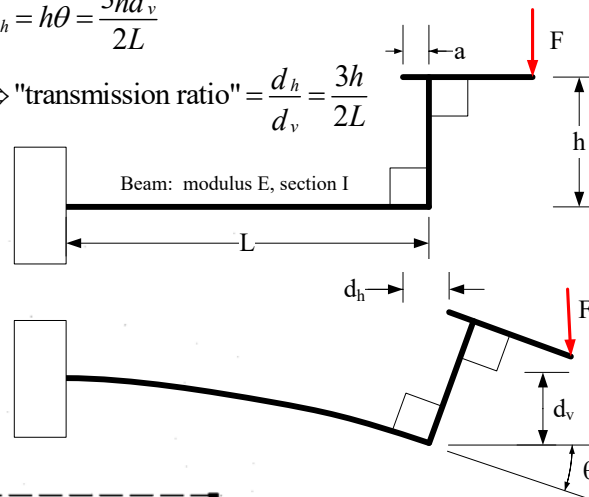


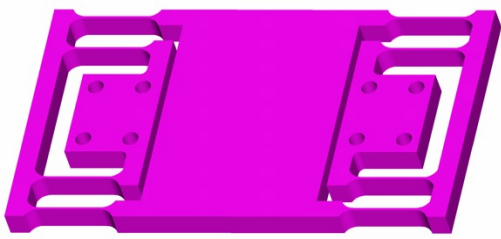
$$d_v = \frac{FL^3}{3EI}$$

$$\theta = \frac{FL^2}{2EI} = \frac{3d_v}{2L}$$

$$d_h = h\theta = \frac{3hd_v}{2L}$$

$$\Rightarrow \text{"transmission ratio"} = \frac{d_h}{d_v} = \frac{3h}{2L}$$



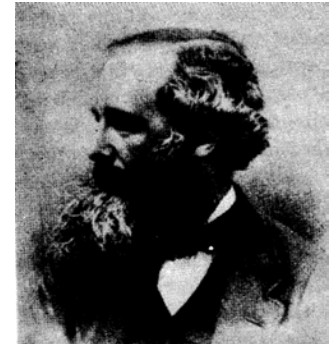


Maxwell & Reciprocity

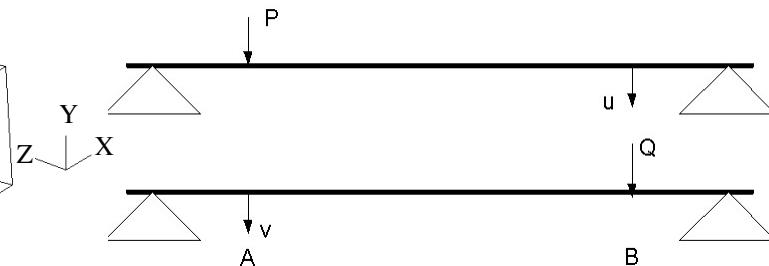
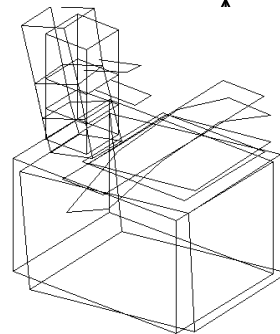
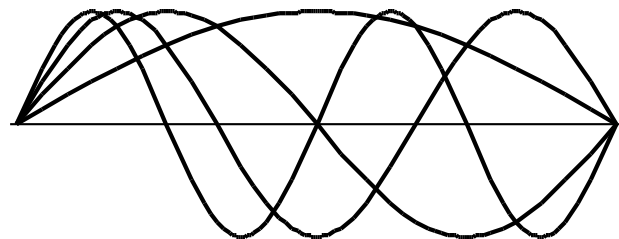
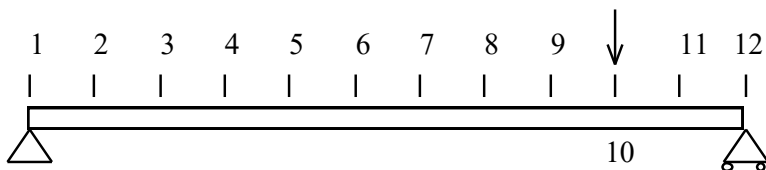
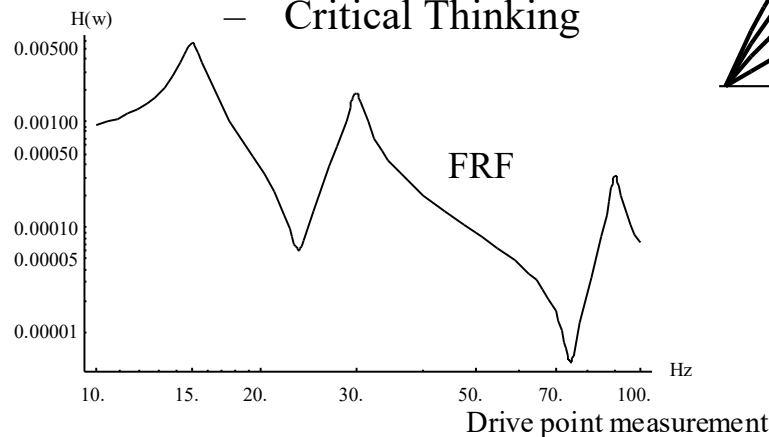


$$\frac{1}{\text{problem}} = \text{opportunity!} \quad \frac{1}{\text{Ow!}} = \text{Ahhhhh!}$$

- Maxwell's theory of *Reciprocity*
 - Let A and B be any two points of an elastic system. Let the displacement of B in any direction U due to a force P acting in any direction V at A be u ; and the displacement of A in the direction V due to a force Q acting in the direction U at B be v . Then $Pv = Qu$ (from Roark and Young Formulas for Stress and Strain)
- The principle of *reciprocity* can be extended in philosophical terms to have a profound effect on measurement and development of concepts
 - Reversal
 - Critical Thinking

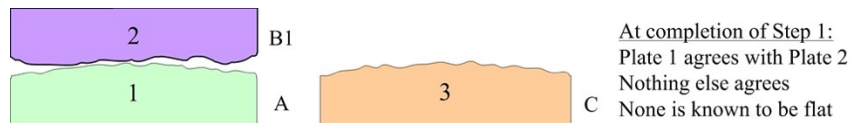


James Clerk Maxwell 1831-1879



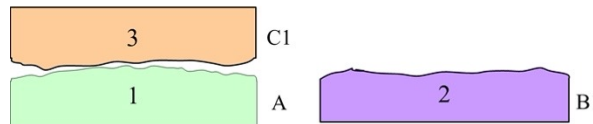
Maxwell & Reciprocity: *Reversal*

- *Reversal* is a method used to remove repeatable measuring instrument errors
 - A principal method for continual advances in the accuracy of mechanical components
- There are many applications for measurement and manufacturing
 - Two bearings rails ground side-by-side can be installed end-to-end
 - A carriage whose bearings are spaced one rail segment apart will not pitch or roll
 - Scraping three plates flat



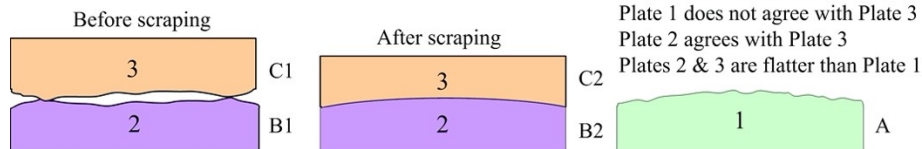
At completion of Step 1:
Plate 1 agrees with Plate 2
Nothing else agrees
None is known to be flat

Step 1: Neither plate is the control plate. This step is completed when there is general agreement between plates 1 and 2



At completion of Step 2:
Plate 2 agrees with Plate 1
Plate 3 agrees with Plate 1
Plate 2 does not agree with Plate 3
None is known to be flat

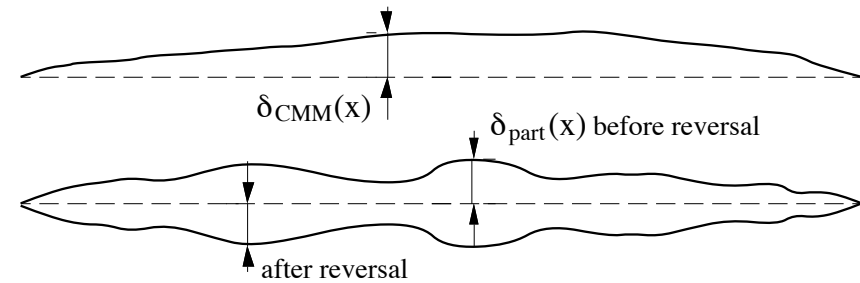
Step 2: Plate 1 is the control plate. This step is completed when plates 1 & 2 have both picked up Plate 1's error



At completion of Step 3:
Plate 1 does not agree with Plate 2
Plate 1 does not agree with Plate 3
Plate 2 agrees with Plate 3
Plates 2 & 3 are flatter than Plate 1

Step 3: Neither plate is the control plate. By scraping some of Plate 1's error off of Plate 2, and some off of Plate 3, Plates 2 & 3 get flatter

After T. Busch, *Fundamentals of Dimensional Metrology*,
Delmar Publishers, Albany, NY, 1964

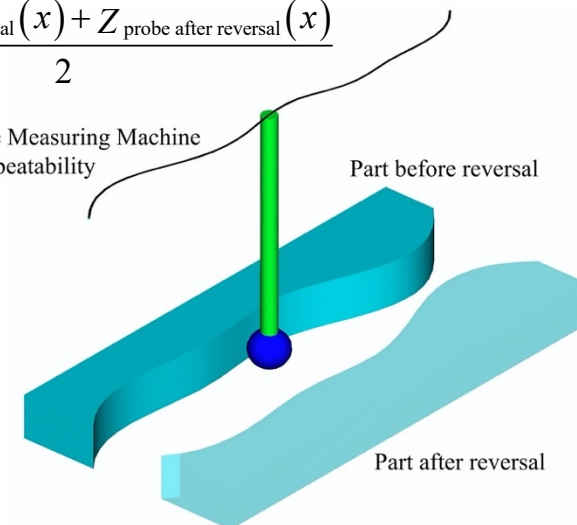


$$Z_{\text{probe before reversal}}(x) = \delta_{CMM}(x) - \delta_{\text{part}}(x)$$

$$Z_{\text{probe after reversal}}(x) = \delta_{CMM}(x) + \delta_{\text{part}}(x)$$

$$\delta_{\text{part}}(x) = \frac{-Z_{\text{probe before reversal}}(x) + Z_{\text{probe after reversal}}(x)}{2}$$

Coordinate Measuring Machine
(CMM) repeatability



Maxwell & Reciprocity: *Critical Thinking*

Rock & Roll Over & Under

*Reciprocity
It's like velocity
Once up to speed
You have no other need
Late at night
On goes the light
Driven by curiosity
You create with ferocity*

- If you are:
 - Happy, turn it around!
 - Unhappy, turn it around!
 - Comfortable on your back, turn over and try lying down on your front.....
- You can make a system *insensitive* to its surroundings, or you can *isolate* a system ...
- If you cannot solve a problem by starting at the beginning, work backwards!
- Example: Roll-off container passive restraint mechanism
 - In the event of an accident, it keeps an otherwise gravity-held container from flipping off the truck



Bill Miskoe, welder and co-inventor

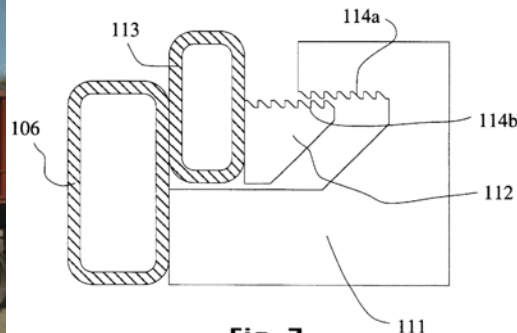
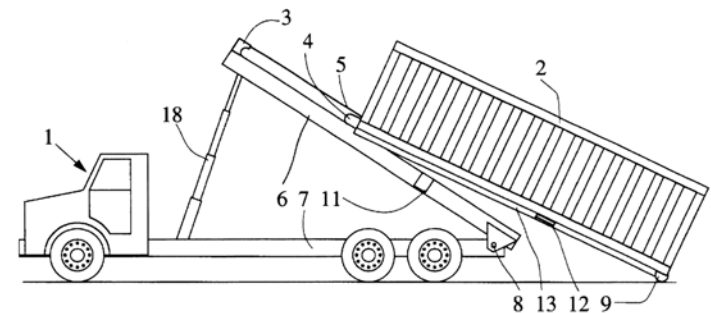
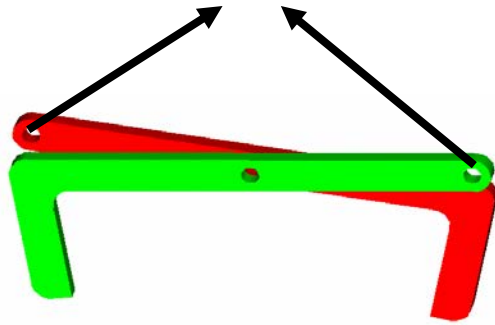


Fig. 7

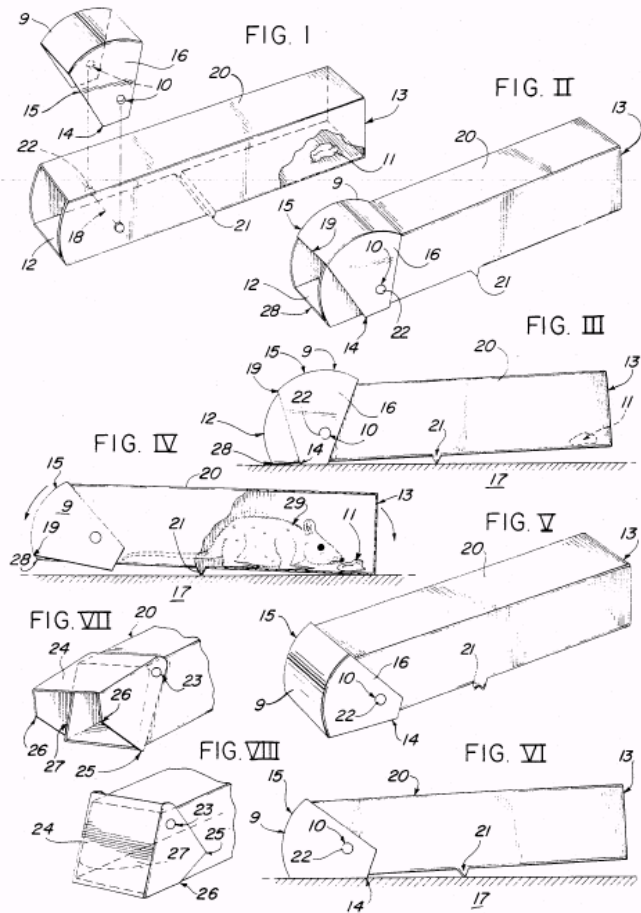
United States Patent [19]		[11] Patent Number:	5,848,869
Slocum et al.		[45] Date of Patent:	Dec. 15, 1998
<hr/>			
[54]	CONTAINER RESTRAINING MECHANISM AND METHOD		
[75]	Inventors: Alexander H. Slocum, Bow; John William Meskoe, Concord, both of N.H.		481367 4/1992 European Pat. Off. 414/480 1080210 12/1954 France 414/500 2686843 8/1993 France 414/500 1430217 3/1969 Germany 414/494 8607019 12/1986 WIPO 414/494
[73]	Assignee: AESOP, Inc., Concord, N.H.		<i>Primary Examiner</i> —Frank E. Werner <i>Attorney, Agent, or Firm</i> —Rines & Rines
[21]	Appl. No.: 759,870		[57] ABSTRACT
[22]	Filed: Dec. 3, 1996		A system and technique for holding down and restraining a roll-off container in place as it is winched into its final position on the bed of a truck or other transport device, wherein, as the roll-off container is winched into position on the truck, a protuberance on the side of the bottom rail of the roll-off container slides into a mating interlocking cradle attached to the truck. The sliding mate can be of a cantilevered spear into a socket, or more generically, a sliding open-ended mate such as a dovetail. In the event of a crash or sudden stop, the roll-off container will thus be retained by the interlocking connection.
[51]	Int. Cl.⁶ B60P 1/65		
[52]	U.S. Cl. 414/500; 414/480; 414/494		
[58]	Field of Search 220/1.5; 414/480, 414/491, 492, 493, 494, 499, 498, 500		
[56]	References Cited		
U.S. PATENT DOCUMENTS			
3,897,882 8/1975 Budoff 414/500			
5,085,448 2/1992 Shubin 414/500 X			
5,284,266 2/1994 Januel et al. 414/498 X			
FOREIGN PATENT DOCUMENTS			
71143 1/1976 Australia 414/500			
5 Claims, 4 Drawing Sheets			



Self-Principles



U.S. Patent Nov. 5, 1985 4,550,523



- The manner in which a design reacts to inputs determines its output
 - Reciprocity would philosophically tell us to look for a solution where a potentially detrimental result can be used to cancel the effect
 - Martial artists practice this principle all the time!
- *Self-Help*: A design that uses the inputs to assist in achieving the desired output
 - An initial effect is used to make the device ready for inputs
 - The supplementary effect is that which is induced by the inputs, and it enhances the output
 - *Example*: Airplane doors act like tapered plugs
 - When the door is shut, latches squeeze the seal, making the cabin airtight
 - As the plane ascends and outside air pressure decreases, the higher inner air pressure causes the door to seal even tighter
 - *Example*: *Back-to-back* angular contact bearings are thermally stable
 - *Example*: Ice tongs
 - *Example*: A better mousetrap!
 - *Example*: Balanced forces on hydrostatic bearings: A.M. van der Wielen, P.H.J. Schellekens, F.T.M. Jaartsveld, Accurate Tool Height Control by Bearing gap Adjustment, Annals of the CIRP, 51(1/200), 351-354, (2002)
- Other *self-principles* similarly exist:
 - *Self Balancing, Self-Reinforcing, Self-Protecting, Self-Limiting, Self-Damaging, Self-Braking, Self-Starting*....

Stability

- All systems are either *stable*, *neutral*, or *unstable*

- Saint-Venant's principle was applied to bearing design to reduce the chance of sliding instability (e.g., a drawer jamming)

- A snap-fit uses an applied force to move from a stable, to a neutrally stable, to an unstable to a final new stable position

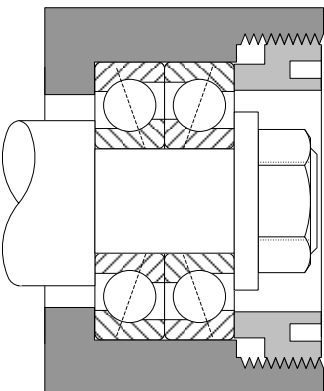
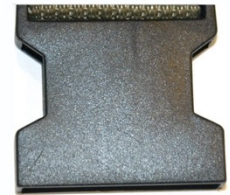
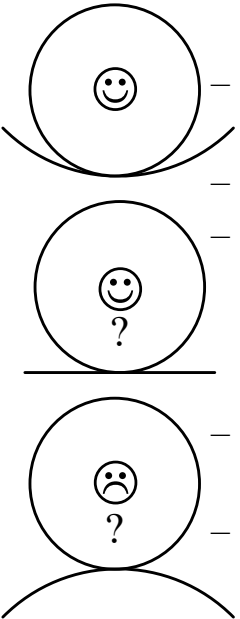
- Wheels allow a system to roll along a flat surface

- As the load on a tall column increases, infinitesimal lateral deflections are acted on by the axial force to become bending moments, which increase the deflections....

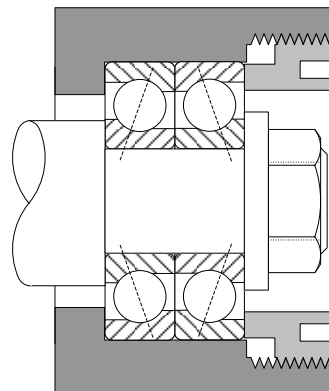
- Reciprocity says this detrimental effect can be useful: fire sprinklers are activated by a column that buckles when it becomes soft...

- *Back-to-back* mounted bearings are intolerant of misalignment, but use axial thermal growth to cancel radial thermal growth for constant preload and thermal stability at high speeds

- *Face-to-face* mounted bearings are tolerant of misalignment, but axial thermal growth adds to radial thermal growth and causes the bearings to become overloaded and seize at high speeds







face-to-face mounting *can* accommodate shaft misalignment but *cannot* tolerate thermal expansion at high speeds



Back-to-back mounting *cannot* accommodate shaft misalignment but *can* tolerate thermal expansion at high speeds

$$\omega_n = k^2 \sqrt{\frac{EI}{\rho L^4}}$$

$$F_{buckle} = \frac{cEI}{L^2}$$

								
	Cantilevered		Simply Supported		Fixed-Simple		Fixed-Fixed	
mode n	k	c	k	c	k	c	k	c
1	1.875	2.47	3.142	9.87	3.927	20.2	4.730	39.5
2	4.694		6.283		7.069		7.853	
3	7.855		9.425		10.210		10.996	
4	10.996		12.566		13.352		14.137	
n	$(2n-1)\pi/2$		$n\pi$		$(4n+1)\pi/4$		$(2n+1)\pi/2$	

Symmetry

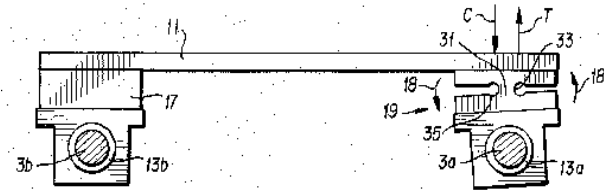
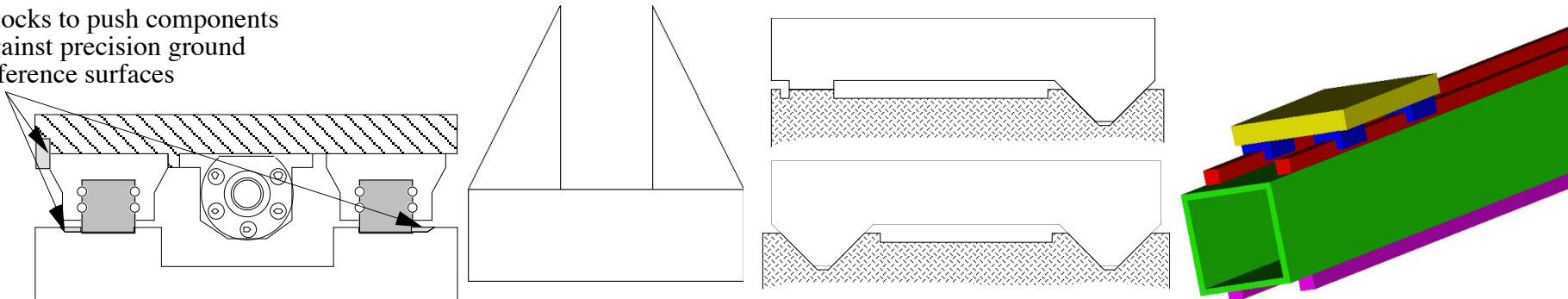
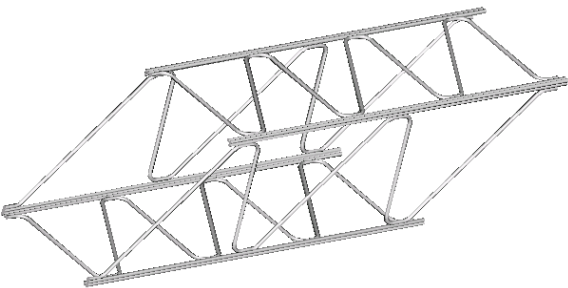


FIG. 3

- *Symmetry* can be a powerful design tool to minimize errors
 - Thermal gradient errors caused by bi-material structures can minimize warping errors
 - Steel rails can be attached to an aluminum structure on the plane of the neutral axis
 - Steel rails on an aluminum structure can be balanced by steel bolted to the opposite side
 - Angular error motions can be reduced by symmetric support of elements
- *Symmetry* can be detrimental (Maxwell applied to symmetry)
 - Differential temperature minimized by adding a heat source can cause the entire structure to heat up
 - Only attempt with extreme care
 - Better to isolate the heat source, temperature control it, use thermal breaks, and insulate the structure
 - A long shaft axially restrained by bearings at both ends can buckle
 - Remember-when you generalize, you are often wrong
 - The question to ask, therefore, is “Can symmetry help or hurt this design?”

Blocks to push components
against precision ground
reference surfaces



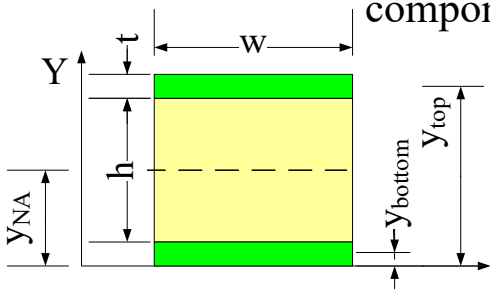


Parallel Axis Theorem



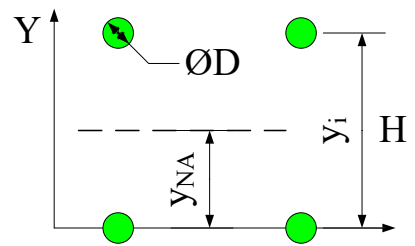
John McBean goes to the extreme!

- The *Parallel Axis Theorem* is useful for calculating the moments of inertia for complex objects
 - The stiffness of a design is proportional to the square of the distance of the component structural members' neutral axes from the assembly's neutral axis

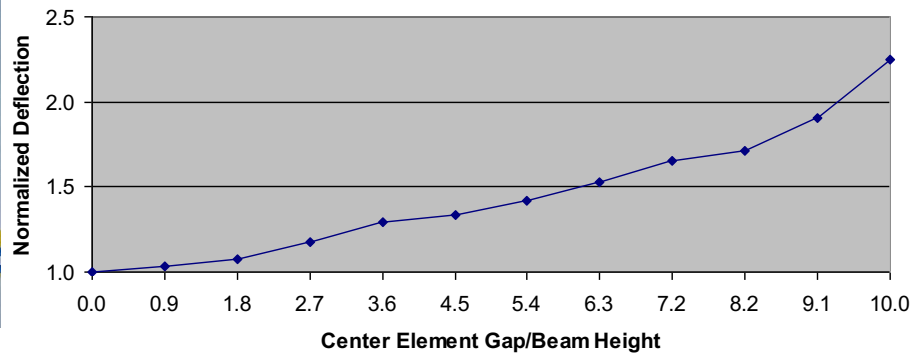
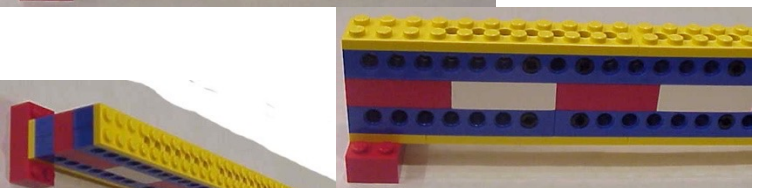
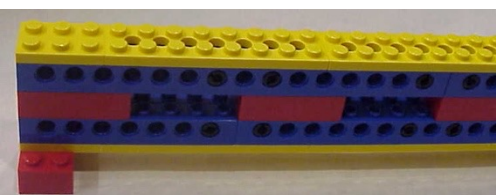


$$y_{NA} = \frac{\sum_{i=1}^N y_i A_i}{\sum_{i=1}^N A_i}$$

$$I = \sum_{i=1}^N I_i + \sum_{i=1}^N (y_i - y_{NA})^2 A_i$$



- The assembly's neutral axis is found in the same manner as the center of gravity, and it is located a distance y_{NA} from an arbitrary plane



Example: Drill string handling crane for the top of a drilling derrick

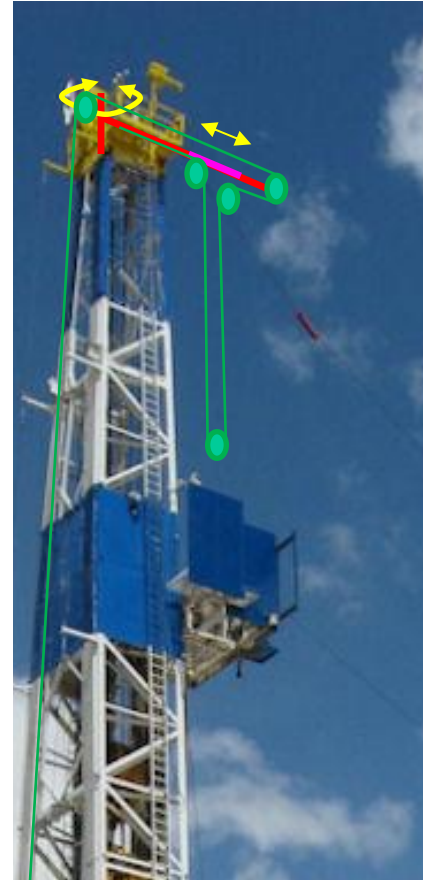
- To change the drill bit, ALL the drill pipe from the hole must be removed and stored vertically in racks ("racking board")
 - A process called "tripping"
- The "Top drive" unit which provides downwards force and torque on the drill string raises the drill string out of the hole.
 - "Slips" (wedges) keep the string from going back into the hole.
- A "Wrench" applies torque, up to 100,000 ft-lbs, to break the threaded joint and then spinners unscrew the drill pipe.
- The Top drive raises the section slightly.
- A worker on the deck throws a rope around the bottom of the drill pipe section and pulls it over so its end is placed in a receiving socket on the drill deck.
- A worker up on the monkey bars throws a rope around the top of the drill string and as the top drive lets go, pulls the top of the drill string over to a corresponding racking place in the racking board to the drill string is nearly vertical and ties it off with a rope.

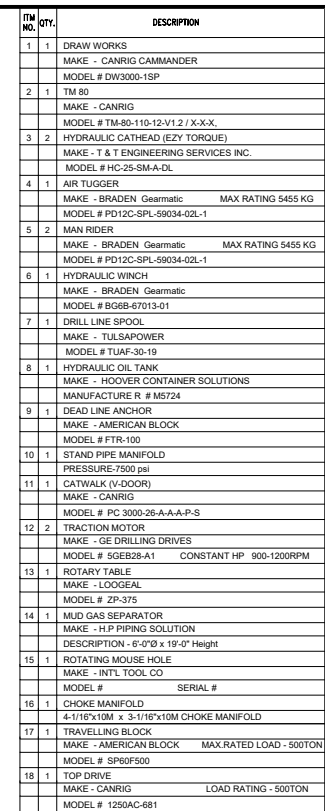
Example: Drill string handling crane for the top of a drilling derrick

- There may be up to up to 300 sections 120 ft long (7-8 miles)
 - Each section may weight up to 3000 pounds.
 - If drill collars in place, design for 5000 pound lift.
- Distance from from well bore to furthest point on racking board is about 16’.
- Manual tripping is a hard and dangerous job and workforce getting older.
 - What if geothermal energy systems become in high demand?
 - Can the industry rise to meet the need?
- Drill floor based hard automation (giant robots) have been prototyped to automate the process
 - Cost is several million dollars
- Can a crane on the derrick (wire rope from a winch) be created for much less cost to accomplish the same thing?

Example: Top Handling Automation Device (THAD)


- Strategy: crane (wire rope from a winch) to handle pipe strings in tripping operation and also obtaining pipe brought up to the drill floor from bround by the catwalk device
- Design for 5000 pound lift.
- Distance from from rear of derrick to furthest point forward 25'
- “Gripper” to grab and lift pipe ideally also controlled by automation
- Initially could be manually set
- Concepts:
 - Arm rotates on slewing ring in horizontal plane, trolley moves along arm
 - R-Theta or “revolute-linear” device
 - Ref: Tower type crane
 - Body rotates on slewing ring in horizontal plane and arm pivots up and down in vertical plane
 - Articulated or “revolute-revolute” device
 - Ref: Boom type crane

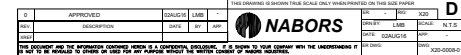




NABORS PACE®-X RIG X20
DRILL FLOOR LAYOUT

B

0	APPROVED	02AUG16	LMB	PKM		DR: _____	SCALE: _____	<div style="border: 1px solid black; padding: 5px; text-align: center;"> B </div>
REV.	DESCRIPTION	DATE	BY	APP.		DRN BY: LMB	SCALE: N.T.S	
XREF						DATE: 01AUG16	APP: PKM	
THIS DOCUMENT AND THE INFORMATION CONTAINED HEREIN IS A CONFIDENTIAL DOCUMENT. IT IS SHOWN TO YOUR COMPANY WITH THE UNDERSTANDING IT IS NOT TO BE REVEALED TO OTHERS OR USED FOR ANY PURPOSE WITHOUT THE WRITTEN CONSENT OF NABORS INDUSTRIES.						DR: DWG:	X20-0005-01	



- Drill string handling by THAD would not be happening when the full load on the top drive is happening
- The moment on the Derrick from THAD is 25% that from the top drive
- Derrick truss structure strength based on first order assessment (parallel axis theorem) of moment of inertia
 - $I = \text{Area corner chord} * \text{Height}^2$

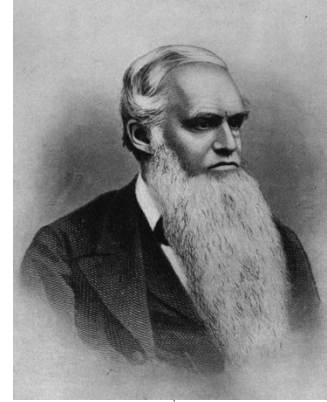
THAD Loads on Derrick		
written 2022.02.25 by Alex Slocum		
Inputs in BLACK , Outputs in BLUE		
Assume all cables from rig deck winches pull up backside of tower		
Static hook load	800,000	lbs
lines to block	12	
Cable tension	66,667	
distance to load center	60	in
spacing of tower leg chords	96	in
net moment bending backwards		
Moment from cable line up wrt centerline	3,200,000	in lbs
Moment from load being lifted	-9,600,000	in lbs
Net moment (bending forwards)	-6,400,000	in lbs
THAD reach fwd from center of rig tower	25.00	ft
	300	in
Static hook load	5,000	lbs
lines to block	2.00	
Cable tension	2,500	
Moment from cable line up wrt centerline	120,000	
Moment from load being lifted	-1,500,000	
Max THAD moment bending forwards	-1,620,000	
Total moment on tower. (Top drive and THAD)	-8,020,000	
Ratio current static hook load for top drive lift to proposed THAD	0.25	
Counterweight cantilever back from center of tower	8.00	ft
	96	in
counterweight mass needed	16,875	lbs
Assume rig tower truss "legs" (chords) are angle irons		
angle size	6.00	in
thickness	0.50	in
area	6.00	in^2
Truss estimated moment of inertia	55,296	in^4
I/c	1,152	
stress allowed in steel	10,000	
Allowable bending moment	11,520,000	
current safety factor	1.80	
safety factor after adding THAD	1.44	

”R-Theta” Arm sizing

- Where should the pivot axis be to not conflict with the sheeves for the main winch cable?
- How should boom be mounted and actuated?
 - Slewing ring and hydraulic or electric motor?
- How should the trolley be actuated?
- What boom structure type?
 - Tube (trolley wheels on corners)?
 - Truss (trolley wheels on chords)
 - I beam (trolley wheels on flange)
- Parallel axis theorem allows for quick first order assessment

Assume a square tube		
Wall thickness	0.5	in
width	16	in
I	1180	in ⁴
I/c	150	in ³
effective cross sectional area for mass estimate	30	in ²
Mass	2651	lbs
Assume a truss		
Angles		
leg	4	in
thick	0.5	in
area	4	in ²
height	18.75	in
I	1406	in ⁴
I/c	150	in ³
effective cross sectional area for mass estimate (braces 40% smaller than chords)	32	in ²
Mass	2784	lbs
Assume an I beam		
Flange width	12	in
flange thick	0.75	in
web thick	0.5	in
Beam height	15.5	in
I	1162	in ⁴
I/c	150	in ³
effective cross sectional area for mass estimate	25	in ²
Mass	2207	lbs

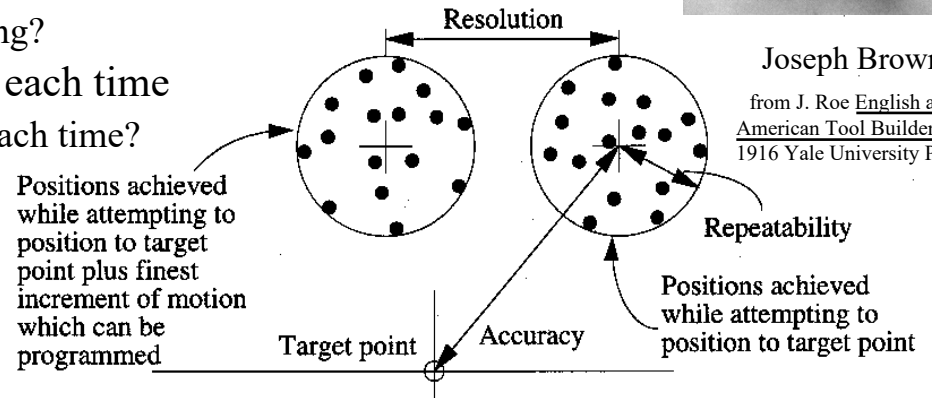
Accuracy, Repeatability, & Resolution



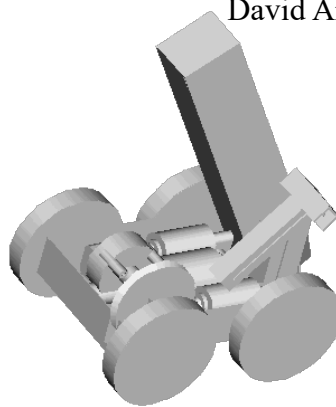
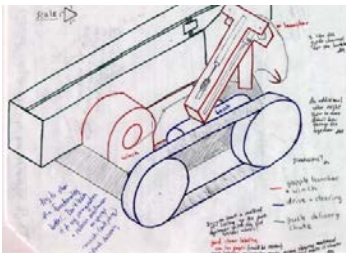
Joseph Brown

from J. Roe English and
American Tool Builders, ©
1916 Yale University Press

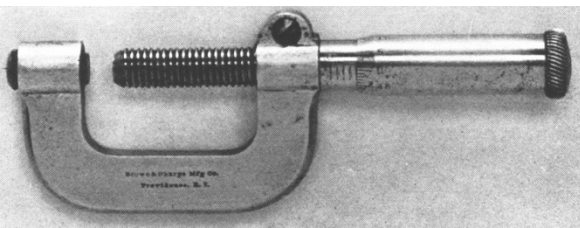
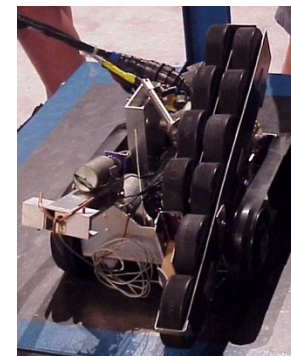
- Anything you design and manufacture is made from parts
 - Parts must have the desired accuracy, and their manufacture has to be repeatable
- *Accuracy*: the ability to tell the truth
 - Can two machines make exactly the same part?
 - Are the parts the exact size shown on the drawing?
- *Repeatability*: the ability to tell the same story each time
 - Can the machine make the exact same motion each time?
 - Are the parts all the same size?
- *Resolution*: the detail to which you tell a story
 - How fine can you adjust a machine?
 - How small a feature can you make?
- How do these affect the design process?



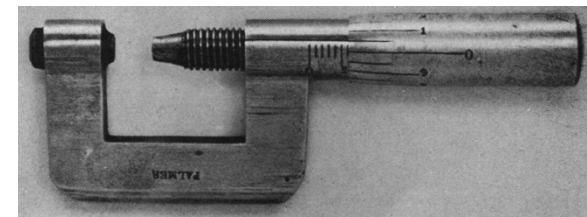
Hook launcher Model	
weight of hook (Kg)	0.05
muzzle velocity	9.4
Number of springs	2
d (draw)	0.095216
Winch model	
radius	0.05
mass	6
w (rpm)	55
torque	2.1
velocity	0.287833



David Arguellis wins “MechEverest” with a machine that repeats every time!



One-inch Micrometer (left) made by Brown & Sharpe, 1868 and
Palmer Micrometer (right) brought from Paris by Brown in 1867
from J. Roe English and American Tool Builders, © 1916 Yale University Press



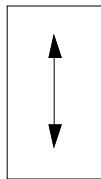
Accuracy, Repeatability, & Resolution: *Mapping*

- It is often most important to obtain mechanical *repeatability*, because *accuracy* can often be obtained by the sensor and control system
 - When the error motions of a machine are *mapped*, the controller multiplies the part height by the axis' pitch & roll to yield the sine error for which orthogonal axes must compensate



Eli Whitney

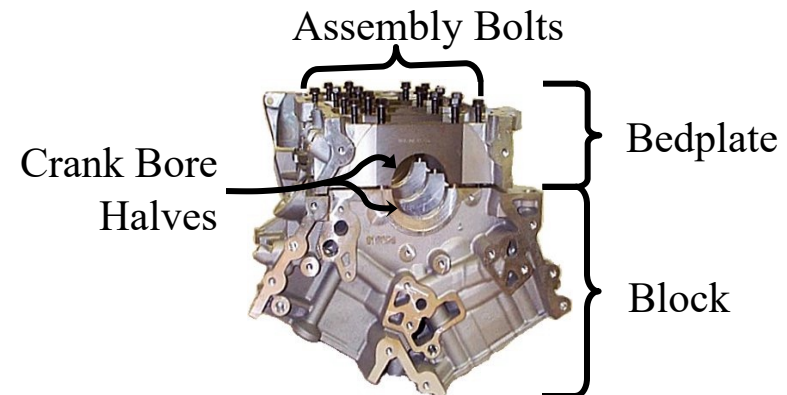
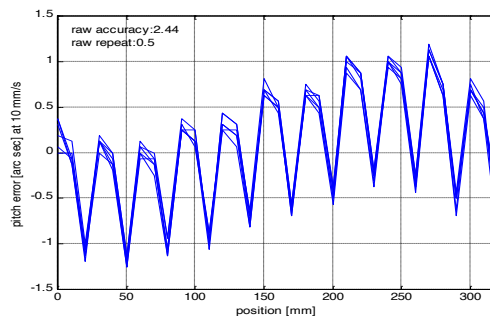
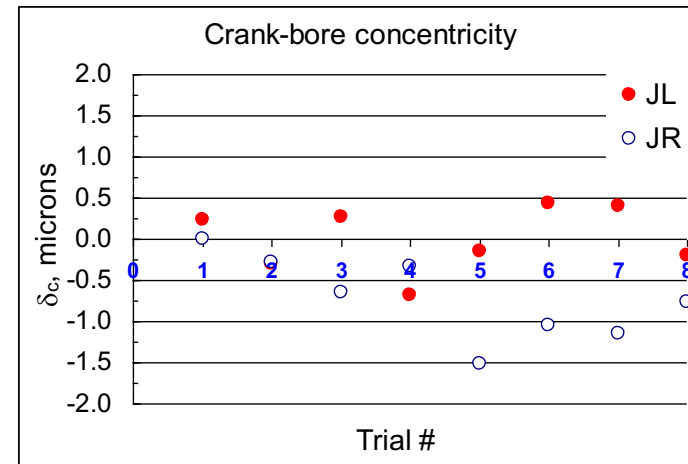
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Y axis: Can be used to compensate for straightness errors in the X axis.

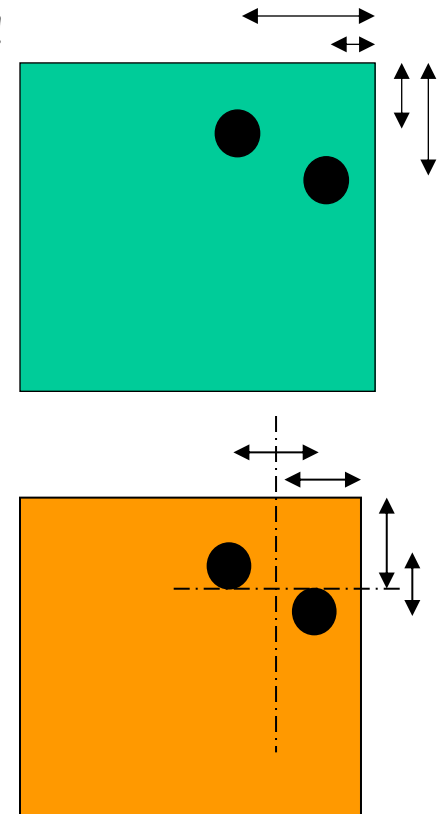
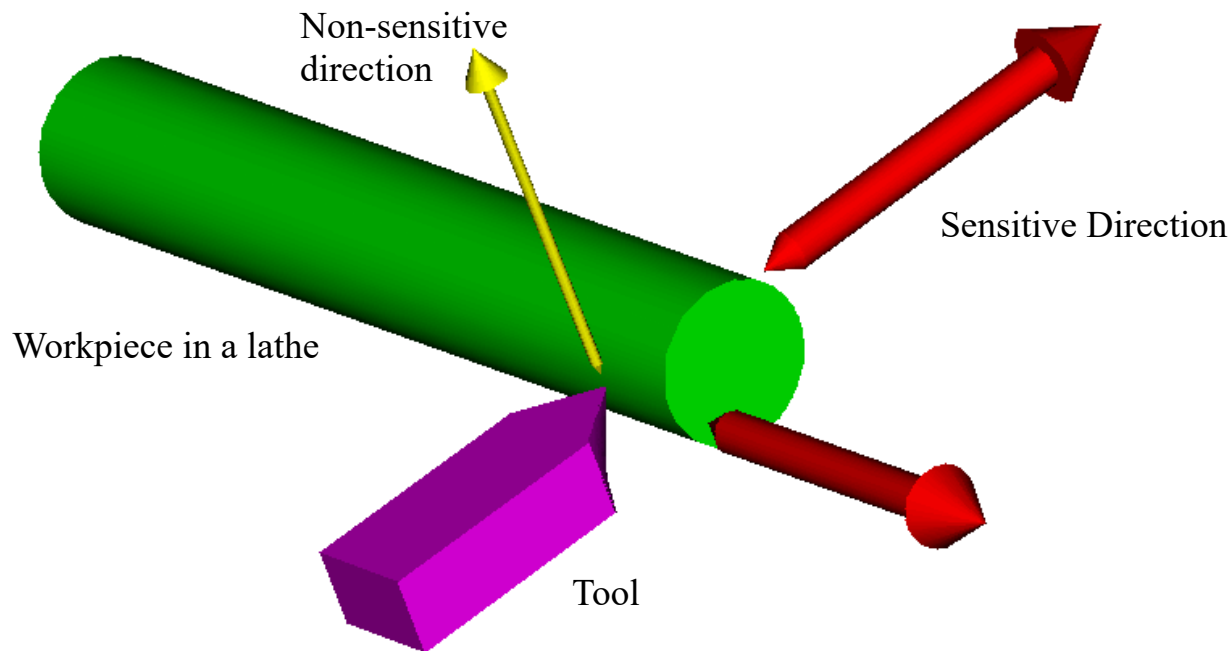


X axis: Can be used to compensate for straightness errors in the Y axis.



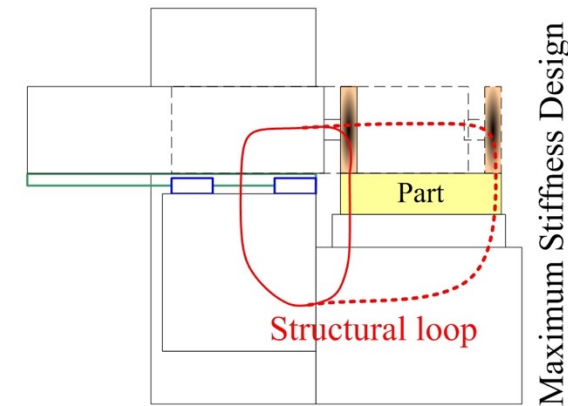
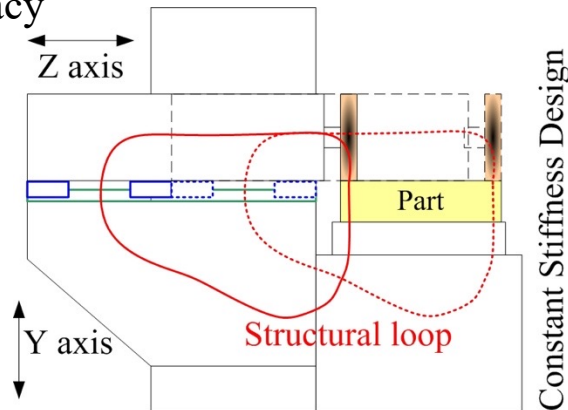
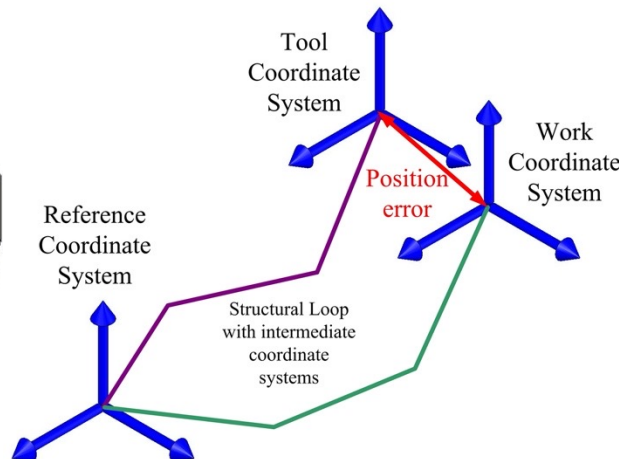
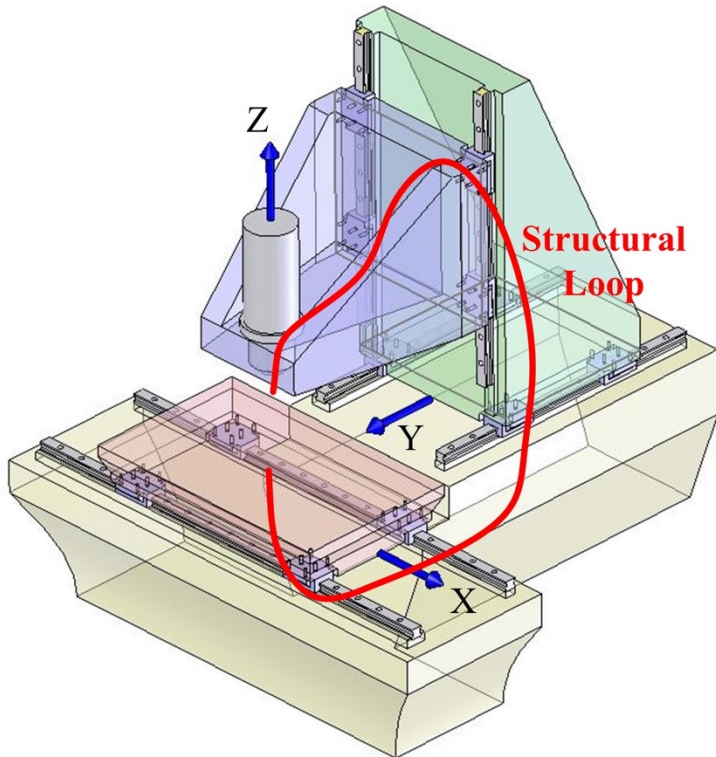
Sensitive Directions & Reference Features

- In addition to *accuracy*, *repeatability*, and *resolution*, we have to ask ourselves, “when is an error really important anyway?”
 - Put a lot of effort into accuracy for the directions in which you need it
 - The *Sensitive Directions*
 - Always be careful to think about where you need precision!



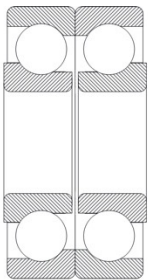
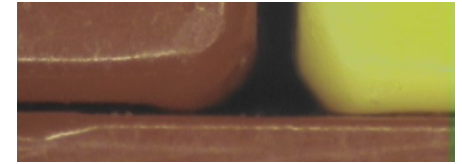
Structural Loops

- The *Structural Loop* is the path that a load takes from the tool to the work
 - It contains joints and structural elements that locate the tool with respect to the workpiece
 - It can be represented as a stick-figure to enable a design engineer to create a *concept*
 - Subtle differences can have a HUGE effect on the performance of a machine
 - The *structural loop* gives an indication of machine stiffness and accuracy
 - *The product of the length of the structural loop and the characteristic manufacturing and component accuracy (e.g., parts per million) is indicative of machine accuracy (ppm)*
 - Long-open structural loops have less stiffness and less accuracy
 - *All along the loop, $F = kx$ rules!*

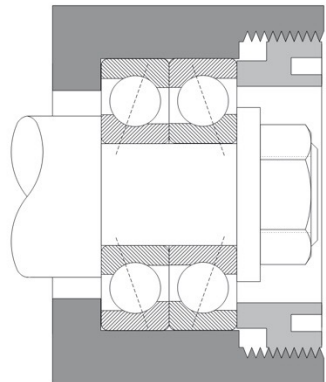


Preload

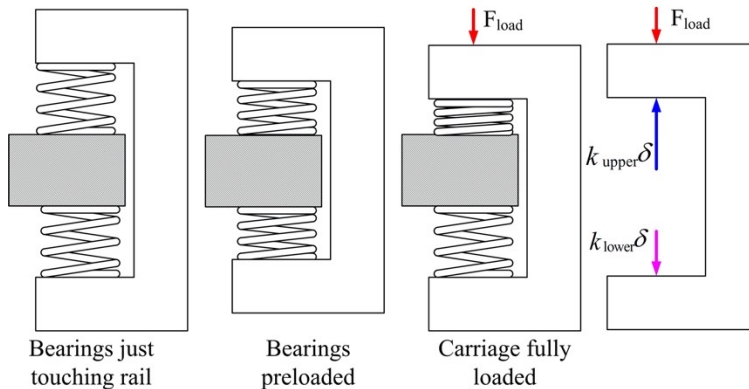
- Components that move relative to one another generally have tolerances that leave clearances between their mating features
 - These clearances result in *backlash* or wobble which is difficult to control
 - An example is the Lego roller coaster on page 3-10
- Because machine elements often have such small compliance, and to account for wear, backlash is often removed with the use of *preload*
 - Preload involves using a spring, or compliance in the mechanism itself, to force components together so there is no clearance between elements



Bearings before mounting (inner ring axial clearance exaggerated)



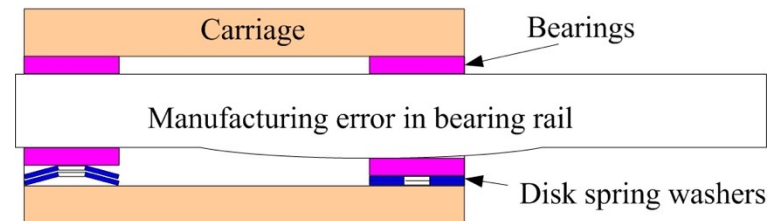
Back-to-back mounting after inner rings are clamped together



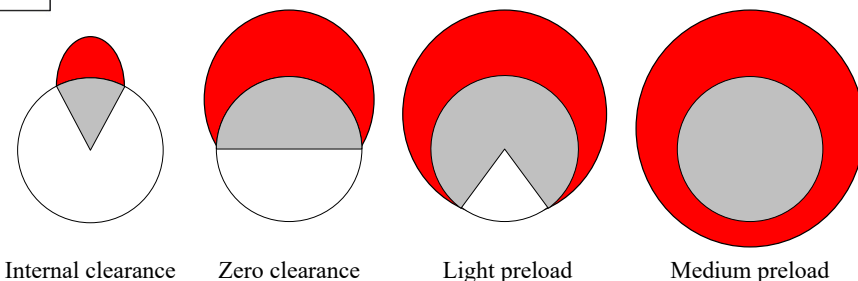
Bearings just touching rail

Bearings preloaded

Carriage fully loaded



Load distribution on rolling elements due to radial load applied to bearings with various preload conditions



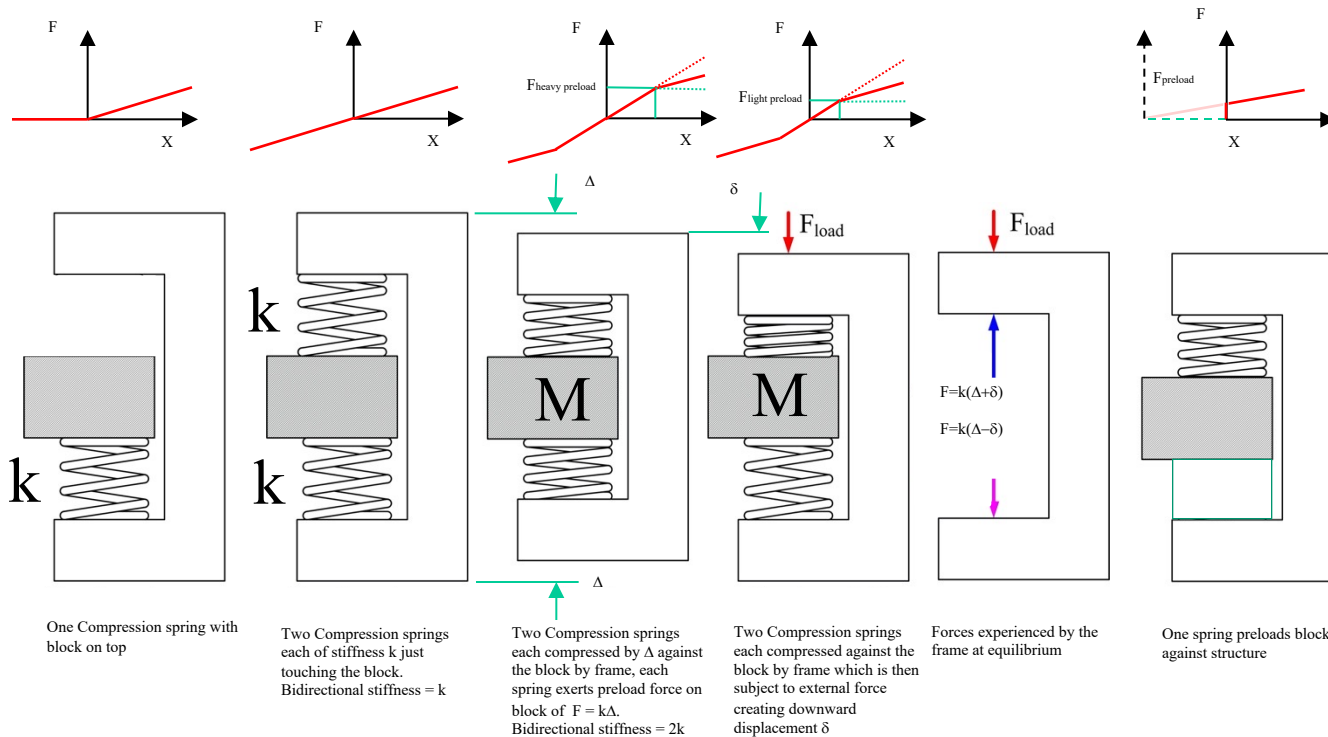
Internal clearance

Zero clearance

Light preload

Medium preload

Spring Preload



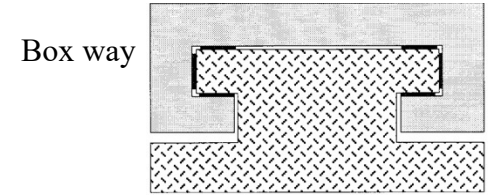
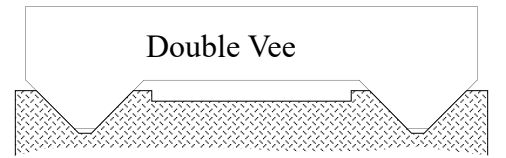
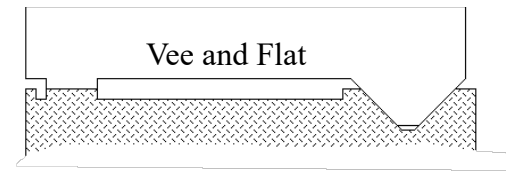
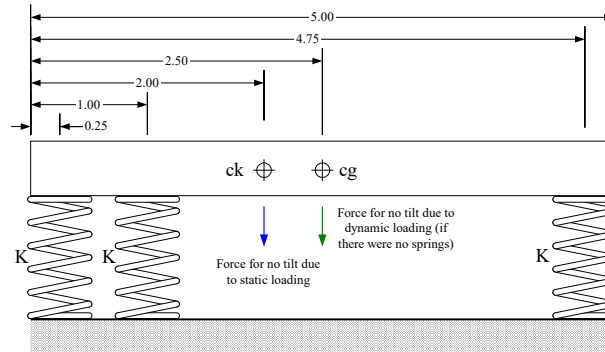
When the compression springs, each of stiffness k and mass m , are preloaded against a center block of mass M which is then displaced by δ , the energy stored is $k\delta^2$. If the mass is suddenly released, then the velocity of the mass M when it returns to the center position will be approximately

$$V_M = \sqrt{\frac{2k\delta^2}{M + m}}$$

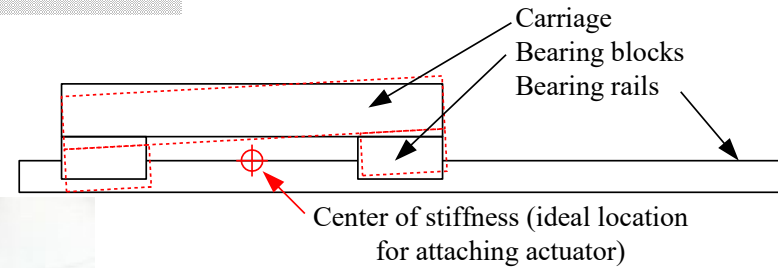
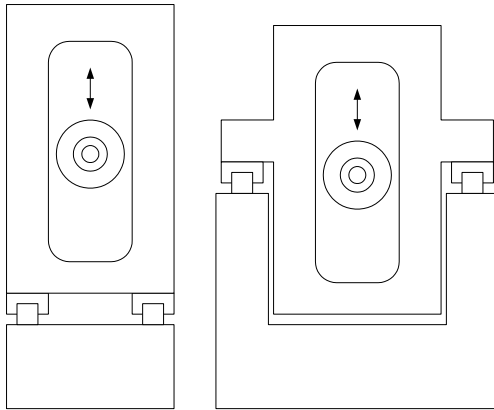
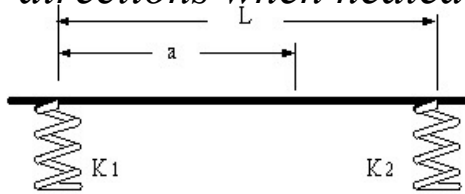
Centers-of-Action

- The *Centers-of-Action* are points at which when a force is applied, no moments are created:

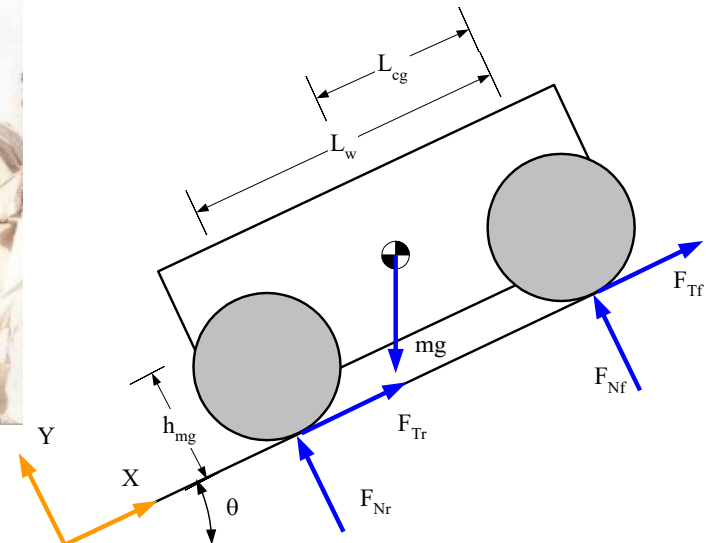
- *Center-of-Mass*
- *Center-of-Stiffness*
- *Center-of-Friction*



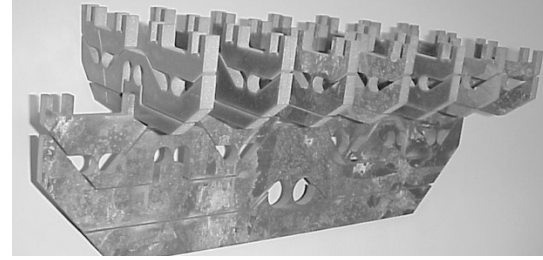
- The *Center-of-Thermal Expansion* is the point about which the structure appears to expand equally in all directions when heated.



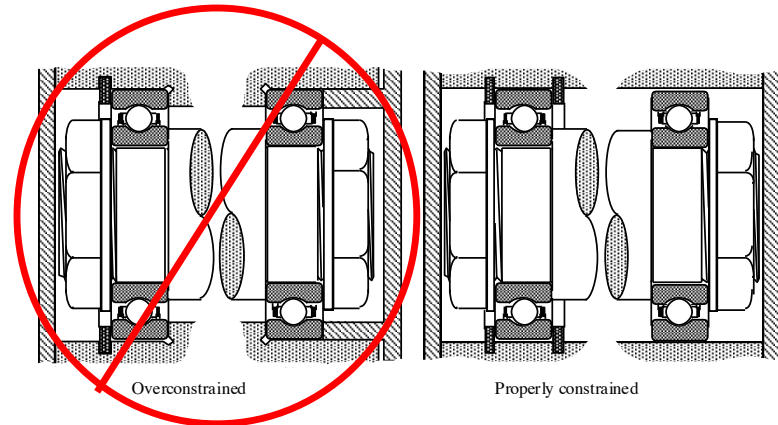
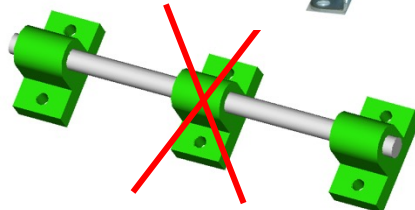
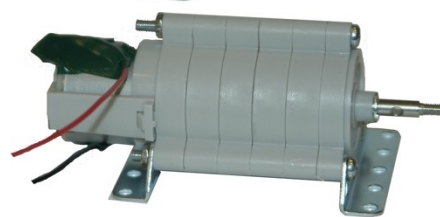
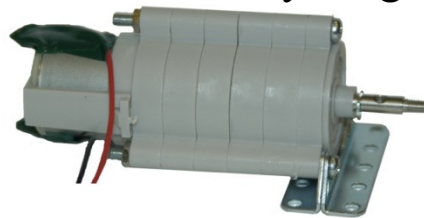
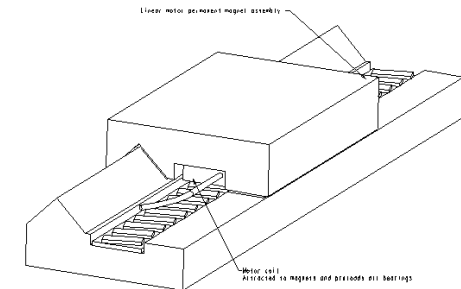
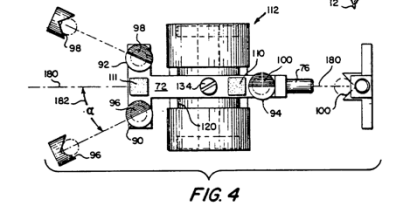
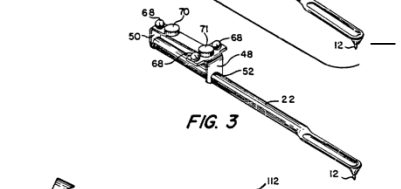
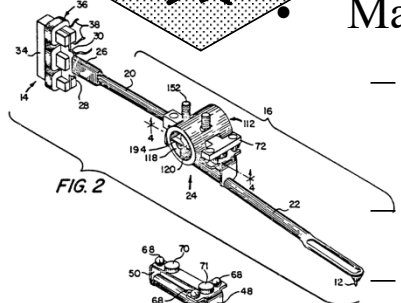
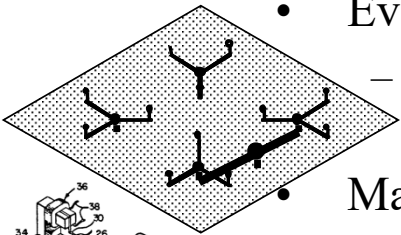
Funny image found on http://zeeb.at/oops/Nothing_Changes.jpg, photographer not credited, would like to, email slocum@mit.edu



Exact Constraint Design



- Every rigid body has 6 *Degrees of Freedom* (DOF)
 - An exactly constrained design has no chance of deforming or having its function impaired be it by assembly, fastener tightening, thermal expansion, or external loads
- Make sure you have constrained what you want to constrain!
 - For a body to have N degrees of freedom free to move, there must be 6-N bearing reaction points!
 - To resist translation, a force is required.
 - To resist rotation, a moment, or two forces acting as a couple, is required!
- Saint-Venant rules! Do not constrain a shaft with more than 2 bearings, unless it is very long...

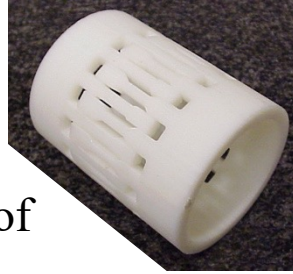


Wiffle (Whupple) trees...

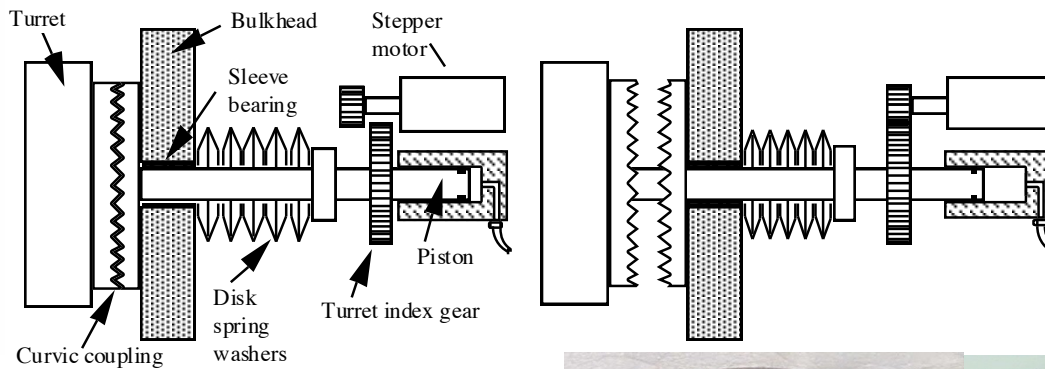
- Mechanism to distribute force evenly using bars (linkages) with "frictionless" joints
 - i.e., equalizer, spreader bar...
 - Practical application: ☺



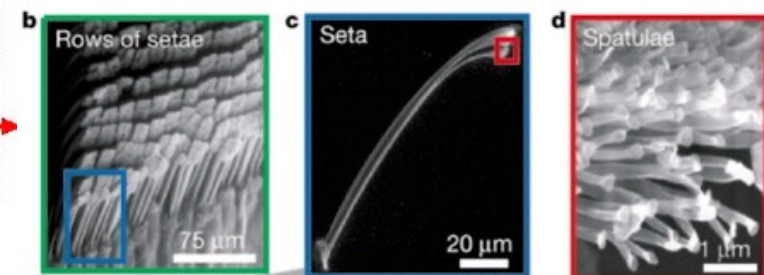
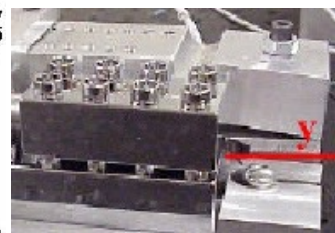
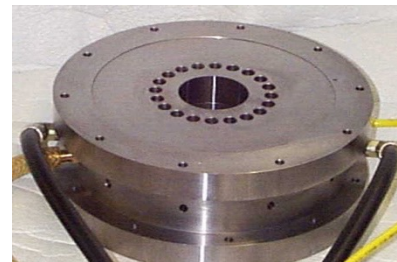
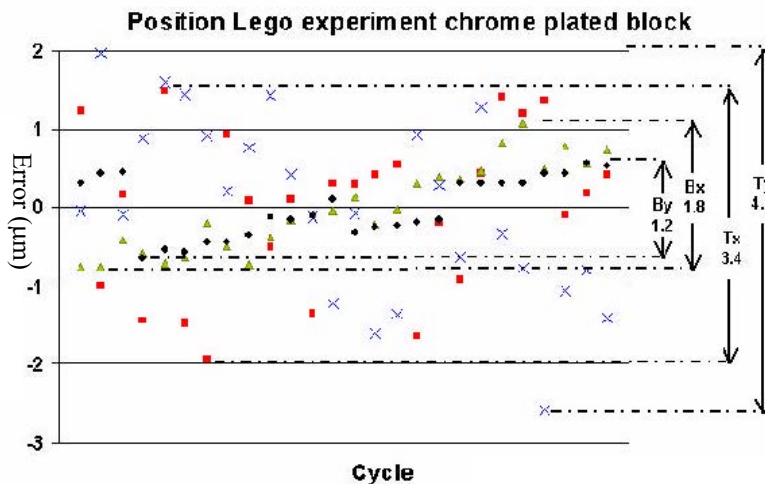
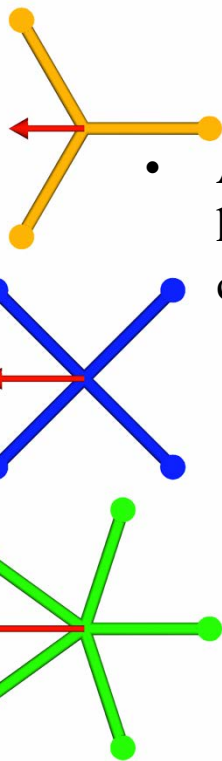
Elastically Averaged Design



- Applying *Reciprocity to Exact Constraint Design* implies that instead of having an exact number of constraints, have an “infinite” number of constraints, so the error in any one will be averaged out!
 - Legos™, five legged chairs, windshield wipers, and Geckos are the most common examples, and many machine components achieve accuracy by elastic averaging



K. Autumn, Y. Liang, W.P. Chan, T. Hsieh, R. Fearing, T.W. Kenny, and R. Full, *Dry Adhesive Force of a Single Gecko Foot-Hair*, Nature, 405: 681-685 (2000)



Stainless Steel Wool!

Precision Engineering 42 (2015) 346–351



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Technical note

Entangled structures as high cycle compression springs

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ABSTRACT

Entangled structures, such as steel wool, can be used as inexpensive, high cycle, low stiffness, thin profile compressive springs where uniform pressure on a surface is required particularly in elevated temperature and/or harsh environments. Mechanical compression tests were performed on a variety of steel wool samples to determine the stress–strain curve behavior over high cycles. After initial conditioning cycles, good repeatability can be obtained with hysteresis dependent on strain. The results show a nonlinear behavior over large strains (>10%) and reasonable linear behavior for strains less than 10%. The properties of an entangled structure spring can be selected to achieve the desired stiffness for a particular application.

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Stick Figures

- Use of *fundamental principles* allows a designer to sketch a machine and error motions and coordinate systems just in terms of a *stick figure*:
 - The sticks join at centers of stiffness, mass, friction, and help to:
 - Define the sensitive directions in a machine
 - Locate coordinate systems
 - Set the stage for error budgeting
 - The designer is no longer encumbered by cross section size or bearing size
 - It helps to prevent the designer from locking in too early
- Error budget and preliminary load analysis can then indicate the required stiffness/load capacity required for each “stick” and “joint”
 - Appropriate cross sections and bearings can then be deterministically selected
- It is a “backwards tasking” solution method that is very very powerful!

