# Maple SYREP <br> Version 2.1 

## Quick Reference

## 1. Loading SYREP:

At the Maple prompt:

```
restart: (not strictly required, but a good idea)
read '/syrepdir/syrep.m': (/syrepdir/ is path to SYREP's directory;
    note the use of back-quotes (') and forward slashes (/).)
Display_digits(5): (Set display precision to desired level.)
```


## 2. Argument conventions:

In all following SYREP function descriptions the arguments follow the guidelines:

| $\}$ | Indicates an optional argument. In some cases the argument is optional for SISO <br> systems,and must be supplied for MIMO systems. When multiple arguments are <br> specified within the brackets, all or none must be supplied. |
| :--- | :--- |
| [arg] | Indicates that arg is a Maple list in the format [item1, item2, $\ldots$, itemN]. The <br> items themselves may be lists. |
| sys | The name assigned to the system at its creation, for example <br> sys := LGraph_to_system(graph, outputs): |
| \{inp, out $\}$ | Input and output variable names. Optional for SISO systems but mandatory for <br> MIMO systems. |
| var | A variable name for use in the output display, for example the Laplace variable in <br> a transfer function. Usually a default name is available. |
| xrange | A Maple range specification of the form min. max, for example <br> Root_locus(mysys,B,0..150,200,-10..0,-20..20) |

## 3. Principal System Generation Procedures:



### 3.1 Source specification sub-list: (LGraph_to_system(), ZGraph_to_system())

List Structure: [tail_node, head_node, source_type, source_variable]
Examples: [1,2,velocity,Vsource], [2,4, current, I], [2,3,As,Vin]
$\left.\left.\begin{array}{|l|l|l|}\hline \text { Across-variable Source } & \text { Through-variable source } & \text { Primary domains } \\ \hline \text { As } & \text { Ts } \\ \text { velocity } \\ \text { angular_velocity } & \begin{array}{l}\text { force } \\ \text { torque } \\ \text { current } \\ \text { poltage }\end{array} & \begin{array}{l}\text { flow, flow_rate } \\ \text { pressure } \\ \text { temperature }\end{array}\end{array} \begin{array}{l}\text { translational } \\ \text { rotational } \\ \text { electrical }\end{array}\right\} \begin{array}{l}\text { fluid } \\ \text { theat_flow_rate }\end{array}\right]$

### 3.2 One-port element specification sub-list: (LGraph_to_system())

List Structure: [tail_node, head_node, 1port_type, parameter \{,across_variable, through_variable\}] Examples: [3,5,inertia, J,WJ,TJ], [2,4,D,3000], [8,4, A, m3, vm3, Fm3]

| Element type name | Parameter | Elemental relationship | Primary domains |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
| A | generalized A-type $(C)$ | $\dot{v}=(1 / C) f$ | generalized |
| C | generalized capacitance $(C)$ | $\dot{v}=(1 / C) f$ | generalized |
| mass | mass $(m)$ | $\dot{v}=(1 / m) f$ | translational |
| inertia | rotary inertia $(J)$ | $\dot{v}=(1 / J) f$ | rotational |
| capacitance | capacitance $(C)$ | $\dot{v}=(1 / C) f$ | electrical,fluid,thermal |
| T | generalized T-type $(L)$ | $\dot{f}=(1 / L) v$ | generalized |
| L | generalized inductance $(L)$ | $\dot{f}=(1 / L) v$ | generalized |
| spring | stiffness $(K)$ | $\dot{f}=K v$ | translational, rotational |
| stiffness | stiffness $(K)$ | $\dot{f}=K v$ | translational, rotational |
| compliance | compliance $(C)$ | $\dot{f}=(1 / C) v$ | translational, rotational |
| inductance | inductance $(L)$ | $\dot{f}=(1 / L) v$ | electrical |
| inertance | inertance $(I)$ | $\dot{f}=(1 / I) v$ | fluid |
| D | generalized D-type $(R)$ | $v=R f$ | generalized |
| R | generalized resistance $(R)$ | $v=R f$ | generalized |
| G | generalized conductance $(G)$ | $f=G v$ | generalized |
| damper | viscous coefficient $(B)$ | $f=B v$ | translational, rotational |
| dashpot | viscous coefficient $(B)$ | $f=B v$ | translational, rotational |
| resistance | resistance $(R)$ | $v=R f$ | electrical, fluid, thermal |
| conductance | conductance $(G)$ | $f=G v$ | elaical, fluid, thermal |

### 3.3 Impedance element sub-list: (ZGraph_to_system())

List Structure: [tail_node, head_node, branch_type, impedance \{,across_variable, through_variable\}]
Examples: $\quad[2,3, Z, R+s * L, v L, i L]$ [ 4,3 , admittance, $s * m+B]$ [11,7, $\mathrm{Y}, 13.33+s * 15.1]$

| Branch type name | Impedance/Admittance | Elemental relationship | Domains |
| :--- | :---: | :---: | :--- |
| impedance | impedance $(Z)$ | $V(s)=Z F(s)$ | all domains |
| Z | impedance $(Z)$ | $V(s)=Z F(s)$ | all domains |
| addmittance | admittance $(Y)$ | $F(s)=Y V(s)$ | all domains |
| Y | admittance $(Y)$ | $F(s)=Y V(s)$ | all domains |

### 3.4 Two-port element sub-list: (LGraph_to_system(), ZGraph_to_system())

Structure: [[tail_a,head_a],[tail_b,head_b] 2port_type,ratio \{,[across_a through_a], [across_b,through_b]\}]
Examples: [[2,3],[7,8],transformer,1/Km,[vback,imotor],[Wm,Tm]] [[1,2],[5,3],GY,r]

| Two-port type name | Ratio | Elemental relationships | Domains |
| :--- | :---: | :---: | :--- |
| TF <br> transformer | $r$ | $v b=r . v a$ <br> $f b=-(1 / r) f a$ | all domains |
| GY <br> gyrator | $r$ | $v b=r . f a$ <br> $f b=-(1 / r) v a$ | all domains |

## 4. Additional System Generation Procedures:

| Procedure | Function |
| :--- | :--- |
| Gain(K) | Generate a system description for a gain block <br> with gain $K$. <br> Generate a system description for an integrator <br> with gain $K$. <br> Generate a system description for a differentiator <br> Differentiator(K) <br> PID(Kp,Ki,Kd) <br> with gain $K$. <br> Generate a system description for a PID con- <br> troller. <br> Cascade_systems(sys1,sys2\{,input,output $\})$ <br> Combine two (non-loading) systems in series: <br> $H(s)=H_{1}(s) H_{2}(s)$ ). <br> Parallel_systems(sys1,sys2\{,input,output $\})$ <br> Combine two (non-loading) systems in parallel: <br> $H(s)=H_{1}(s)+H_{2}(s)$. <br> SISO(sys,inp,out) |

## 5. Impedance manipulation Procedures:

| Procedure | Function |
| :--- | :--- |
| Z_series(Z1, Z2, $\ldots, \mathrm{Zn})$ | Returns the impedance of the series connection of an arbitrary <br> number of impedances. <br> Returns the impedance of the parallel connection of an arbitrary <br> number of impedances. <br> Returns the admittance of the series connection of an arbitrary <br> number of admittances. <br> Returns the admittance of the parallel connection of an arbitrary <br> number of admittances. <br> Reseries(Y1, Y2, $\ldots, \mathrm{Yn})$ <br> Returns an admittance $Y=1 / Z$ <br> Returns an impedance $Z=1 / Y$ |
| Z_to_Y(Z) <br> Y_to_Z(Y) | Y1, Y2, $\ldots, \mathrm{Yn)}$ |

## 6. System Description and Property Procedures:

| Procedure | Function |
| :---: | :---: |
| A matrix(sys) | Returns the system A matrix |
| B_matrix(sys) | Returns the system B matrix |
| C_matrix(sys) | Returns the system C matrix |
| D_matrix(sys) | Returns the system D matrix |
| Ematrix(sys) | Returns the system E matrix |
| F_matrix(sys) | Returns the system F matrix |
| System_order (sys) | Returns the system order |
| State_variables(sys) | Returns the vector of state-variable names |
| System_Inputs (sys) | Returns a vector of the system input variable names. |
| System_Outputs (sys) | Returns a vector of the system output variable names. |
| State_equations(sys) | Displays the system state and output equations in matrix form. |
| Differential_equation(sys $\{$,inp,out\}) | Displays the differential equation (in differential $(S)$ operator notation) relating a single output to a single input. |
| Transfer_function(sys\{,inp,out $\{$, var\}) | Returns the transfer function relating a single output to a single input. |
| Transfer_function_matrix (sys $\{$, var $\}$ ) | Returns the transfer function matrix relating all outputs to all inputs. |
| System_char_poly (sys\{,var\}) | Returns the system characteristic polynomial. |
| System_eigenvalues (sys) | Returns the system eigenvalues. |
| System_poles(sys) | Returns the system poles (same as the system eigenvalues). |
| System_zeros(sys\{, inp,out ${ }^{\text {( }}$ ) | Returns the zeros of the transfer function between a given input and output. |
| Pole_zero_plot (sys $\{$, inp,out $\}$ ) | Displays the pole-zero plot for the transfer function between a given input and output. |
| System_type(sys) | Returns the system "type", that is the number of free integrators (poles at the origin of the $s$-plane). |
| Root_locus(sys, param, prange, nsteps \{, xrange\}\{,yrange\}) | Displays a generalized root-locus for the variation of any system parameter. |
| Controllability matrix(sys) | Returns the system controllability matrix. |
| Controllability (sys) | Returns the rank of the system controllability matrix. |
| Controllable(sys) | Returns true if system is controllable, false otherwise. |
| Observability_matrix(sys) | Returns the system observability matrix. |
| Observability(sys) | Returns the rank of the system observability matrix. |
| Observable(sys) | Returns true if system is observable, false otherwise. |
| Position_error_constant (sys) | Returns the position error constant, $\lim (s \rightarrow 0)\{G(s)\}$. |
| Velocity_error_constant (sys) | Returns the velocity error constant, $\lim (s \rightarrow 0)\{s G(s)\}$. |
| Accel_error_constant (sys) | Returns the acceleration error constant, $\lim (s \rightarrow 0)\left\{s^{2} G(s)\right\}$. |
| Time_constant(sys) | Returns the time constant $\tau$ (s) of a first order system. |
| Natural_frequency (sys) | Returns the undamped natural frequency $\omega_{n}(\mathrm{rad} / \mathrm{s})$ of a second order system. |
| Damping_ratio(sys) | Returns the damping ratio $\zeta$ of a second order system |
| System_exponential(sys,t) | Compute the matrix exponential $e^{\mathbf{A} t}$ for the system. |

## 7. Time Domain Response Procedures:

| Procedure | Function |
| :---: | :---: |
| Step_response(sys\{,inp,out\}) | Returns the system unit step response function between a given input and output. |
| Impulse_response (sys $\{$, inp,out $\}$ ) | Returns the system impulse response function between a given input and output. |
| Ramp_response(sys\{,inp,out\}) | Returns the system ramp response function between a given input and output. |
| System_response(sys, function $\{$, inp,out $\}$ ) | Returns the response of a system to an arbitrary input function. |
| Final_value(sys,stepsize\{,inp,out ${ }^{\text {a }}$ ) | Returns the final value of the response to a step of size stepsize. |
| Output_IC_response(sys,ic) | Returns the response of a SISO system output to a given set of initial conditions on the system output variable. |
| State_IC_response(sys,ic\{,out $\}$ ) | Returns the response of a system output to a given set of initial conditions on the system states. |

## 8. Control Systems Procedures::

| Procedure | Function |
| :---: | :---: |
| $\begin{aligned} & \text { Closed_loop_system(plant, ctrl\{,feedback }\} \\ & \{\text {,inp,out }\}) \end{aligned}$ | Returns a system representing the closed-loop SISO system with output feedback, and the given controller and sensor dynamics. |
| ```Open_loop_system(plant,ctrl{,feedback} {,inp,out}) Phase_margin(sys)``` | Returns a system representing an open-loop SISO system with output feedback, and controller and sensor dynamics. Returns the phase margin (deg) of an open-loop SISO system. |
| Gain_margin(sys) | Returns the gain margin (dB) of an open-loop SISO system. |
| State_feedback(plant, gain_matrix) | Generates a description for the system formed with full state feedback as specified by the gain matrix. |
| Ackerman(plant, char_poly) | Uses Ackerman's formula to return the state feedback gain matrix to achieve the closed-loop pole placement specified by the polynomial char_poly. |

## 9. Frequency Domain Response Procedures:

| Procedure | Function |
| :---: | :---: |
| Frequency_response_matrix(sys\{,var\}) | Returns the frequency response matrix relating all outputs to all inputs. |
| Frequency_response(sys $\{$, inp,out $\}\{, \operatorname{var}\})$ | Returns an ndividual frequency response function relating a single output to a single input. |
| Frequency_response_magnitude(sys\{,inp,out $\{$, var\}) | Returns the magnitude function relating a single output to a single input. The value of the magnitude function at a particular frequency can be found by substituting a numerical value for 'var'. |
| Frequency_response_phase(sys \{,inp,out $\{$, var\}) | Returns the phase function relating a single output to a single input. The phase response at a particular frequency may be found by substituting a numerical value for 'var'. |
| Find_magnitude(sys, mag\{,inp,out $\}$, frange $\}$ ) | Returns the frequencies ( $\mathrm{rad} / \mathrm{s}$ ) at which the frequency response has the given magnitude 'mag'. |
| Find_phase(sys, phase\{,inp,out $\}$, frange $\}$ ) | Returns the frequencies ( $\mathrm{rad} / \mathrm{s}$ ) at which the frequency response has the given phase 'phase'. |
| Bode_magnitude(sys, frange\{,inp,out $\}$ ) | Displays a Bode magnitude plot (in decibels) of the transfer function between a given input and output. |
| Bode_phase(sys, frange\{,inp,out\}) | Displays a Bode phase plot (in degrees) of the transfer function between a given input and output. |
| Polar_plot(sys, frange\{,inp,out\}\{,npoints\}) | Displays the polar form of the frequency response function |
| LogMag_phase(sys, frange\{,inp,out $\{$, npoints $\}$ ) | Displays the log-magnitude ( dB ) versus phase (deg) form of the frequency response function. |

## 10. Utility Procedures:

| Procedure | Function |
| :--- | :--- |
| Version() <br> Display_digits(n) | Displays the version of SYREP <br> Sets the display precision returned by SYREP <br> procedures. |

