

EDM Experiments vs TeV-Scale New Physics

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Based on: [arXiv:2104.02679](https://arxiv.org/abs/2104.02679) with Daniel Aloni,
Pouya Asadi, Yuichiro Nakai, Motoo Suzuki

Question

Electron EDM experiments are now probing mass scales well above 1 TeV.

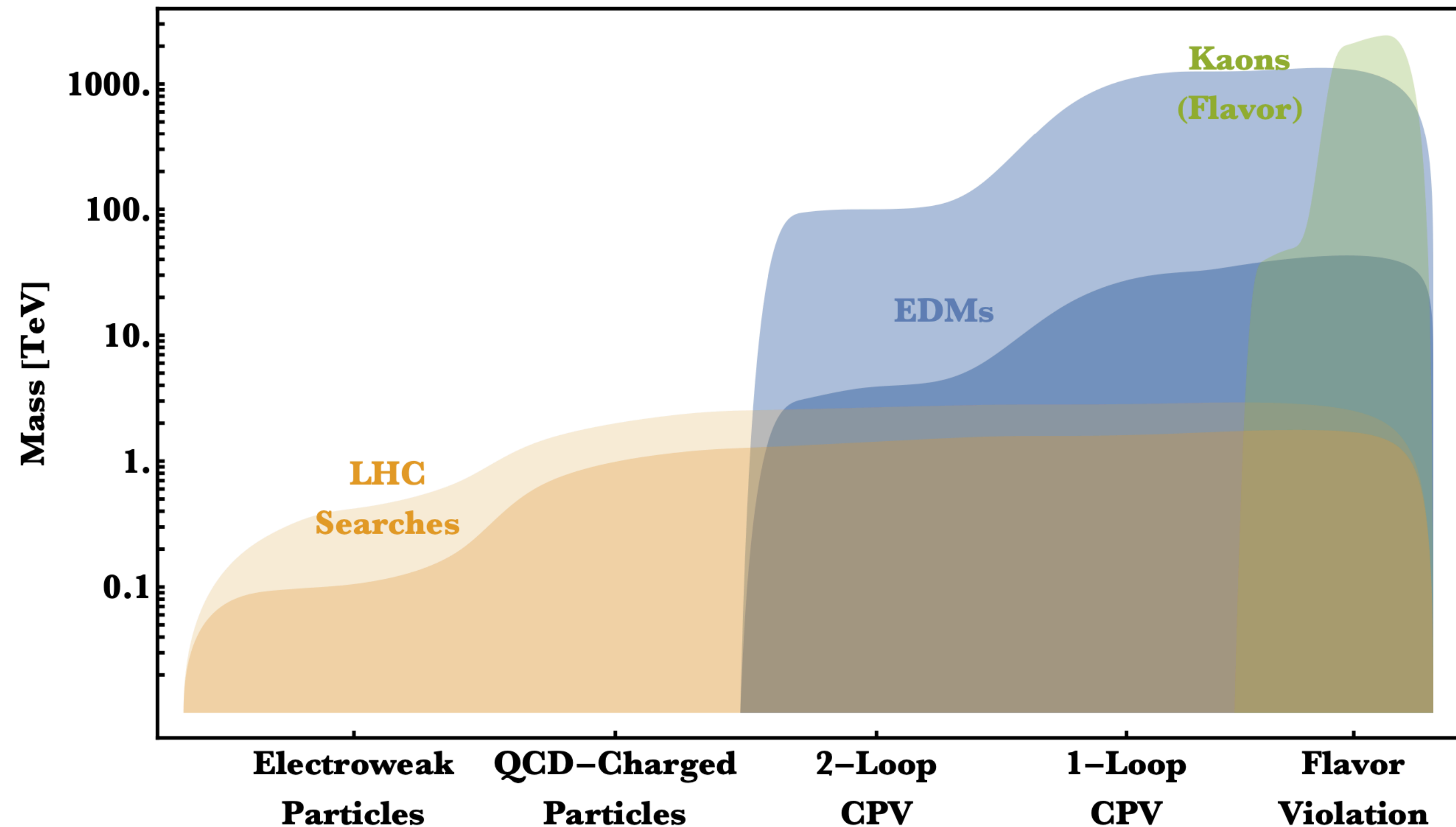
Colliders and muon $g - 2$ experiments are looking for particles around 1 TeV.

Are EDM experiments bad news for such searches?

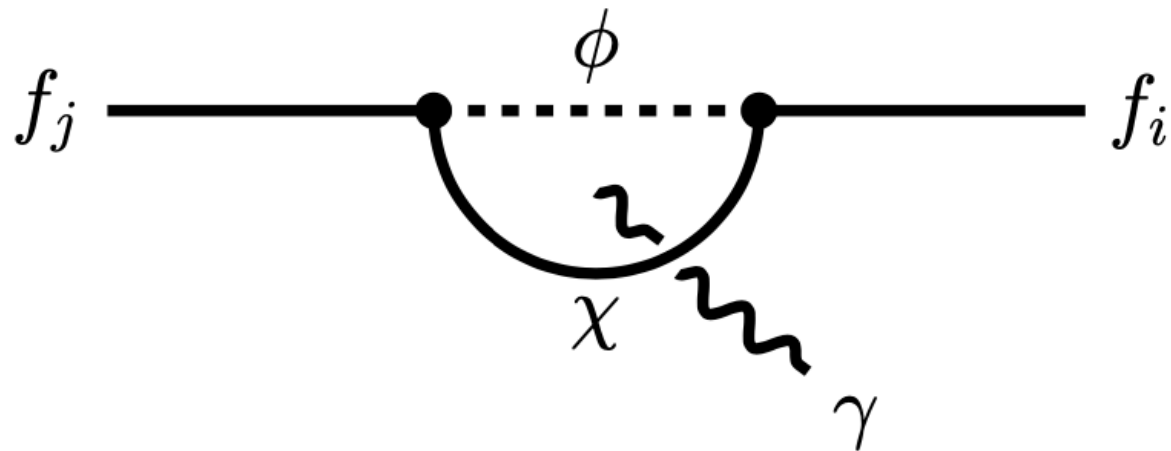
To answer this, we should think more about the fundamental physics of **CP** and **flavor**.

Mass Reach Comparison: A Cartoon

← Fewer Symmetries Violated



Lepton Dipole Operators



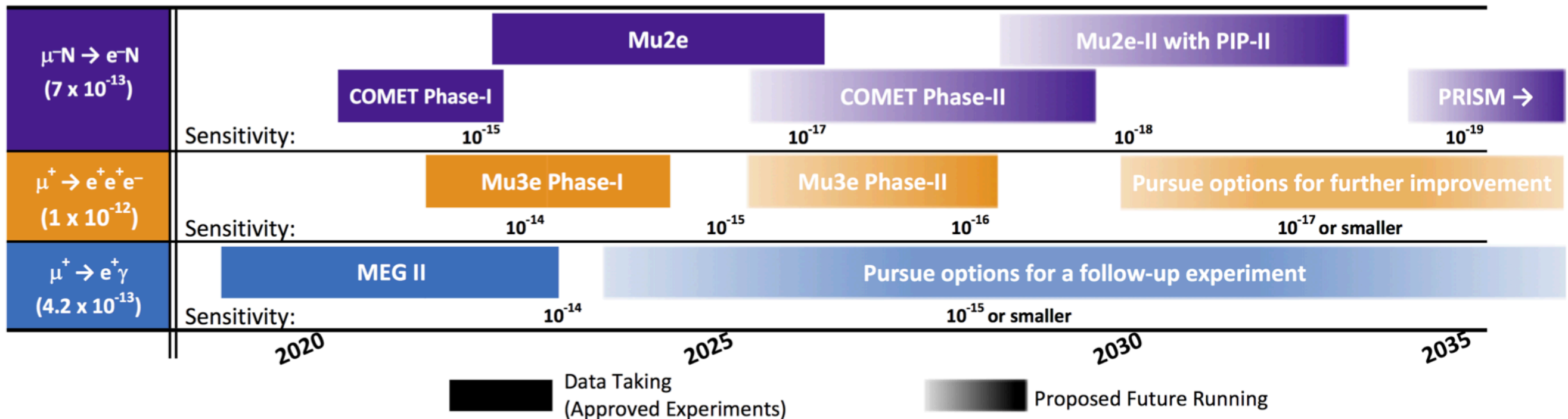
- Electron EDM
- Muon $g - 2$
- $\mu \rightarrow e\gamma$
- $\tau \rightarrow \mu\gamma, \tau \rightarrow e\gamma$

If we see new physics in one of these, do we expect to see new physics in all of these?

Is new physics in muon $g - 2$ already excluded? E.g., by lack of new physics in the electron EDM?

Charged Lepton Flavor Violation

Searches for Charged-Lepton Flavor Violation in Experiments using Intense Muon Beams



Source: Baldini et al., 1812.06540, submission to 2020 European Strategy from COMET, MEG, Mu2e and Mu3e collaborations

Comparisons: Flavor & CP Observables

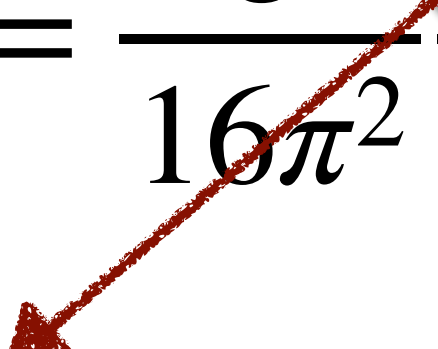
Observable	Current bound	Current Λ (TeV)	Future reach	Future Λ (TeV)
eEDM	$1.1 \times 10^{-29} e \text{ cm}$	1.0×10^3	$\sim 10^{-32} e \text{ cm}$	3.3×10^4
BR ($\mu \rightarrow e\gamma$)	4.2×10^{-13}	57.	$\sim 10^{-14}$	1.5×10^2
R ($\mu N \rightarrow eN$)	7×10^{-13} (Au)	12.	$\sim 10^{-17}$ (Al)	1.8×10^2
BR ($\mu \rightarrow 3e$)	10^{-12}	13.	$\sim 10^{-16}$	1.3×10^2

Bound based on
$$C_{ij} = \frac{eg^2}{16\pi^2} \frac{m_\mu}{\Lambda^2}$$

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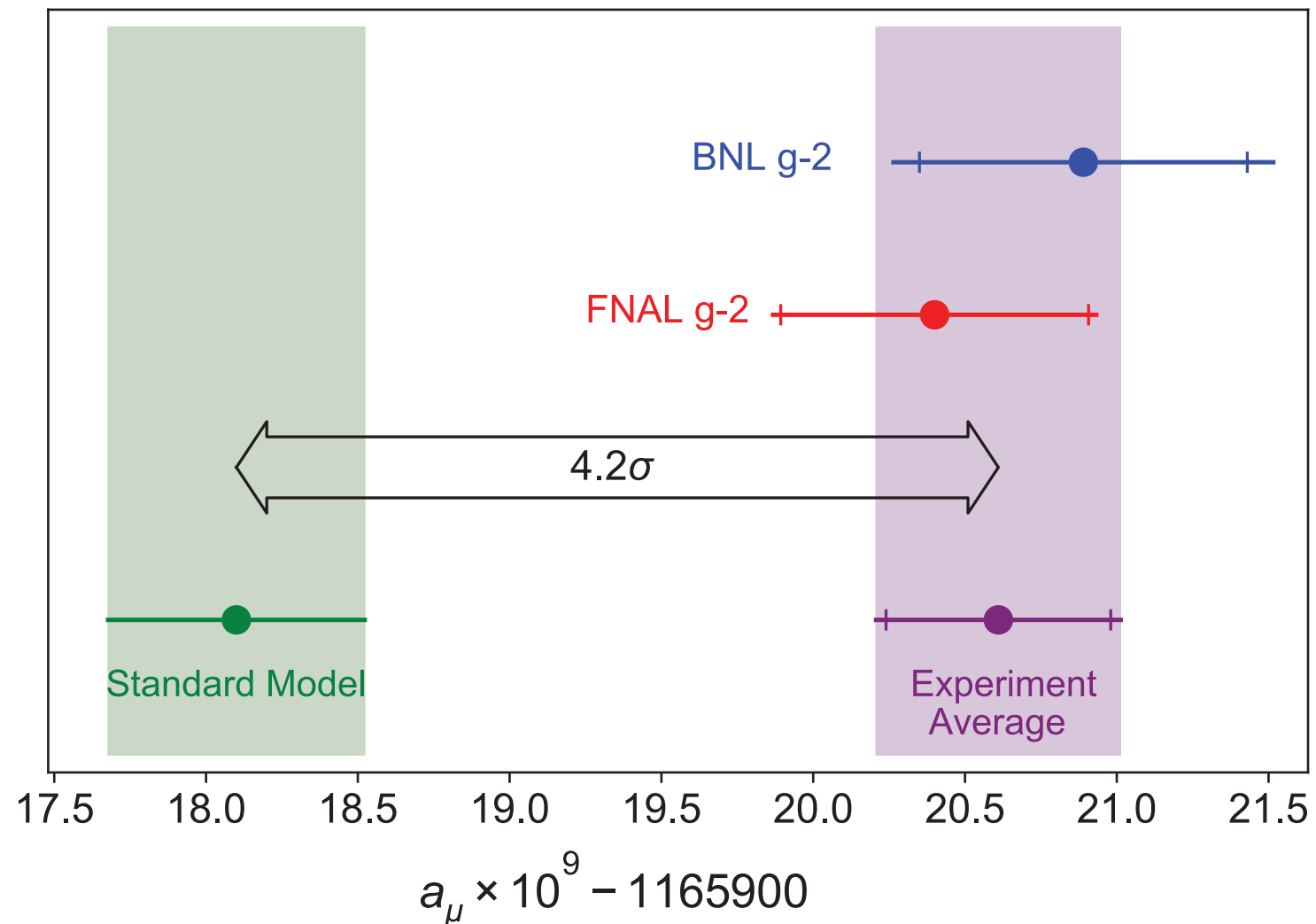
$$C_{ij} = \frac{eg^2 m_\mu}{16\pi^2 \Lambda^2}$$


Somewhat arbitrary choice! **Not** MFV.

Rough attempt at apples-to-apples comparison.

Models of flavor/CP change which are best.

Fermilab's Update on Muon $g - 2$



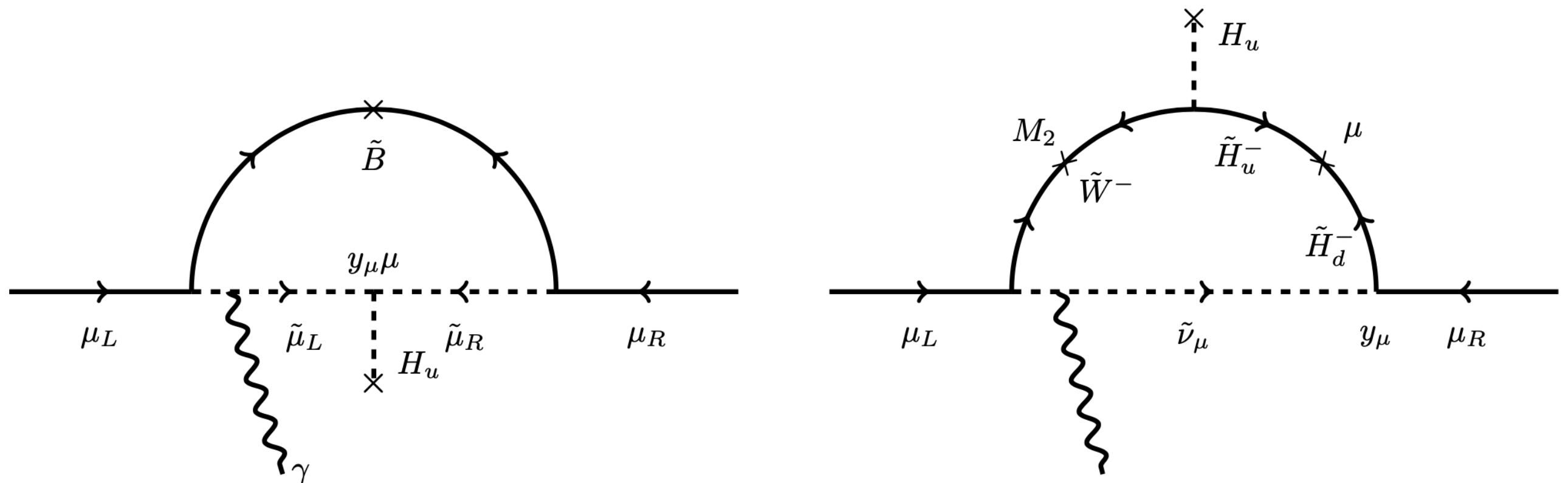
LHC Run 3 should be targeting electroweak physics (e.g. sleptons/charginos/neutralinos in SUSY, but more generally). But ***not ruled out yet.***

Muon $g - 2$ and SUSY

Basic dimensional analysis: new physics around weak scale!

$$\Delta a_\mu \sim \left(\frac{g^2}{8\pi^2} \right) \left(\frac{m_\mu}{M_{\text{BSM}}} \right)^2 \sim 2.5 \times 10^{-9} \Rightarrow M_{\text{BSM}} \sim 150 \text{ GeV}$$

e.g., from smuon/bino or sneutrino/chargino loops:

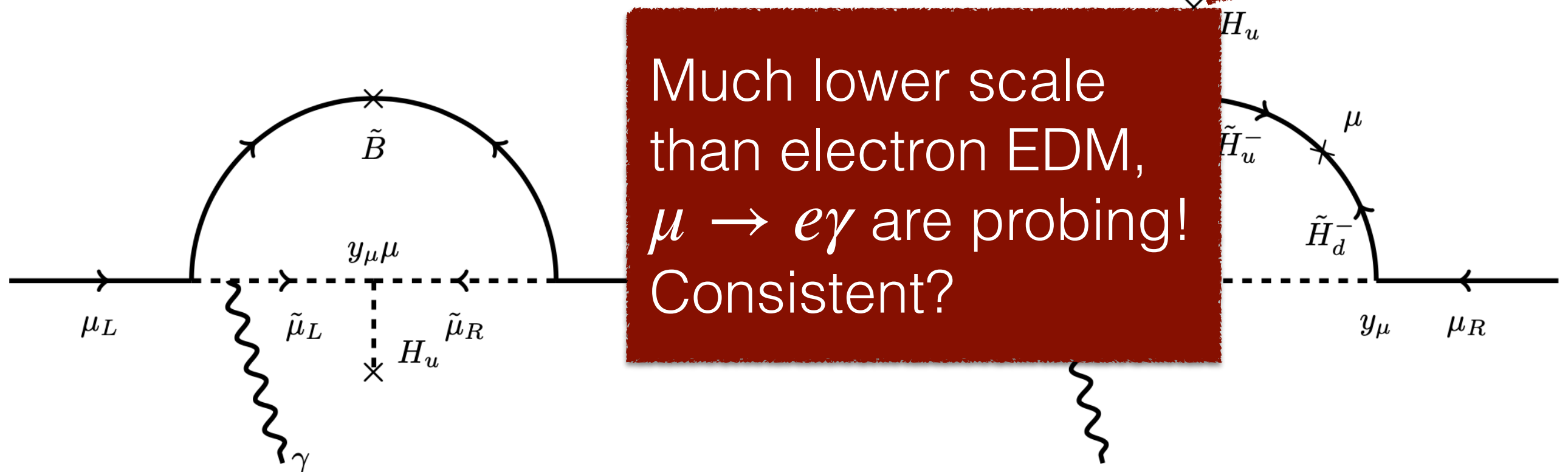


Muon $g - 2$ and SUSY

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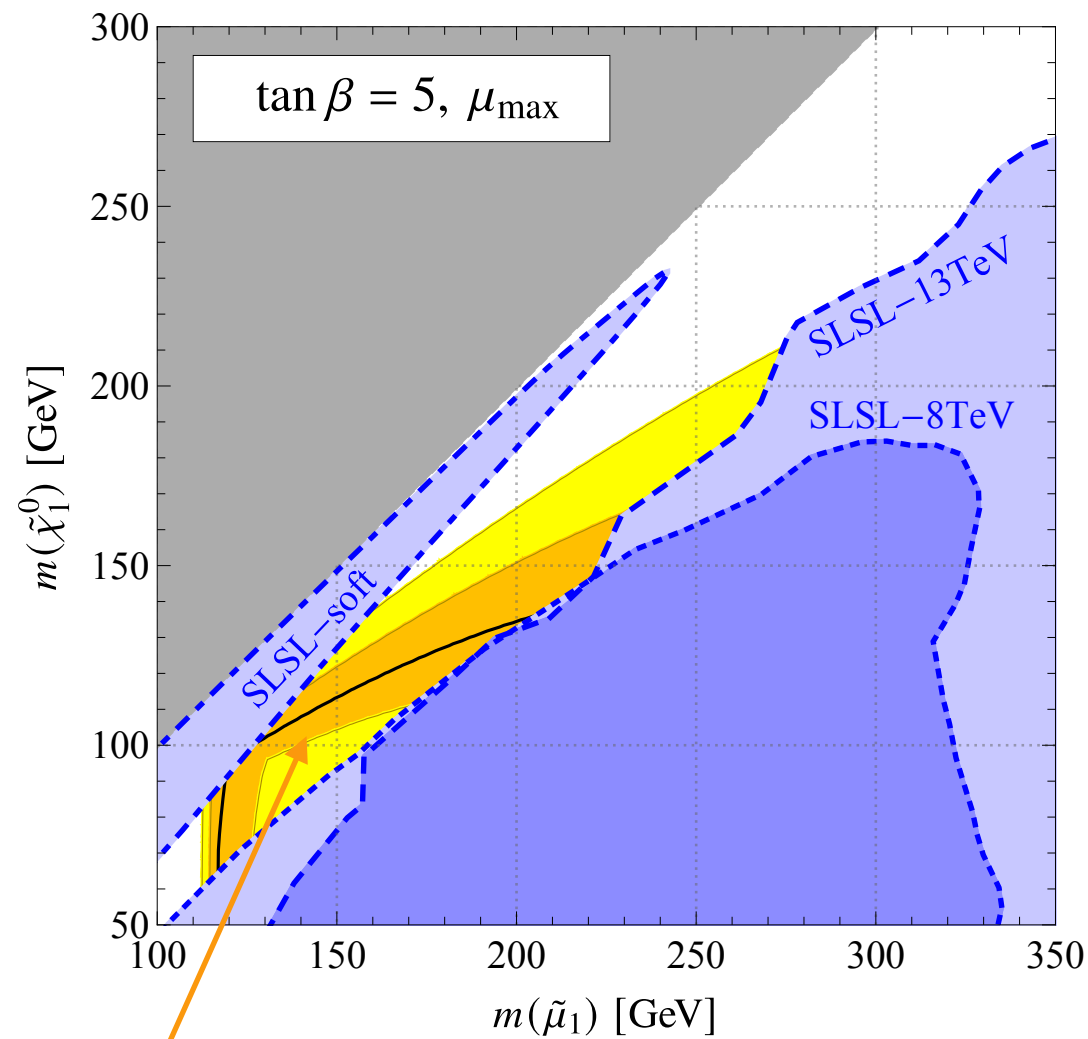
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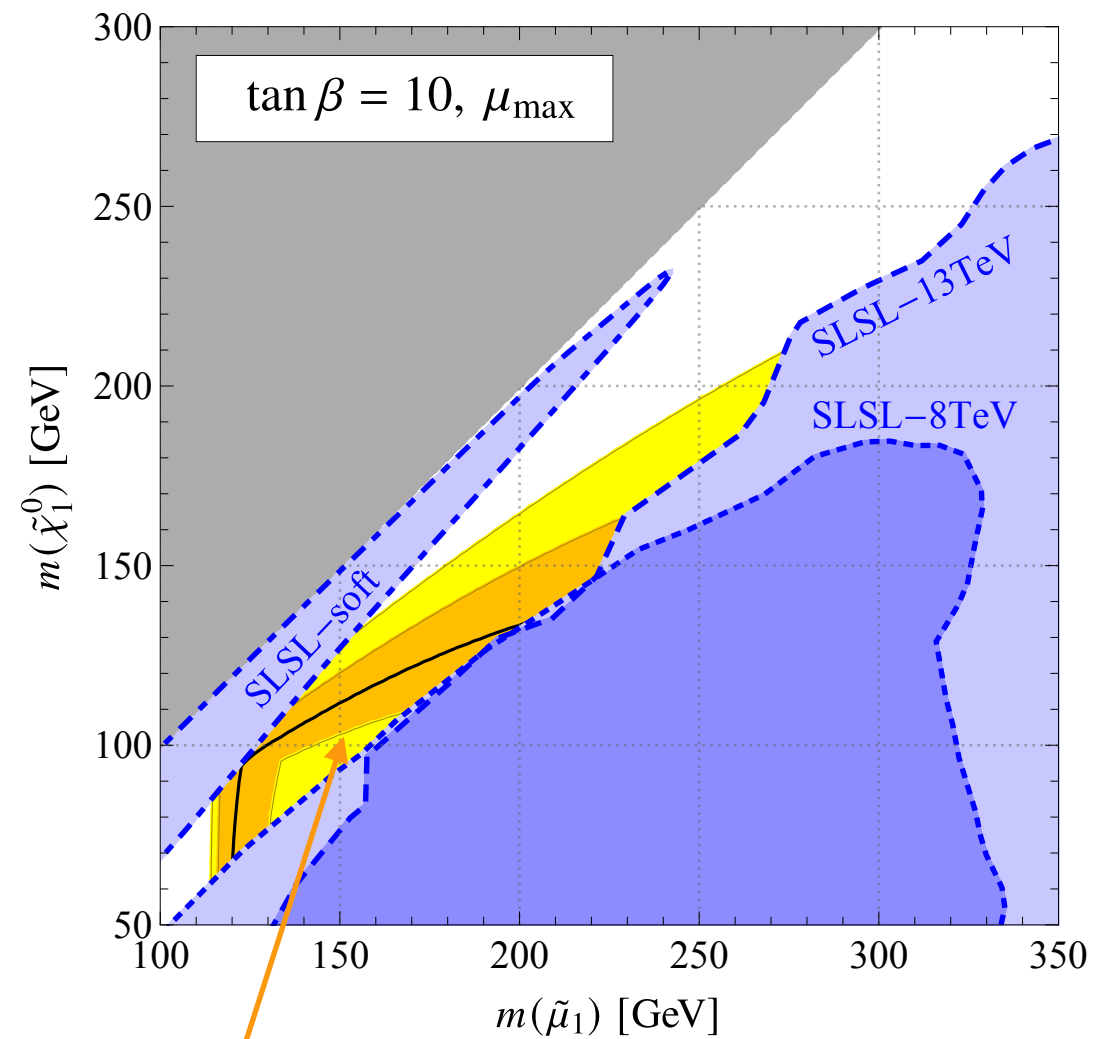
Example: bino dominated loop $\propto \frac{\alpha_Y m_\mu^2 M_1 \mu}{4\pi m_{\tilde{\mu}_L}^2 m_{\tilde{\mu}_R}^2} \tan \beta$

smuons, bino **Escapes LHC discovery so far.**



g-2

(A) $\tan \beta = 5$

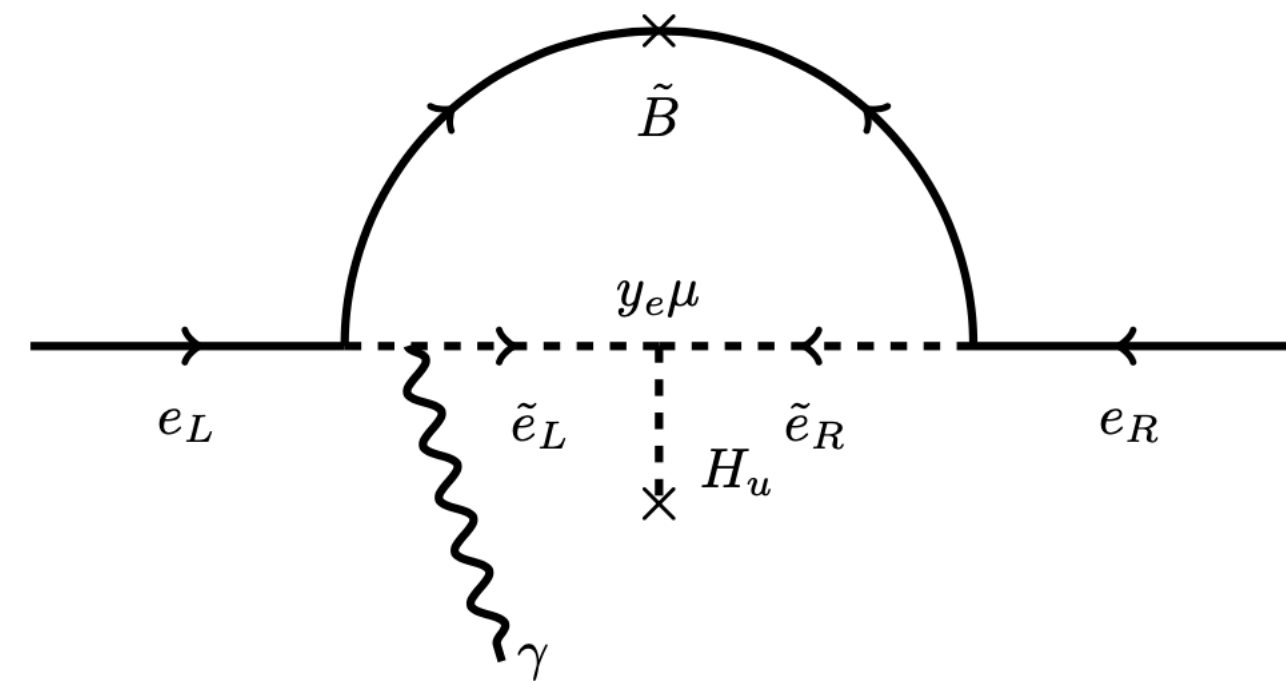


g-2

(B) $\tan \beta = 10$

Endo, Hamaguchi, Iwamoto, Kitahara 2104.03217

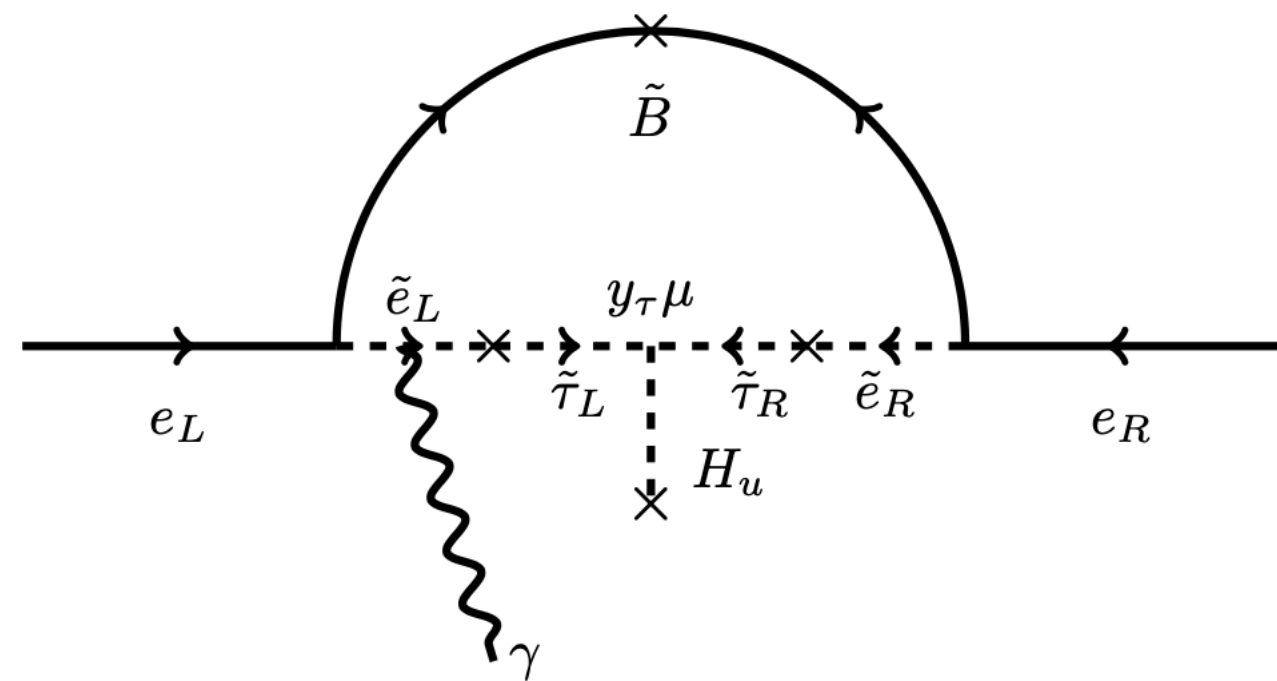
CP Violation with and without Flavor Violation



$$\propto m_e (\mu M_1)$$

higgsino
mass

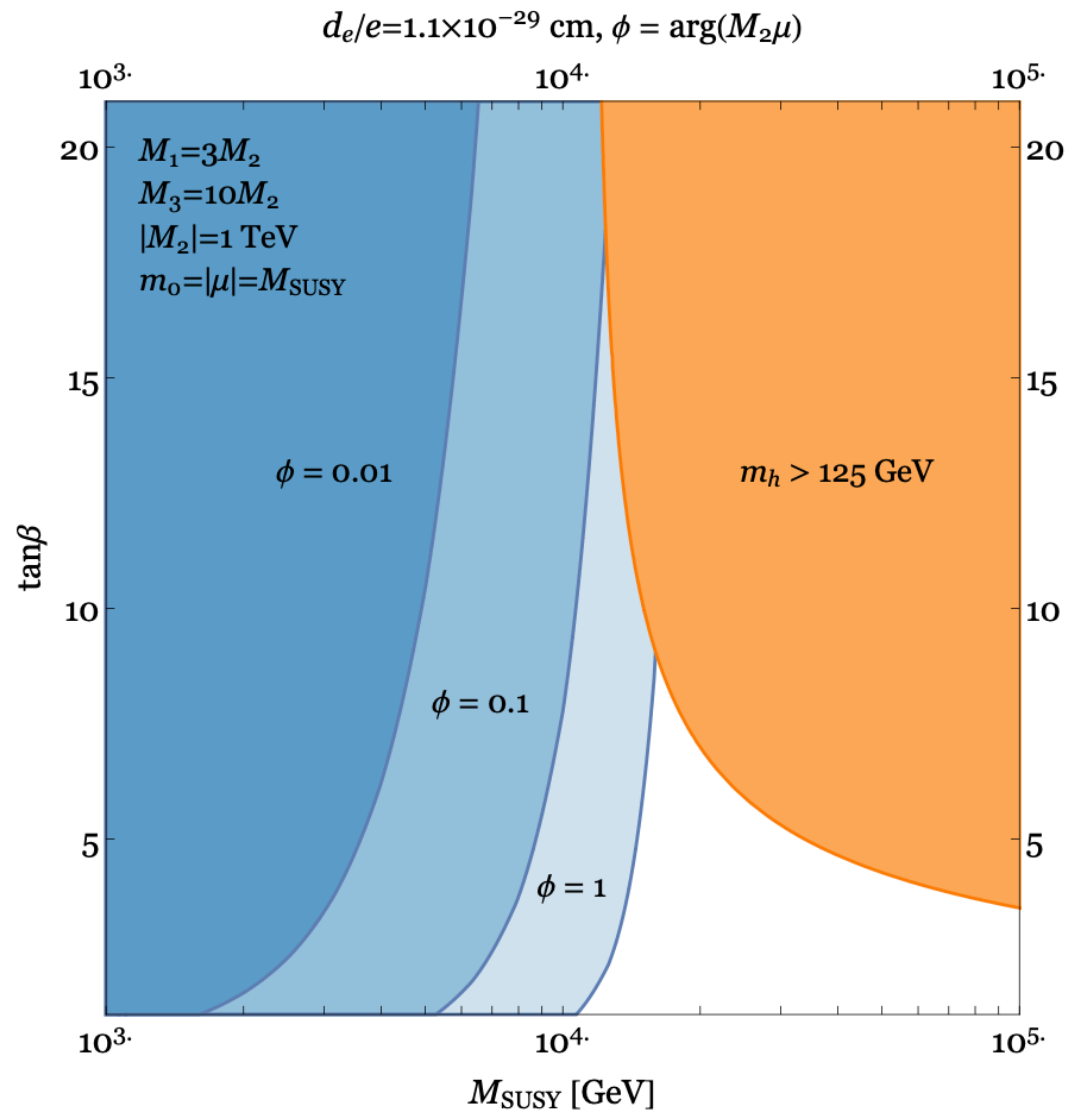
bino
mass



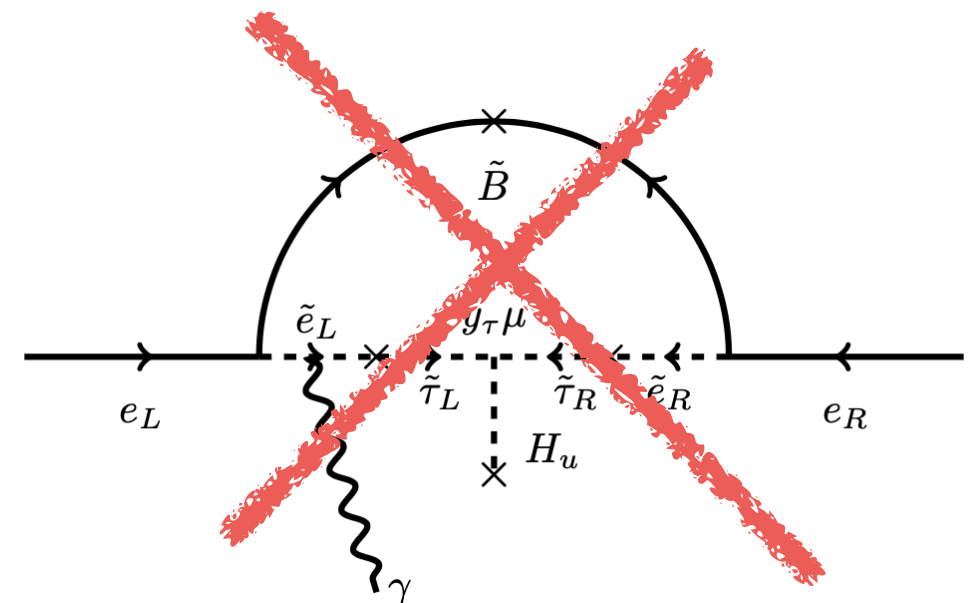
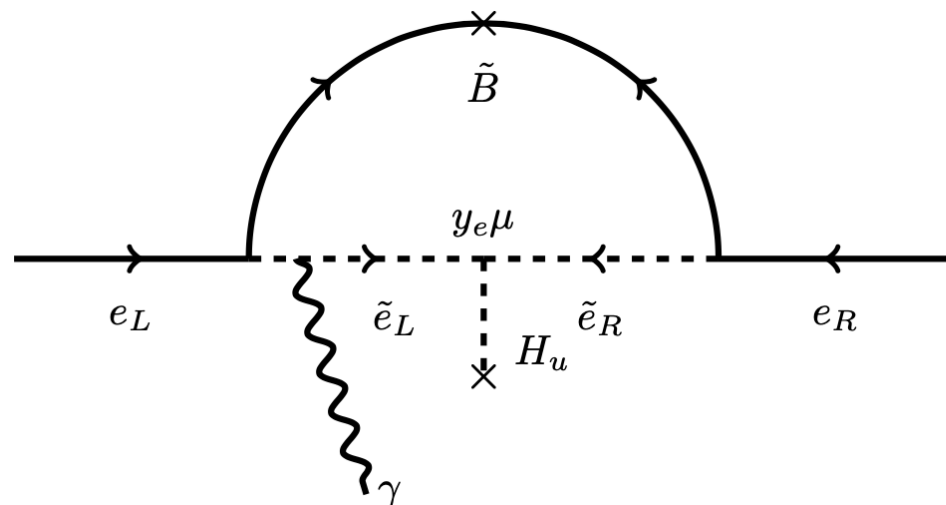
$$\propto m_\tau (\mu M_1 (\delta_{e\tau}^{LL}) (\delta_{\tau e}^{RR}))$$

slepton flavor
mixing

EDM Bounds with CP but no Flavor Violation

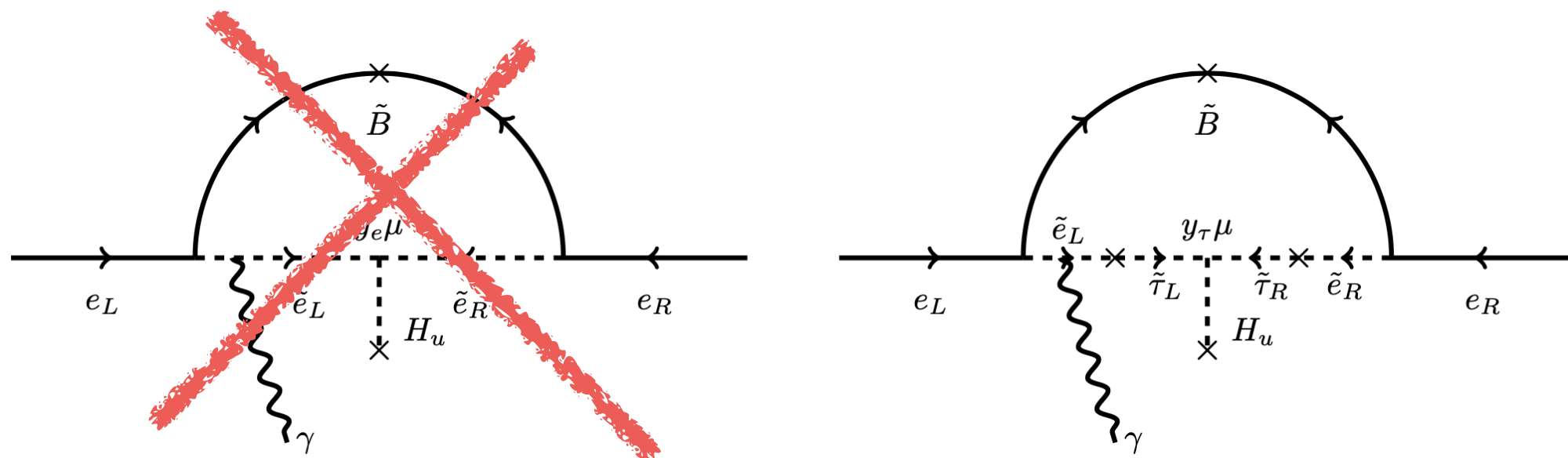


In the past, when estimating the mass scale probes by EDMs, I have generally assumed **Minimal Flavor Violation**, expecting flavor violation to usually make bounds **stronger**.



EDM Bounds with Correlated Flavor and CP Violation

However, in some models it may be the other way around: flavor-violating interactions can be the *dominant source of CP violation*.



To explain such a model, I should first review the notion of “**horizontal symmetries.**”

Flavor puzzle

Patterns of masses and mixings

$$\begin{aligned}
 & (Y_u)_{ij} (h \cdot q_i) \bar{u}_j + (Y_d)_{ij} h^\dagger q_i \bar{d}_j + (Y_e)_{ij} h^\dagger \ell_i \bar{e}_j \\
 & \quad (1,2)_{1/2} (3,2)_{1/6} (\bar{3},1)_{-2/3} \quad (1,2)_{-1/2} (3,2)_{1/6} (\bar{3},1)_{1/3} \quad (1,2)_{-1/2} (1,2)_{-1/2} (1,1)_1
 \end{aligned}$$

Mass eigenvalues in GeV:

$$173, 1.3, 0.002 \quad 4.2, 0.093, 0.005 \quad 1.8, 0.106, 0.0005$$

Three to five orders of magnitude spread. Mixings also very structured (in quark sector):

$$\begin{bmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| & |V_{ts}| & |V_{tb}| \end{bmatrix} = \begin{bmatrix} 0.97370 \pm 0.00014 & 0.2245 \pm 0.0008 & 0.00382 \pm 0.00024 \\ 0.221 \pm 0.004 & 0.987 \pm 0.011 & 0.0410 \pm 0.0014 \\ 0.0080 \pm 0.0003 & 0.0388 \pm 0.0011 & 1.013 \pm 0.030 \end{bmatrix}.$$

Froggatt-Nielsen models

One or more additional U(1) charges, *different in different generations*. (“**Horizontal symmetry**.”)

Example: $H(h) = 0$

$$H(q_1) = 3, H(q_2) = 2, H(q_3) = 0$$

$$H(\bar{u}_1) = 4, H(\bar{u}_2) = 1, H(\bar{u}_3) = 0$$

This allows **only** the top-quark Yukawa coupling,

$$(Y_u)_{33}(h \cdot q_3)\bar{u}_3$$

because it is H-neutral, explaining why the top is so heavy.

Froggatt-Nielsen models

Don't want to **completely** forbid other masses. Suppose the H-symmetry is **spontaneously broken** by the vacuum expectation value of a gauge-singlet scalar S :

$$H(S) = -1, \quad \frac{\langle S \rangle}{\Lambda} \sim \lambda \approx 0.2$$

In this way we can reproduce small masses/mixings, e.g., with our charge assignments:

$$c_{22} \left(\frac{S}{\Lambda} \right)^3 (h \cdot q_2) \bar{u}_2 \sim c_{22} \lambda^3 (h \cdot q_2) \bar{u}_2 \sim \mathcal{O}(1) \times (1.4 \text{ GeV}) c \bar{c}$$

$$c_{11} \left(\frac{S}{\Lambda} \right)^7 (h \cdot q_1) \bar{u}_1 \sim c_{11} \lambda^7 (h \cdot q_1) \bar{u}_1 \sim \mathcal{O}(1) \times (2.2 \text{ MeV}) u \bar{u}$$

CP as a spontaneously broken symmetry

CP as a fundamental symmetry, **spontaneously broken.**

Not hard to arrange, e.g., supersymmetric example:

$$W = X(S_1 \bar{S}_1 - \lambda^4) + Y(c_1 S_2^4 + c_2 S_2^3 S_1^3 + c_3 S_1^6)$$

$$\langle S_1 \rangle = \lambda^2, \quad \langle S_2 \rangle^2 = \frac{-c_2 \pm \sqrt{c_2^2 - 4c_1 c_3}}{2c_1} \langle S_1 \rangle^3 \sim e^{i \times \mathcal{O}(1)} \lambda^6$$

Plays a role in some proposed solutions to the Strong CP problem (Nelson / Barr)

CP as a spontaneously broken symmetry

CP as a fundamental symmetry, **spontaneously broken.**

Not hard to arrange, e.g.

$$W = X(S_1 \bar{S}_1 - \lambda^4$$

Invariant, O(1) CPV phase when solving for minimum of potential.

Example:

$$\langle S_1 \rangle = \lambda^2, \quad \langle S_2 \rangle^2 = \frac{-c_2 \pm \sqrt{c_2^2 - 4c_1 c_3}}{2c_1} \langle S_1 \rangle^3 \sim e^{i \times \mathcal{O}(1)} \lambda^6$$

Plays a role in some proposed solutions to the Strong CP problem (Nelson / Barr)

The Nir-Rattazzi Idea

CP as a fundamental symmetry, **spontaneously broken, by VEVs of fields carrying flavor (horizontal) charge.**

$$H(S_1) = -2, \quad H(S_2) = -3$$

Yukawa terms can acquire CPV phases, e.g.,

$$\left(\frac{S_2}{\Lambda}\right) (h \cdot q_i) \bar{u}_j \text{ allowed if } H(q_i) + H(\bar{u}_j) = 3.$$

Not hard to build a model that gets the CKM phase right.

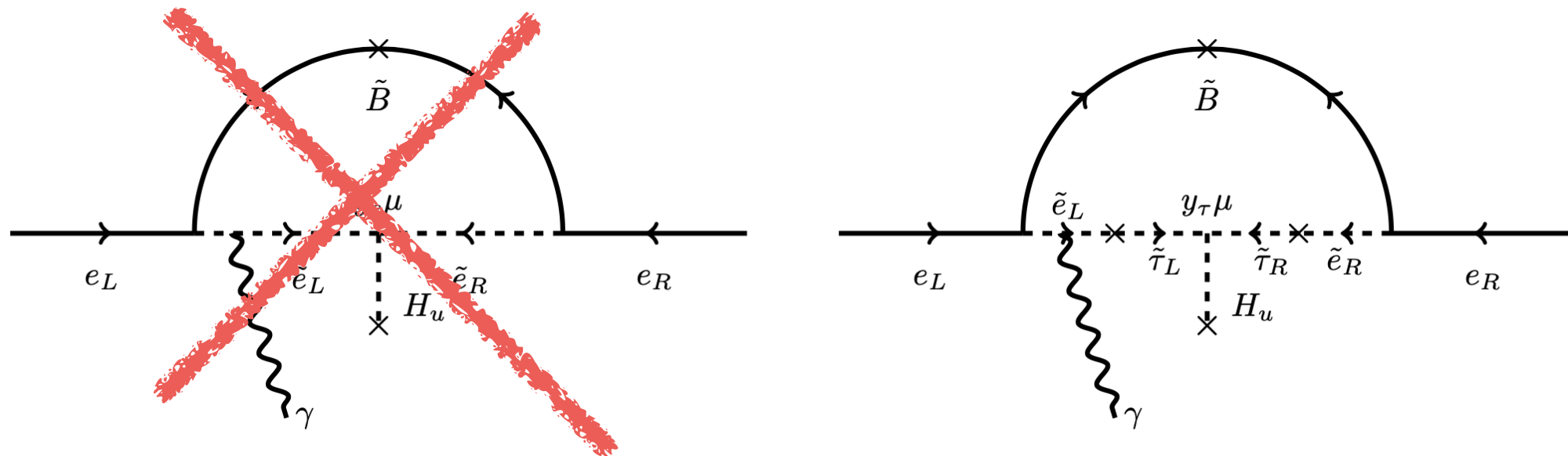
Yosef Nir and Riccardo Rattazzi, arXiv:hep-ph/9603233

Suppressed CPV *without* Flavor Violation

If CP violation comes only from flavor-violating VEVs, then **flavor-conserving CPV is very suppressed.**

$$\mu \sim \mu_0 \left[1 + \left(\frac{S_1^\dagger}{\Lambda} \right)^3 \left(\frac{S_2}{\Lambda} \right)^2 \right] \sim \mu_0 (1 + \mathcal{O}(10^{-9})i)$$

Can completely change expectations about relative size of EDM contributions, EDMs versus $\mu \rightarrow e\gamma$



Our Recent Work

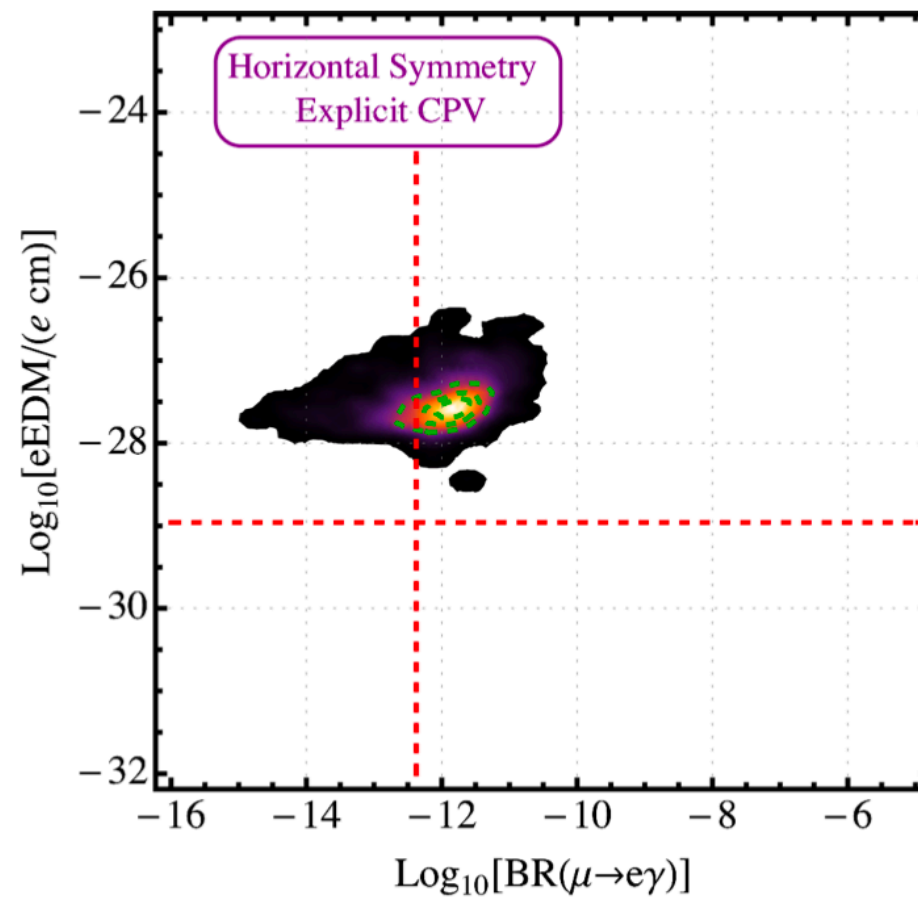
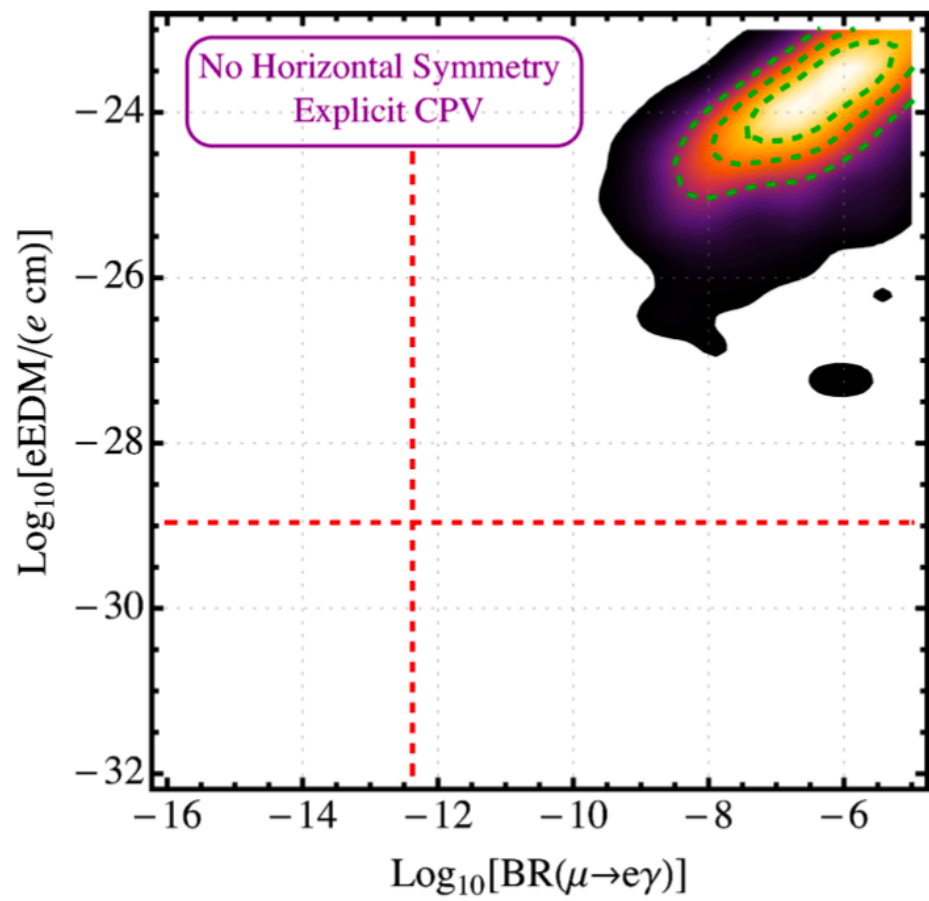
We have extended the Nir-Rattazzi idea to the **lepton sector**, including **Majorana neutrino masses**.

For horizontal charges that achieve the right pattern of masses and mixings, we can compute the electron EDM, charged lepton flavor violation, and muon $g - 2$, and understand the relative reach.

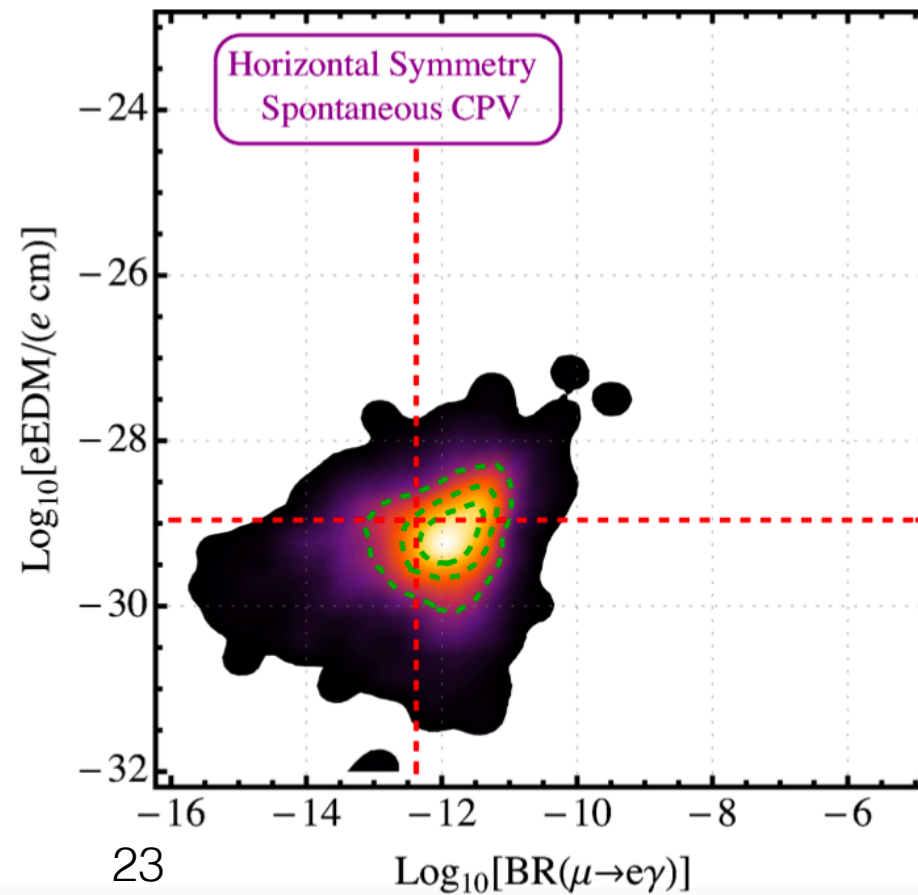
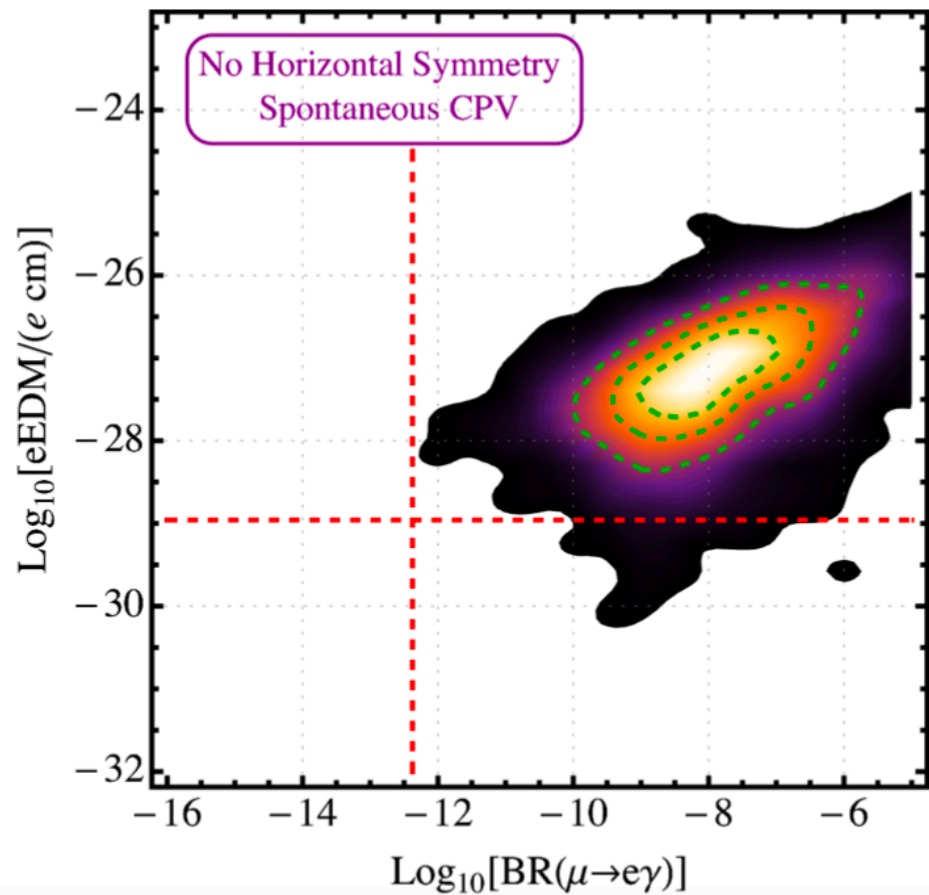
(Simplest models can't fit muon $g - 2$ without substantial fine-tuning; work in progress achieves this.)

arXiv:2104.02679 with Daniel Aloni, Pouya Asadi, Yuichiro Nakai, Motoo Suzuki

Flavor and CP symmetries

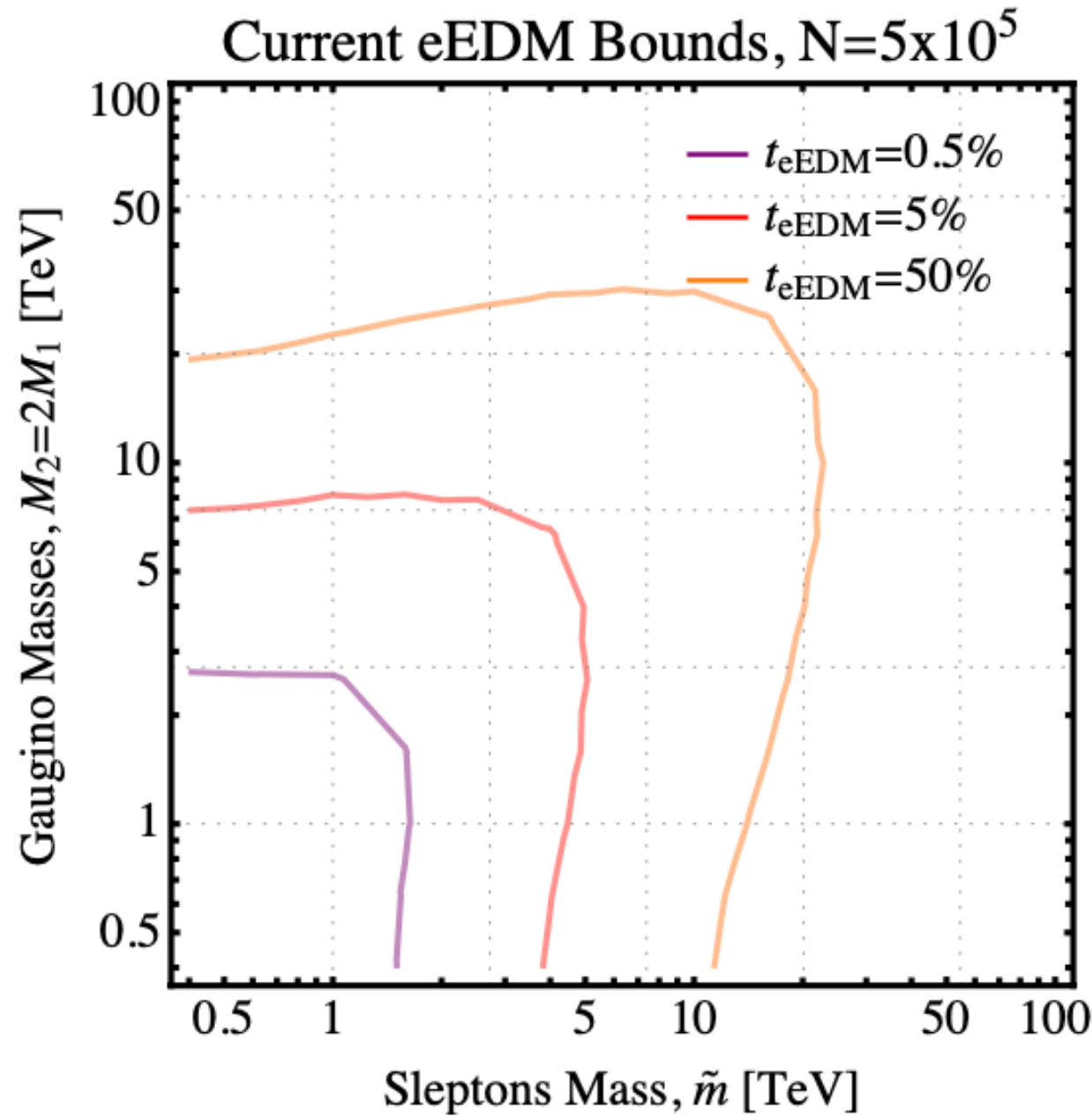


~10 TeV scalars,
1 TeV gauginos

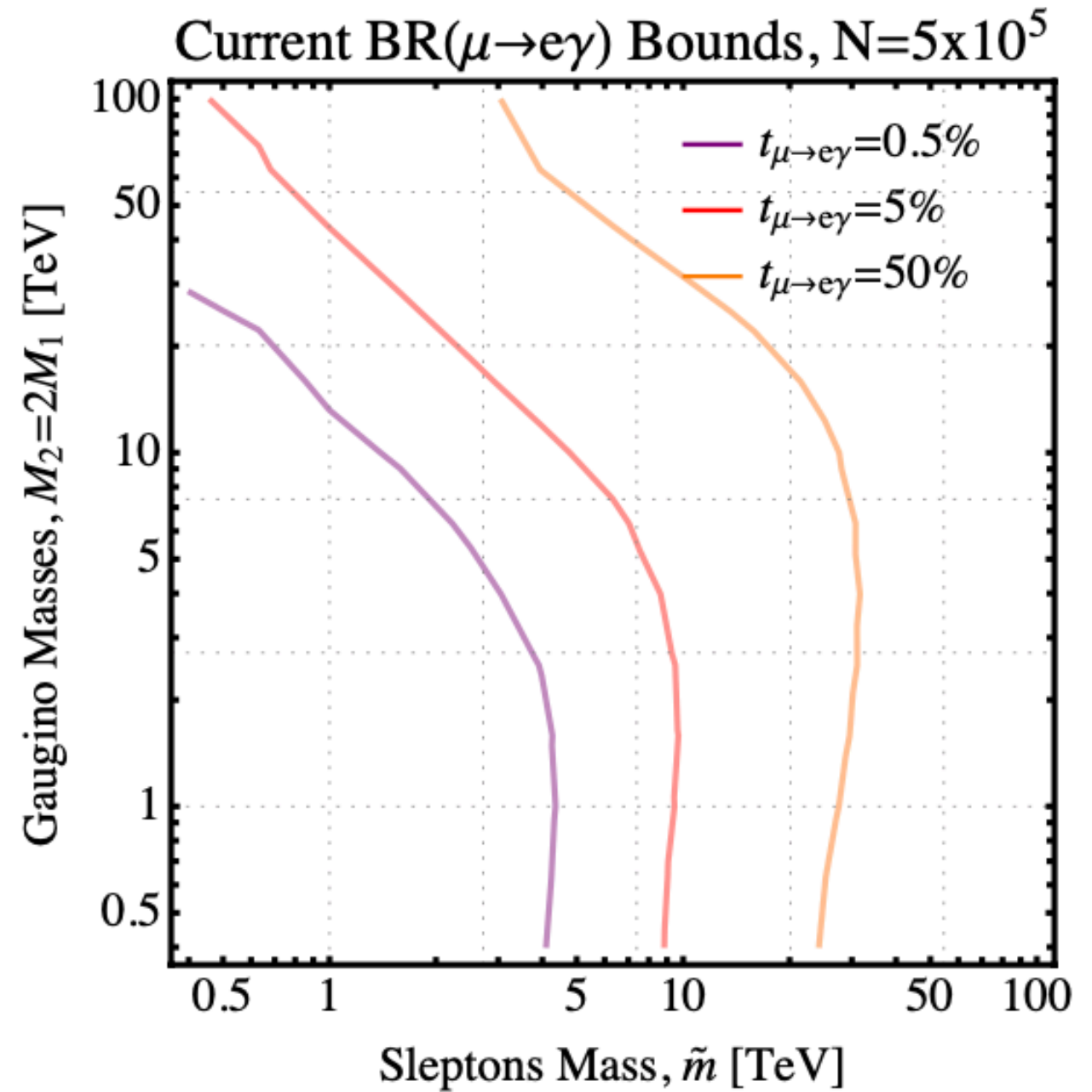


Aloni, Asadi,
Nakai, MR,
Suzuki '21

Current Bounds on a Flavor Model

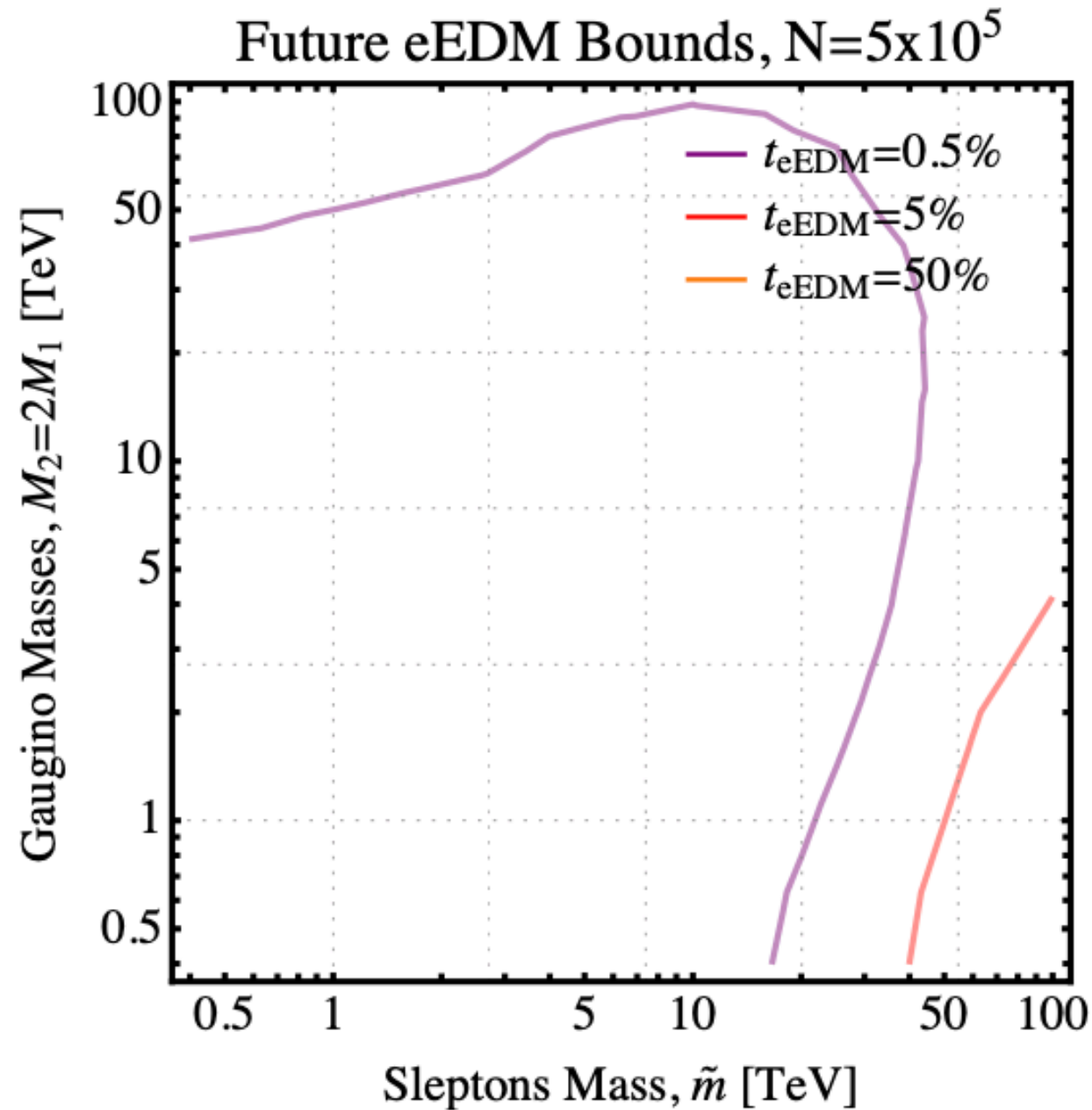


$$1.1 \times 10^{-29} e \text{ cm}$$

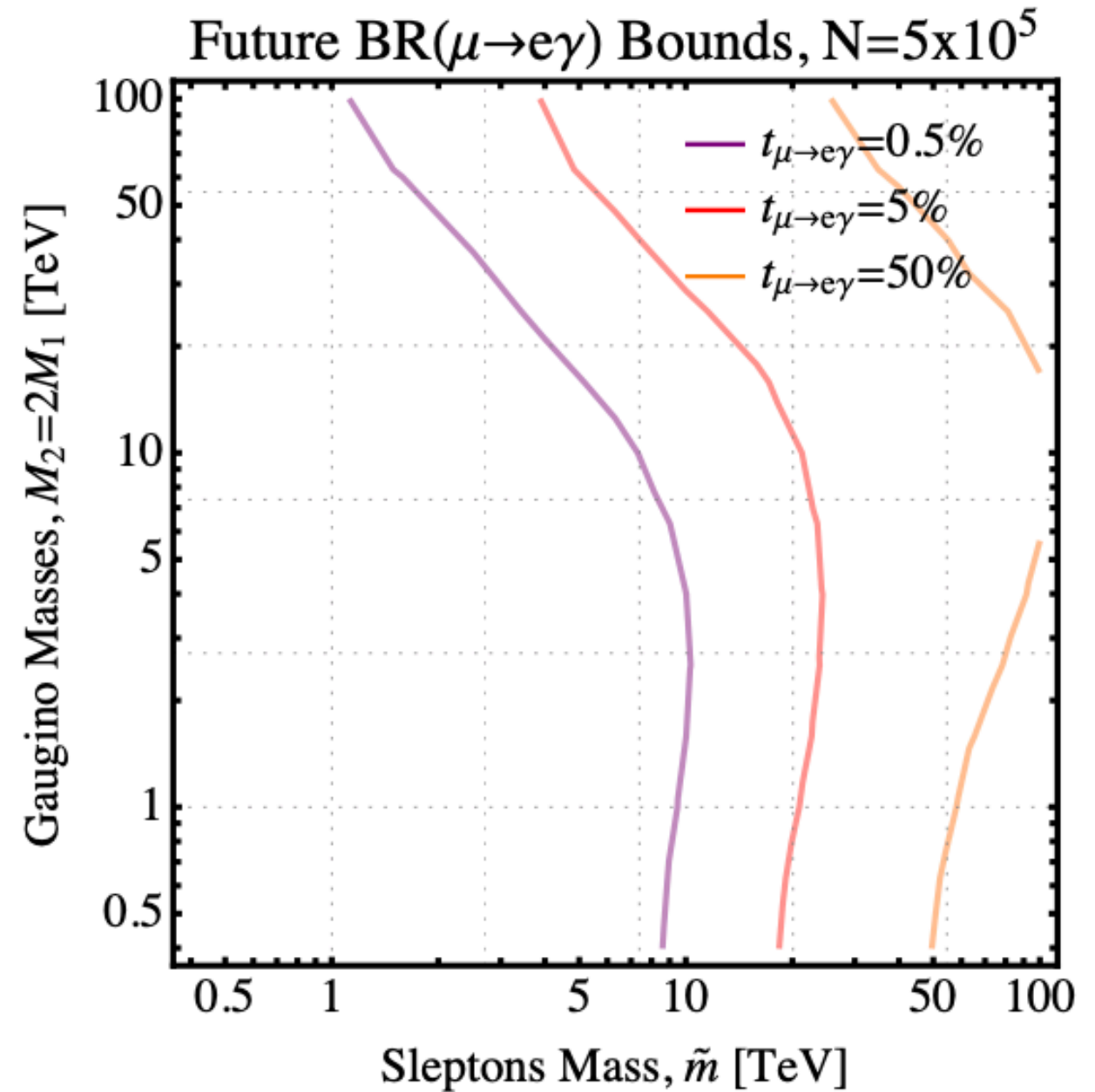


$$4.2 \times 10^{-13}$$

Future Bounds on a Flavor Model



$$10^{-32} e \text{ cm}$$



$$10^{-14}$$

Note square-root vs. 1/4-power scaling

Conclusions

EDMs can arise from TeV-scale particles if both flavor and CP are spontaneously broken symmetries.

Conceptual questions: what does it mean for CP to be a gauge symmetry? Cosmological defects?

The coming ~decade of experiments could give rise to **correlated signals** in EDMs, $g - 2$, $\mu \rightarrow e\gamma$, neutrino CP phase. Pattern as “**fingerprint**” of underlying fundamental physics.