# Opportunities for Radioactive Molecules in Tests of Fundamental Symmetries and Searches for New Physics

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# Conventional Wisdom in the Classification of Atomic/Molecular EDM Experiments

**Diamagnetic** systems (contain *no* unpaired electrons) are mainly sensitive to **hadronic** sources of CP violation – e.g., **Hg**, **Xe**, **n** 

Paramagnetic systems (contain *one or more* unpaired electrons) are mainly sensitive to **leptonic** sources of CP violation – e.g., **ThO**, **HfF**<sup>+</sup>, **YbF**, **TI**, **Cs** 

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For **semi-leptonic** sources of CP violation, the story is more complicated – the "classification" generally depends on whether the interactions involve mainly **electron spin** or **nuclear spin** 

Over the past decade, molecular experiments have improved the sensitivity to electron EDM  $d_e$  by more than 100-fold:

**232ThO bound:**  $|d_e| < 10^{-29} e \text{ cm}$ 

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# What about sensitivity of paramagnetic systems to hadronic CP violation?

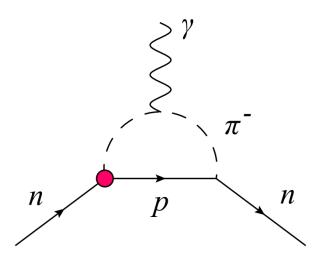
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Illustrative example: 
$$\mathcal{L} = \theta \frac{g_s^2}{32\pi^2} G\tilde{G}$$

Nucleon EDMs: [Crewther, Di Vecchia, Veneziano, Witten, PLB 88, 123 (1979)]

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#### **Nucleon EDMs**



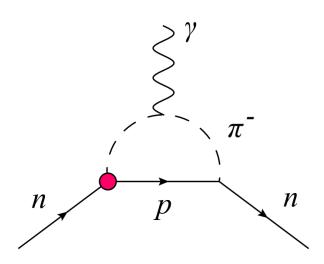
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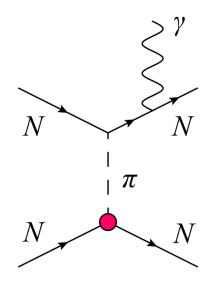
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#### **CP-violating intranuclear forces**



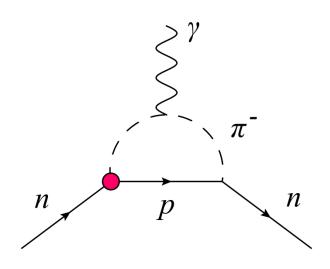
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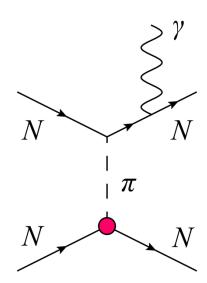
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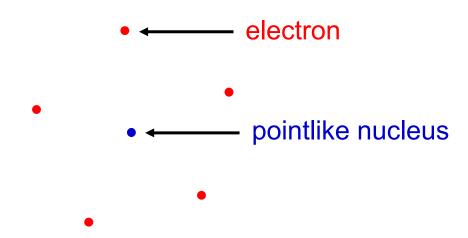
#### **CP-violating intranuclear forces**



In nuclei, tree-level CP-violating intranuclear forces dominate over **loop-induced** nucleon EDMs [loop factor =  $1/(8\pi^2)$ ].

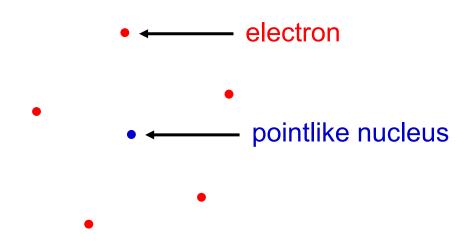
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**Schiff's Theorem:** "In a neutral atom made up of point-like non-relativistic charged particles (interacting only electrostatically), the constituent EDMs are screened from an external electric field."



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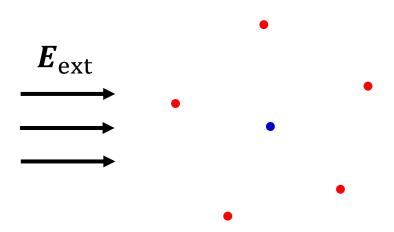
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Classical explanation for nuclear EDM: A neutral atom does not accelerate in an external electric field!

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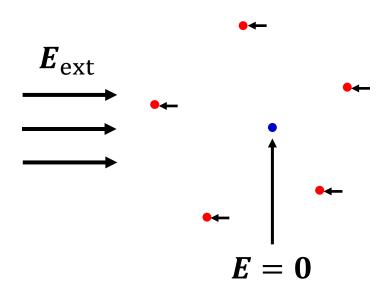
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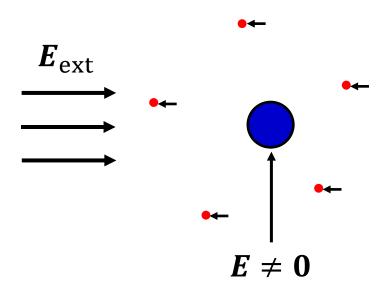
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## Lifting of Schiff's Theorem

[Sandars, PRL 19, 1396 (1967)],

[O. Sushkov, Flambaum, Khriplovich, JETP 60, 873 (1984)]

In real (heavy) atoms: Incomplete screening of external electric field due to finite nuclear size, parametrised by nuclear Schiff moment.

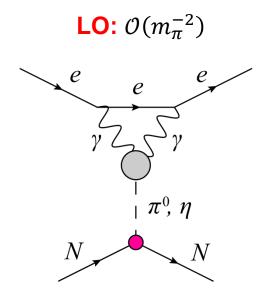


[Flambaum, Pospelov, Ritz, Stadnik, PRD 102, 035001 (2020)]

Hadronic CP-violating effects arise via 2γ-exchange starting at 2-loop level

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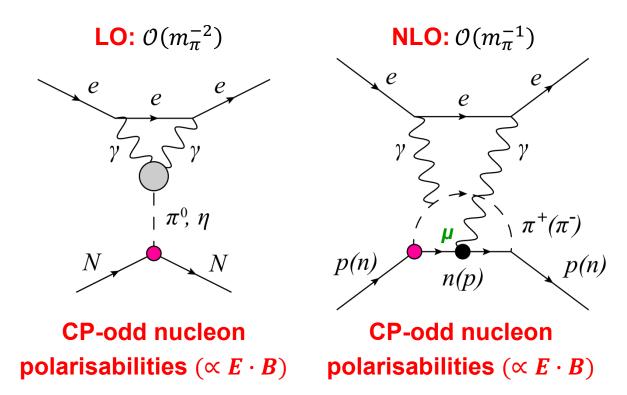
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CP-odd nucleon polarisabilities ( $\propto E \cdot B$ )

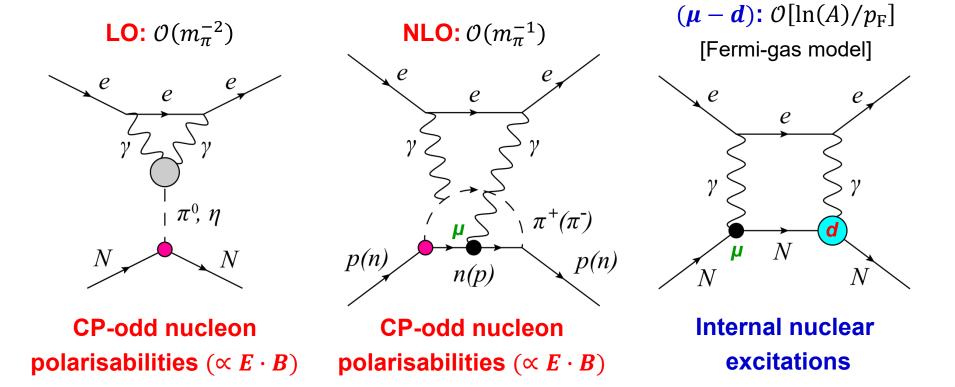
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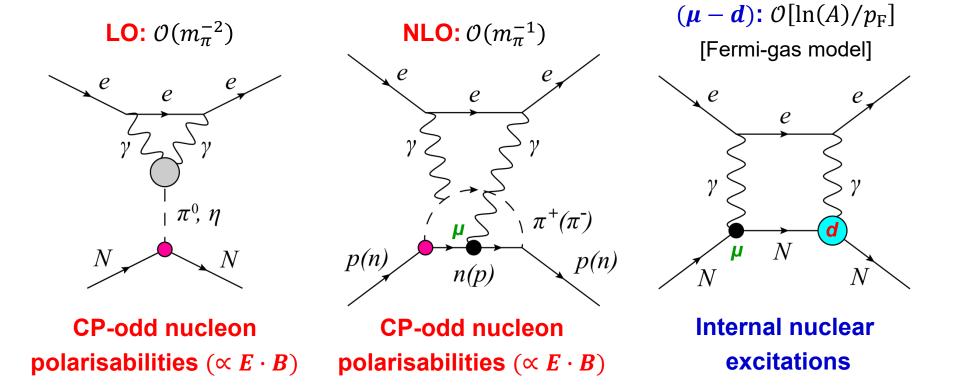
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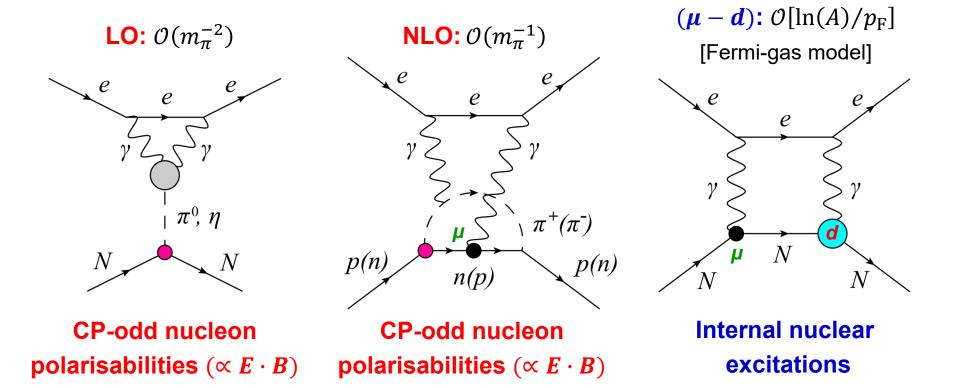
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- Hadronic CP-violating effects arise via 2γ-exchange starting at 2-loop level
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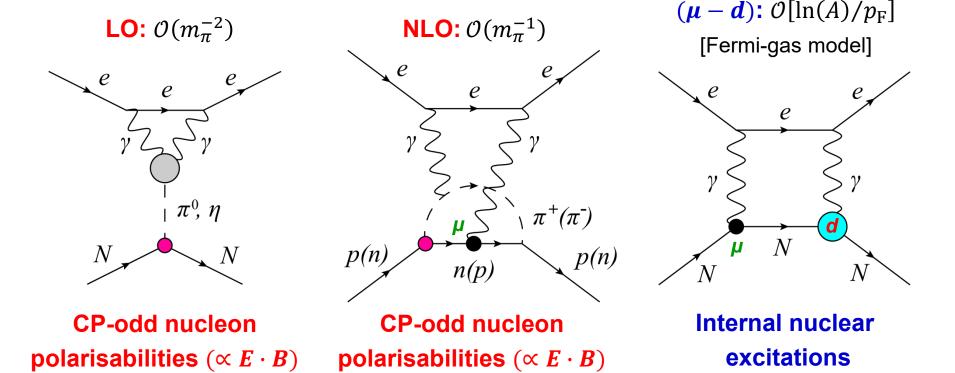
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- Hadronic CP-violating effects arise via 2γ-exchange starting at 2-loop level
- One of photons interacts magnetically with nucleus => no Schiff screening
  - O(A)-enhanced CP-odd nuclear scalar polarisability



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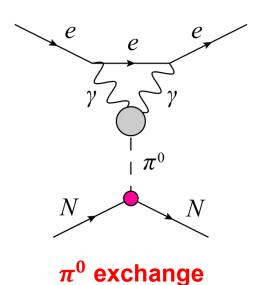
- Hadronic CP-violating effects arise via 2γ-exchange starting at 2-loop level
- One of photons interacts magnetically with nucleus => no Schiff screening
  - O(A)-enhanced CP-odd nuclear scalar polarisability
  - Operative even in spinless nuclei (e.g., <sup>232</sup>ThO, <sup>180</sup>HfF+)



## Isoscalar CP-Odd $\pi$ -N Coupling

[Flambaum, Pospelov, Ritz, Stadnik, PRD 102, 035001 (2020)]

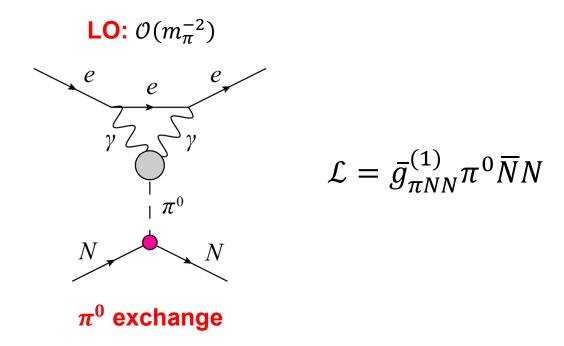
**LO**:  $\mathcal{O}(m_{\pi}^{-2})$ 



$$\mathcal{L} = \bar{g}_{\pi NN}^{(1)} \pi^0 \bar{N} N$$

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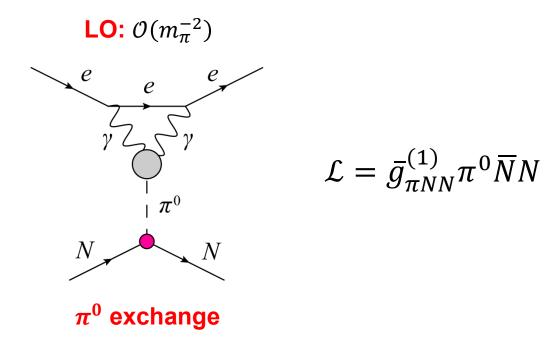
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In molecules with *spinless* nuclei (e.g.,  $^{232}$ ThO,  $^{180}$ HfF+), effect dominated by a "**bulk**" property of the nucleus that grows with A in a regular manner, with *no contribution* from the nuclear Schiff moment mechanism (needs  $I \neq 0$ )

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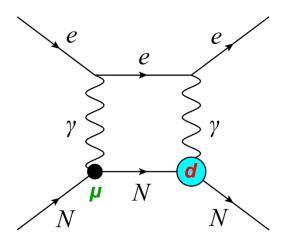
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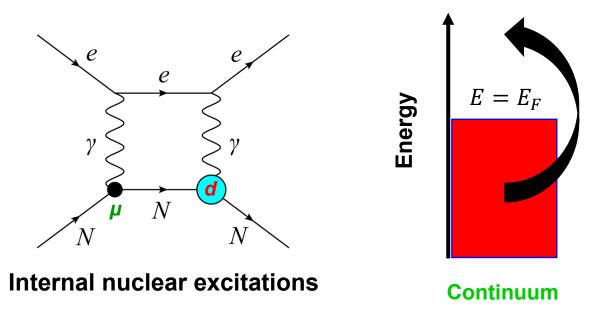
=> Clean bounds, since less sensitivity to details of nuclear structure (cf. strong sensitivity of <sup>199</sup>Hg Schiff moment to assumptions about underlying nuclear structure – different models give different signs for sensitivity coefficient)

[Flambaum, Pospelov, Ritz, Stadnik, PRD 102, 035001 (2020)]



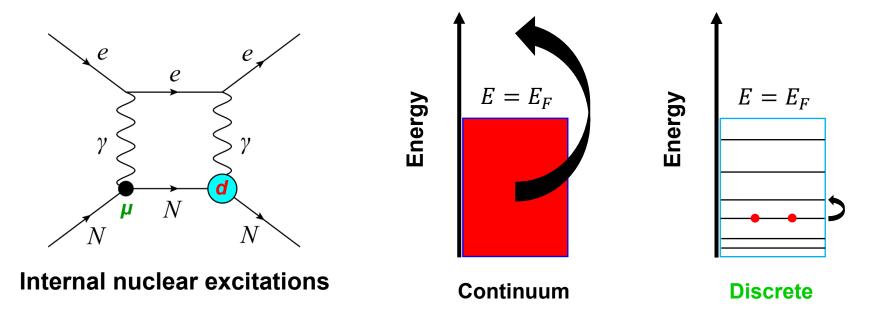
Internal nuclear excitations

[Flambaum, Pospelov, Ritz, Stadnik, PRD 102, 035001 (2020)]



Excitations to continuum above Fermi surface:  $\sim \ln(A)/p_{\rm F}$  [Fermi-gas model]

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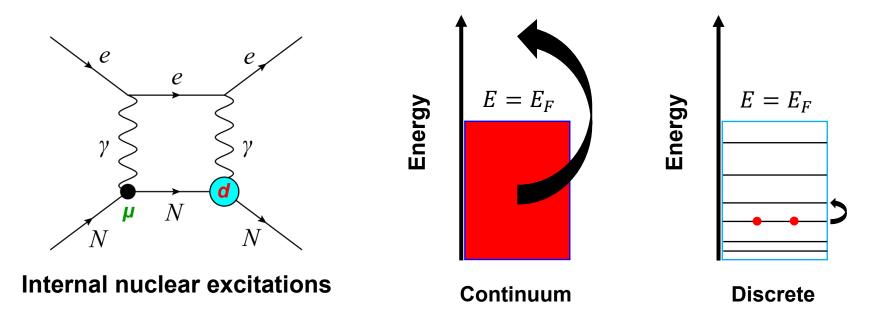


Excitations to continuum above Fermi surface:  $\sim \ln(A)/p_{\rm F}$  [Fermi-gas model]

Discrete transitions between L-S doublets:  $\sim [\mathcal{O}(10)/A] \times (1/\Delta E_{\text{nucl}})$ 

[Giant resonance model – Flambaum, Samsonov, Tran Tan, JHEP 10 (2020) 077]

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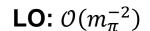
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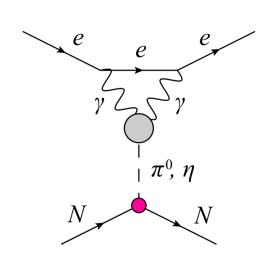
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For  $A \sim 200$  and  $\Delta E_{\rm nucl} \sim$  several MeV, the two contributions are comparable in size (and of the same sign)

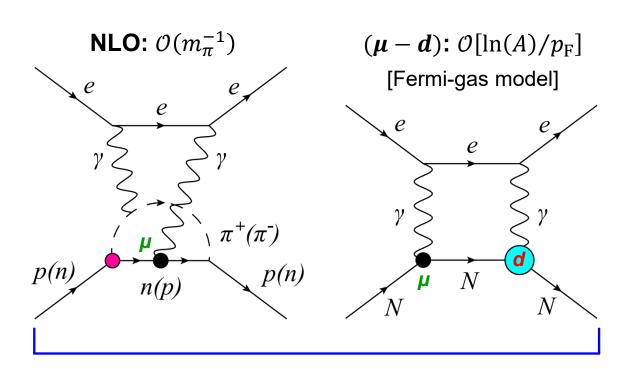
# QCD Vacuum Angle $\mathcal{L} = \theta \frac{g_s^2}{32\pi^2} G\tilde{G}$

[Flambaum, Pospelov, Ritz, Stadnik, PRD 102, 035001 (2020)]





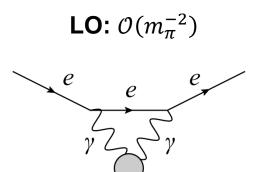
 $\pi^0$ ,  $\eta$  contributions: **opposite** sign (near-cancellation in heavy nuclei)



p, n contributions: **same** sign

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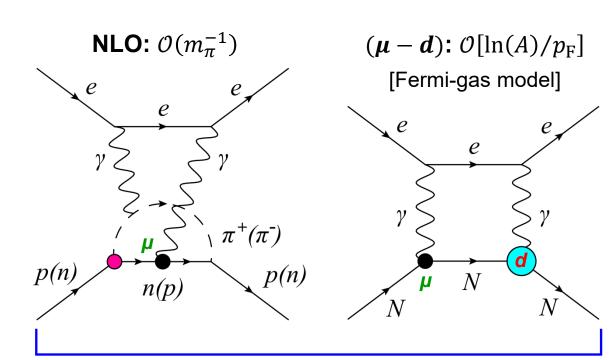
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N



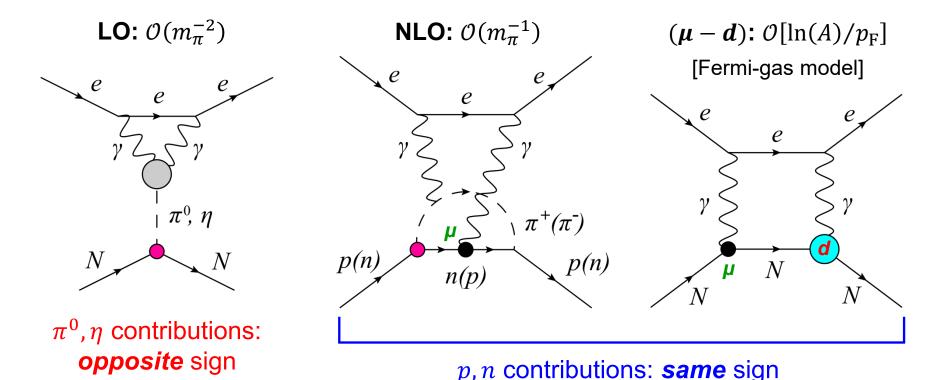
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For  $Z \sim 80 \& A \sim 200$ :  $C_{SP}(\theta) \approx \left[0.1_{LO} + 1.0_{NLO} + 1.7_{(\mu-d)}\right] \times 10^{-2} \theta \approx 0.03\theta$ 

$$\mathcal{L}_{\text{contact}} = -\frac{G_F C_{\text{SP}} \overline{N} N \overline{e} i \gamma_5 e}{\sqrt{2}}$$

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**Future work:**  $\eta'$  contribution and other N<sup>2</sup>LO contributions, nuclear in-medium effects (NLO process), nuclear structure effects [( $\mu - d$ ) process]

#### Bounds on Hadronic CP Violation Parameters

ThO bounds: [Flambaum, Pospelov, Ritz, Stadnik, PRD 102, 035001 (2020)]

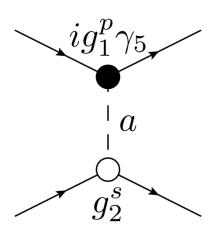
System	$\left  ar{g}_{\pi NN}^{(1)}  ight $	$\left  \tilde{d}_u - \tilde{d}_d \right  $ (cm)	$ d_p $ (e cm)	heta
ThO	$4\times10^{-10}$	$2\times10^{-24}$	$2\times10^{-23}$	$3 \times 10^{-8}$
n	$1.1 \times 10^{-10}$	$5 \times 10^{-25}$		$2.0 \times 10^{-10}$
Hg	$1 \times 10^{-12}$	$5 \times 10^{-27}$	$2.0 \times 10^{-25}$	$1.5 \times 10^{-10}$
Xe	$6.7 \times 10^{-8}$	$3 \times 10^{-22}$	$3.2 \times 10^{-22}$	$3.2 \times 10^{-6}$

Current bounds from molecules are  $\sim 10-100$  times weaker than from Hg & n, but are  $\sim 10-100$  times stronger than bounds from Xe

<sup>\*</sup> These limits can formally be null within nuclear uncertainties

#### P,T-Violating Forces Mediated by Dark Bosons

[Stadnik, Dzuba, Flambaum, *PRL* **120**, 013202 (2018)], [Dzuba, Flambaum, Samsonov, Stadnik, *PRD* **98**, 035048 (2018)]

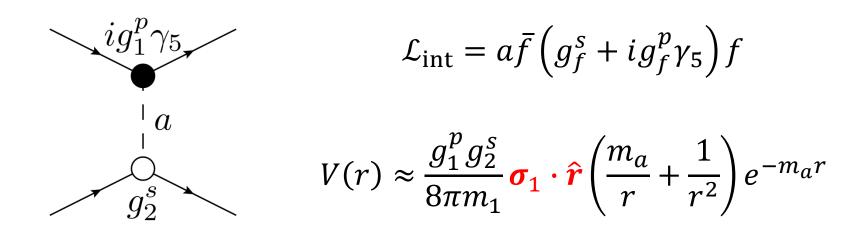


$$\mathcal{L}_{\text{int}} = a\bar{f} \left( g_f^s + i g_f^p \gamma_5 \right) f$$

$$V(r) \approx \frac{g_1^p g_2^s}{8\pi m_1} \boldsymbol{\sigma}_1 \cdot \hat{\boldsymbol{r}} \left( \frac{m_a}{r} + \frac{1}{r^2} \right) e^{-m_a r}$$

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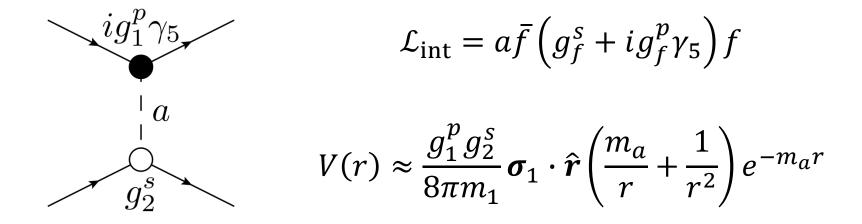
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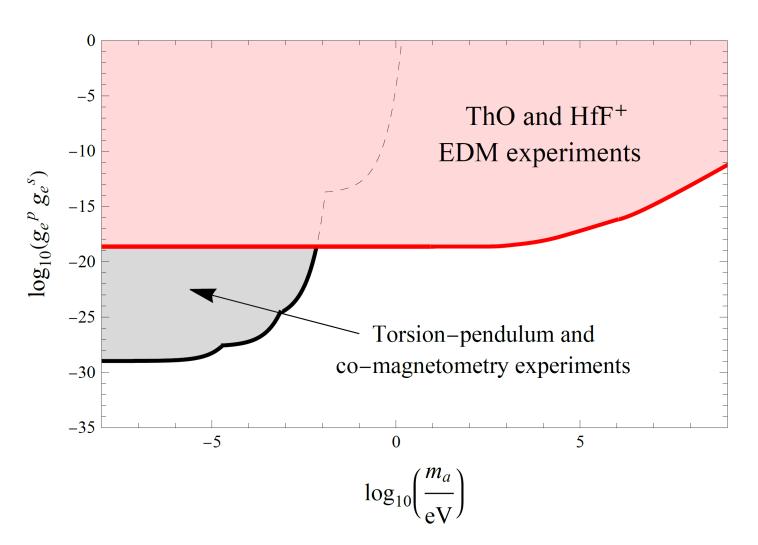


P,T-violating forces => Atomic and Molecular EDMs

If exchanged boson is sufficiently low-mass, then P,T-violating forces are long-range on the scale of atom/molecule, and the non-vanishing contribution arises from the Thomas-Fermi length scale  $r \sim a_{\rm B}/Z^{1/3}$ 

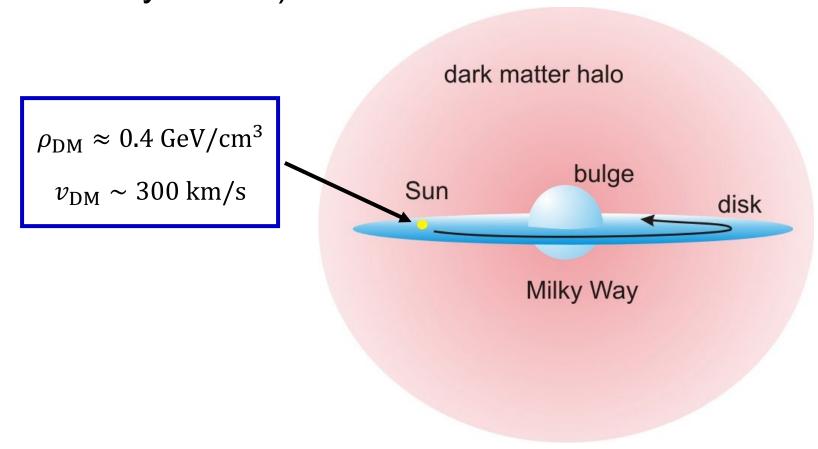
### Constraints on Scalar-Pseudoscalar Electron-Electron Interaction

**EDM constraints:** [Stadnik, Dzuba, Flambaum, *PRL* **120**, 013202 (2018); arXiv:1708.00486]

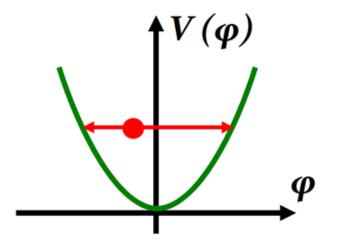


#### **Dark Matter**

Strong astrophysical evidence for existence of **dark matter** (~5 times more dark matter than ordinary matter)



#### Oscillating Electric Dipole Moments

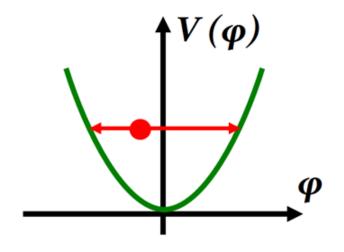


$$\varphi(t) = \varphi_0 \cos\left(m_{\varphi} c^2 t/\hbar\right),$$
 
$$\left\langle \rho_{\varphi} \right\rangle \approx m_{\varphi}^2 \varphi_0^2/2$$

### Oscillating Electric Dipole Moments

Nucleons: [Graham, Rajendran, PRD 84, 055013 (2011)]

Atoms and molecules: [Stadnik, Flambaum, PRD 89, 043522 (2014)]; [Flambaum, Pospelov, Ritz, Stadnik, PRD 102, 035001 (2020)]



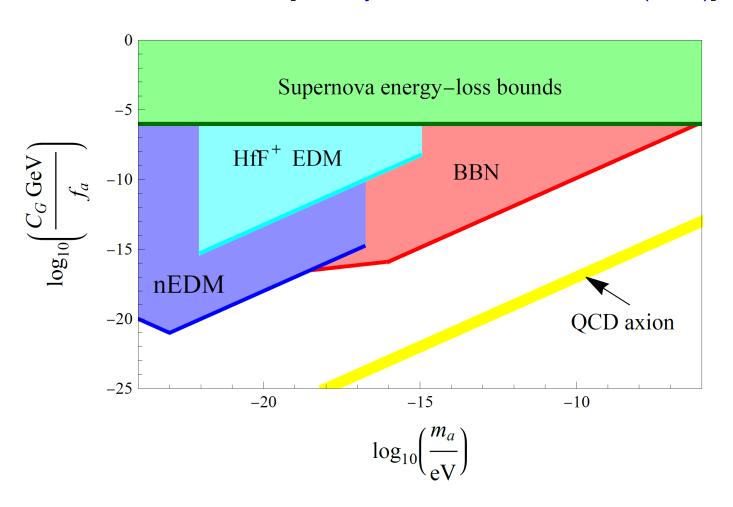
$$\varphi(t) = \varphi_0 \cos(m_{\varphi} c^2 t/\hbar),$$
 
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$$\mathcal{L} = \frac{C_G g_s^2}{32\pi^2 f_a} \varphi_0 \cos(m_{\varphi} t) G\tilde{G} \Rightarrow \begin{pmatrix} d(t) \propto J \cos(m_{\varphi} t), \\ H_{\text{EDM}}(t) = d(t) \cdot E \end{pmatrix}$$

cf. 
$$\mathcal{L} = \frac{\theta}{32\pi^2} \frac{g_s^2}{32\pi^2} G\tilde{G} \Rightarrow \theta \leftrightarrow \frac{C_G \varphi_0 \cos(m_{\varphi} t)}{f_a}$$

# Constraints on Interaction of Axion Dark Matter with Gluons

nEDM constraints: [nEDM collaboration, *PRX* **7**, 041034 (2017)] HfF+ EDM constraints: [Roussy *et al.*, *PRL* **126**, 171301 (2021)]



#### Summary

- Plethora of opportunities for radioactive molecules in tests of fundamental symmetries and searches for new physics:
  - Paramagnetic molecules sensitive to hadronic sources of CP violation via two-photon-exchange processes (*regardless* of nucleus spin; i.e., operative for *spinless* nuclei, such as in <sup>232</sup>ThO, <sup>180</sup>HfF+)
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  - Low-mass bosonic dark matter can induce oscillating-in-time EDMs

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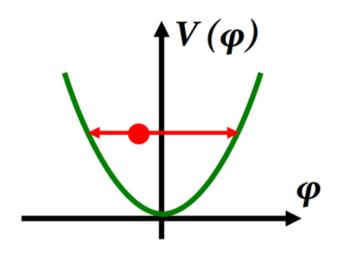
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#### Further work:

- For two-photon-exchange processes: nuclear structure effects, nuclear in-medium effects,  $\eta'$  and other N<sup>2</sup>LO contributions
- For nucleon-spin-dependent phenomena: improved knowledge of proton and neutron spin contributions in heavy nuclei
- Improved calculations of Schiff moments of heavy nuclei

# Back-Up Slides

• Low-mass spin-0 particles form a coherently oscillating classical field  $\varphi(t) = \varphi_0 \cos \left( m_\varphi c^2 t / \hbar \right)$ , with energy density  $\langle \rho_\varphi \rangle \approx m_\varphi^2 \varphi_0^2 / 2 \ (\rho_{\rm DM,local} \approx 0.4 \ {\rm GeV/cm^3})$ 



$$V(\varphi) = \frac{m_{\varphi}^2 \varphi^2}{2}$$

$$\ddot{\varphi} + m_{\varphi}^2 \varphi \approx 0$$

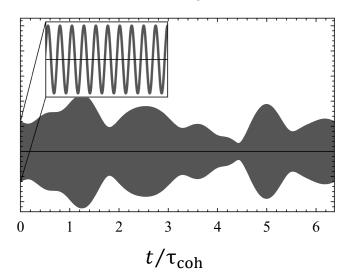
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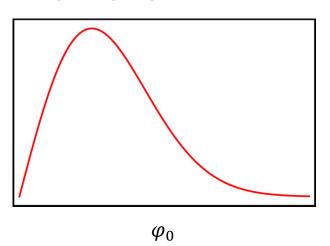
$$\Delta E_{\varphi}/E_{\varphi} \sim \langle v_{\varphi}^2 \rangle/c^2 \sim 10^{-6} \ \Rightarrow \ \tau_{\rm coh} \sim 2\pi/\Delta E_{\varphi} \sim 10^6 T_{\rm osc}$$
 
$$\uparrow \qquad \qquad v_{\rm DM} \sim 300 \ {\rm km/s}$$

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#### Evolution of $\varphi_0$ with time



### Probability distribution function of $\varphi_0$ (e.g., Rayleigh distribution)



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- $10^{-21}~{\rm eV} \lesssim m_{\varphi} \lesssim 1~{\rm eV} \iff 10^{-7}~{\rm Hz} \lesssim f_{\rm DM} \lesssim 10^{14}~{\rm eV}$   $T_{\rm osc} \sim 1~{\rm month}$  IR frequencies

Lyman-α forest measurements [suppression of structures for  $L \lesssim \mathcal{O}(\lambda_{dB,\varphi})$ ]

[Related figure-of-merit:  $\lambda_{\mathrm{dB},\varphi}/2\pi \leq L_{\mathrm{dwarf\,galaxy}} \sim 100 \,\mathrm{pc} \ \Rightarrow \ m_{\varphi} \gtrsim 10^{-21} \,\mathrm{eV}$ ]

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Wave-like signatures [cf. particle-like signatures of WIMP DM]