

# ELECTRONIC STRUCTURE OF EXOTIC ATOMS AND MOLECULES

A. Borschevsky



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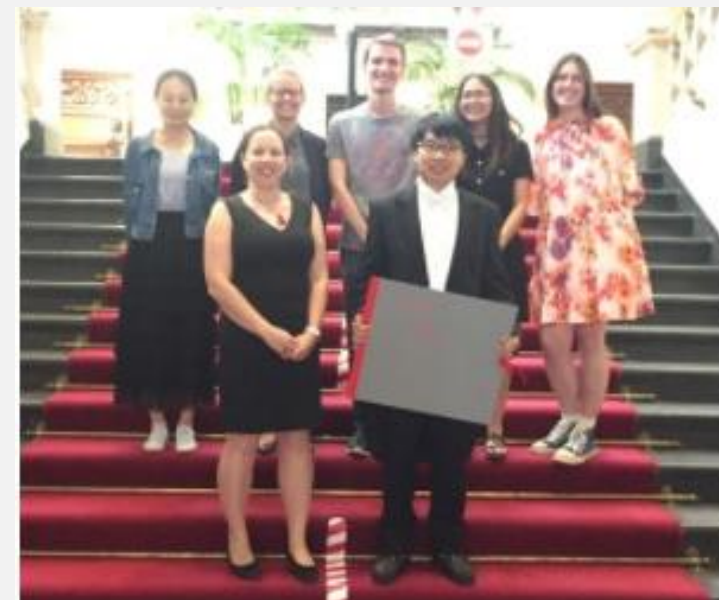
- University of Groningen

### Research:

Using computational chemistry tools to address fundamental problems in physics:

- Search for new physics with low-energy precision measurements
  - Violation of fundamental symmetries in atoms and in molecules
  - Search for variation of fundamental constants
- Highly accurate calculations of spectra and properties of heavy and superheavy atoms and highly charged ions

**Most work done in collaboration with experimental groups**





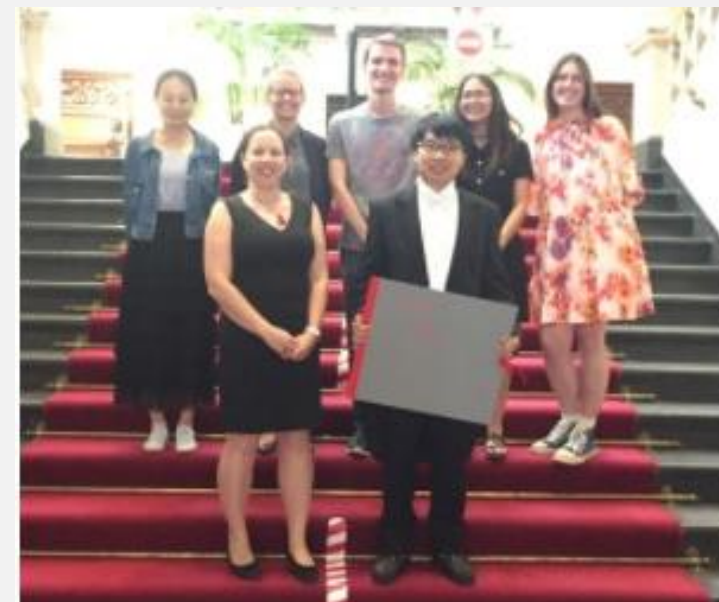
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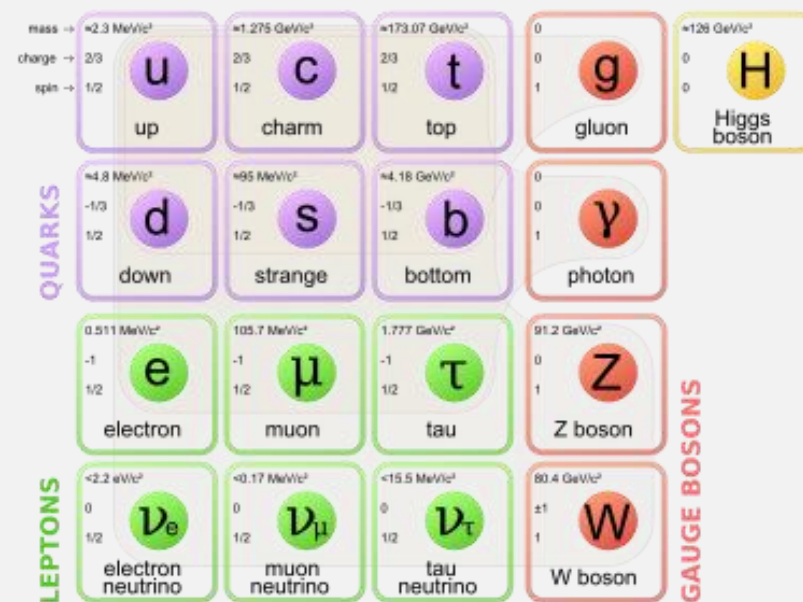
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MOTIVATION

## Why look for physics beyond the Standard Model (SM)?

- The SM is currently the best fitting physical description of the world around us.
- So far successfully explained the majority of observed natural phenomena and has strong predictive power (Higgs boson, top quark, tau neutrino)
- But... it is incomplete



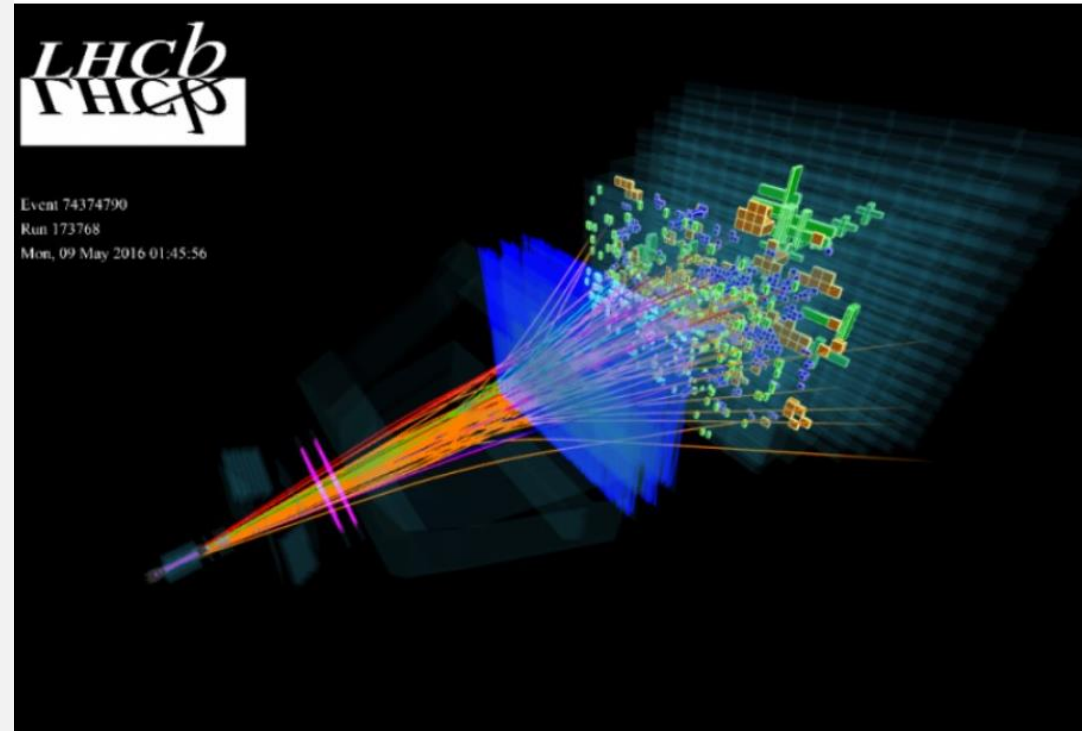
## Why look for physics beyond the Standard Model (SM)?

- Extensions to the SM attempt to fill these knowledge gaps.
  - Grand Unified Theories, String Theory, SUSY, ...
- These extensions predict new physical phenomena beyond the SM.
  - Variation of fundamental constants (VFC)
  - Violation of fundamental symmetries ( $CP, P, T$ )
- (non) discovery of these phenomena allows to discriminate between extensions or new theories.



## Why look for physics beyond the SM with atoms and molecules?

- Accelerator research (LHCb, T2K, etc.)
- **Table-top experiments**



A panoramic picture of the four meter long traveling-wave decelerator that has been built in Groningen. It is in use for decelerating packets of the heavy diatomic molecule SrF, which is a prototypical system for the investigation of broken symmetries.

# Why look for physics beyond the SM with atoms and molecules?

- **Table-top experiments: promising alternative to high energy research**
  - Versatile, sensitive to different phenomena
    - Parity violation
    - EDMs (electron, hadronic)
    - Variation of fundamental constants
    - Dark matter
    - ..
  - Various enhancement effects → high sensitivity
  - Small scale
  - (Relatively) inexpensive

Search for new physics with atoms and molecules

M. S. Safronova, D. Budker, D. DeMille, Derek F. Jackson Kimball, A. Derevianko, and Charles W. Clark  
Rev. Mod. Phys. **90**, 025008 – Published 29 June 2018



A panoramic picture of the four meter long traveling-wave decelerator that has been built in Groningen. It is in use for decelerating packets of the heavy diatomic molecule SrF, which is a prototypical system for the investigation of broken symmetries.



## How can (atomic and molecular) theory be of use?

- Insight into effect on molecular properties
- Identification of promising candidates for measurements
  - High sensitivity
  - Experimental considerations (stability, laser-coolability, etc.)
- Practical parameters for experiments
- Parameters for the interpretation of the results

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For use in experiments:

- Reliable predictions based on high accuracy calculations
- Preference for *ab initio* methods (predictive power)
- Possibility of assigning uncertainties

**Choice of computational method becomes important**

# COMPUTATIONAL METHODS

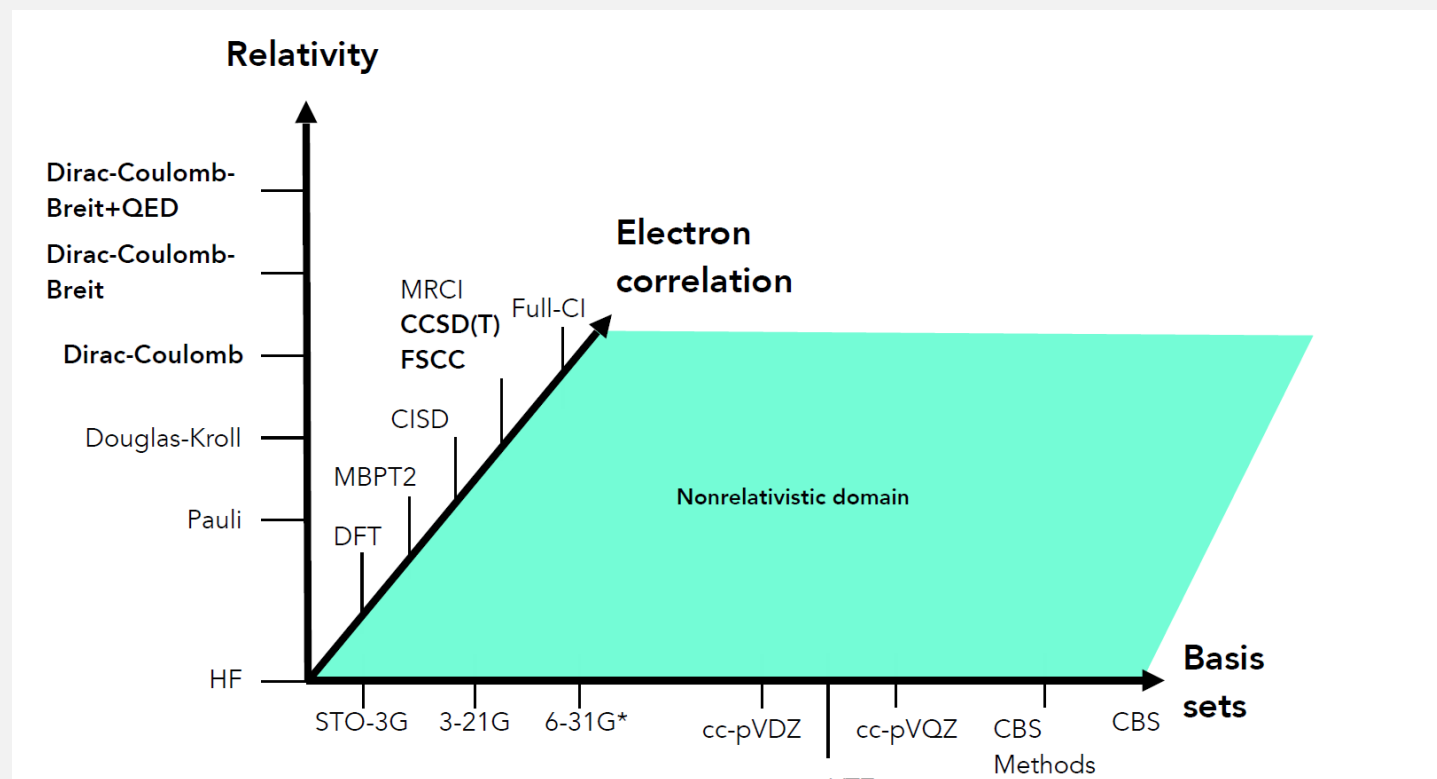
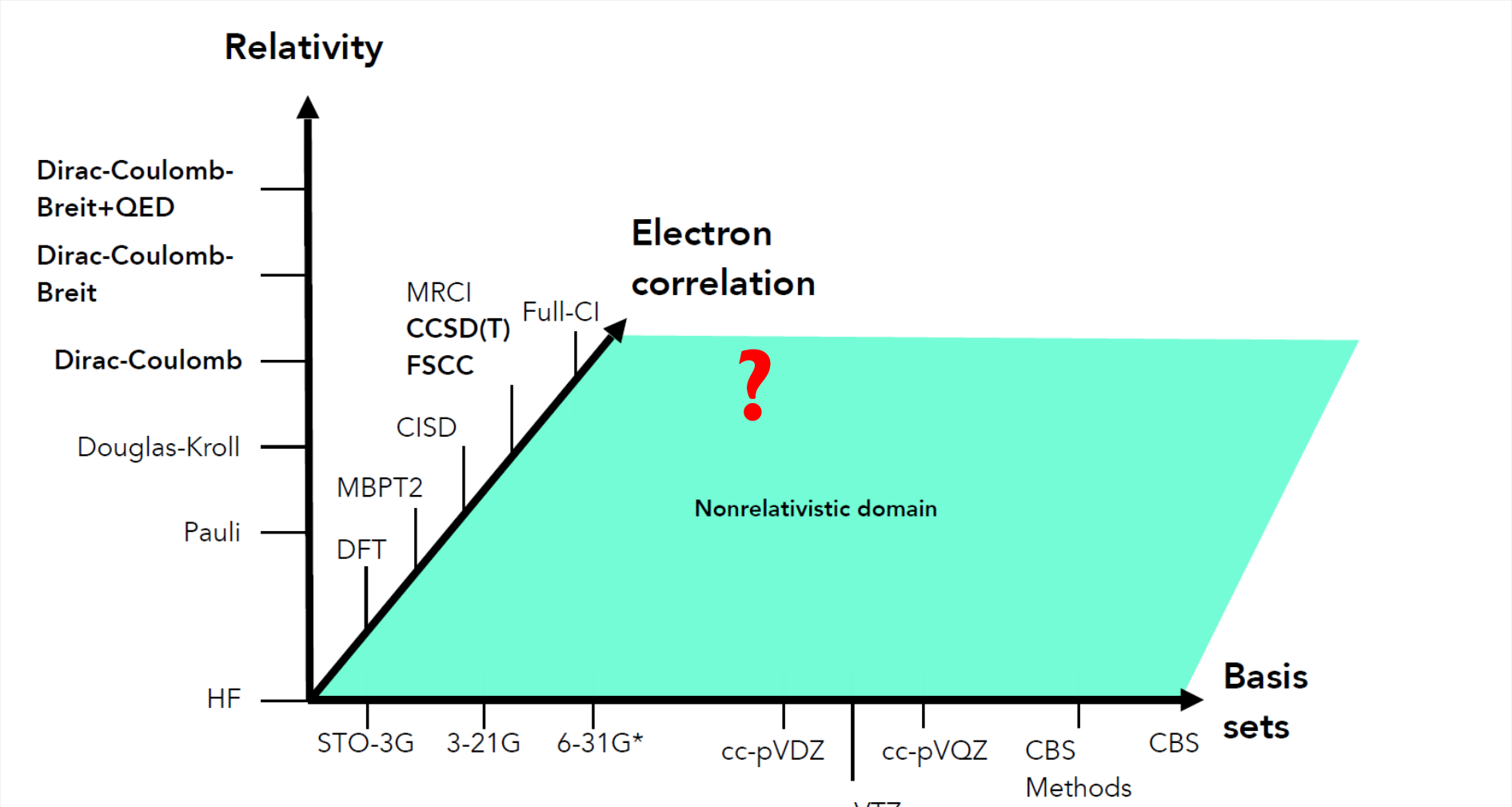


Figure courtesy of P. Schwerdtfeger



## What do we want to calculate?

- Coupling parameters describing the effect of  $P(T)$ -violating phenomena (or variation of constants) on electronic structure
  - Relativistic in nature, hence relativistic methods
- Atomic and molecular parameters needed in experiments
  - (usually) heavy (radioactive) systems, hence relativistic methods
- High accuracy
  - State-of-the-art treatment of correlation, large basis sets
- Uncertainty estimates
  - Robust, transparent methods



## Relativistic coupled cluster

- Based on the 4c Dirac Hamiltonian
- Accurate, size-consistent
- **CCSD(T)** - single reference coupled cluster

Closed shell systems/systems with one dominant configuration (good example: BaF,  $X^2\Sigma$ )

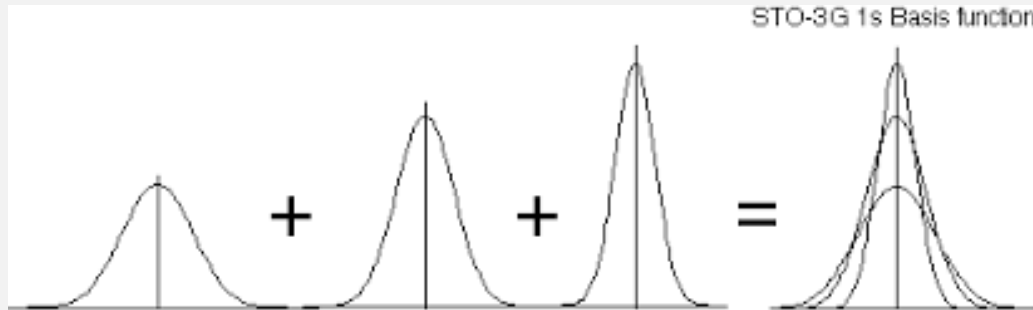
- **FSCC** – multireference Fock space coupled cluster

Open shell systems, excited states, bond dissociation (good example: ThO  $^3\Delta_1$  or any atomic spectrum)

Use the suitable method, or both in complementary manner.

## Basis sets

- Sets of (Gaussian) functions that are used to represent the electronic WF.
- Atom specific, different basis sets for different properties



$$g = x^{\ell} y^m z^n e^{-\alpha r^2}$$

Gaussian type orbital

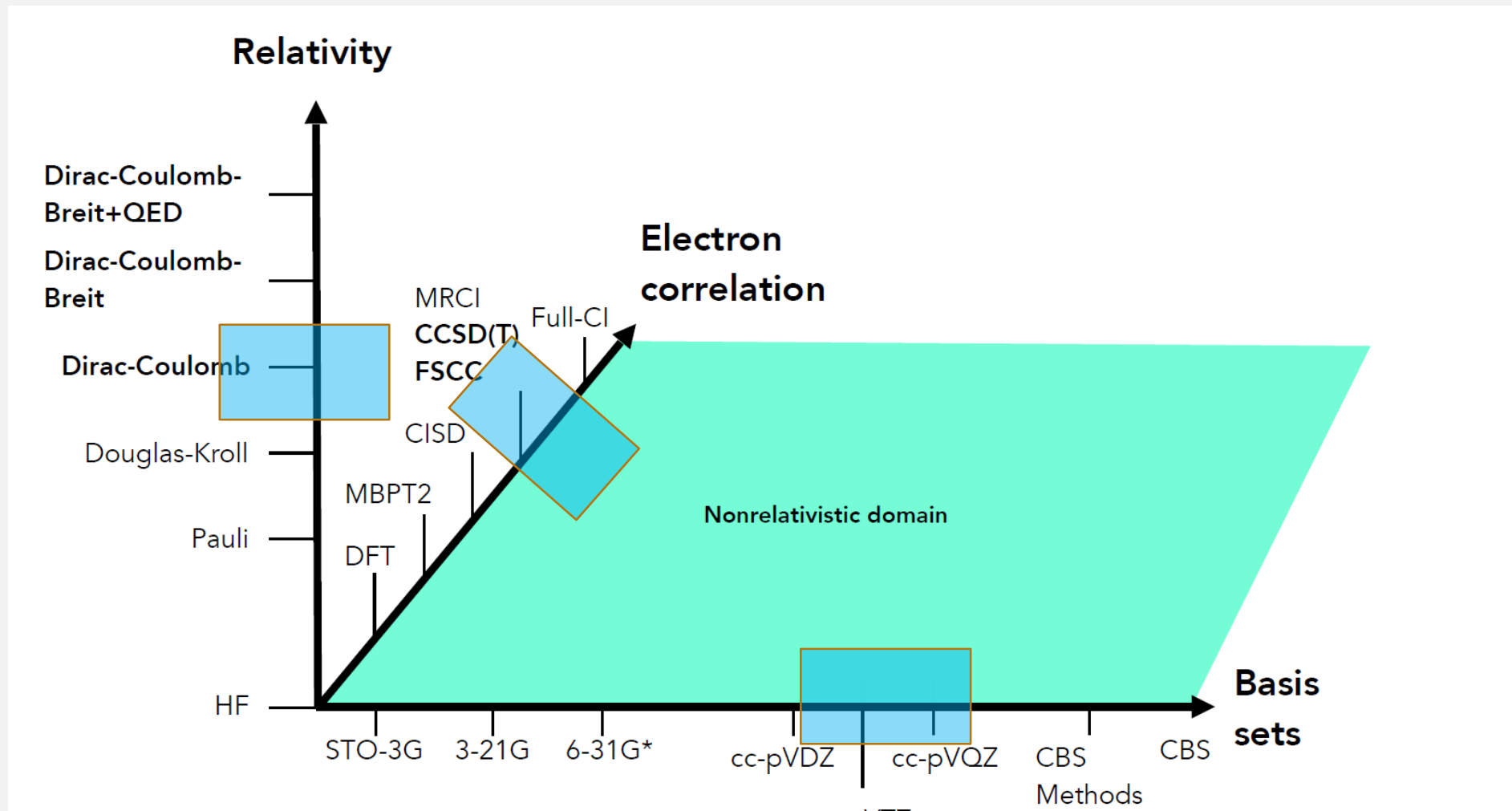
type of function:  
 $\ell = m = n = 0$  for s type  
 $\ell$  or  $m$  or  $n = 1$  for p type  
etc.

'exponent'  $\alpha$

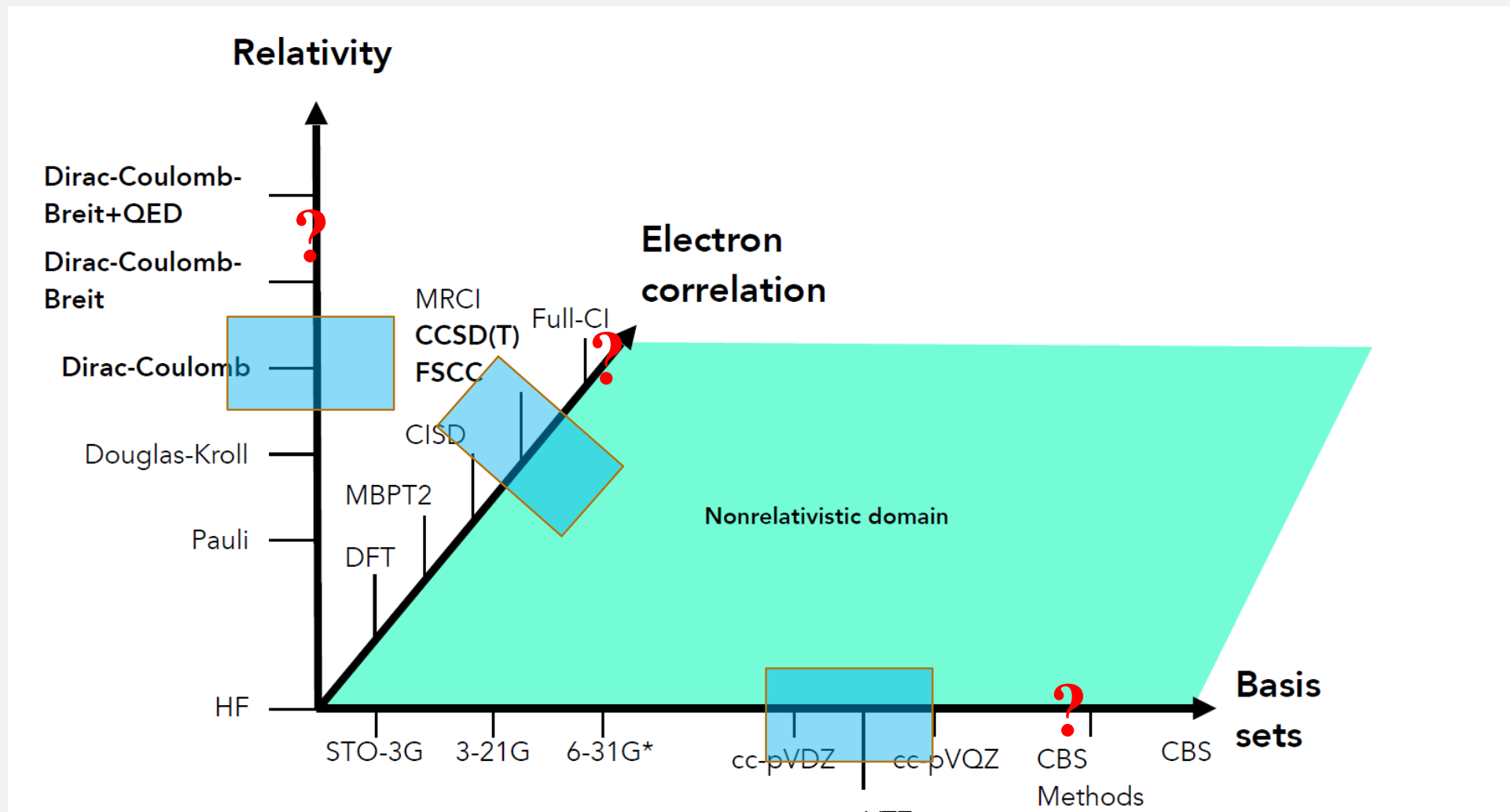
- Dyall's relativistic basis sets; augmented and extended to convergence

(K.G. Dyall, Theor. Chem Acc. 2002, 2004, 2006, 2007, 2009, 2011, 2012, etc.)

# Relativistic coupled cluster



# How do we assign uncertainties?



## Software

- Tel Aviv atomic computational package (TRAFS-3C)

Tel-Aviv Relativistic Atomic Fock-Space coupled cluster code, written by E.Eliav and U.Kaldor, with contributions from Y. Ishikawa, A. Landau, A. Borschevsky and H. Yakobi.

- DIRAC18 computational package

DIRAC, a relativistic *ab initio* electronic structure program, release DIRAC18 (2018)

and:

- MRCC code of Kallay et al., [www.mrcc.hu](http://www.mrcc.hu) (higher excitations)
- CFOUR package, <http://www.cfour.de> (geometry optimisation of polyatomic molecules)



## What can we calculate?

- Atomic properties: energies, IPs, EAs, spectra, **hyperfine structure parameters**, polarisabilities
- Molecular properties: geometries, spectroscopic constants, electronic structure, Franck-Condon Factors (FCFs), transition strengths
- Specific properties:
  - $W_d, W_s$  (eEDM experiments)
  - $W_A$  (NSD-PV, nuclear anapole moments)
  - $W_M$  (nuclear magnetic quadrupole moments)
  - Sensitivity to variation of  $\alpha$
  - ...
- CCSD(T), FSCC (applicable to different systems/states)
- Expected accuracy:  $\sim 10$  meV for energies
- **Systematic investigation of effect of computational parameters and uncertainty evaluation**

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- ✗ Computationally expensive
- ✗ FSCC is limited to systems with up to two valence electrons/holes
- ✗ Some properties not (yet) available, e.g. Schiff moment sensitivity factors

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# APPLICATIONS

- Search for eEDM in BaF molecules:
  - Laser cooling scheme
  - Sensitivity to eEDM: new method + uncertainty evaluation
  - Sanity check: HFS constants in BaF
- Same methods, new stuff:
  - IP of RaF
  - Polyatomic molecules

# NL-eEDM

## Measuring the electron-EDM with BaF molecules

### Scientific staff:

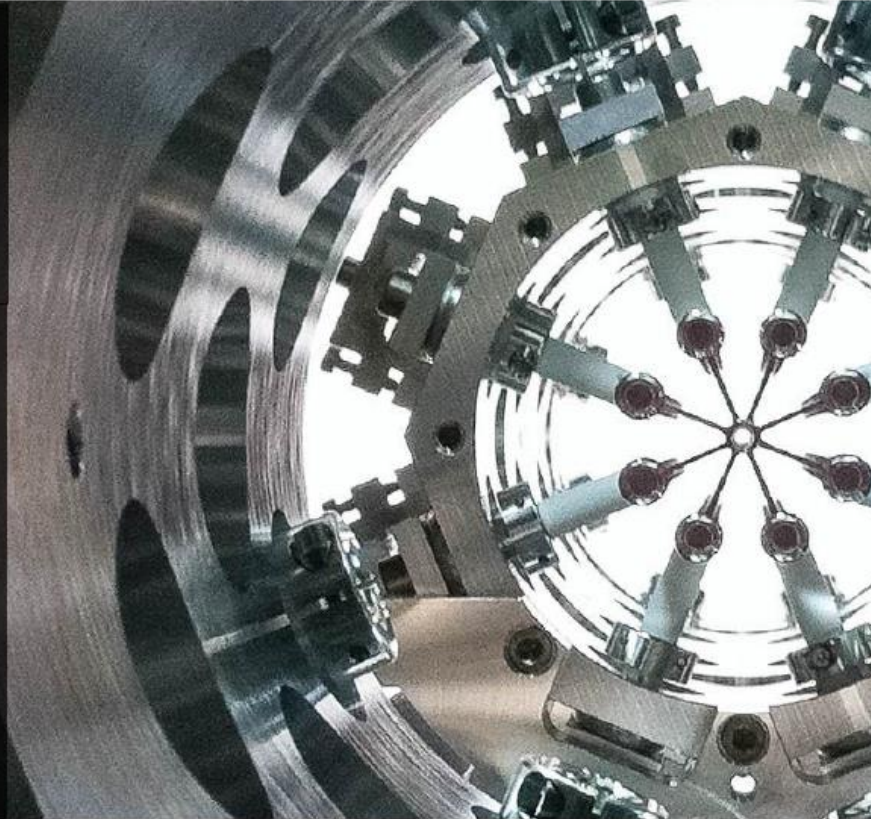
Anastasia Borschevsky  
Rick Bethlem  
Steven Hoekstra  
Klaus Jungmann  
Rob Timmermans  
Wim Ubachs  
Lorenz Willmann

### PhD students:

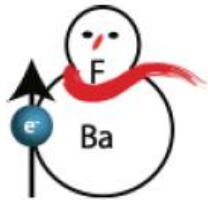
Parul Aggarwal  
Alexander Boeschoten  
Kevin Esajas  
Pi Haase  
Yongliang Hao  
Virginia Marshall  
Thomas Meijknecht  
Maarten Mooij  
Anno Touwen  
Artem Zapara

### Postdocs

Malika Denis  
Yanning Yin



NL-eEDM collaboration



university of  
 groningen  
 van swinderen institute for  
 particle physics and gravity

Nikhef

Dutch National Institute for (astro)Particle Physics



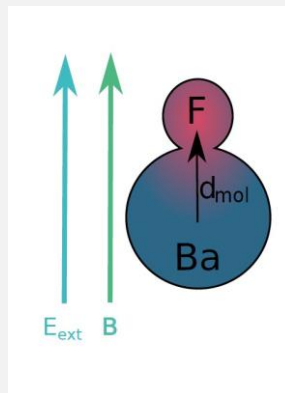
VRIJE  
UNIVERSITEIT  
AMSTERDAM



# Electron EDM

- Standard Model prediction:  $\sim 10^{-38}$  e\*cm
- SM extensions predict much larger values
- Measurement will provide signal of new physics

- Use a molecule!
- YbF, ThO, HfF<sup>+</sup>, ...
- Upper limit  $10^{-29}$  e\*cm, with ThO\*



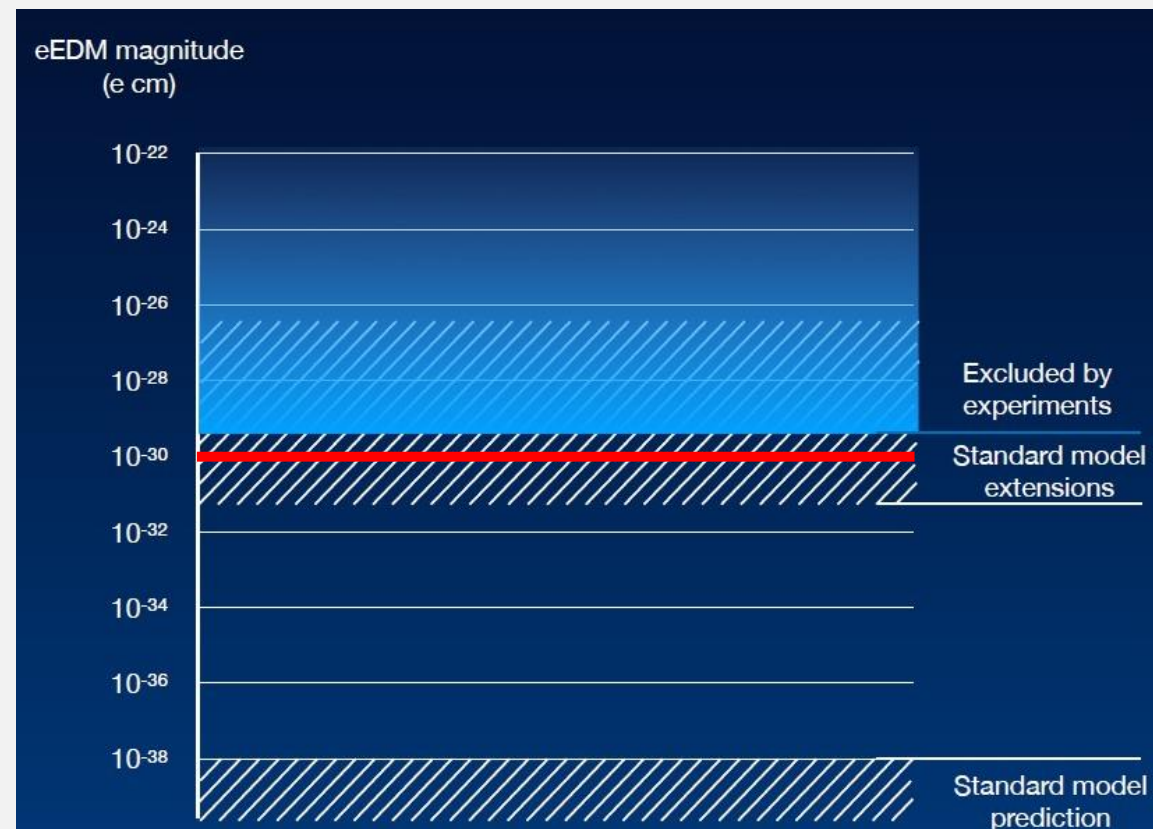
## Improved limit on the electric dipole moment of the electron

ACME Collaboration

*Nature* 562, 355–360(2018) | Cite this article

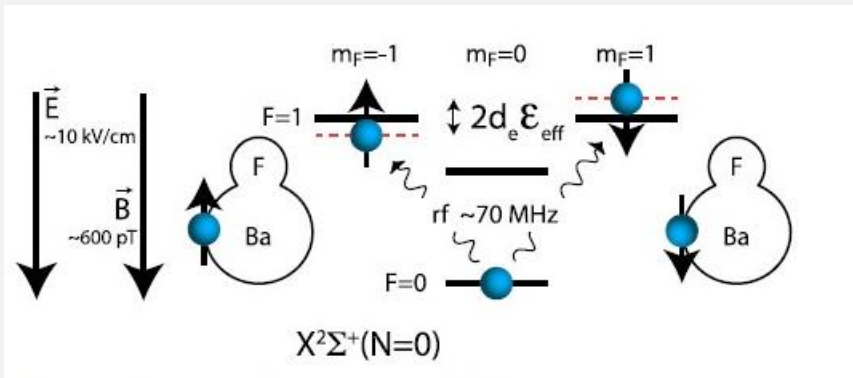
17k Accesses | 191 Citations | 360 Altmetric | Metrics

- ... and **BaF**
  - Experimental advantages (laser cooling, Stark deceleration)

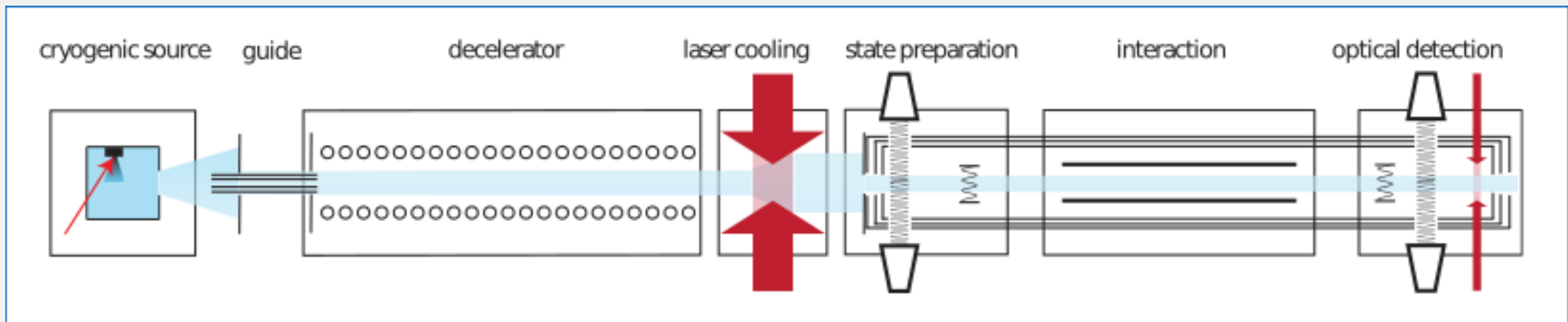


## The experiment:

- The EDM signal is detectable through a difference in the total accumulated phase for the parallel and the antiparallel orientation of the external magnetic and the electric fields.

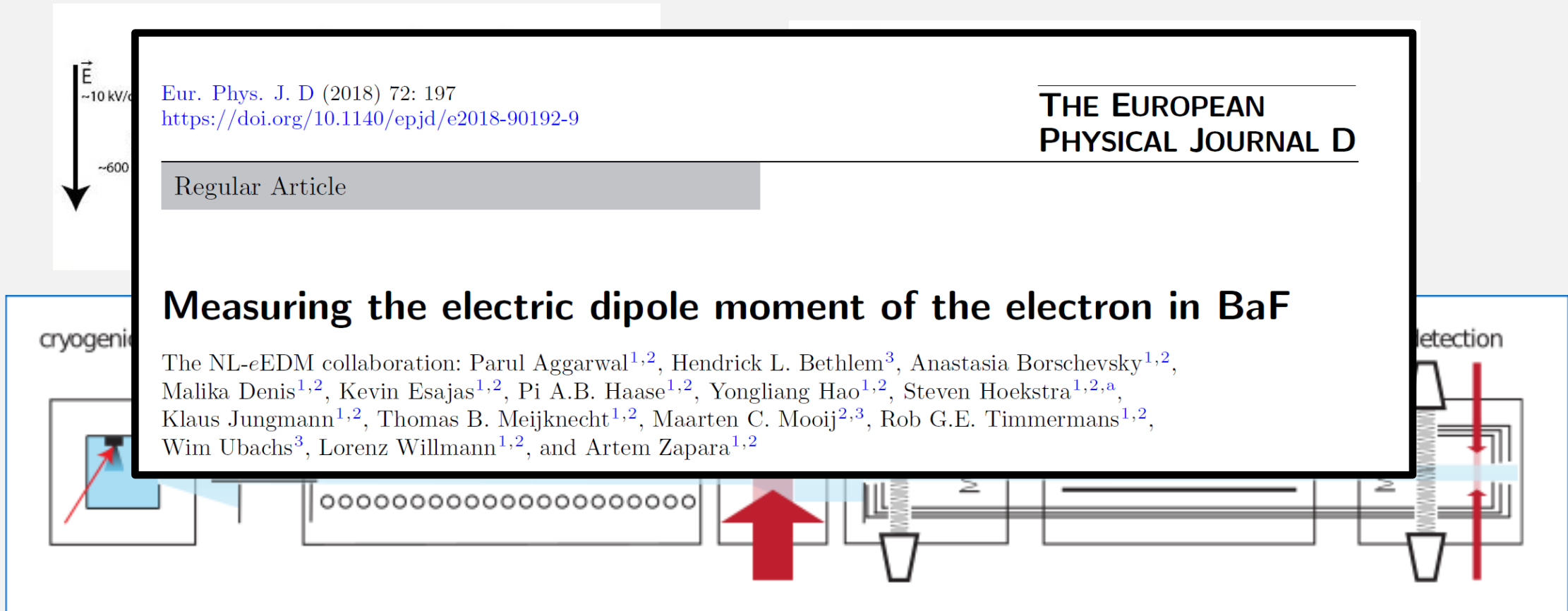


$$\sigma_d = \frac{1}{2|P|W_d\langle\mathbf{S}\cdot\mathbf{n}\rangle\tau\sqrt{N}}$$



## The experiment:

- The EDM signal is detectable through a difference in the total accumulated phase for the parallel and the antiparallel orientation of the external magnetic and the electric fields.



$\vec{E}$   
~10 kV/cm  
~600 G

Eur. Phys. J. D (2018) 72: 197  
<https://doi.org/10.1140/epjd/e2018-90192-9>

THE EUROPEAN  
PHYSICAL JOURNAL D

Regular Article

### Measuring the electric dipole moment of the electron in BaF

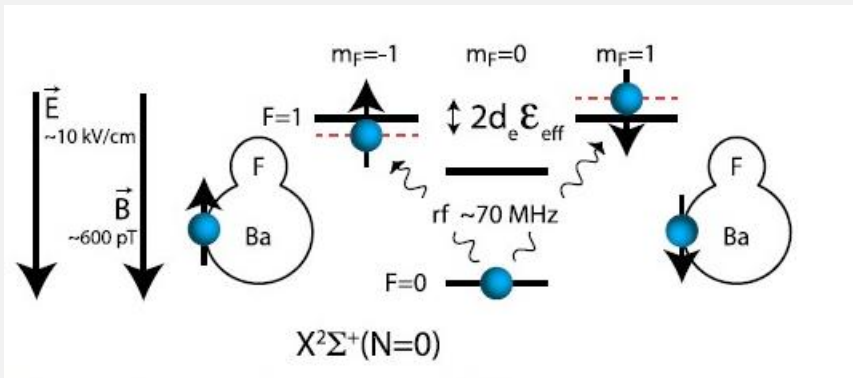
The NL-eEDM collaboration: Parul Aggarwal<sup>1,2</sup>, Hendrick L. Bethlem<sup>3</sup>, Anastasia Borschevsky<sup>1,2</sup>, Malika Denis<sup>1,2</sup>, Kevin Esajas<sup>1,2</sup>, Pi A.B. Haase<sup>1,2</sup>, Yongliang Hao<sup>1,2</sup>, Steven Hoekstra<sup>1,2,a</sup>, Klaus Jungmann<sup>1,2</sup>, Thomas B. Meijknecht<sup>1,2</sup>, Maarten C. Mooij<sup>2,3</sup>, Rob G.E. Timmermans<sup>1,2</sup>, Wim Ubachs<sup>3</sup>, Lorenz Willmann<sup>1,2</sup>, and Artem Zapara<sup>1,2</sup>

cryogenic

detection

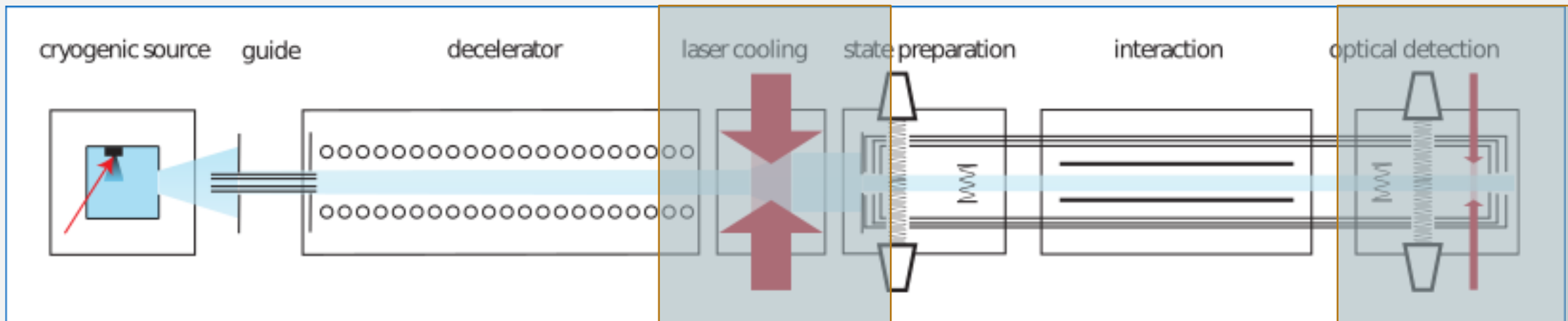
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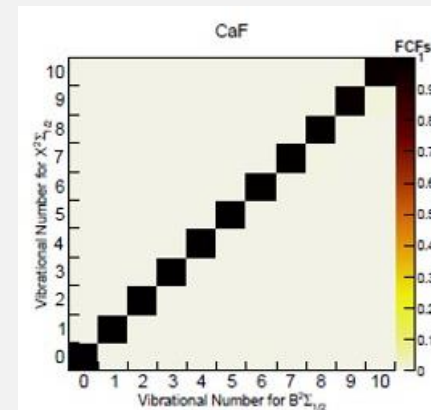
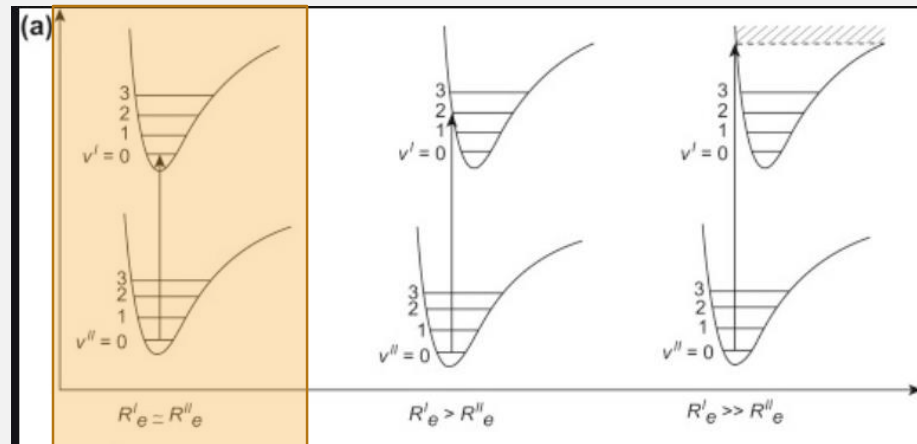
$$\sigma_d = \frac{1}{2|P|W_d \langle \mathbf{S} \cdot \mathbf{n} \rangle \tau \sqrt{N}}$$

$$E_{eff} = 2W_d$$



## Laser cooling:

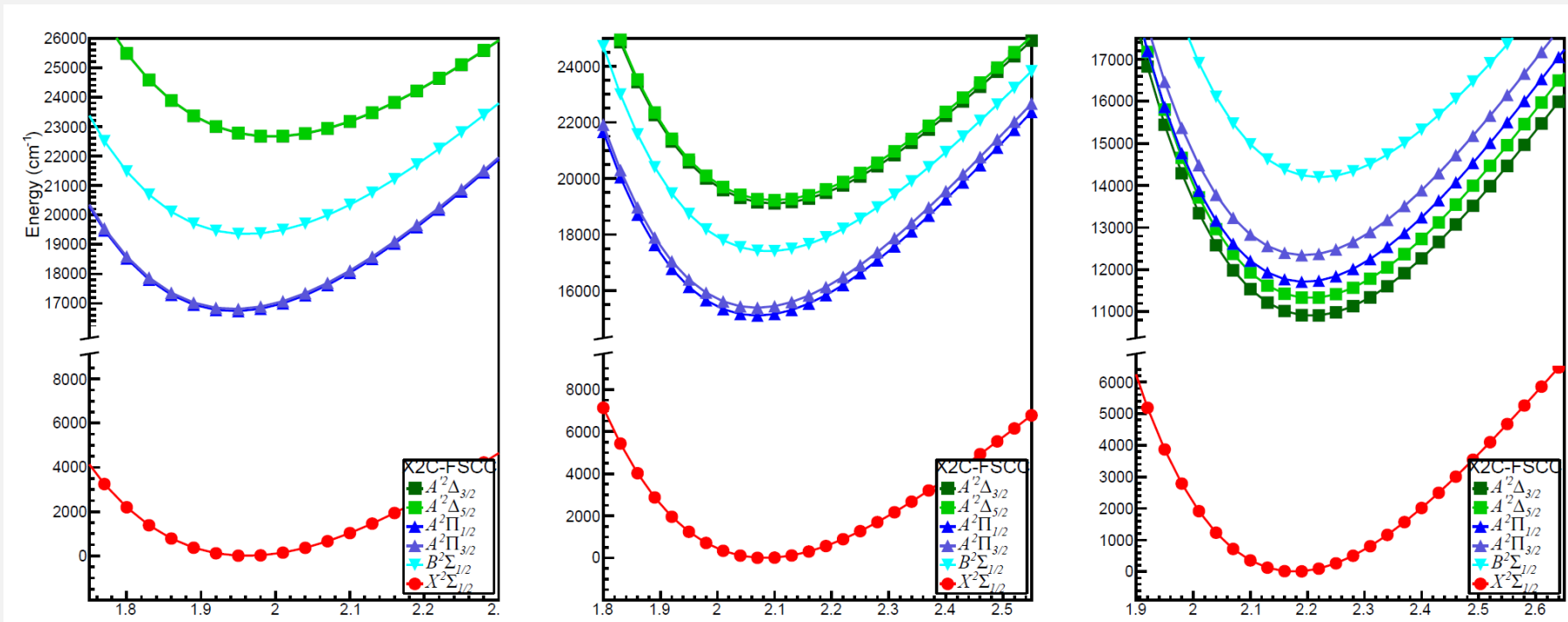
- Using light to slow transverse motion of the molecules
- We need to identify the optimal cooling scheme (transition):
  - Short lifetime (efficient cooling)
  - Diagonal Frank-Condon factors (FCFs), to avoid leaks



- Needed: potential energy curves, spectroscopic constants, FCFs, transition dipole moments, etc.

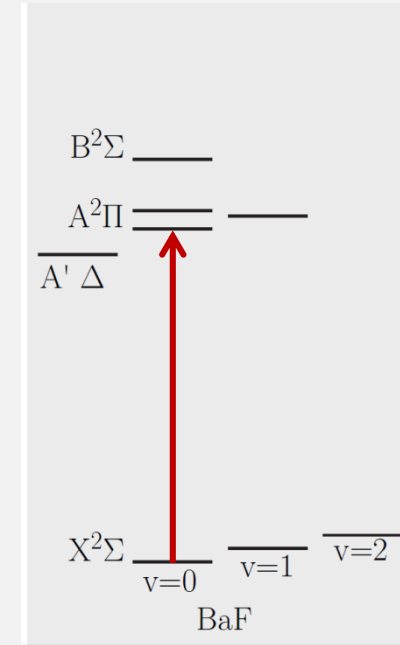
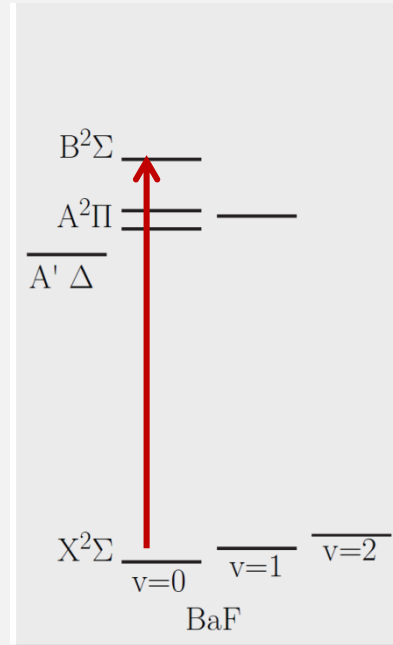
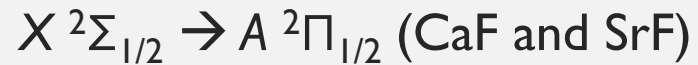
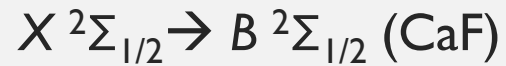
# Laser cooling:

Relativistic FSCC calculations for the 6 lowest electronic states of CaF, SrF, and BaF



## Laser cooling:

- Two possible cooling schemes:



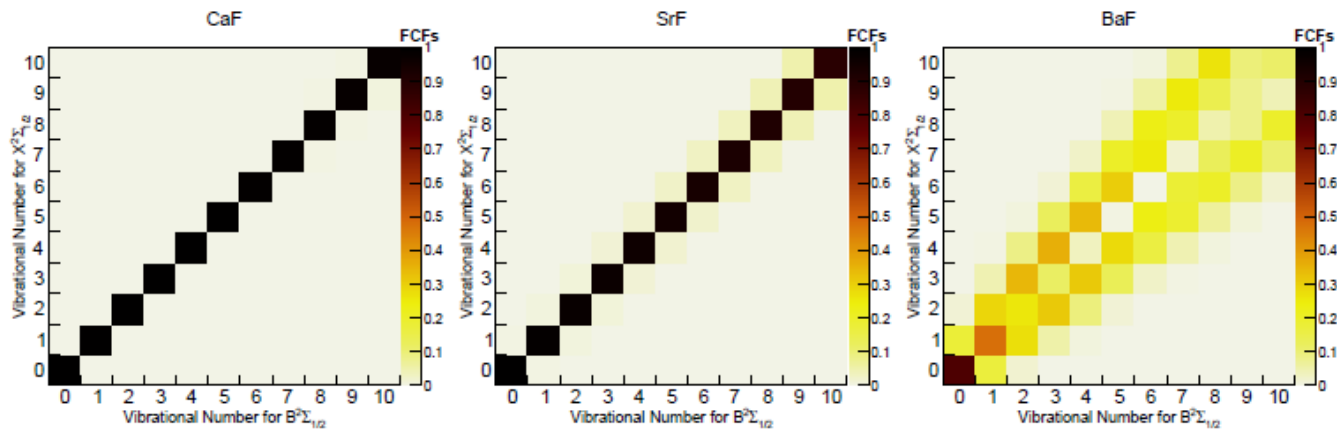
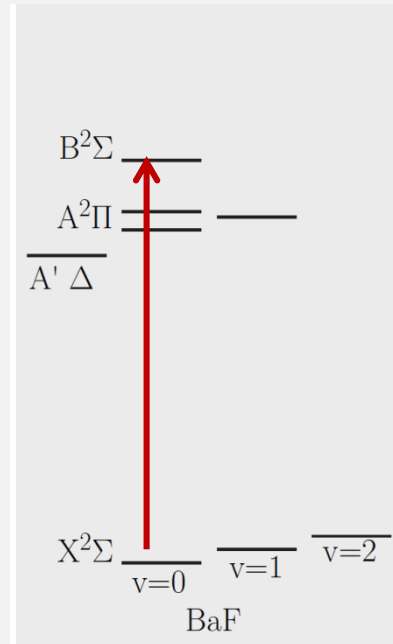
- Use calculated FCFs (measure of overlap of vibrational wavefunctions) to determine the appropriate scheme
- Diagonal FCFs  $\rightarrow$  efficient cooling

# Laser cooling:

- Two possible cooling schemes:



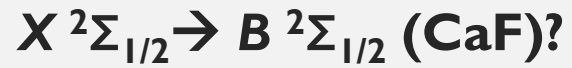
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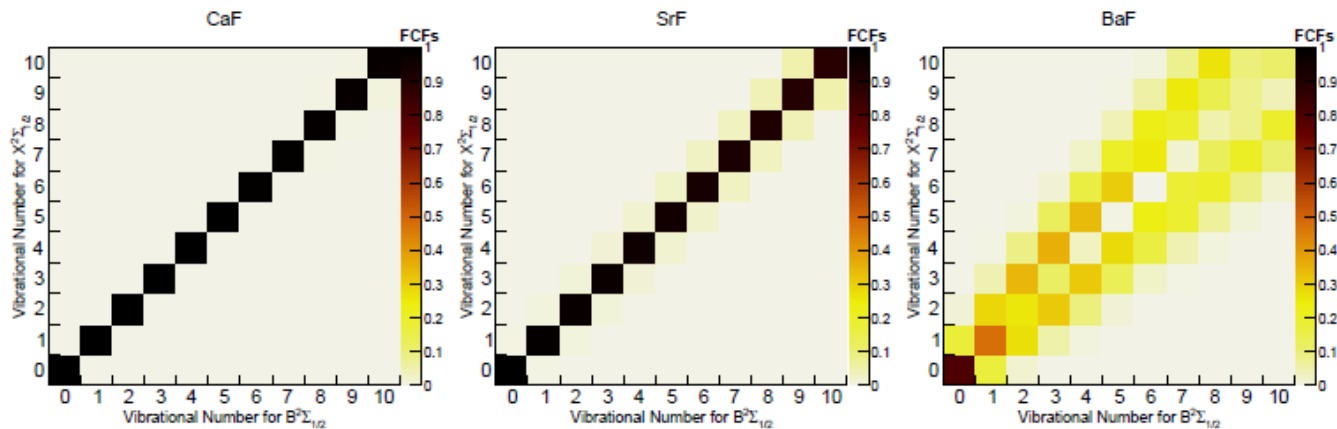
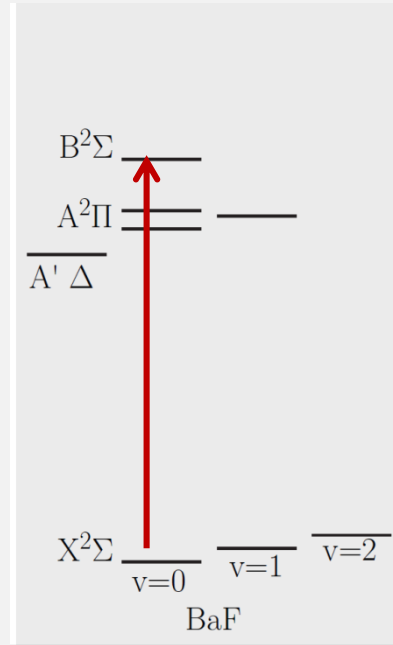
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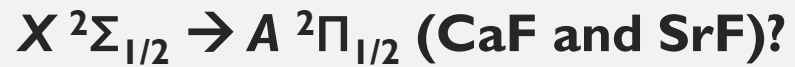
Nope 😞

- Diagonal FCFs  $\rightarrow$  efficient cooling

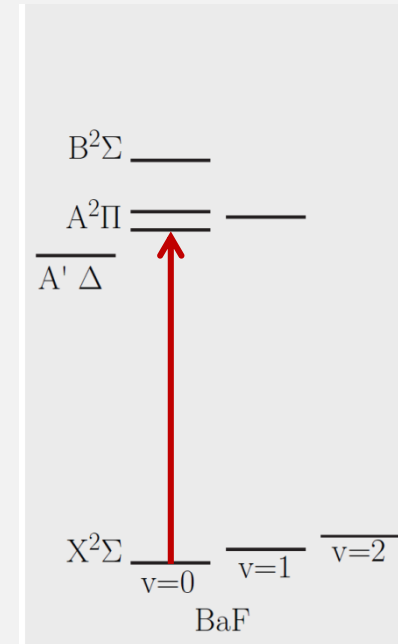
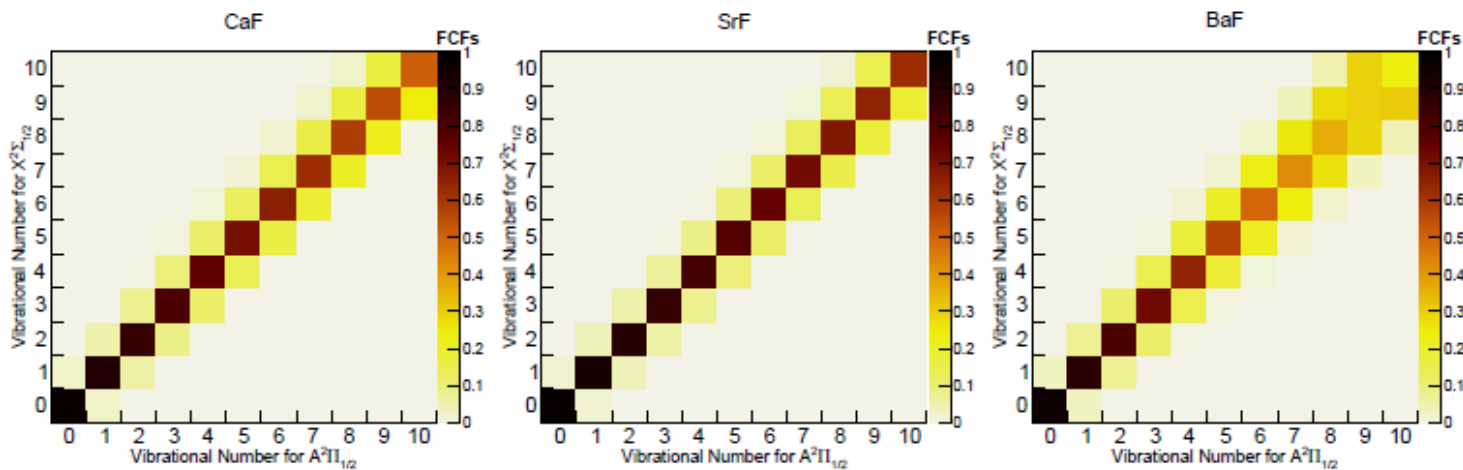


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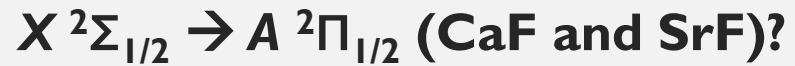


- Diagonal FCFs  $\rightarrow$  efficient cooling



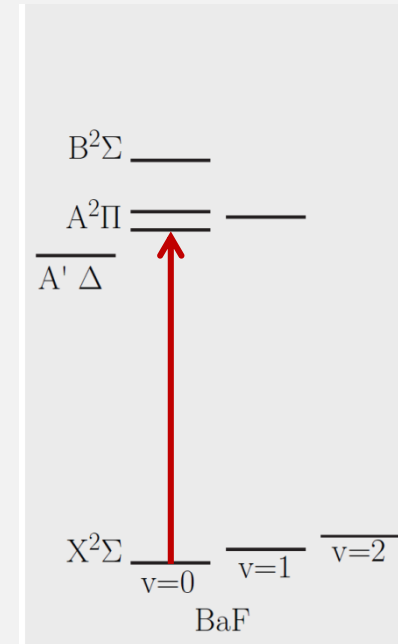
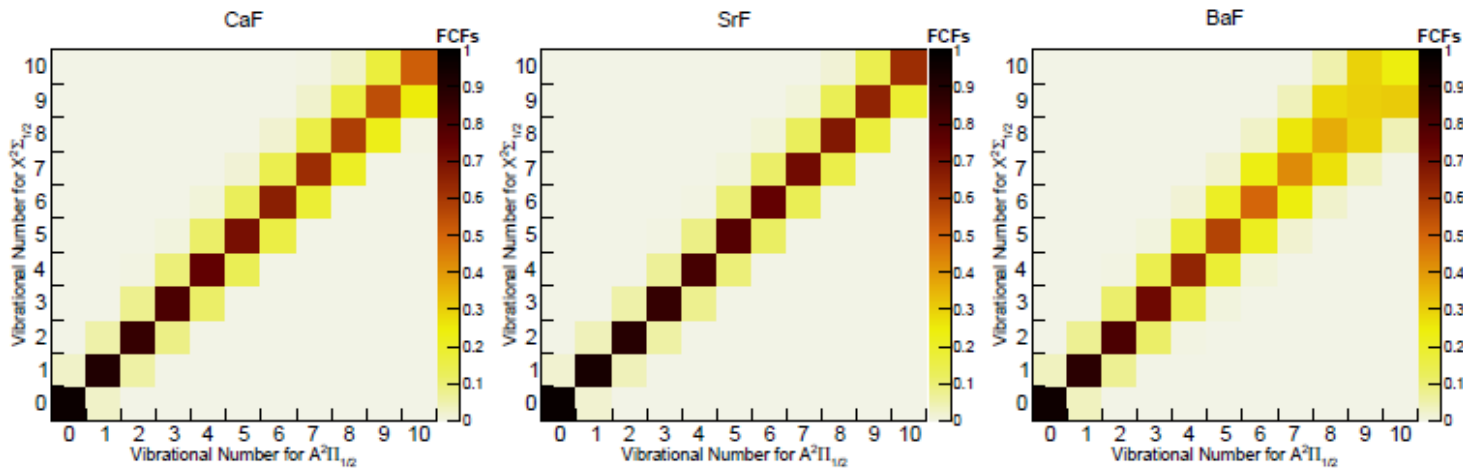
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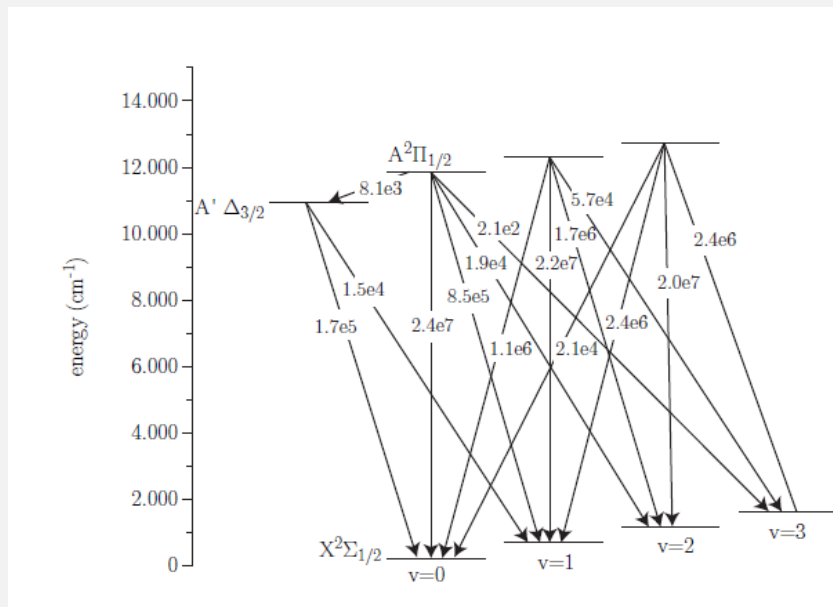
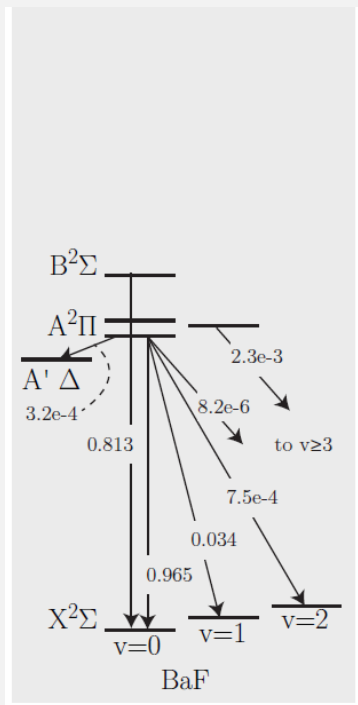


Yes! 😊

- Diagonal FCFs  $\rightarrow$  efficient cooling



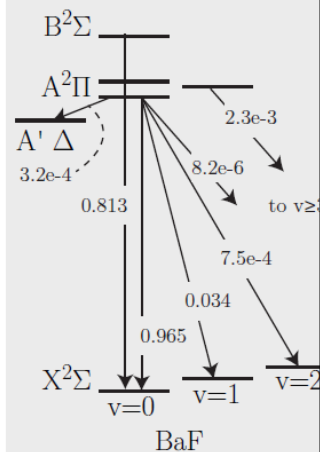
# Cooling scheme:



Yongliang Hao

Transition	Repump	CaF	SrF	BaF
$X - A$	no repump	25	36	19
	$v = 1$ repump	$7.9 \times 10^2$	$1.6 \times 10^3$	$6.4 \times 10^2$
	$v = 2$ repump	$2.2 \times 10^4$	$6.2 \times 10^4$	$2.1 \times 10^3$
	$\Delta$ repump			$7.6 \times 10^4$
$X - B$	no repump	$4.0 \times 10^3$	$1.9 \times 10^2$	3.4
	$v = 1$ repump	$4.1 \times 10^3$	$3.8 \times 10^4$	43

# Cooling scheme:



The Journal  
of Chemical Physics

ARTICLE

scitation.org/journal/jcp

## High accuracy theoretical investigations of CaF, SrF, and BaF and implications for laser-cooling

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Yongliang Hao,<sup>1,2</sup> Lukáš F. Pašteka,<sup>3</sup> Lucas Visscher,<sup>4</sup> Parul Aggarwal,<sup>1,2</sup> Hendrick L. Bethlem,<sup>5</sup> Alexander Boeschoten,<sup>1,2</sup> Anastasia Borschevsky,<sup>1,2,a)</sup> Malika Denis,<sup>1,2</sup> Kevin Esajas,<sup>1,2</sup> Steven Hoekstra,<sup>1,2</sup> Klaus Jungmann,<sup>1,2</sup> Virginia R. Marshall,<sup>1,2</sup> Thomas B. Meijknecht,<sup>1,2</sup> Maarten C. Mooij,<sup>5</sup> Rob C. E. Timmermans,<sup>1,2</sup> Anno Touwen,<sup>1,2</sup> Wim Ubachs,<sup>5</sup> Lorenz Willmann,<sup>1,2</sup> Yanning Yin,<sup>1,2</sup> and Artem Zapara<sup>1,2</sup> (NL-eEDM Collaboration)

$A = B$	no repump	$4.0 \times 10^3$	$1.9 \times 10^4$	5.4
	$v = 1$ repump	$4.1 \times 10^3$	$3.8 \times 10^4$	43



## Interpreting the experiment

$$\hat{H}^{P,T} = (W_d d_e + W_s \kappa_s) \hat{S} \cdot \hat{n}$$

$d_e$ - electron EDM,  $\kappa_s$  - *S-PS* electron-nucleon interaction

$W_d, W_s$ - molecule (and state) specific enhancement factors; depend on electronic structure and must come from theory.

$$\Delta E = (W_d d_e + W_s \kappa_s) \langle \hat{S} \cdot \hat{n} \rangle (E_{\text{ext}})$$

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$$\Delta E = (W_d d_e + W_s \kappa_s) \langle \hat{S} \cdot \hat{n} \rangle (E_{\text{ext}})$$

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## Electric dipole moments: A global analysis

Timothy Chupp and Michael Ramsey-Musolf  
 Phys. Rev. C **91**, 035502 – Published 6 March 2015

Investigations of optimal combinations of molecules:

- K. Gaul, S. Marquardt, T. Isaev, and R. Berger, Phys. Rev. A **99**, 032509 (2019)
- A. Sunaga, M. Abe, V. S. Prasanna, T. Aoki, and M. Hada, J. Phys. B **53**, 015102 (2019)

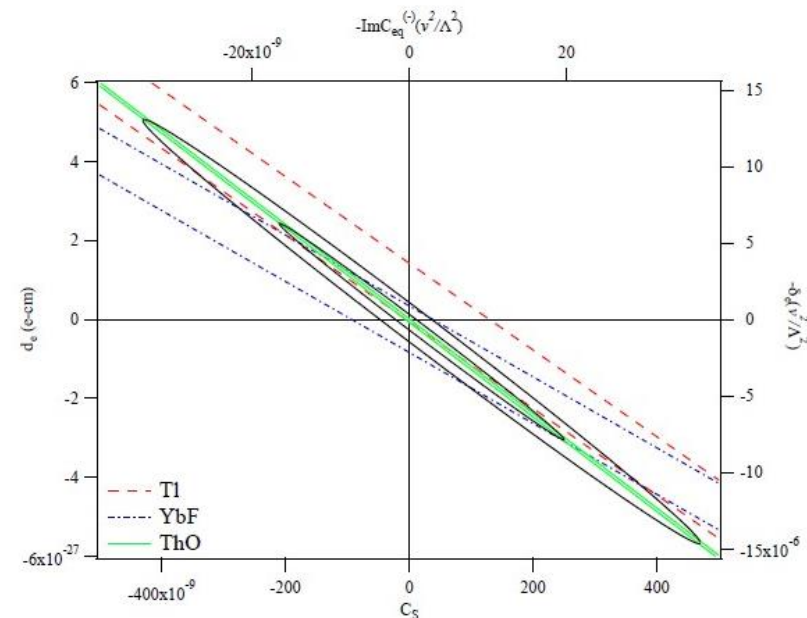


FIG. 1: Electron edm  $d_e$  as a function of  $C_S$  from the experimental results in Tl, YbF and ThO. Also shown are 68% and 95% error ellipses representing the best-fit for the paramagnetic systems and including  $d_A(^{199}\text{Hg})$  as discussed in the text. Also shown are the constraints on the dimensionless Wilson coefficients  $\delta_e$  and  $\text{Im} C_{eq}^{(-)}$  times the squared scale ratio  $(v/\Lambda)^2$ .

## Interpreting the experiment

$$\hat{H}^{\text{P,T}} = (W_d d_e + W_s k_s) \hat{\mathbf{S}} \cdot \hat{\mathbf{n}}$$

$$H^{\text{EDM}} = 2cd_e \sum_{i=1}^n v \gamma^0(i) \gamma^5(i) \mathbf{p}^2(i)$$

$$W_d = \frac{1}{d_e} \langle \psi_\Omega | H^{\text{EDM}} | \psi_\Omega \rangle$$

$$H_S = i \frac{G_F}{\sqrt{2}} Z \mathcal{K}_S \sum_{i=1}^n \gamma^0 \gamma^5 \rho_A(r_i)$$

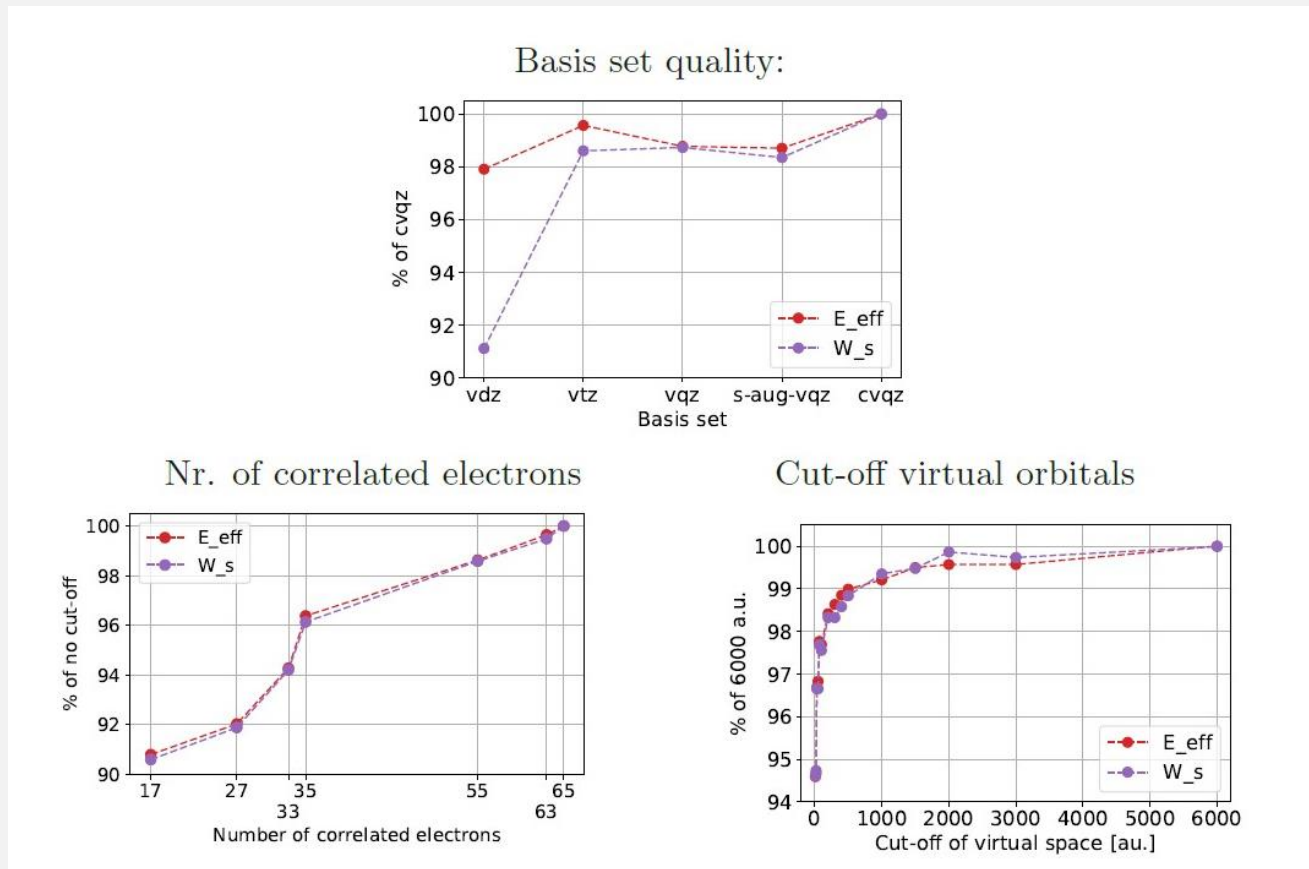
$$W_S = \frac{1}{\mathcal{K}_S \Omega} \langle \psi_\Omega | H_S | \psi_\Omega \rangle$$

- Use relativistic CCSD(T) to calculate  $W_d$  and  $W_s$ .
- Systematically improve the calculation up to convergence
- Perform an extensive computational study to estimate uncertainties



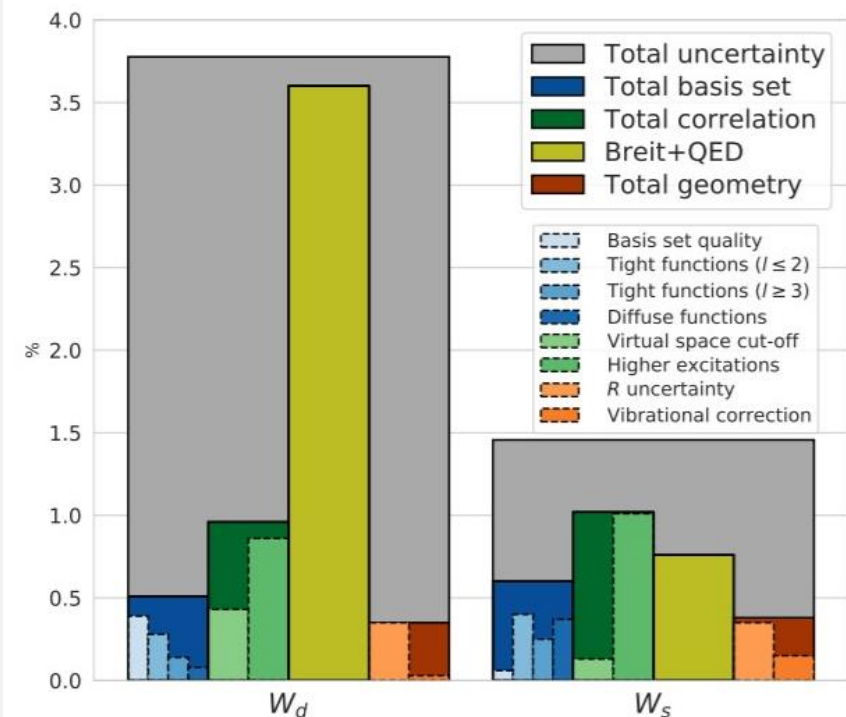
# Interpreting the experiment

- Use relativistic CCSD(T) to calculate  $W_d$  and  $W_s$ .
- Systematically improve the calculation up to convergence

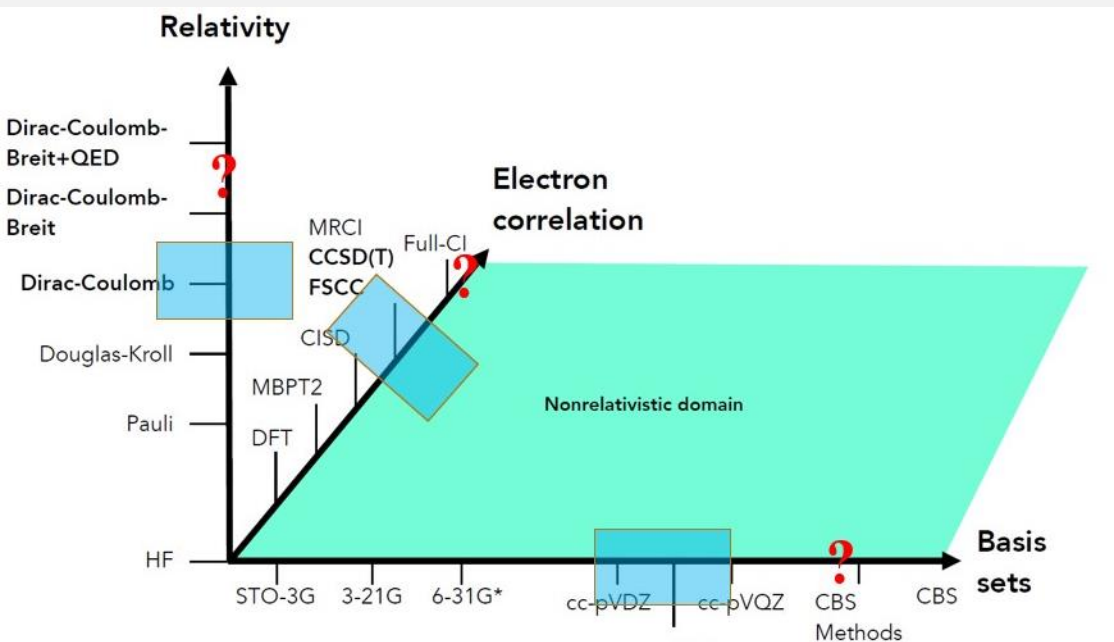


# Interpreting the experiment

- Use relativistic CCSD(T) to calculate  $W_d$  and  $W_s$  in BaF
- Systematically improve the calculation up to convergence
- Perform an extensive computational study to estimate uncertainties



Source	Estimation scheme	$\delta W_d$	$\delta W_s$
<b>Basis set</b>			
Quality	$(vqz - vtz)/2$	0.012	0.005
Diffuse funct.	s-aug-vqz - vqz	0.002	0.031
Tight funct. $l \leq 2$	(s, p, d)	0.009	0.033
Tight funct. $l \geq 3$	aeqz - cvqz	0.004	0.021
<b>Correlation</b>			
Virtual space cut-off	6000 a.u. - 2000 a.u.	0.014	0.011
Higher excitations	$(CCSD-T - CCSD+T) \cdot 2$	0.027	0.084
<b>Relativity</b>			
Breit+QED	$(DC+\Delta G - DC) \cdot 2$	0.113	0.064
<b>Geometry</b>			
R uncertainty	$R - (R - \delta R)$ (aetz)	0.011	0.029
Vibrational effects	$R_e - v_0$ (aetz)	0.001	0.013
Total			
sum	$\sqrt{\sum_i \delta_i^2}$	0.119	0.122
%		3.79	1.47



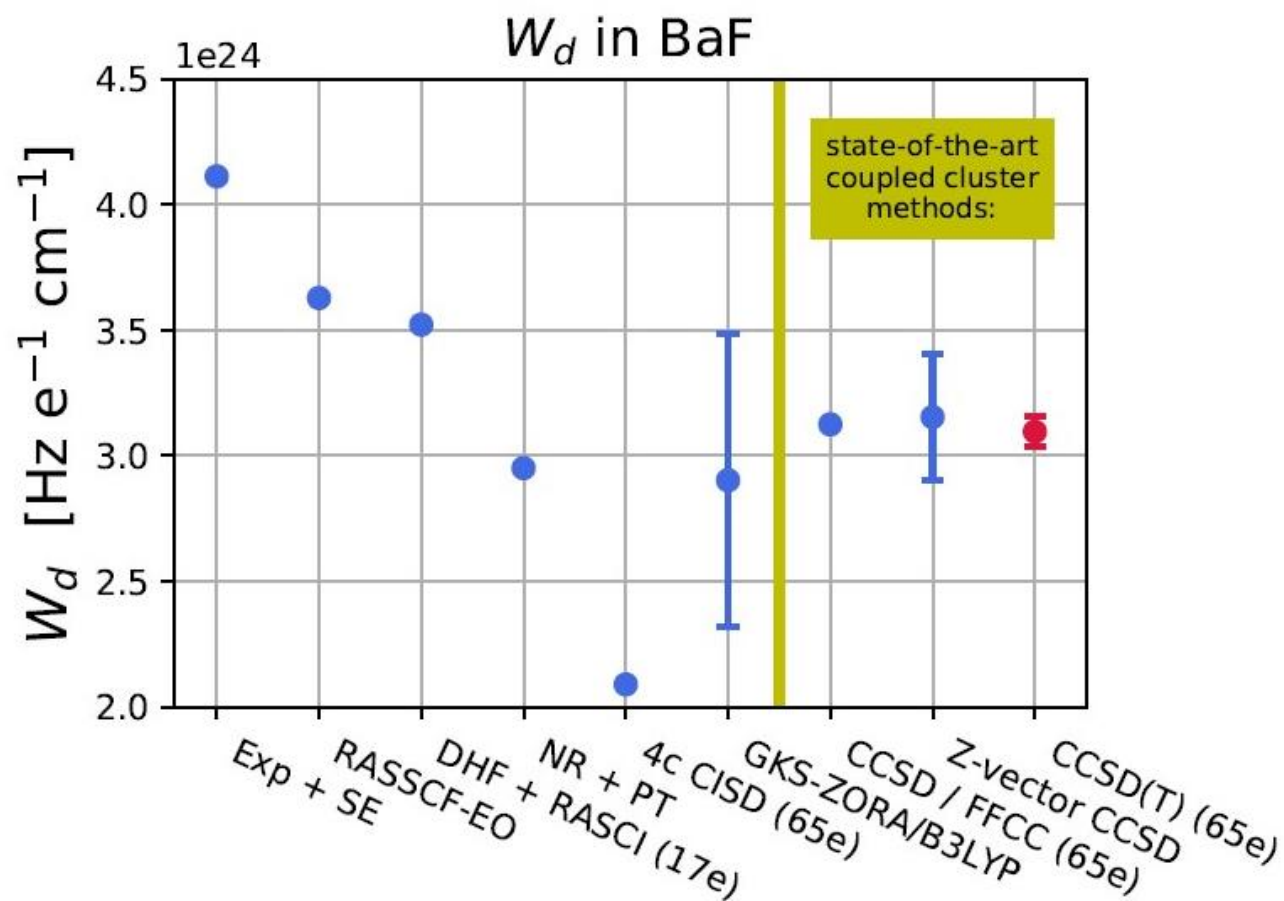
# Interpreting the experiment

- Final recommended values:

BaF	$W_d^*$ [ $\frac{10^{24}\text{Hz}}{e\text{ cm}}$ ]	$W_s$ [Hz]
DC CCSD(T)	3.13 (3.8%)	8.29 (1.5%)



Pi Haase



# Interpreting the experiment

- Final recommended values:

BaF	$10^{24}$
DC CCS	

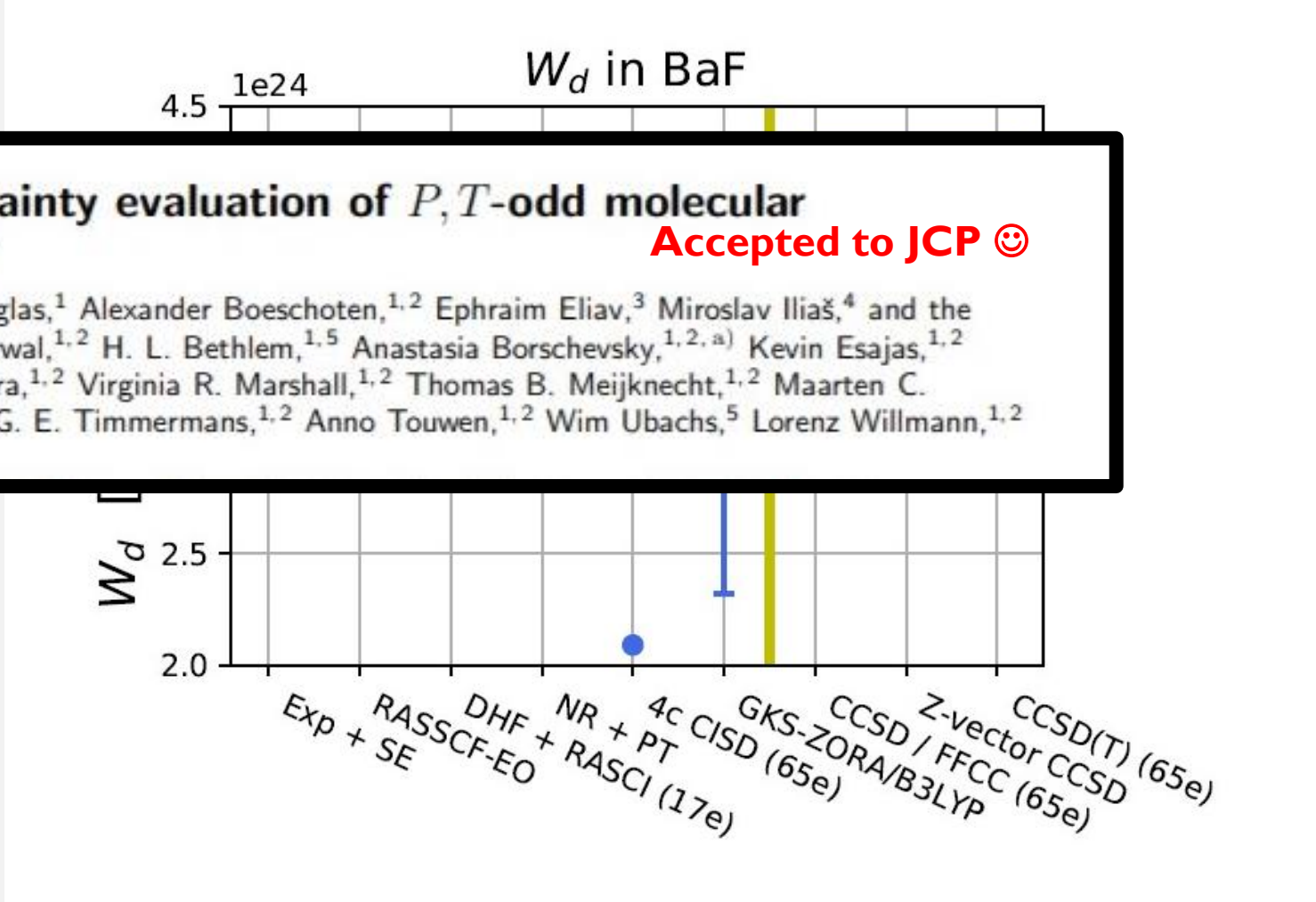
**Systematic study and uncertainty evaluation of  $P, T$ -odd molecular enhancement factors in BaF**

**Accepted to JCP 😊**

Pi A. B. Haase,<sup>1,2</sup> Diewertje J. Doeglas,<sup>1</sup> Alexander Boeschoten,<sup>1,2</sup> Ephraim Eliav,<sup>3</sup> Miroslav Iliáš,<sup>4</sup> and the eEDM collaboration:<sup>1,2</sup> Parul Aggarwal,<sup>1,2</sup> H. L. Bethlem,<sup>1,5</sup> Anastasia Borschevsky,<sup>1,2, a)</sup> Kevin Esajas,<sup>1,2</sup> Yongliang Hao,<sup>1,2, b)</sup> Steven Hoekstra,<sup>1,2</sup> Virginia R. Marshall,<sup>1,2</sup> Thomas B. Meijknecht,<sup>1,2</sup> Maarten C. Mooij,<sup>2,5</sup> Kees Steinebach,<sup>1, c)</sup> Rob G. E. Timmermans,<sup>1,2</sup> Anno Touwen,<sup>1,2</sup> Wim Ubachs,<sup>5</sup> Lorenz Willmann,<sup>1,2</sup> and Yanning Yin<sup>1,2, d)</sup>



Pi Haase



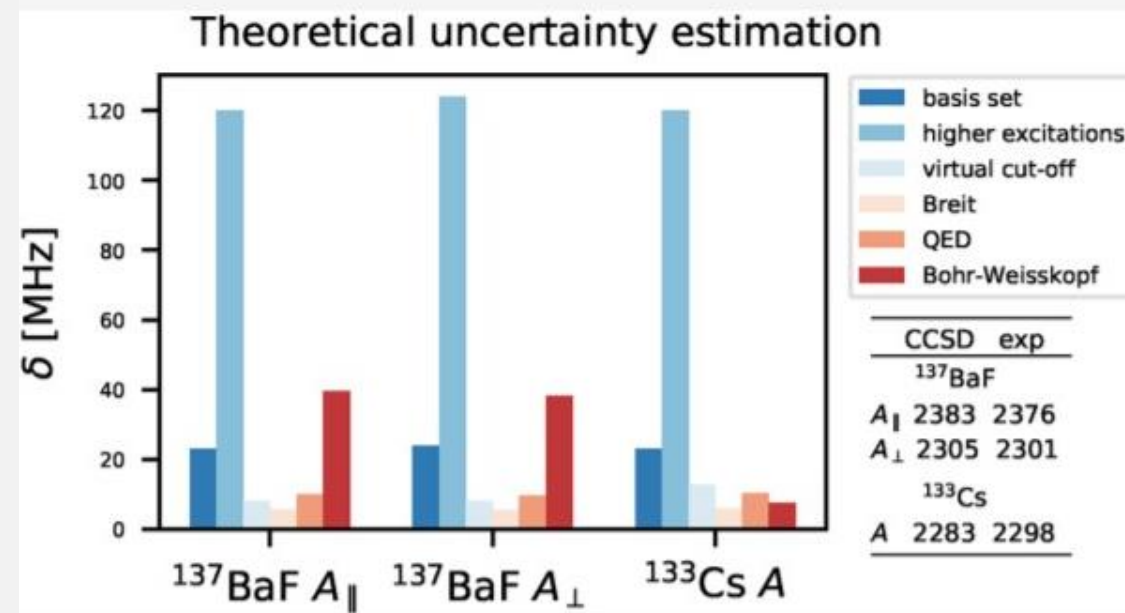
## Interpreting the experiment

- Is the uncertainty estimate realistic?
- Use a similar property, where comparison to experiment is possible, as a sanity check
- Magnetic hyperfine structure constants

BaF	$W_d^* [\frac{10^{24}\text{Hz}}{e\text{ cm}}]$	$W_s [\text{Hz}]$
DC CCSD(T)	3.13 (3.8%)	8.29 (1.5%)

Table 8.  $A_{\parallel}$  and  $A_{\perp}$  of  $^{137}\text{Ba}$  in BaF (MHz)

method	$^{137}\text{BaF}$			
	$A_{\parallel}$	%(exp)	$A_{\perp}$	%(exp)
GRECP SCF-EO <sup>90</sup>	2264	-4.71	2186	-5.00
GRECP RASSCF-EO <sup>90</sup>	2272	-4.38	2200	-4.39
DF RASCI <sup>91</sup>	2240	-5.72	2144	-6.82
DF MBPT <sup>91</sup>	2314	-2.61	2254	-2.04
DC CCSD (this work)	2383(129)	0.29	2305(132)	0.17
exp <sup>77</sup>	2376(12)		2301(9)	





## Interpreting the experiment

- Is the uncertainty estimate realistic?



Pi Haase

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Article

# Hyperfine Structure Constants on the Relativistic Coupled Cluster Level with Associated Uncertainties

Pi A. B. Haase,\* Ephraim Eliav, Miroslav Iliaš, and Anastasia Borschevsky



Cite This: *J. Phys. Chem. A* 2020, 124, 3157–3169



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NEW STUFF

## IP of RaF

Laser-cooled RaF as a promising candidate to measure molecular parity violation

T. A. Isaev, S. Hoekstra, and R. Berger  
Phys. Rev. A **82**, 052521 – Published 24 November 2010

Article | [Open Access](#) | Published: 27 May 2020

## Spectroscopy of short-lived radioactive molecules

R. F. Garcia Ruiz , R. Berger , [...]X. F. Yang

*Nature* **581**, 396–400 (2020) | [Cite this article](#)

## PHYSICAL REVIEW LETTERS

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Accepted Paper

## Isotope shifts of radium monofluoride molecules

Phys. Rev. Lett.

S. M. Udrescu et al.

Accepted 19 May 2021

Approaching meV level for transition energies in the radium monofluoride molecule RaF and radium cation Ra<sup>+</sup> by including quantum-electrodynamics effects

J. Chem. Phys. **154**, 201101 (2021); <https://doi.org/10.1063/5.0053659>

 Leonid V. Skripnikov<sup>a)</sup>

Nuclear magnetization distribution effect in molecules: Ra<sup>+</sup> and RaF hyperfine structure 

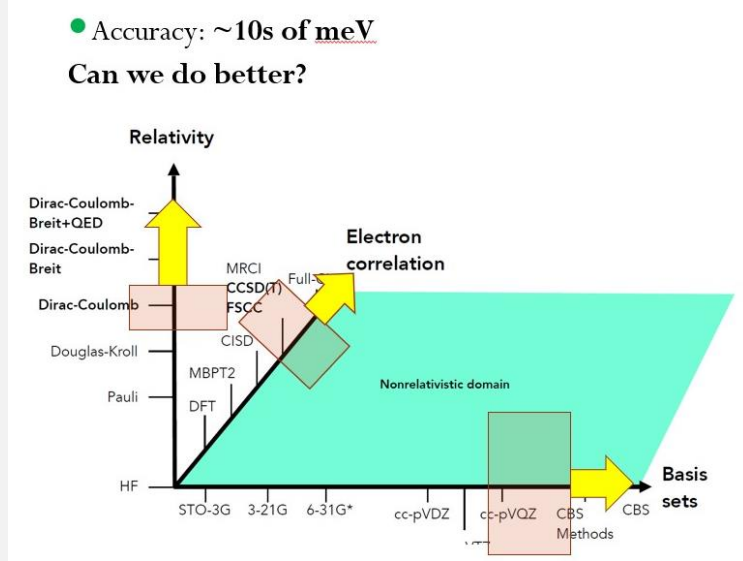
J. Chem. Phys. **153**, 114114 (2020); <https://doi.org/10.1063/5.0024103>

 Leonid V. Skripnikov<sup>1,2,a)</sup>



# IP of RaF

- Aim for highest accuracy: 4c CCSD(T)+higher order corrections

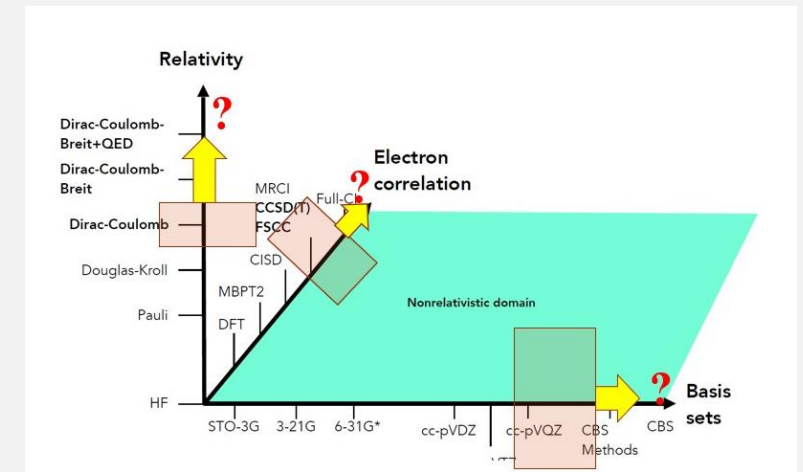


Method/contribution	IP (eV)	Contribution (eV)
4c-CCSD (s-cv4z)	4.926	
4c-CCSD(T) (s-cv4z)	4.972	0.046
4c-CCSD(T) (CBS)	4.978	0.006
4c-CCSDT (CBS)	4.980	0.002
4c-CCSDT (CBS)+Breit*	4.982	0.002
4c-CCSDT (CBS)+Breit+QED*	4.970	-0.012
Correction for final active space	4.977	0.007
<b>Final prediction</b>	<b>4.977</b>	

\*Obtained for Ra<sup>+</sup>

# IP of RaF

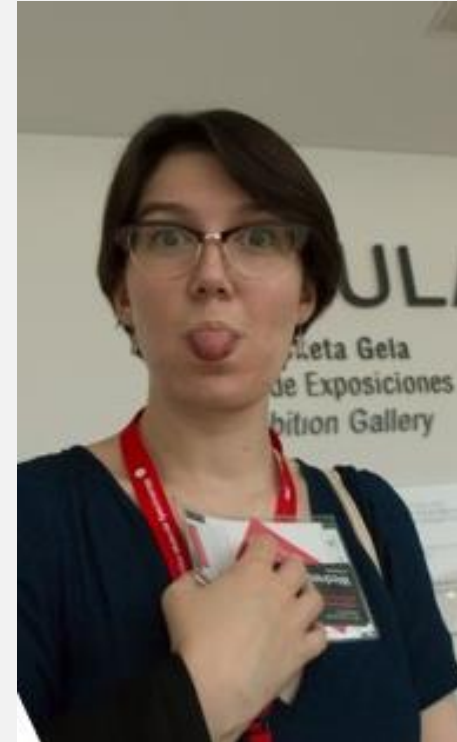
- Uncertainty evaluation



Type	Source	IP (eV)	How?
<b>Basis set</b>	Extrapolation error	0.003	(CBS- s-cv4z)/2
	Diffuse functions	0.001	(d-v4z – sv4z)/2
	Basis type	0.003	v3z vs. ae3z
<b>Relativity</b>	Higher order QED	0.005	$\Delta\lambda/2$
<b>Correlation</b>	Correlation space	0.002	all e- vs. 35 e
	Higher excitations	0.001	(T-(T))/2
<b>Total uncertainty</b>		<b>0.010</b>	

## IP of RaF

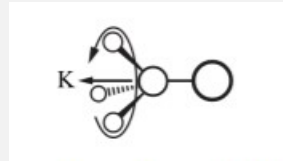
- Final recommended value for adiabatic IP: **4.977+/- 0.010**
- Waiting for experimental confirmation (or disproof)



Aleksandra Kiuberis

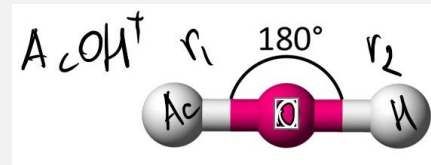
## Polyatomic molecules

- On Monday we learned: polyatomic molecules are awesome
- We agree



- Molecules to investigate:

- $\text{BaCH}_3, \text{YbCH}_3$ : symmetric top molecules
- $\text{AcOH}^+$ : linear system



- Could be used in experiments to measure eEDM (but also NMQM, or anapole moments, etc.)
- Investigate sensitivity to eEDM

## Polyatomic molecules

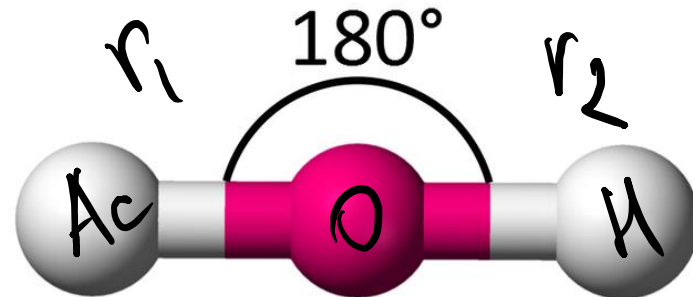
- For polyatomic molecules computational costs play an important role
- Two step process:
  - Geometry optimisation: scalar relativistic approach, pseudopotentials, CCSD(T)
  - Calculations of sensitivity parameters: 4c-CCSD(T)/FSCC, error estimate
- Makes the calculations feasible

# Polyatomic molecules

- For polyatomic molecules computational costs play an important role
- Two step process:
  - **Geometry optimisation: scalar relativistic approach, pseudopotentials, CCSD(T)**
  - Calculations of sensitivity parameters: 4c-CCSD(T)/FSCC, error estimate
- Makes the calculations feasible



Molecule	M—C(Å)	C—H(Å)	MCH (°)
BaCH <sub>3</sub>	2.55	1.10	113
YbCH <sub>3</sub>	2.39	1.09	112



$r_1$	2.057
$r_2$	0.957

SR-CCSD(T) level of theory with ANO-RCC-PV $n$ Z basis set;  $n = 5$  for BaCH<sub>3</sub> and  $n = 4$  for YbCH<sub>3</sub>.

# Polyatomic molecules

- For polyatomic molecules computational costs play an important role
- Two step process:
  - Geometry optimisation: scalar relativistic approach, pseudopotentials, CCSD(T)
  - **Calculations of sensitivity parameters: 4c-CCSD(T)/FSCC, error estimate**
- Makes the calculations feasible

## Systematic study and uncertainty evaluation of $P, T$ -odd molecular enhancement factors in BaF

Pi A. B. Haase,<sup>1,2</sup> Diewertje J. Doeglas,<sup>1</sup> Alexander Boeschoten,<sup>1,2</sup> Ephraim Eliav,<sup>3</sup> Miroslav Iliáš,<sup>4</sup> and the eEDM collaboration:<sup>1,2</sup> Parul Aggarwal,<sup>1,2</sup> H. L. Bethlem,<sup>1,5</sup> Anastasia Borschevsky,<sup>1,2,a)</sup> Kevin Esajas,<sup>1,2</sup> Yongliang Hao,<sup>1,2,b)</sup> Steven Hoekstra,<sup>1,2</sup> Virginia R. Marshall,<sup>1,2</sup> Thomas B. Meijknecht,<sup>1,2</sup> Maarten C. Mooij,<sup>2,5</sup> Kees Steinebach,<sup>1,c)</sup> Rob G. E. Timmermans,<sup>1,2</sup> Anno Touwen,<sup>1,2</sup> Wim Ubachs,<sup>5</sup> Lorenz Willmann,<sup>1,2</sup> and Yanning Yin<sup>1,2,d)</sup>

## Enhancement factor for the electric dipole moment of the electron in the BaOH and YbOH molecules

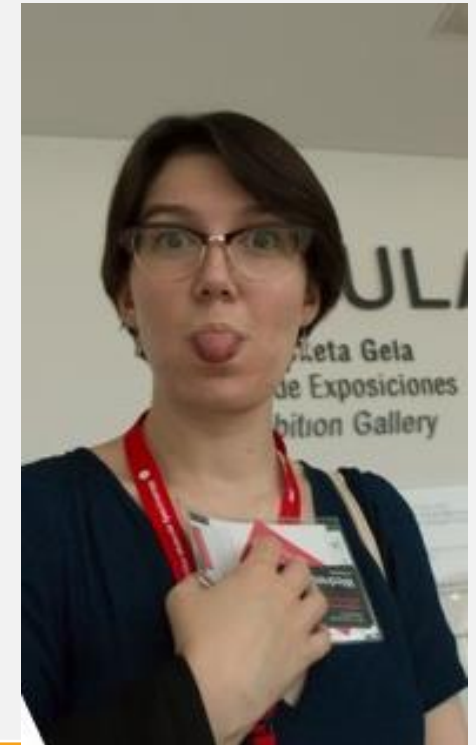
Malika Denis,<sup>1,\*</sup> Pi A. B. Haase,<sup>1</sup> Rob G. E. Timmermans,<sup>1</sup> Ephraim Eliav,<sup>2</sup> Nicholas R. Hutzler,<sup>3</sup> and Anastasia Borschevsky<sup>1</sup>

	$W_d$ [GV/cm]
<b>BaCH<sub>3</sub></b>	<b>3.45 (4.5%)</b>
BaF*	3.31 (3.8%)
BaOH**	3.21 (3.2 %)
<b>YbCH<sub>3</sub></b>	<b>14.0 (3.6 %)</b>
YbF**	11.8
YbOH**	11.7 (4.3%)
<b>AcOH<sup>+</sup></b>	<b>27.8</b>

# Polyatomic molecules

- For polyatomic molecules computational cost plays an important role
- Two step process:
  - Geometry optimisation: scalar relativistic, dispersion-corrected, CCSD(T)
  - **Calculations of sensitivity parameters: CCSD(T)/FSCC, error estimate**

**Preliminary Values**



Aleksandra Kiuberis



Yuly Andrea Chamorro Mena

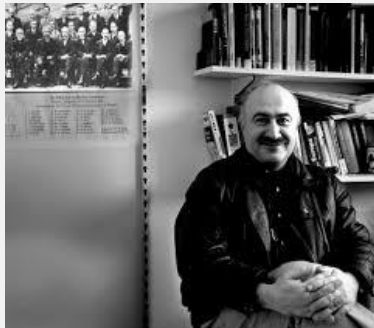
Molecular calculations for *P, T*-odd molecular  
<sup>2</sup> Ephraim Eliav,<sup>3</sup> Miroslav Iliaš,<sup>4</sup> and the  
Anastasia Borschevsky,<sup>1,2, a)</sup> Kevin Esajas,<sup>1,2</sup>  
Thomas B. Meijknecht,<sup>1,2</sup> Maarten C.  
van den Broek,<sup>1,2</sup> Wim Ubachs,<sup>5</sup> Lorenz Willmann,<sup>1,2</sup>  
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<b>AcOH<sup>+</sup></b>	<b>27.8</b>



# CONCLUSIONS

- State of the art high accuracy computational approach
- Versatile method: many possible applications
- Reliable predictions, uncertainty estimates possible
- Close collaborations with experimental groups
  
- These are very exciting times!



Ephraim Eliav



Miroslav Ilias



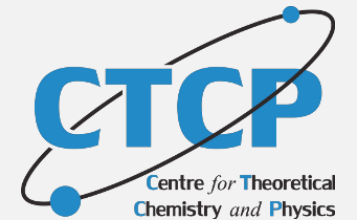
Lukas Pasteka



Victor Flambaum



Peter Schwerdtfeger



# RELATIVISTIC COUPLED CLUSTER

- Based on the 4c Dirac Hamiltonian
- Exponential wave operator:

$$\Psi = \exp(S)\Psi_0 = \left(1 + S + \frac{S^2}{2!} + \dots\right)\Psi_0$$

- $S$  is the excitation operator:

$$S = S_1 + S_2 + \dots + S_N; \quad S_1 = \sum_{ia} s_i^a a_a^\dagger a_i; \quad S_2 = \sum_{ijab} s_{ij}^{ab} a_a^\dagger a_b^\dagger a_j a_i$$

- CC energy equations:

$$\langle \Phi_0 | (H - E_{\text{CCSD}}) \exp(S_1 + S_2) | \Phi_0 \rangle = 0$$

- Accurate, all-order in PT, size-extensive, and size-consistent

# Reaching meV accuracy

Complete basis set limit extrapolation

